NATIONAL FORENSIC SCIENCES UNIVERSITY, DELHI CAMPUS B-Tech, 2nd Sem. Mid-Semester Examination

Date: 12.05.2022

Subject Name: Engineering Mathematics

Time: 90 minutes **Total Marks: 50**

Instructions: All questions are mandatory.

1. Prove that: [10] $_{0}\int^{\pi 2} \sin^{2m-1}x \cdot \cos^{2n-1}x \, dx = \Gamma(m) \Gamma(n) / 2\Gamma(m+n) ; m>0 \& n>0$

2. (a)

Evaluate:
$$I = {}_{0}\int^{2} x^{2} / \sqrt{(2-x)}$$
 . dx (b) $\frac{4}{3} + \frac{\sqrt{6}}{3}$

Evaluate: $1 = \int_0^\infty dx / (1+x^4)$ [5] 4+ 50 = 4+50

3. Using reduction method prove that:
$$\int sin^n(x)dx = \frac{-Sin^{n-1}(x)Cos(x)}{n} + \frac{n-1}{n}Sin^{n-2}(x)dx$$
 [10]

Evaluate
$$\int_{0}^{4a} \int_{\frac{x^{2}}{4a}}^{2\sqrt{ax}} dy dx$$
 by changing the order of integration. [10]

5. Evaluate $\int_0^1 \int_0^{\sqrt{1+x^2}} \frac{1}{(1+x^2+u^2)} dy dx$

$$\beta(m,n) \int_{-\infty}^{1} x^{m-1} + (1-x)^{h-3} dx$$

$$(1+x^{2}) = \frac{1+x^{4}+\sqrt{1+x^{2}}}{3} + \frac{1+x^{4}+\sqrt{1+x^{2}}}{3}$$

$$(1+x^{2}) \left[1+\sqrt{\frac{1+x^{2}}{3}}\right]^{1}$$

5. Evaluate
$$\int_{0}^{1} \int_{0}^{\sqrt{1+x^{2}}} \frac{1}{(1+x^{2}+y^{2})} dydx$$

$$\Rightarrow 0 - 1 \cdot 1 \Rightarrow 2 \cdot 29 \Rightarrow \frac{49}{3} - \frac{49}{49}$$

$$\Rightarrow \frac{2 \cdot 29}{3} - \frac{49}{9} \Rightarrow \frac{169 - 129}{129}$$

$$\Rightarrow \frac{2 \cdot 49}{3} \Rightarrow \frac{169 - 129}{129} \Rightarrow$$

NATIONAL FORENSIC SCIENCES UNIVERSITY

B.Tech-M.Tech computer Science and Engineering - Semester - II - August-2022

Subject Code: CTBTCSE SII P2

Subject Name: Engineering Mathematics 2

Time:11:00AM to 2:00PM

Date: 08/08/2022

Total Marks: 100

Instructions:

- 1. Write down each question on separate page.
- 2. Attempt all questions.
- 3. Make suitable assumptions wherever necessary.

4. Figures to the right indicate full marks.

Marks

Q.1 (a) Evaluate
$$\int_{0}^{1} \frac{x^{9}}{\sqrt{1-x^{2}}} dx$$

(b) Define Reduction formula for $\int_{0}^{\frac{\pi}{2}} \sin^{n} x dx$

(c) Evaluate $\int_{0}^{\pi} (1-\cos\theta)^{3} d\theta$

or

(c) Evaluate $\int_{0}^{5} \sqrt{x(5-x)^{3}} dx$

Q.2 (a) Define Gamma function and prove $\Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$

(b) Using Gamma function prove
$$\Gamma(n) = 2 \int_{0}^{\infty} e^{-x^{2}} x^{2n-1} dx$$

(c) Evaluate
$$\int_{0}^{\infty} \frac{x^{5} (1-x^{4})}{(1+x)^{18}} dx$$

(c) Find the length of the arc of the curve
$$x = a\cos\theta$$
 and $y = a\sin\theta$.

07

Q.3 (a) Evaluate
$$\int_{0}^{1} \int_{0}^{x} (xy^2 + 1) dy dx$$
 05

(b) Evaluate
$$\int_{0}^{2} \int_{y^{2}}^{4} (x^{2} + y^{2}) dxdy$$
 by changing the order of integration. 05

	(c) Evaluate $\iint_{R} (x^2 + y^2) dA$, R is the annular region between the two circles	07
	15 Symmetry 17 (c) 15 Symmetry 17 (d) 15 Symmetry 17 (e) 15 Symmetry	
	or the region bounded by the surface	07
	1 . 1 = 4 between the planes y	05
Q.4	(a) Solve $x\sqrt{1+y^2}dx + y\sqrt{1+x^2}dy = 0$ (b) Solve $(x^2y^2 + xy + 1)ydx + (x^2y^2 - xy + 1)xdy = 0$	05
	(b) Solve $(x^2y^2 + xy + 1)ydx + (x^2y^2 + $	07
	(c) Define Leibnitz linear equation and so dx x	
	$(2x^2 + 3y^2 - 7)xdx - (3x^2 + 2y^2 - 8)ydy = 0$	07
Q.5	Solve $(2x^{2} + 3y^{2})^{n}$ (a) Discuss the converges of $(i)\sum_{n=1}^{\infty} \left(\frac{n}{n+1}\right)^{2} (ii)\sum_{n=1}^{\infty} \frac{6^{n} + 7^{n}}{8^{n}}$	05
Q.S	Discuss the converges of n=1 (1+1)	05
	(b) Discuss the converges of $\sum (\sqrt[3]{n^3 + 1} - n)$ (c) Find the radius of the converges and interval of converges of the series	06
	(c) Find the radius of the converges and the	
	$\sum_{n=0}^{\infty} \frac{\left(-1\right)^{n} \left(x+2\right)^{n}}{n}$	
	$\sum_{n=0}^{2} n$	05
0.6	(a) Test the converges of the series $\frac{1}{1!} + \frac{3}{2!} + \frac{5}{3!} + \frac{7}{4!} + \dots$	05
Q.0	(b)	03
	(c) Find the area of surface generated by revolving curve $y = 2\sqrt{x}$, $1 \le x \le 2$, about $x - axis$.	06