

Enrolment No. _____

NATIONAL FORENSIC SCIENCES UNIVERSITY, DELHI CAMPUS
B. Tech – M. Tech Computer Science & Engineering (Cyber Security) - Semester V
September 2023, Term Assessment-1

Subject Code: CTBTCSE SV P4
Subject Name: Theory of Computation

Date: 19/09/2023 (Afternoon)
Time: 11:30 am – 12:15 pm
Total Marks: 25

Instructions: All the questions are compulsory

Section A (5 * 2 Mark)

1. Define a DFA.
2. The number of states required to accept the language $L = \{w : |w| \bmod 3 = 0\}$; where $\Sigma = \{a, b\}$ is ____.
3. ____ number of states required to design the DFA for Question number 2 in Section B.
4. The number of states required in the minimal dfa $L = \{w | w \in \{0, 1\}^*, \text{the number of 0's is divisible by 2 and number of 1's is divisible by 5, respectively is } ______.$
5. The number of possible substring of length 5 over $\Sigma = \{a, b, 0, 1, 2\}$ is ____.

Section B (3 * 5 Mark)

1. Construct a NFA that recognizes the set of all strings on $\Sigma = \{a, b\}$ starting with the prefix ab. Also, give its state transition table.
2. Design a dfa for the languages $L = \{ba^n : n \geq 1, n \neq 5\}$.
3. Construct a minimal that accepts the language L, represented by the $\Sigma^*0011\Sigma^*$, where $\Sigma = \{a, b\}$.

~~~~~ End ~~~~~

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Enrolment No. \_\_\_\_\_

NATIONAL FORENSIC SCIENCES UNIVERSITY, DELHI CAMPUS

B. Tech - M. Tech CSE (CS) – Semester V, October-November 2023

Mid Semester Examination

Subject Code: CTBTCSE SV P4

Subject Name: Theory of Computation

Date: 02/11/2023

Time: 1 Hr 30 Min

Total Marks: 50

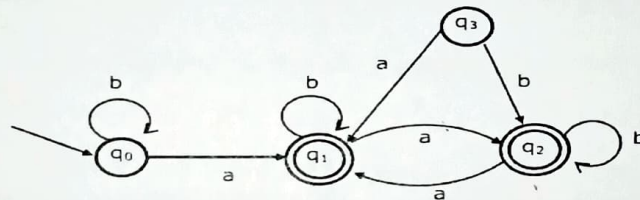
All the questions are compulsory.

### Section A (5\* 3 Mark)

1. Let  $N$  be an NFA with  $n$  states & let  $k$  be the number of states of a minimal DFA which is equivalent to  $N$ . The relations between  $n$  &  $k$  is \_\_\_\_.
2. Give an example finite set and infinite set-in set builder form.
3. Consider the regular expression  $(0+1)^N$  times. The minimum state finite automaton that recognizes the language represented by this regular expression contains \_\_\_\_ states.
4. Check whether  $L = \{a^n b^l \mid n \leq l\}$  is regular or not.
5. The number of reflexive relations on an  $n$ -element set is \_\_\_\_.

### Section B

1. Consider the following Finite State Automaton:

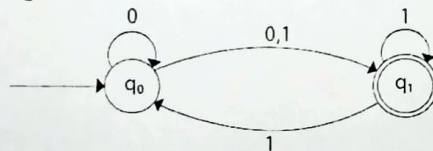


Derive the regular expression using Arden's Theorem.

(5 Mark)

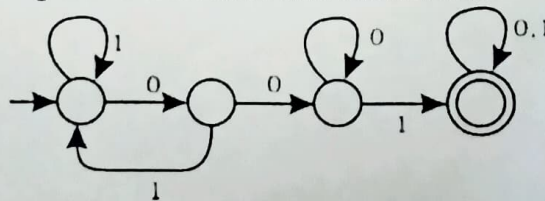
2. Convert the given NFA to DFA.

(5 Mark)



3. State Pumping Lemma theorem with example.
4. Consider the following deterministic finite state automaton  $M$ .

(5 Mark)



Let  $S$  denote the set of seven bit binary strings in which the first, the fourth, and the last bits are 1. The number of strings in  $S$  that are accepted by  $M$  is \_\_\_\_.

(5 Mark)

5. The minimum possible number of states of a deterministic finite automaton that accepts the regular language  $L = \{w_1 a w_2 \mid w_1, w_2 \in \{a, b\}^*, |w_1| = 2, |w_2| \geq 3\}$ .

(5 Mark)

6. Discuss with example Moore & Mealy machine.

(10 Mark)

~~~~~ End ~~~~~

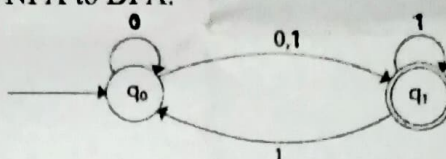

Seat No.: _____

Enrolment No. _____

NATIONAL FORENSIC SCIENCES UNIVERSITY**B. Tech. - M. Tech. CSE (CS) - Semester – V - Jan-2024****Subject Code: CTBTCSE SV P4****Date: 04/01/2024****Subject Name: Theory of Computation****Time: 11:00 AM to 2:00 PM****Total Marks: 100****Instructions:**

1. Write down each question on a separate page.
2. Attempt all questions.
3. Make suitable assumptions wherever necessary.
4. Figures to the right indicate full marks.

| | | |
|------------------------|--|-----------|
| Q.1 (A) | Find the number of transitive relations for a set of n-element. | 04 |
| Attempt Any two | | |
| Q.1 (B) | <p>I. Construct the truth table for the following statements.
 (i) $\neg p \wedge \neg q$ (ii) $(\neg p \rightarrow r) \wedge (p \leftrightarrow q)$</p> <p>II. Prove that the sum of cubes of n natural numbers is equal to $([n(n+1)]/2)^2$ for all n natural numbers. (Hint: use mathematical induction)</p> <p>III. Define the term alphabet, string, and language. Also, give their relationship.</p> | 16 |
| Q.2 (A) | Construct a minimal DFA that accepts a language L over input alphabets $\Sigma = \{a, b\}$ such that L is the set of all strings starting with 'aa' or 'bb'. | 04 |
| Attempt Any two | | |
| Q.2 (B) | <p>I. Derive the regular expression for the DFA given below:</p> <pre> graph LR q0((q0)) -- a --> q1(((q1))) q1 -- b --> q0 q1 -- a --> q2(((q2))) q2 -- b --> q1 q2 -- a --> q3((q3)) q3 -- b --> q2 q3 -- a --> q1 </pre> <p>II. State with example Pumping Lemma for regular language.</p> <p>III. Construct a minimal DFA that accepts the language L over the alphabet $\Sigma = \{0, 1\}$.
 $L = \{w \in \{0, 1\}^* \mid w \text{ does not contain three or more consecutive } 1's\}$</p> | 16 |
| Q.3 (A) | Check the grammar is ambiguous or not. (Hint: use the string "abbaba")
$G = \{S \rightarrow SS, S \rightarrow ab, S \rightarrow ba, S \rightarrow \epsilon\}$ | 04 |
| Attempt Any two | | |
| Q.3 (B) | <p>I. Convert the Given context free grammar into its equivalent CNF.
 $S \rightarrow ASB$
 $A \rightarrow aAS a \epsilon$
 $B \rightarrow SbS A bb$</p> <p>II. Construct a PDA for language $L = \{0^n 1^m 2^m 3^n \mid n \geq 1, m \geq 1\}$</p> | 16 |

| | | |
|---------|---|----|
| | III. Distinguish between DPDA and NPDA with example. | |
| Q.4 (A) | Define Turing machine with a suitable example. | 04 |
| | Attempt Any two | |
| Q.4 (B) | I. Design a Turing machine for the language $a^n b^n c^n \mid n \geq 1$
II. Discuss with example the ambiguity property in CFG.
III. Design a Turing machine to find 1's complement of a binary number. | 16 |
| Q.5 (A) | Check whether $L = \{a^n b^m \mid n = m\}$ is CFL or not using Pumping lemma. | 04 |
| | Attempt Any two | |
| Q.5 (B) | I. Differentiate with example deterministic and non-deterministic Turing machine with example.
II. Convert the given NFA to DFA. | 16 |
| |  <pre> graph LR start(()) --> q0((q0)) q0 -- 0 --> q0 q0 -- "0,1" --> q1(((q1))) q1 -- 1 --> q0 </pre> | |
| | III. Discuss with example Moore & Mealy machine. | |

~~~~~ End ~~~~~