

# CES-27 Processamento Distribuído

Termination Detection

Prof Juliana Bezerra  
Prof Celso Hirata  
Prof Vitor Curtis

# Outline

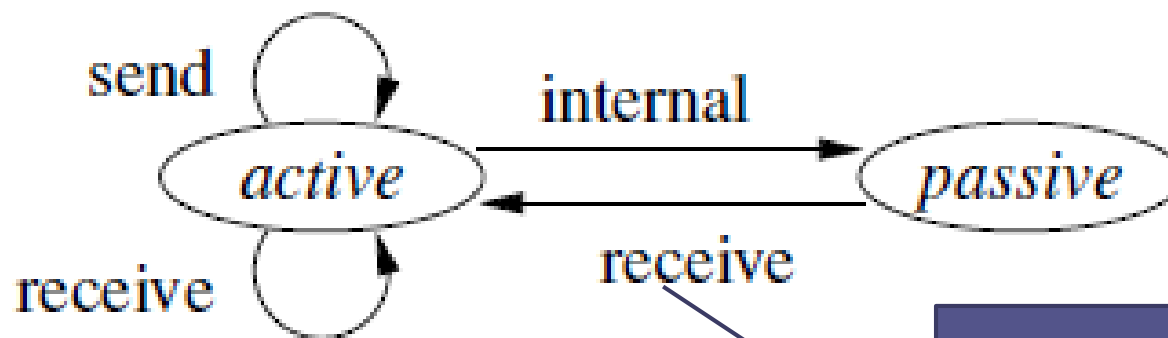
- Motivation
- Dijkstra's Token Algorithm
- Dijkstra-Scholten Algorithm
- Shavit-Francez Algorithm
- Rana's Algorithm

# Motivation

- **Termination detection for diffusing computation**
  - “The activity of a finite computation may propagate over a network of machines, when machines may delegate (repeatedly) subtasks to their neighbors; when such a computation is fired from a single machine, we call it a diffusing computation” (Dijkstra & Scholten, 1979)
- A distributed algorithm is **terminated** if all **processes are in a terminal state and no messages (**basic**) are in transit**
  - The **basic algorithm** is the algorithm for which termination is being detected
  - The **control algorithm** is the termination detection algorithm employed
- The **control algorithm** in general consists of two parts:
  - Termination detection  $\Rightarrow$  our focus
  - Announcement  $\Rightarrow$  simple
    - The process, which detects termination, can act as a master
    - Send a terminate message to everyone
    - Collect the results and print them
    - Send a shutdown message to everyone
    - Stop

# Motivation

- **Termination detection** is a fundamental and challenging problem in distributed computing, because **no process has complete knowledge of the global configuration** of the network
  - A **terminated process** may be **reactivated** by a message from another process
  - Ideally, termination detection does not require freezing the basic execution
  - Process model:



Only messages of **basic** algorithm make the process *active* again

# Concept: Wave Algorithms

The way the wave flows is up to you!  
It depends on the chosen topology.  
E.g. Directed ring  
E.g. Undirected ring

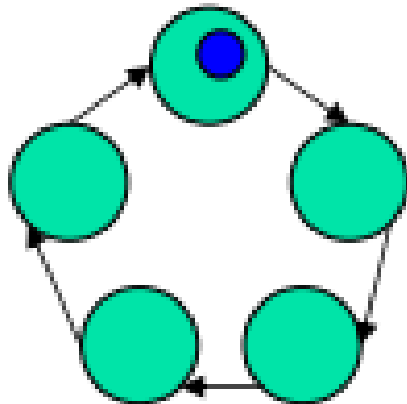
- In **wave algorithms**, each computation gives rise to one or more **decisions** in which **all processes have a say**
  - **They can not complete** if any process  **$p$**  **refuses** to take part in its execution
    - In this case,  $p$  refused because  $p$  did something (after the wave algorithm started) that not characterizes the decision
- A wave is **initiated by one process**, and in the end one *decide event* happens at the initiator
  - There can be concurrent calls of a **wave** algorithm, **initiated by different processes**
    - Then usually for each **wave** the messages are **marked with the ID of its initiator**
  - If a wave does not complete, then typically another wave will complete successfully later on

# Outline

- Motivation
- Dijkstra's Token Algorithm
- Dijkstra-Scholten Algorithm
- Shavit-Francez Algorithm
- Rana's Algorithm

# Dijkstra's Token Algorithm

- An initial idea:
  - Imagine the processes to be arranged in a ring
  - Process 1 inserts a token, traveling from process  $i$  to process  $i + 1$  and back to process 1
  - The token only leaves a process if the process turns inactive
  - Process 1 determines whether the system can be shut down
- That does not work...
  - A process may become active after having sent the token
  - To fix this: Dijkstra's Token Algorithm!



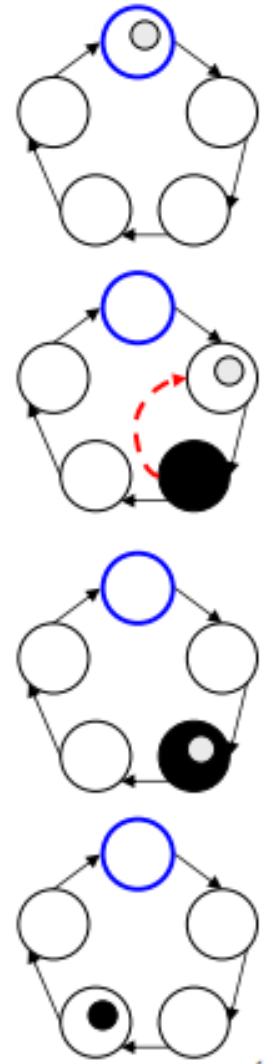
Remember:

- The ring is used only by the control algorithm (i.e. termination detection)
- In the basic algorithm, processes can communicate with each other (without the ring)

# Dijkstra's Token Algorithm

- Algorithm:
  - 1) When  $P_1$  turns inactive, it turns white and sends a white token to  $P_2$
  - 2) If  $P_i$  sends a message to  $P_j$  and  $j < i$ , then  $P_i$  turns black
    - $P_i$  is a suspect for reactivating process  $P_j$
  - 3) If  $P_i$  has the token and it is idle, it passes the token. The token becomes black if  $P_i$  is black
  - 4) After passing tokens, processes become white
    - Indicating that the process is inactive
  - 5) The algorithm terminates when  $P_1$  receives a white token and it is idle

Basic message!





# Dijkstra's Token Algorithm

- Performance:  $O(N)$  in time
  - $N$  is the number of processes
- $P_1$  may become active again before getting back the token
  - Is it possible to detect termination wrongly? No!
- For a small number of processes, algorithm is acceptable.
- For large numbers of processes, this becomes a significant overhead
- **Messages must be delivered in order for the protocol to work!**
- There are similar approaches for this algorithm:
  - J. Misra, “**Detecting Termination of Distributed Computations Using Markers**”, 2nd ACM Symposium on PODC, Aug. 1983.

# Outline

- Motivation
- Dijkstra's Token Algorithm
- Dijkstra-Scholten Algorithm
- Shavit-Francez Algorithm
- Rana's Algorithm

# Dijkstra-Scholten Algorithm

- Reference: E. W. Dijkstra and C. S. Scholten  
**"Termination Detection for Diffusing Computations"**, Information Processing Letters, Vol. 11, No. 1, Aug. **1980**.
- Termination detection algorithm for a **centralized basic algorithm** on an **undirected network**.



One process initiated  
the basic algorithm

We will track messages  
of the basic algorithm

A process can  
send/receive messages  
to/of any other  
process

# Dijkstra-Scholten Algorithm

An use of spanning tree,  
where processes are  
nodes of tree and edges  
are connections

- The main idea:
  - To build a tree, rooted in the initiator of the basic algorithm
  - The tree contains:
    - all active processes, and
    - passive processes that have active descendants in the tree
  - If a basic message from a process  $p$  makes a process  $q$  active, then  $q$  becomes a child of  $p$  in the tree
  - A process can quit the tree only if it is passive and has no children left in the tree
    - In that case, it informs its parent that it is no longer a child
  - Termination is detected by the initiator when the tree has disappeared

There are other algorithms that use the concept of spanning tree!

# Dijkstra-Scholten Algorithm

You decide how to implement the tree!

- Algorithm:
  - Initially the tree  $T$  consists only of the initiator
  - When  $p$  sends a basic message,  $cc_p = cc_p + 1$ .
    - To count my children
  - Let this message be received by  $q$ :
    - If  $q$  isn't yet in  $T$ , it joins  $T$  with parent  $p$  and  $cc_q = 0$
    - If  $q$  is already in  $T$ , it sends a control message to  $p$  that it isn't a new child of  $p$ . Upon receipt of this message,  $cc_p = cc_p - 1$
  - When a **non-initiator**  $p$  is **passive** and  $cc_p = 0$ , it quits  $T$  and informs its parent that it is no longer a child
    - Note:  $p$  informs its parent using a control message. So its parent decreases  $cc$
  - When the **initiator** is passive and  $cc_{\text{initiator}} = 0$ , termination is detected

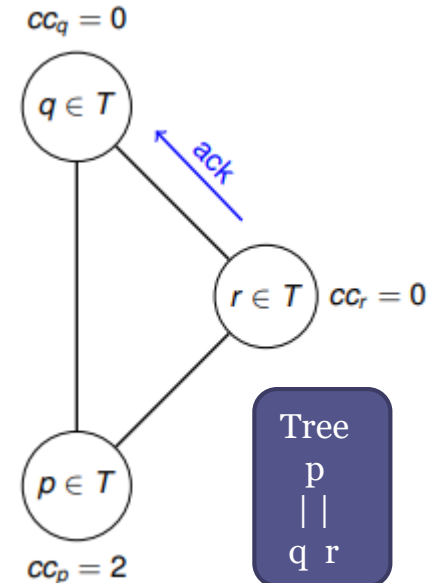
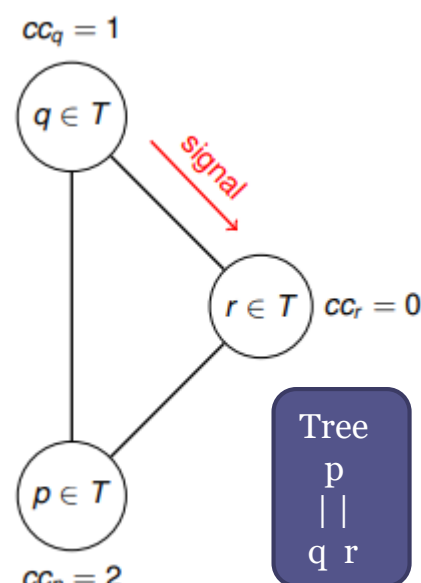
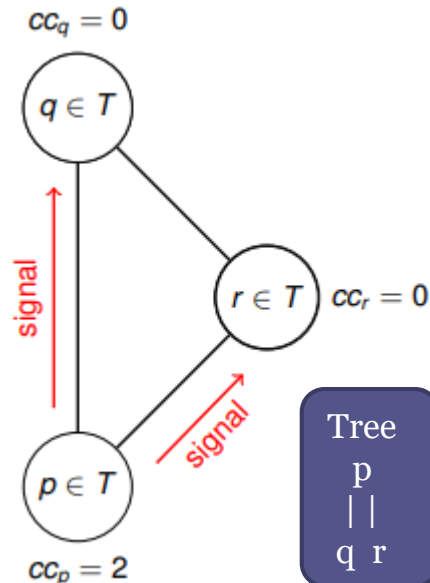
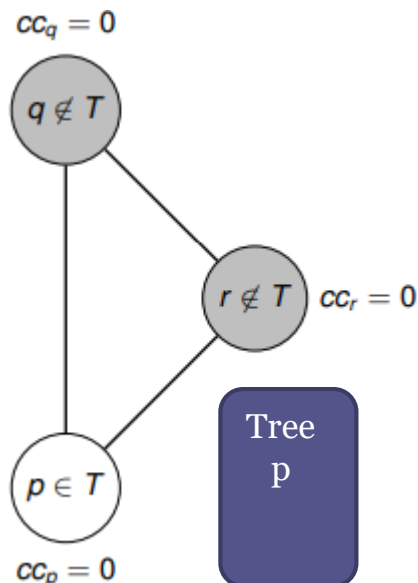
Drawback: Requires one control message for every basic message  
Note: In the next examples, control message is the *ack* (acknowledgement)

# Dijkstra-Scholten Algorithm

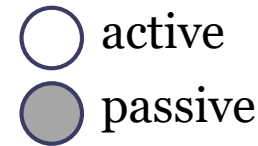
○ active  
● passive

- Example:

- Three processes  $p$ ,  $q$ , and  $r$
- Chosen topology: undirected ring
- At the start, the initiator  $p$  sends basic messages to  $q$  and  $r$ , and sets  $cc_p$  to 2
  - Upon receipt of these messages,  $q$  and  $r$  both become active, and join  $T$  with parent  $p$
- $q$  sends a basic message to  $r$ , and sets  $cc_q$  to 1.
- Upon receipt of this message,  $r$  sends back an acknowledgment, which causes  $q$  to decrease  $cc_q$  to 0

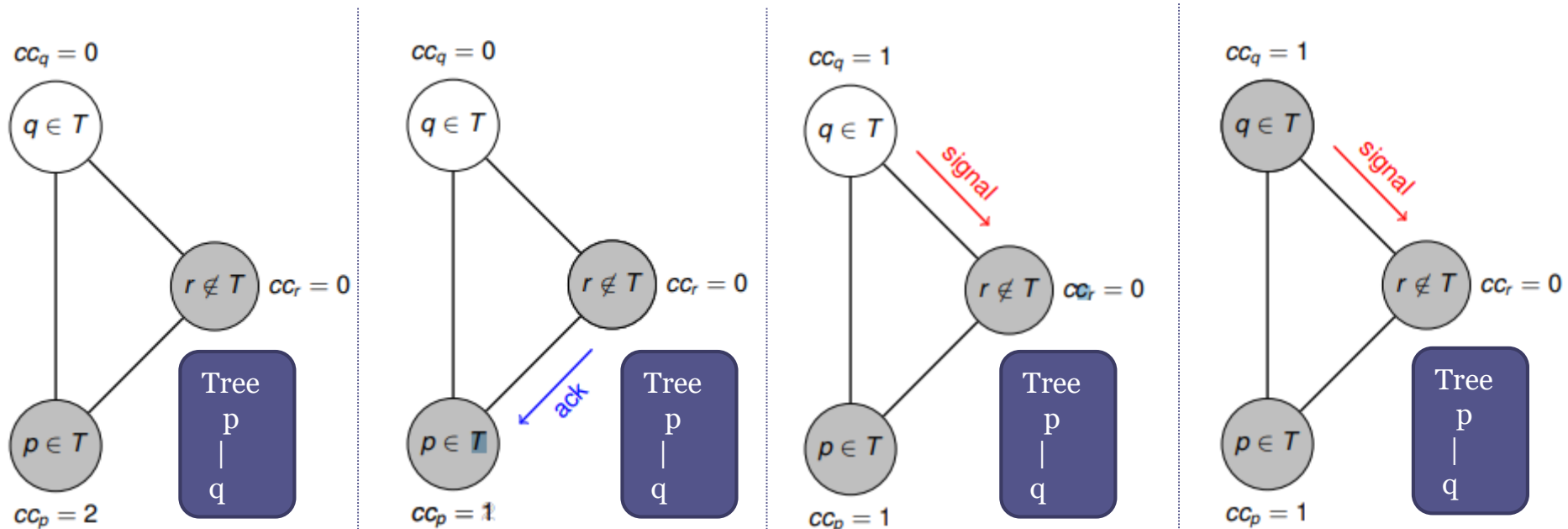


# Dijkstra-Scholten Algorithm



- Example (cont):

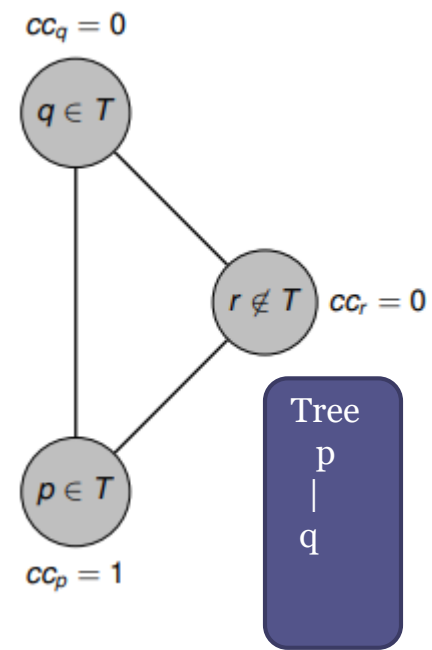
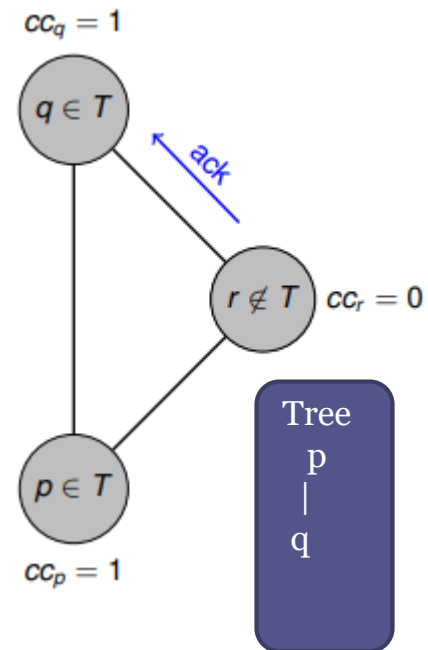
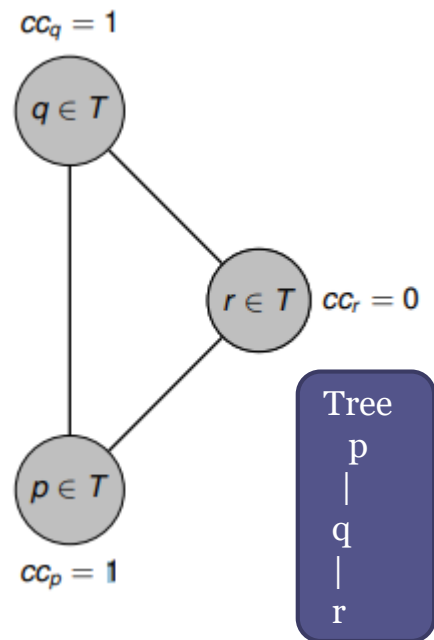
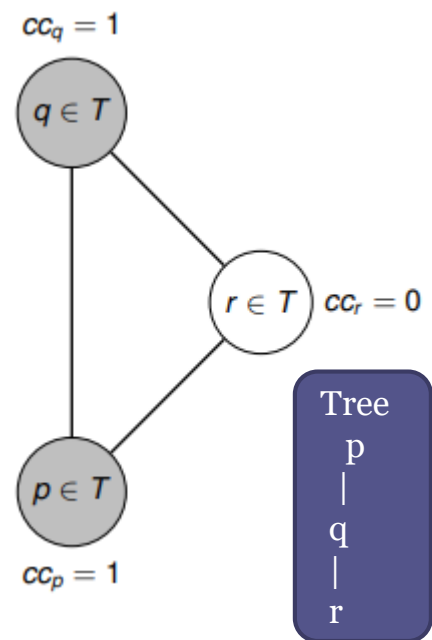
- $p$  becomes passive. (Since  $cc_p = 2$ , it remains in  $T$ )
- $r$  becomes passive. Since  $cc_r = 0$ , it sends an acknowledgment to its parent  $p$ , which causes  $p$  to decrease  $cc_p$  to 1
- $q$  sends a basic message to  $r$ , and sets  $cc_q$  to 1
- $q$  becomes passive (Since  $cc_q = 1$ , it remains in  $T$ )
- Note that all three processes are now passive, but there is still a message traveling from  $q$  to  $r$



# Dijkstra-Scholten Algorithm

○ active  
● passive

- Example (cont):
  - Upon receipt of message from  $q$  to  $r$ ,  $r$  becomes active again, and joins  $T$  with parent  $q$
  - $r$  becomes passive. Since  $cc_r = 0$ , it sends an acknowledgment to its parent  $q$  which causes  $q$  to decrease  $cc_q$  to 0



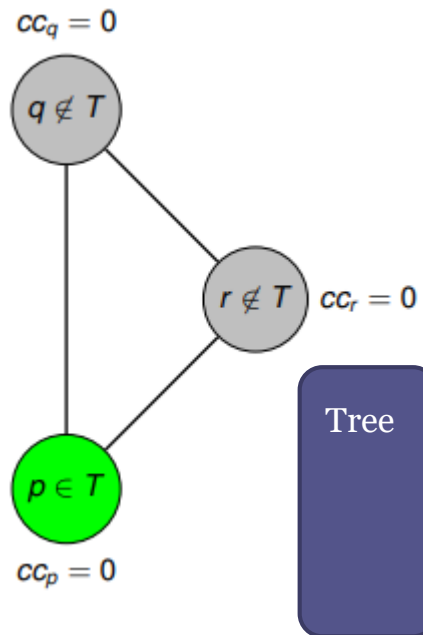
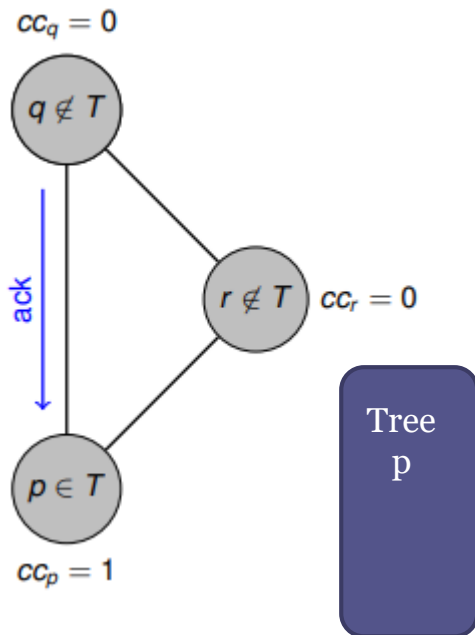


# Dijkstra-Scholten Algorithm

○ active  
● passive

- Example (cont):

- Since  $q$  is passive and  $cc_q = 0$ , it sends an acknowledgment to its parent  $p$ , which causes  $p$  to decrease  $cc_p$  to 0
- Since  $p$  is passive and  $cc_p = 0$ , it detects termination



# Outline

- Motivation
- Dijkstra's Token Algorithm
- Dijkstra-Scholten Algorithm
- Shavit-Francez Algorithm
- Rana's Algorithm

# Shavit-Francez Algorithm

- It generalizes Dijkstra-Scholten Algorithm to **decentralized** basic computations (**multiple initiators**)
- The idea:
  - To maintain not one tree, but a forest of (disjoint) trees, one for each initiator
  - Initially, each initiator constitutes a tree in the forest
  - A process can only join a tree if it is not yet in a tree in the forest
  - For the rest, the algorithm proceeds exactly as the Dijkstra-Scholten algorithm

# Shavit-Francez Algorithm

- The difference:
  - When an initiator detects that its tree has disappeared, it cannot immediately detect termination
    - There can be other trees (with active processes)
  - Instead, this initiator starts a wave, tagged with its ID
    - Only processes, which are not in a tree, participate
    - If such a wave does not complete
      - Another initiator of which the tree has not yet disappeared will start a subsequent wave
      - And the last tree to disappear is guaranteed to start a wave that will complete

# Outline

- Motivation
- Dijkstra's Token Algorithm
- Dijkstra-Scholten Algorithm
- Shavit-Francez Algorithm
- Rana's Algorithm

# Rana's Algorithm

- Termination detection algorithm for a **decentralized basic algorithm** on an **undirected network**



Any process can initiate the termination detection

A process can send/receive messages to/of any other process

- It is an example of a **wave algorithm**

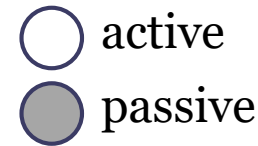
# Rana's Algorithm

- The idea:
  - Each basic message is **acknowledged**
  - Lamport's logical clock provides (basic and control) events with a **timestamp**
    - The timestamp of a process is the **highest timestamp** of its events so far (initially it is 0)
  - Let process  $p$  at time  $t$  become quiet, i.e. (1)  $p$  is passive, and (2) all basic messages it sent have been acknowledged
    - Then  $p$  starts a wave (of control messages), tagged with  $t$  (and  $p$ )
    - Only processes that have been quiet in a **time**  $\leq t$  take part in the wave
    - If the wave completes, termination is detected

So basic messages do not contribute to logical clocks  
To avoid a full-blown logical clock!

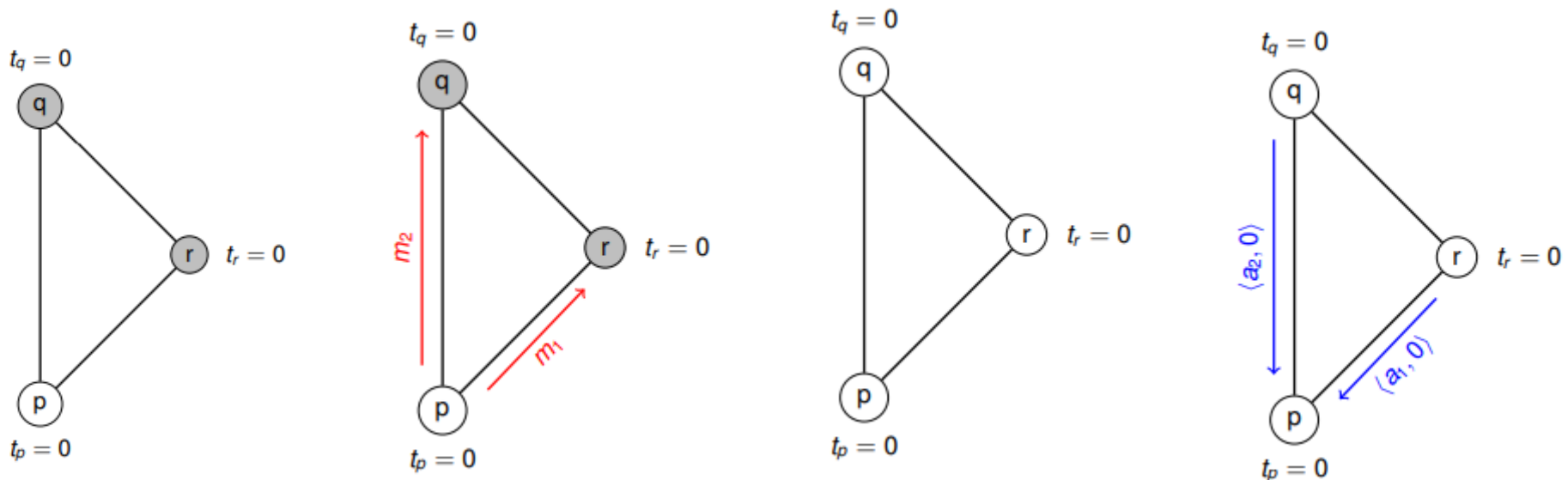
- It suffices that only the control messages (acknowledgments and wave messages) are taken into account in logical clocks
  - A wave tagged with timestamp  $t$  puts the clock of each recipient to  $t$  (if its value is not  $\geq t$  already)
  - Each acknowledgment is tagged with the timestamp  $t$  of the sender and puts the clock of the receiver to  $t + 1$  (if its value is not  $\geq t + 1$  already)

# Rana's Algorithm



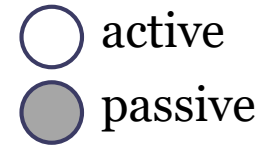
- Example

- Consider three processes  $p$ ,  $q$ , and  $r$
- Chosen topology: undirected ring
- Initially, all processes have logical time 0, and only  $p$  is active
- $p$  sends basic messages  $m_1$  to  $r$  and  $m_2$  to  $q$ , which make  $q$  and  $r$  active.
- Next,  $q$  and  $r$  send an acknowledgment  $\langle a_2, 0 \rangle$  and  $\langle a_1, 0 \rangle$  respectively

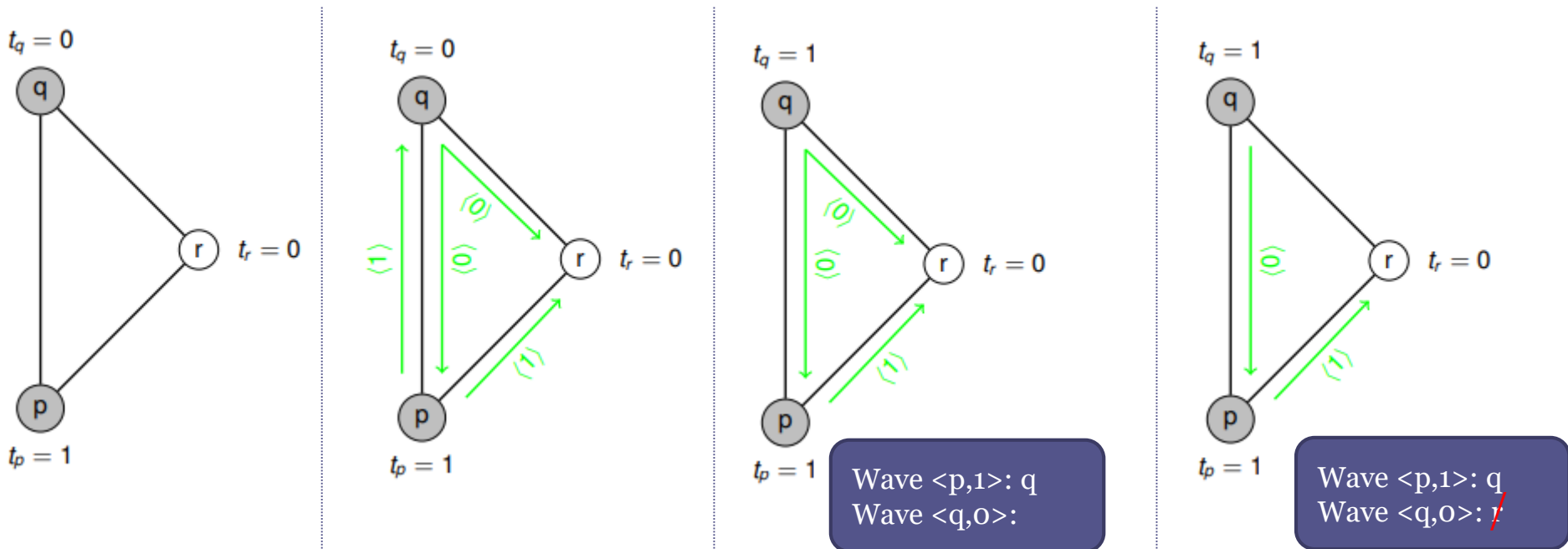




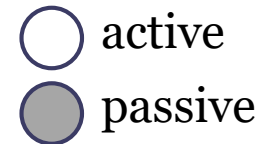
# Rana's Algorithm



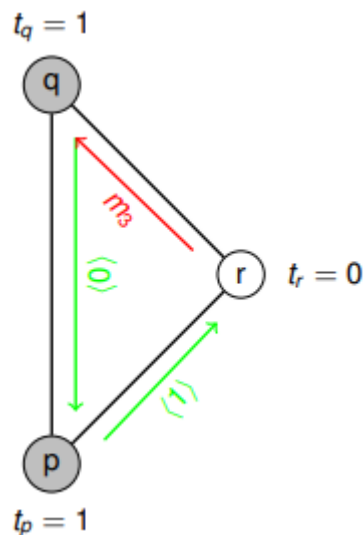
- Example (cont)
  - $p$  receives both acknowledgments, setting its time to 1
  - $p$  and  $q$  become passive.
    - Next,  $p$  and  $q$  both start a wave, tagged with 1 and 0, respectively
  - The wave of  $p$  first visits  $q$ , setting its time to 1
    - $q$  takes part in the wave, because it is quiet from time 0 onward
  - The wave of  $q$  first visits  $r$ 
    - $r$  refuses to take part in the wave, because it is active



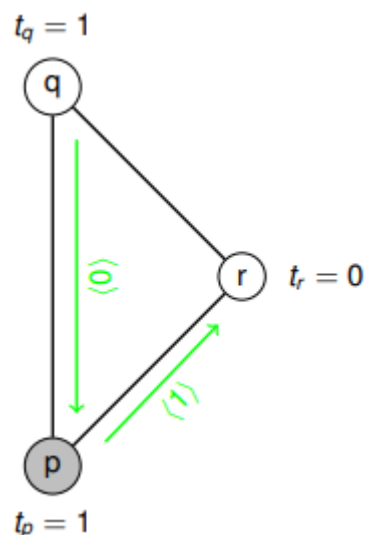
# Rana's Algorithm



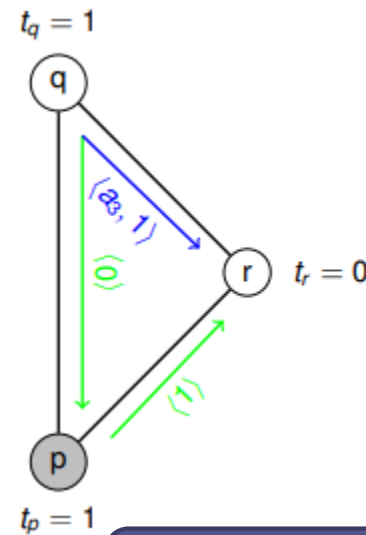
- Example (cont)
  - $r$  sends a basic message  $m_3$  to  $q$
  - Upon receipt of this message,  $q$  becomes active and sends back an acknowledgment  $\langle a_3, 1 \rangle$ .
  - When  $r$  receives this acknowledgment, its clock value becomes 2



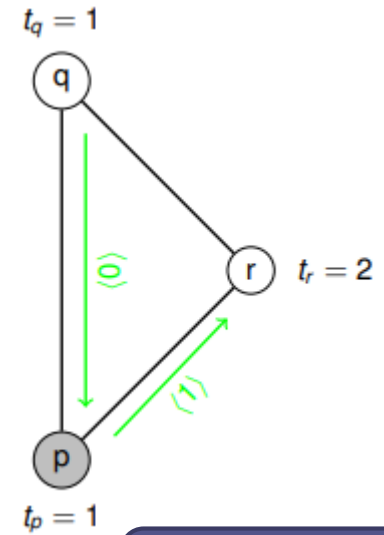
Wave  $\langle p, 1 \rangle$ :  $q$   
Wave  $\langle q, 0 \rangle$ :  $r$



Wave  $\langle p, 1 \rangle$ :  $q$   
Wave  $\langle q, 0 \rangle$ :  $r$



Wave  $\langle p, 1 \rangle$ :  $q$   
Wave  $\langle q, 0 \rangle$ :  $r$



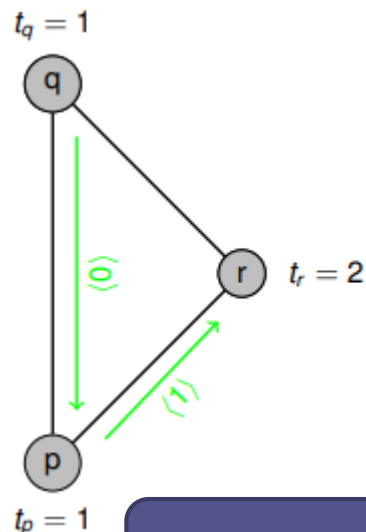
Wave  $\langle p, 1 \rangle$ :  $q$   
Wave  $\langle q, 0 \rangle$ :  $r$

# Rana's Algorithm

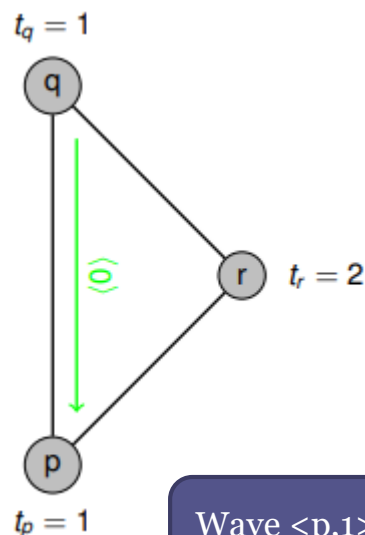
○ active  
● passive

## • Example

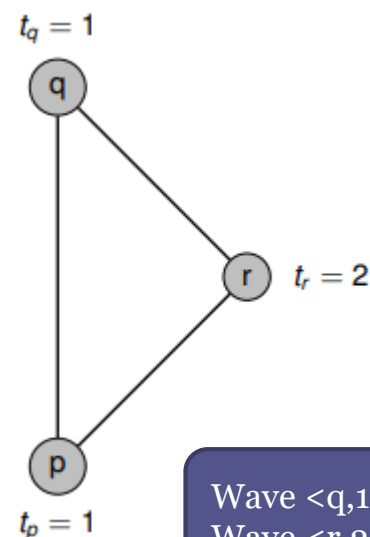
- $q$  and  $r$  become passive.
- $r$  refuses to take part in  $p$ 's wave, because  $r$  is quiet from time 2 onward, while the wave is tagged with 1
- $p$  refuses to take part in  $q$ 's wave. Similar reason!
- $q$  and  $r$  both start a wave, tagged with 1 and 2, respectively.
- The wave of  $r$  completes, and  $r$  detects termination



Wave  $\langle p, 1 \rangle$ :  $q, r$   
Wave  $\langle q, 0 \rangle$ :  $r$



Wave  $\langle p, 1 \rangle$ :  $q, r$   
Wave  $\langle q, 0 \rangle$ :  $r, p$



Wave  $\langle q, 1 \rangle$ :  $p, r$   
Wave  $\langle r, 2 \rangle$ :  $p, q$

# Other algorithms in literature

- Papers:
  - Matocha, J. and Camp, T. A taxonomy of distributed termination detection algorithms. The Journal of Systems and Software, 43, **1998**
- More recent papers
  - Hasrat, I.R. and Atif, M. Formal Specification and Analysis of Termination Detection by Weight-throwing Protocol. International Journal of Advanced Computer Science and Applications(IJACSA), Volume 9 Issue 4, **2018**.