

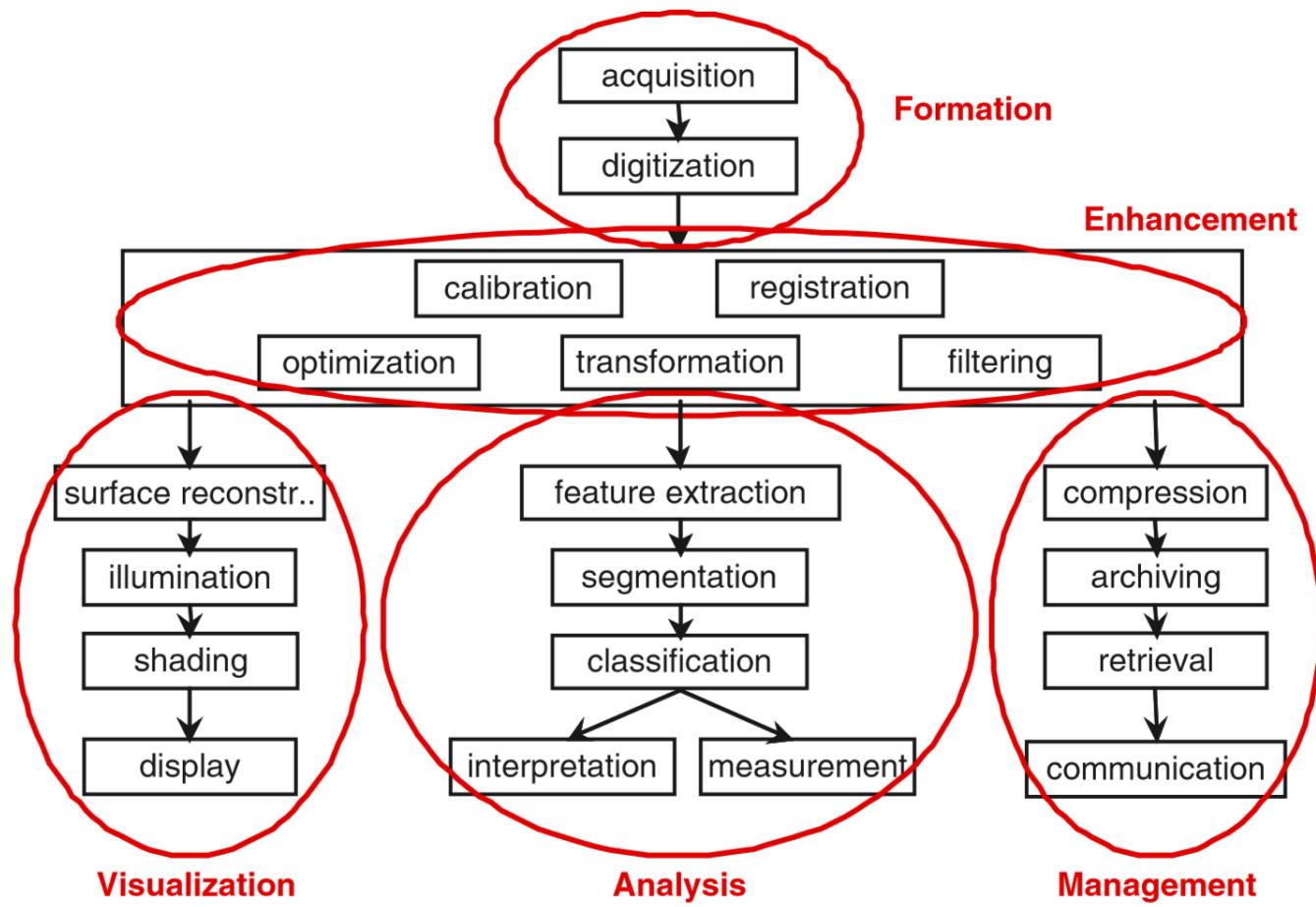
Applied Imaging Concepts: An introduction to image processing and analysis

Sara Rolfe

8/26/19



3D imaging conceptual workflow



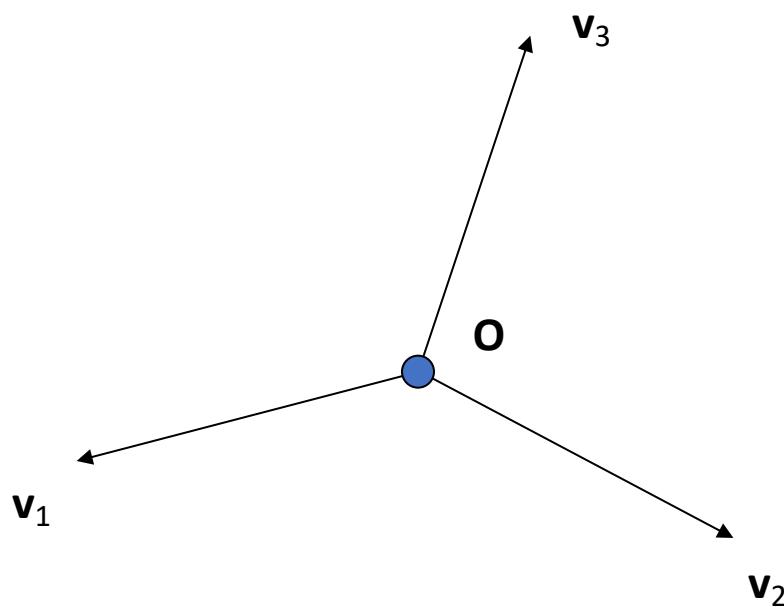
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Outline

- Image Formation
 - Coordinate systems
 - Digitization and quantization
 - Resolution
- Image Enhancement
 - Filtering and transformations
 - Registration
- Image Analysis
 - Segmentation
- Image Visualization
 - Surface reconstruction
 - Display



What is a Coordinate System?

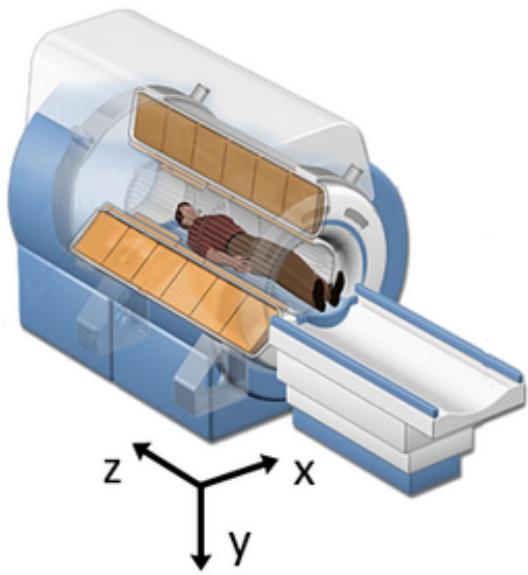


A *coordinate system* for a three-dimensional space is a point **O** called the *origin* along with three linearly independent vectors \mathbf{v}_1 , \mathbf{v}_2 , and \mathbf{v}_3 .

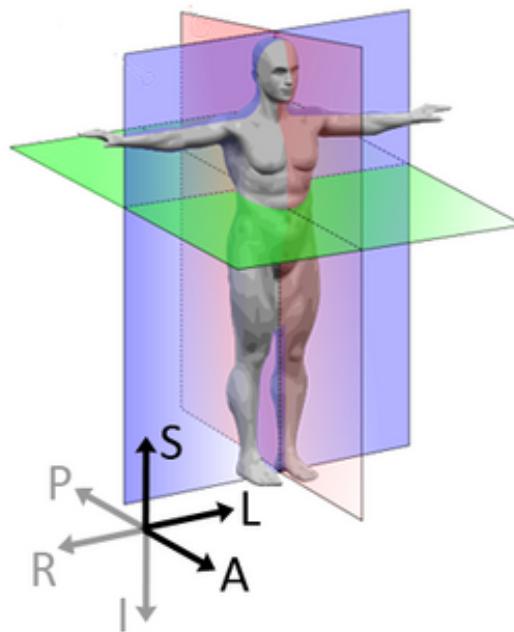
Linearly independent here means no two of the vectors are parallel and the three vectors do not all lie in the same plane.



Coordinate Systems



World Coordinate
System



Anatomical Coordinate
System

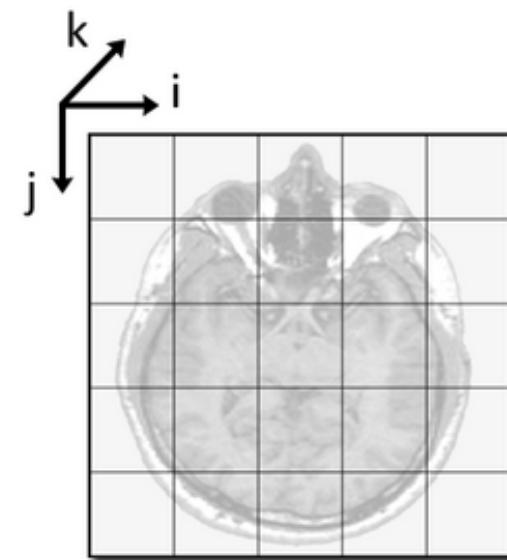


Image Coordinate
System

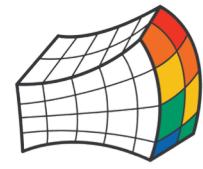
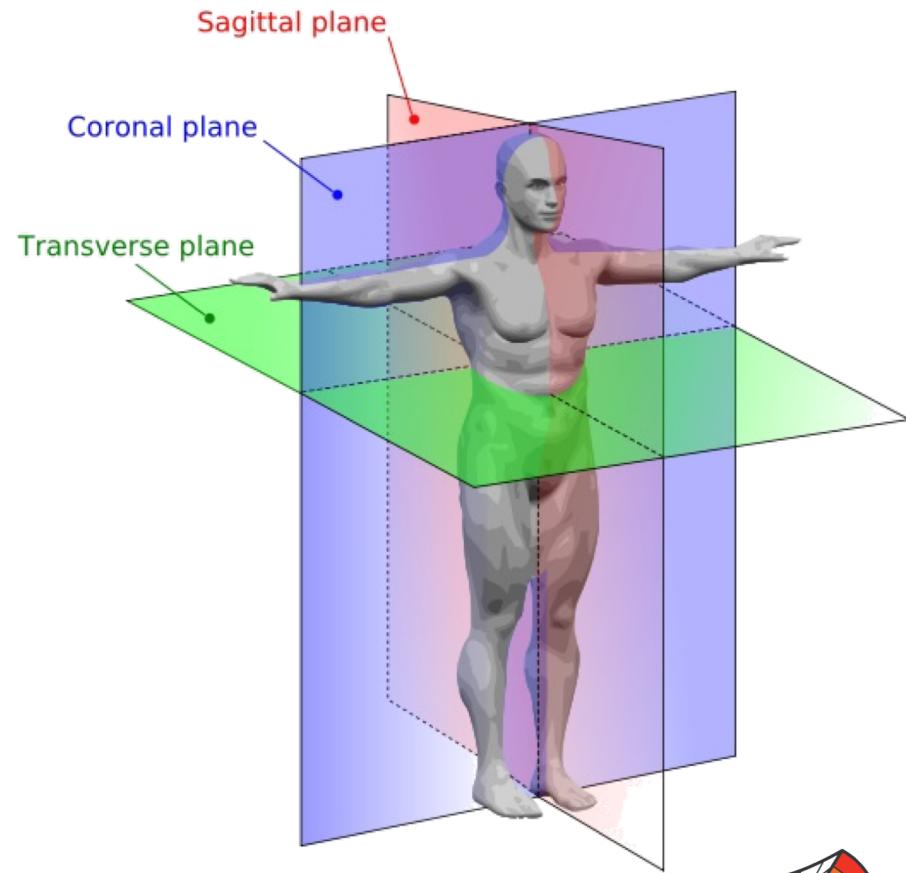


Anatomical coordinate system

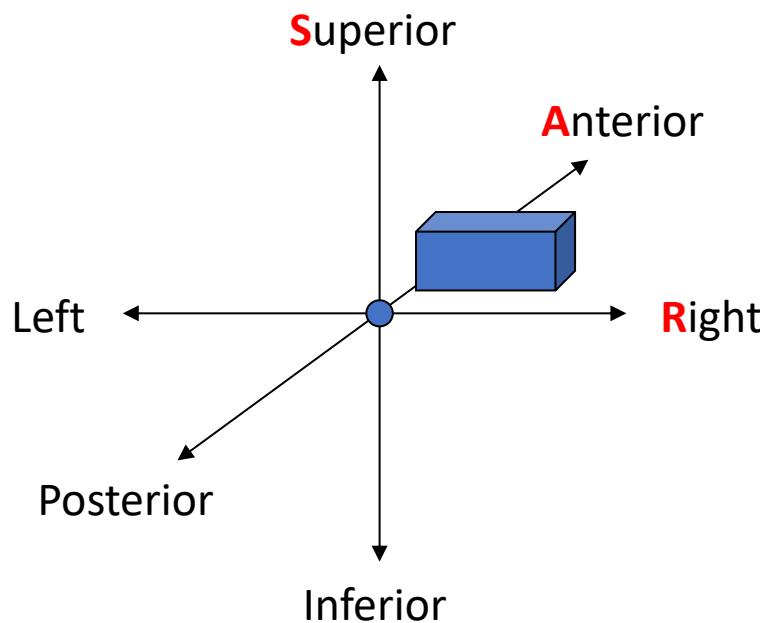
This space consists of three planes to describe the standard anatomical position of a human:

- ***axial plane*** is parallel to the ground and separates the head (Superior) from the feet (Inferior)
- ***coronal plane*** is perpendicular to the ground and separates the front from (Anterior) the back (Posterior)
- ***sagittal plane*** separates the Left from the Right

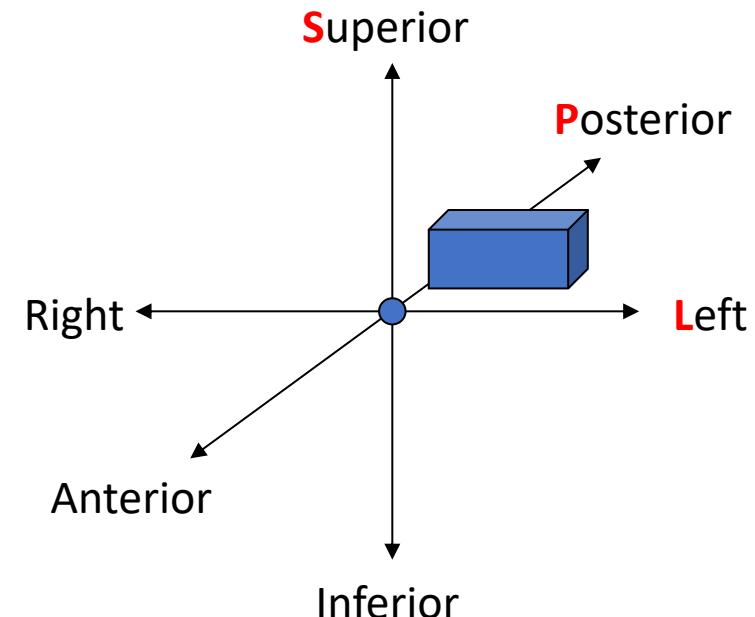
This coordinate system is fixed with respect to the scan table and the object or subject being scanned. Different medical applications use different definitions of this 3D basis



Anatomical coordinate system: RAS vs LPS



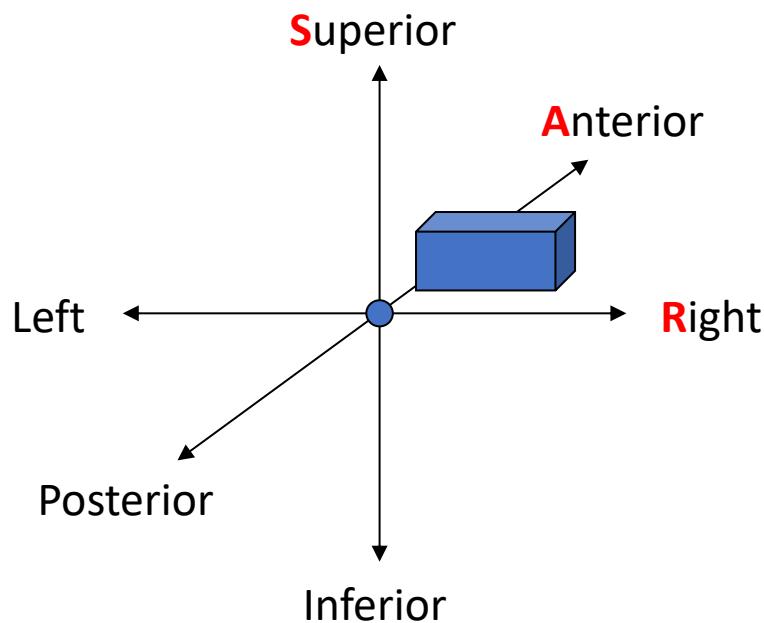
RAS (Right, Anterior, Superior): 3D Slicer



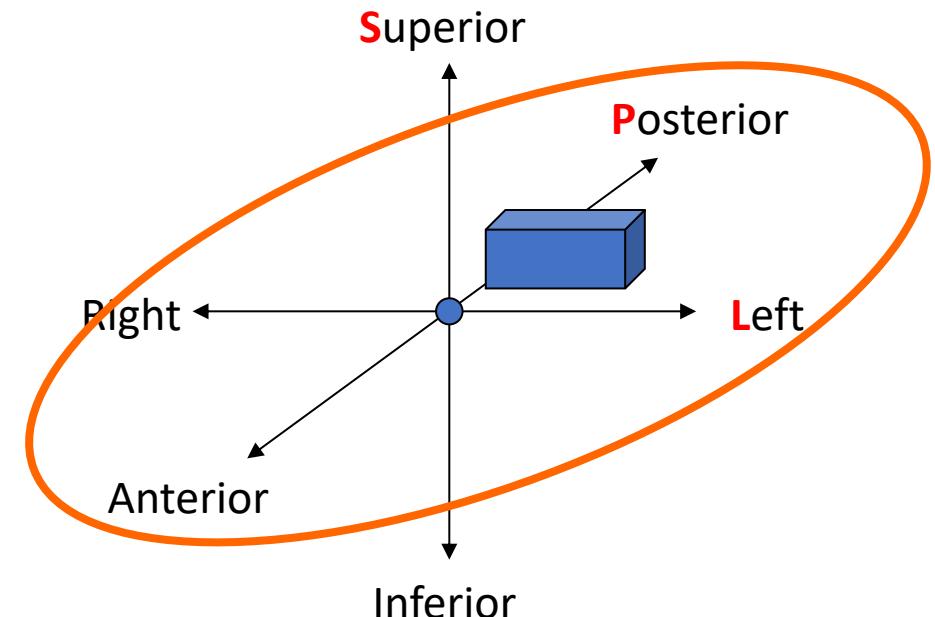
LPS (Left, Posterior, Superior): DICOM images,
ITK toolkit



Anatomical coordinate system: RAS vs LPS



RAS (Right, Anterior, Superior): 3D Slicer

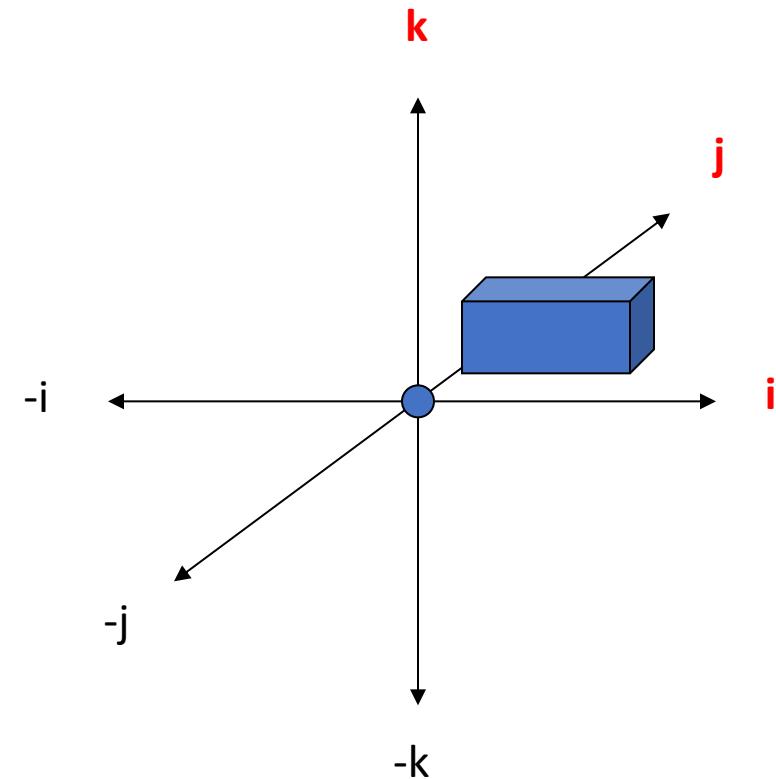


LPS (Left, Posterior, Superior): DICOM images,
ITK toolkit



The IJK Image Coordinate System

Every medical scanner has its own coordinate system called the *IJK coordinate system*. The IJK coordinate system represents the actual rectangular prism of data that is scanned, instead of the position of the scan table



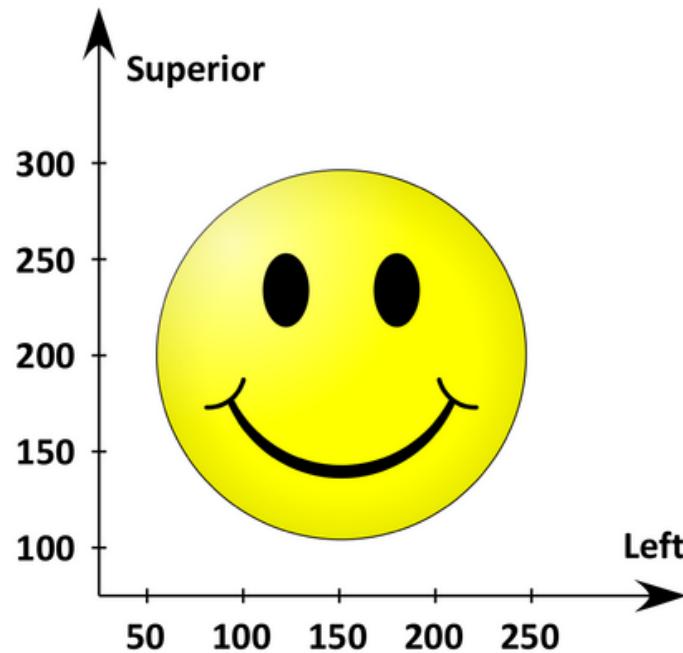
Coordinate System Conversion

We frequently need to convert between coordinate systems, such as RAS and IJK.

The mapping from one coordinate system to another is a 3D *affine transformation*: a sequence of transformations consisting of a shear, a reflection, a rotation, a scaling, and a translation.



What do all of these mean



LPS Anatomical space

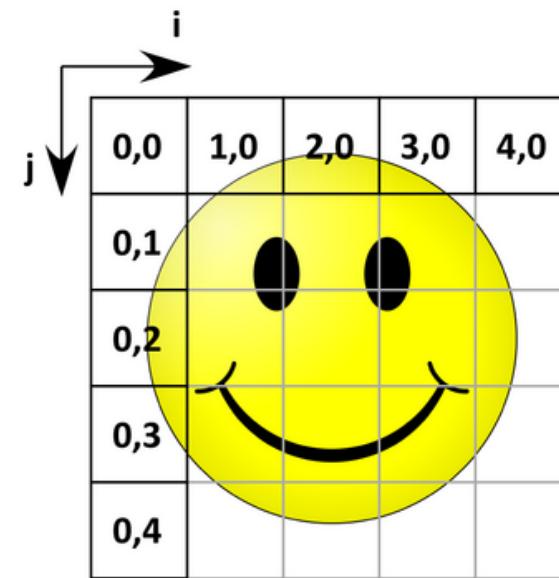
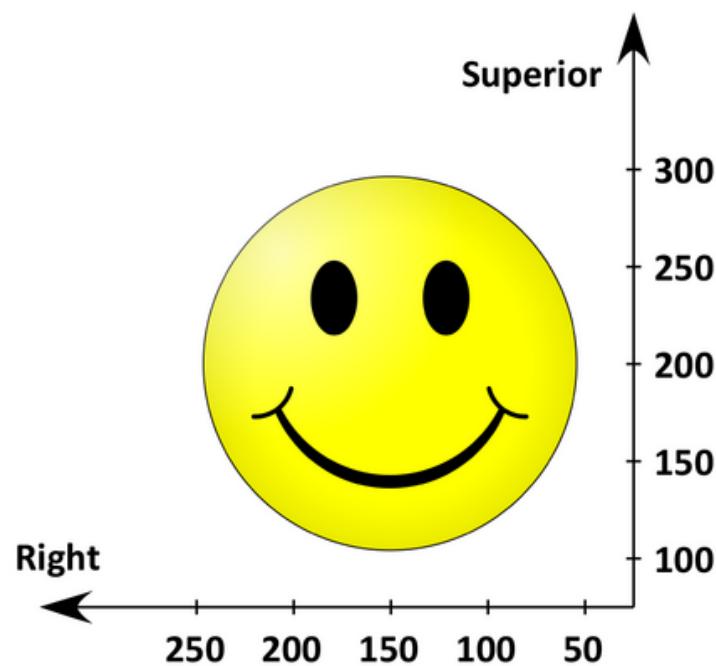


Image Coordinate System



What do all of these mean



RAS Anatomical space

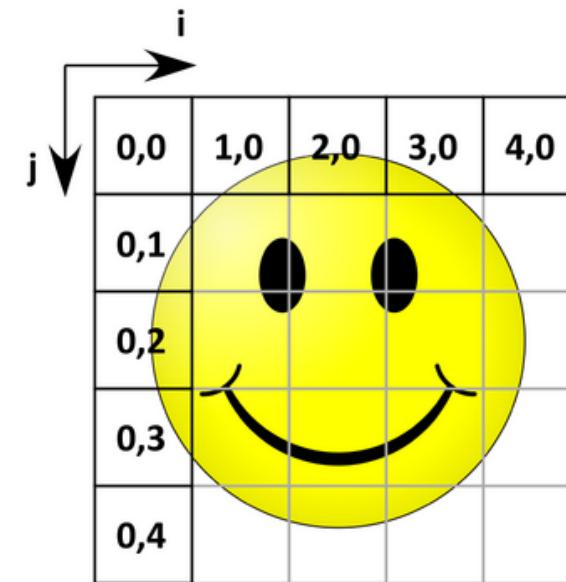
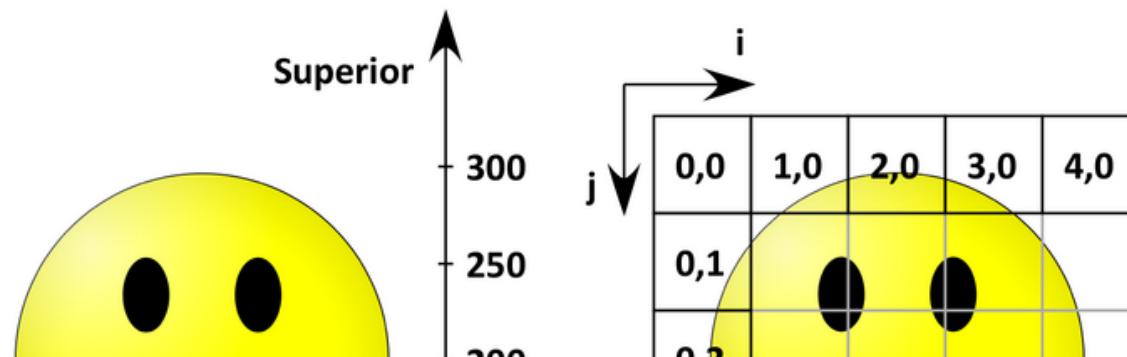


Image Coordinate System



What do all of these mean



KNOW YOUR DATA AND SOFTWARE

RAS Anatomical space

Image Coordinate System

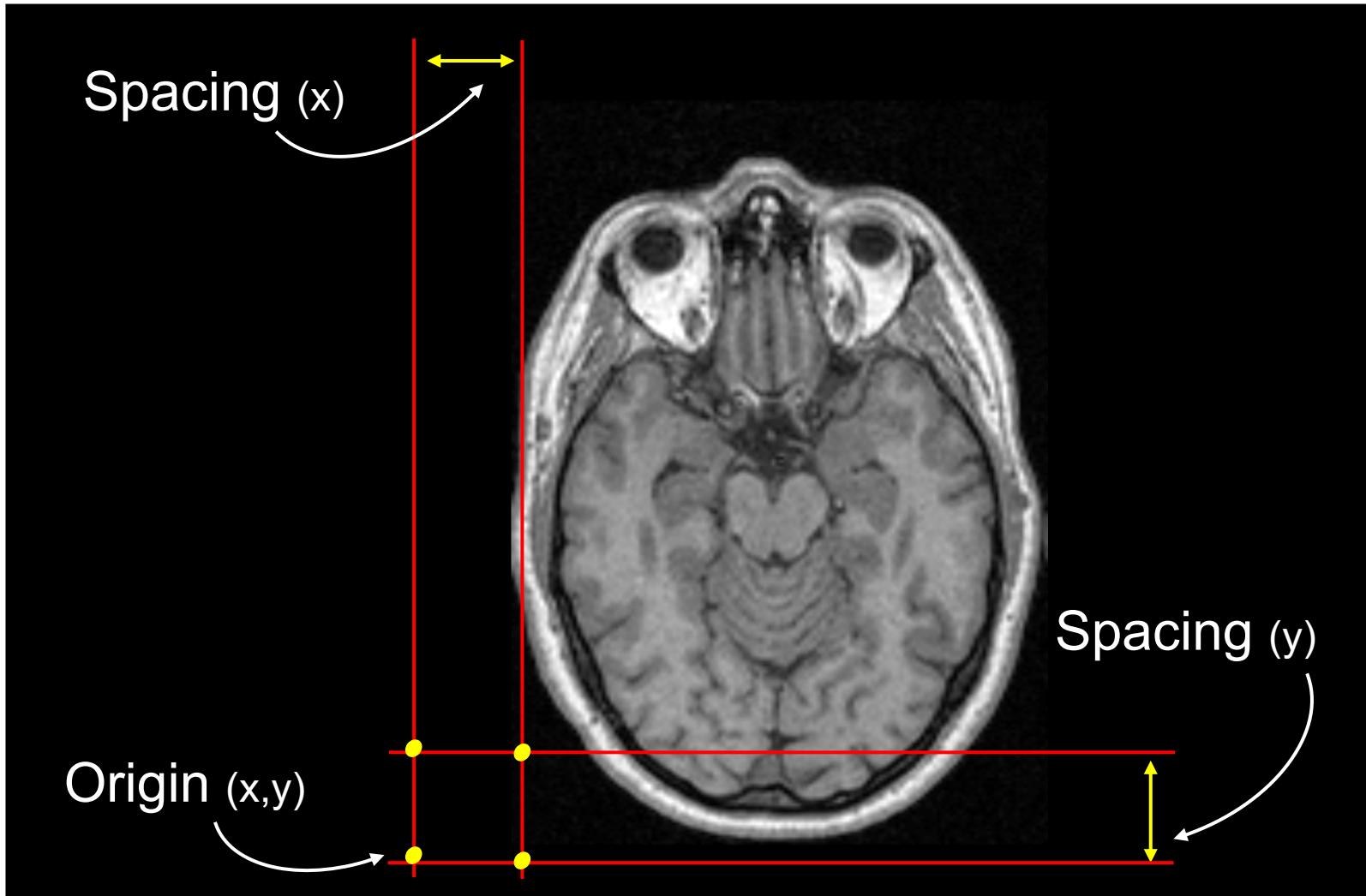


What is an image?

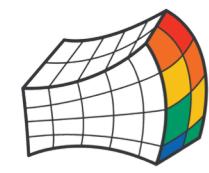
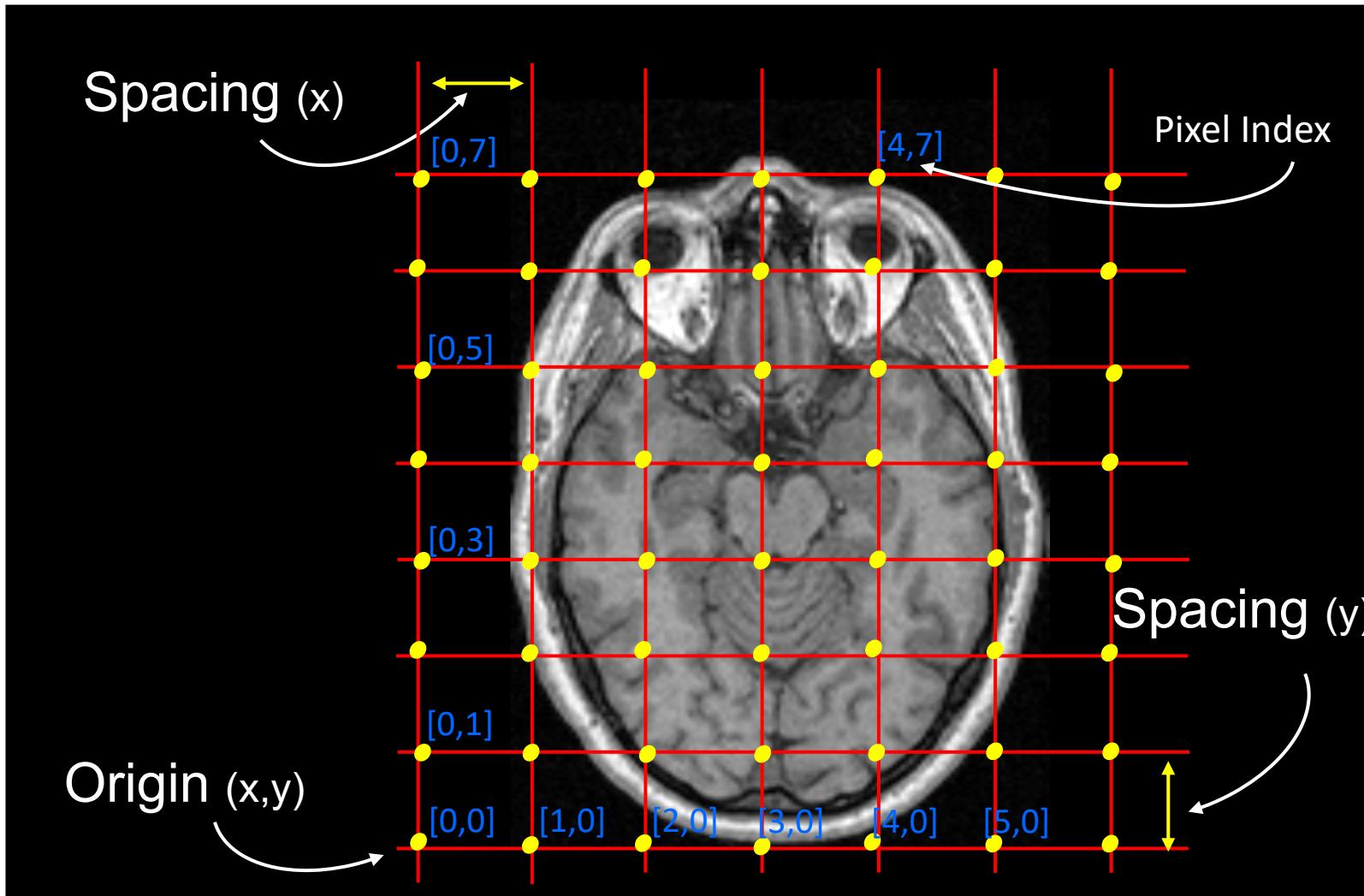
An image is a sampling of a continuous field using a discrete grid



What is an image?



What is an image?



Digitization

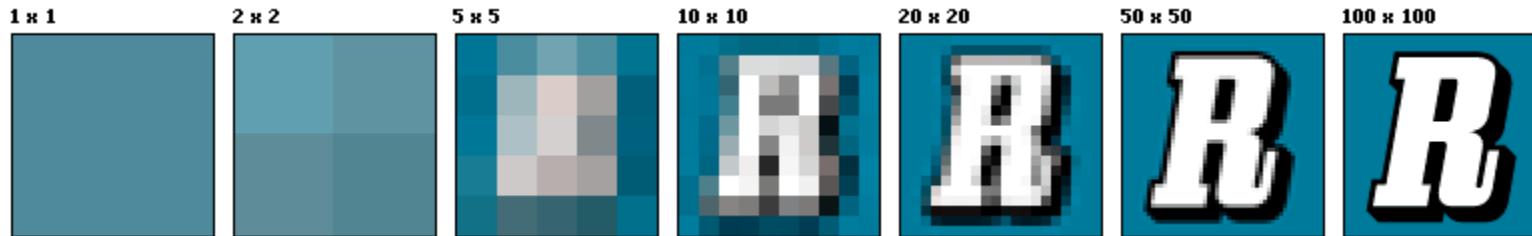
- Digitization is the process of representing a continuous object with discrete values on a discrete grid.
 - Resolution: spatial sampling
 - Quantification: value range
- Values in an image are samples on a pixel (2D) or voxel matrix (3D)



Resolution

Resolution is the capability of sensor to observe or measure the smallest object clearly with distinct boundaries. MicroCT scanners have resolutions from sub-micron range to 100s of microns (1000 micron = 1 mm).

Pixel is unit of digital image. How big of a physical structure a pixel represents depends on the resolution (i.e. resolution and pixel size are inversely proportional).



Resolution in 3D

Similar to pixel, **voxel is a unit of digital volume:**

Resolution in each dimension is not necessarily identical: That's especially true for human imaging, where the sampling in Z is a lot coarser than X and Y (i.e. they take far fewer slices, but within a slice you see everything you need to see in high-detail). In this case the voxels are said to be **ANISOTROPIC**. If all dimensions are identical then the voxels are **ISOTROPIC**



Bits and Bytes

- A “bit” is the smallest unit of storage, storing either a 0 or 1
- n bits yield 2^n distinct patterns

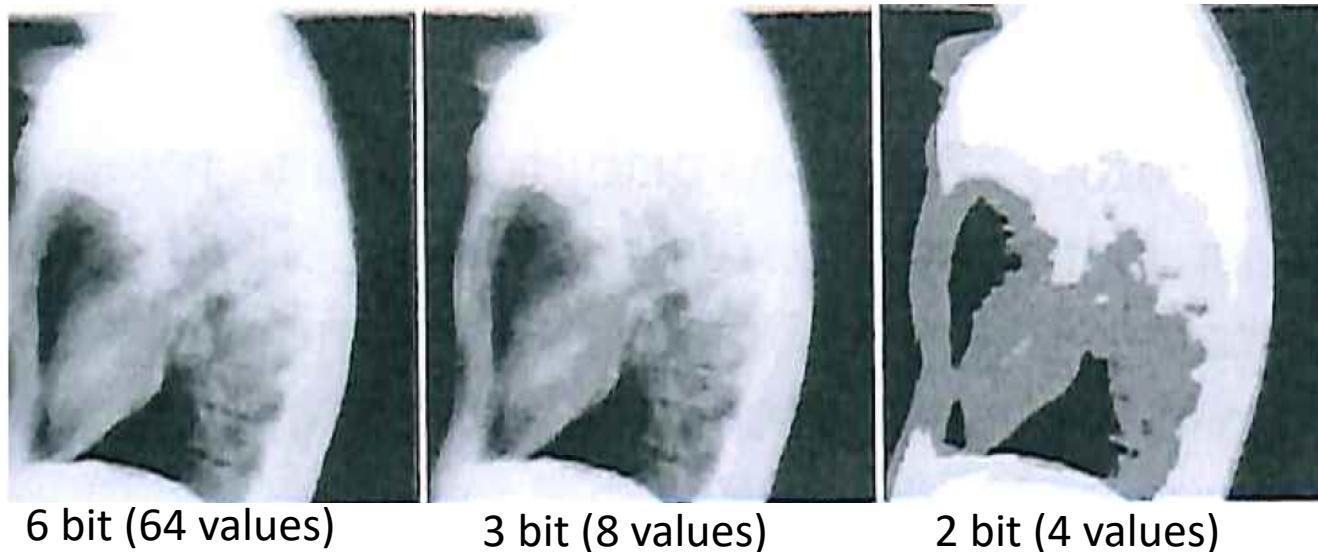
Number of bits	Different Patterns	Number of Patterns
1	0, 1	=2
2	00, 01, 10, 11	=4
3	000, 001, 010, 011 100, 101, 110, 111	=8

- One byte = collection of 8 bits
- All storage is measured in bytes
 - Kilobyte, KB, ~ 1 thousand bytes
 - Megabyte, MB, ~ 1 million bytes
 - Gigabyte, GB, ~ 1 billion bytes
 - Terabyte, TB, ~ 1 trillion bytes



Quantization

- Quantization refers to the digitization of the value range
 - Grayscale image: 8 bits (256 possible states)
 - Color image: 24 bits (16,777,216 possible states)
 - CT scans: 12 bits (4,096 possible states)



Quantization and image size

You have a CT scan of a human subject that is **256 pixels wide, 256 pixels high**, and consists of **256 slices** and the image depth is **16 bit**.

How big is this data set?



Quantization and image size

You have a CT scan of a human subject that is **256 pixels wide, 256 pixels high**, and consists of **256 slices** and the image depth is **16 bit**.

How big is this data set?

8 bit = 1 byte

$$256 \times 256 \times 256 \times (16/8) = 33,554,432 \text{ Bytes}$$
$$\sim 32\text{MB}$$



So what do those mean to me?

As a general rule, you need at least **4-6 times as large RAM** than your dataset.

If you want to visualize your dataset in full resolution, you need a **GPU** that has at least **1.5 times as large VRAM** than your dataset.

A typical high-resolution microCT dataset is **1024 x 1024 x 1024** in dimensions.

If image depth is 8 bit this = **1024MB or 1GB**

So in case of 1GB volume, you need at least 6GB of RAM and a GPU with 1.5GB of VRAM.



Memory Limitations:

- **A 32 bit OS can only address 4GB of RAM** regardless of how much physical RAM your computer has.
- **Memory fragmentation:** The available memory isn't contiguous, but consists of many small fragments. This results in out of memory errors the OS reports that the sufficient memory is available. This was a common issue on Windows platforms but has been improving.



Image compression

Goal: Reduce the amount of data required to represent the information in a digital image

- Can be lossy or lossless
- Eliminates redundancy in the data:
 - **Coding**: optimize number of bits required to code information in image
 - **Interpixel**: exploit correlations between neighboring pixels
 - **Psychovisual**: discard data that is perceptually insignificant



What format NOT to use?

JPEG

Or any other lossy compression format. Why are we doing all this work if we are going to throw them out when we save?



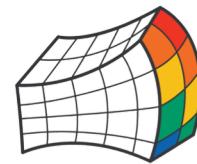
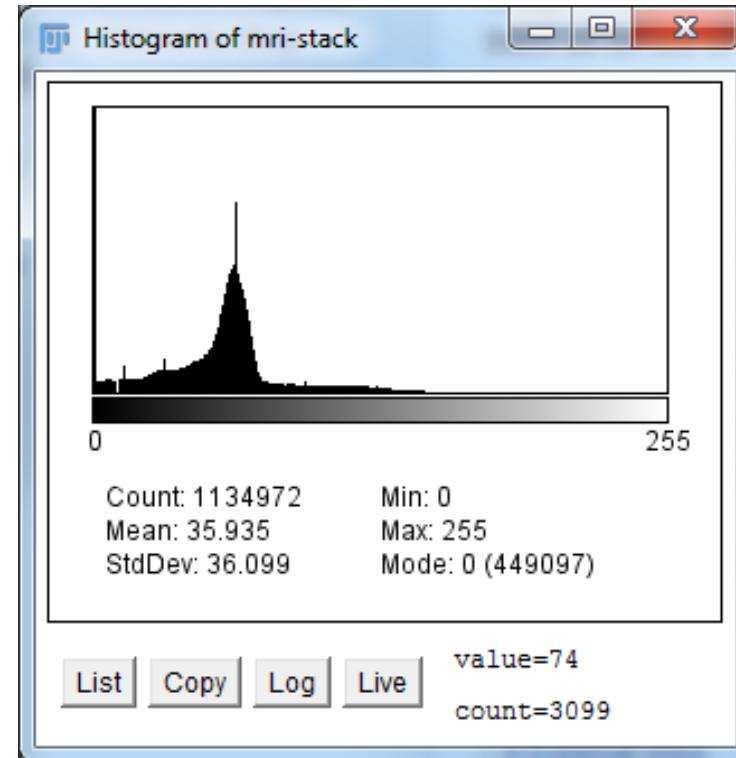
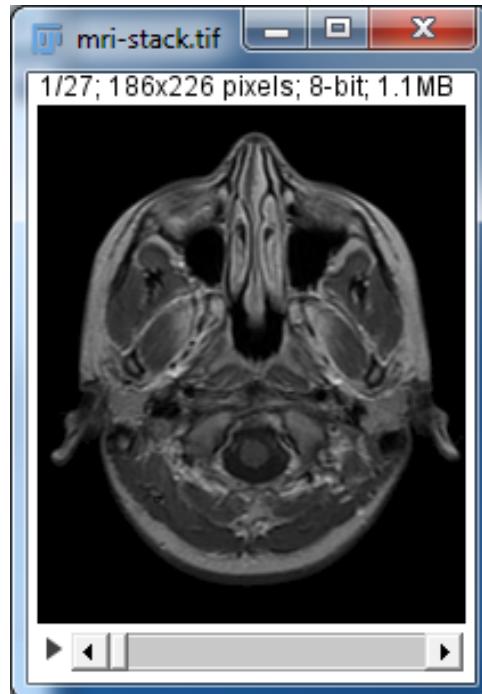
Image enhancement

- Image enhancements are low-level operations that are preformed without knowledge of the content of an image
- Why?
 - Remove noise
 - Sharpen image, etc.
- Examples
 - Histogram transformations
 - Convolution
 - Mathematical morphology
 - Registration



Image Histogram

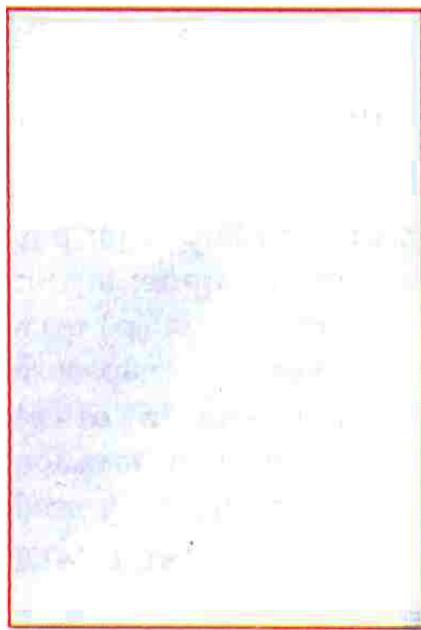
An image histogram shows the frequency distribution of the pixel values (in this context grayscale) in a digital image. It plots the number of pixels for each tonal value.



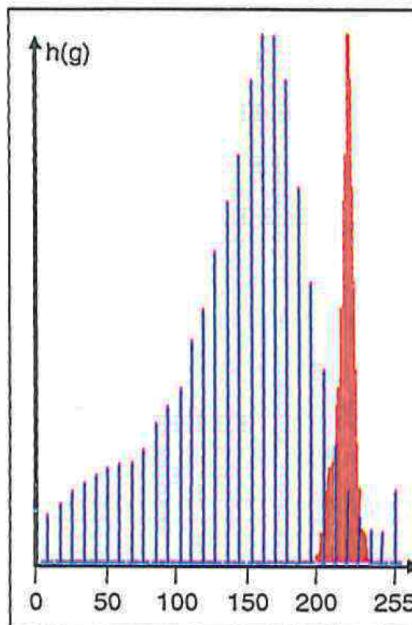
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Histogram transformation

- Simple pixel transforms can be defined using the histogram
- In this example the gray scale values of the image in (A) are stretched, resulting in the improved contrast in (C)



A. Original image



B. Original and
stretched histograms



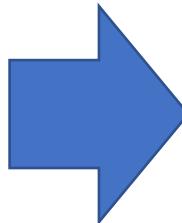
C. Enhanced image

Spatial image filtering

Modify the intensity values of a pixel based on a function of the intensity values from a local neighborhood around that pixel.

4	2	8
4	36	41
1	31	44

Function $f(x)$



	19	



Spatial image filtering

Modify the intensity values of a pixel based on a function of the intensity values from a local neighborhood around that pixel.

4	2	8
4	36	41
1	31	44

Function $f(x)$



	19	

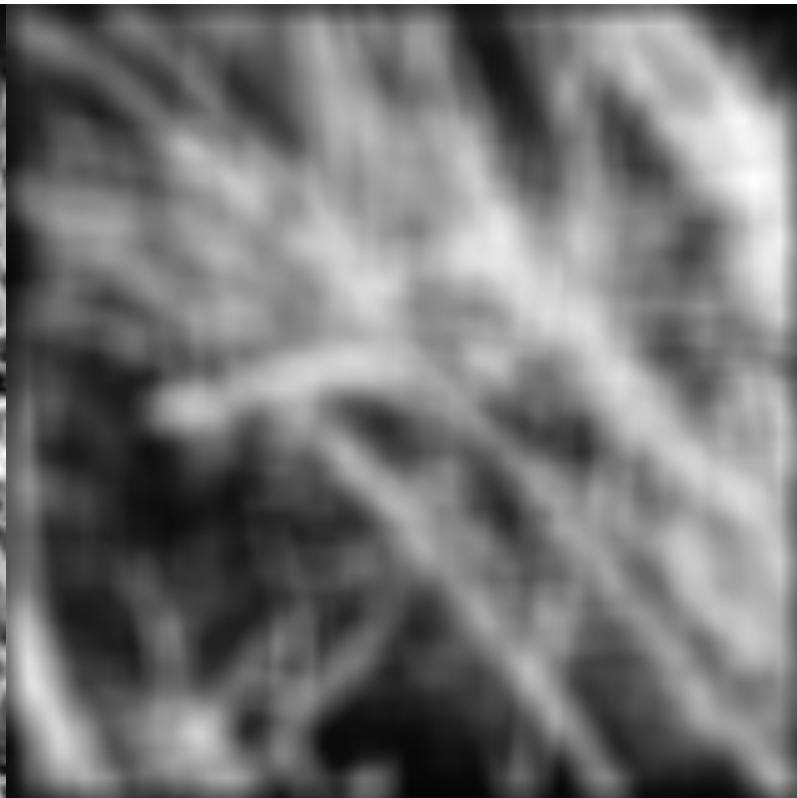
$$f(x) = \frac{1}{n} \sum_i^n x_i$$

*Mean filtering/ moving average
Removes sharp features*



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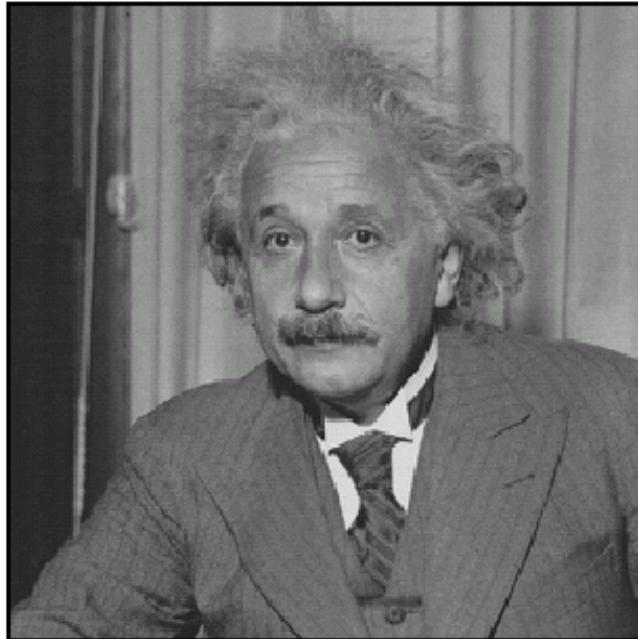
Smoothing with a mean filter



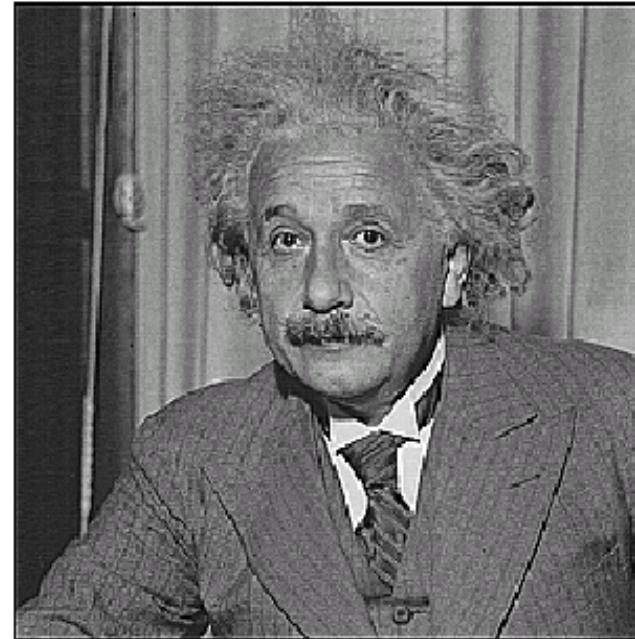
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Sharpening

Sharpening function $g(x) = 2x - f(x)$, $f(x) = \frac{1}{n} \sum_i^n x_i$



before



after

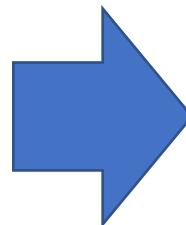


Convolutional Filters

- Filters that use a linear combination of pixels in a spatial neighborhood are often defined as **convolution** with a template, or “kernel”
- The weights of the template are determined by the filter’s kernel and determine the effect of the filter
- The kernel is shifted to each pixel location

a	b	c
d	x	e
f	g	h

Function $f(x)$



	y	



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Common kernel choices

1	2	1
0	0	0
-1	-2	-1

Sobel
Horizontal Edge
(absolute value)

0	1	0
0	0	0
0	-1	0

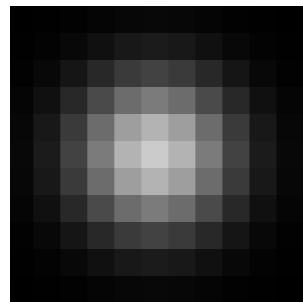
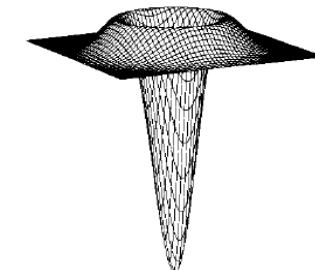
Vertical Gradient

0	0	0
-1	0	1
0	0	0

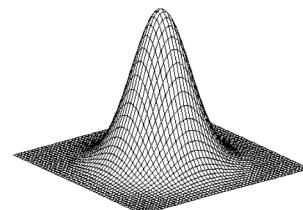
Horizontal Gradient

0	1	0
1	-4	1
0	1	0

LaPlacian of Gaussian
2D edge detection



Gaussian smoothing
Weight contribution by nearness



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Mathematical morphology

- Set of logical operations performed primarily on binary images
- Frequently used to clean up shapes after pixel-based segmentation
- Binary mathematical morphology consists of two basic operations
 - **Dilation: based on logical AND**
 - **Erosion: based on logical OR**

and several composite relations

- **Closing: dilation followed by erosion**
- **Opening: erosion followed by dilation**
- **Skeleton: erosion with various structuring elements**



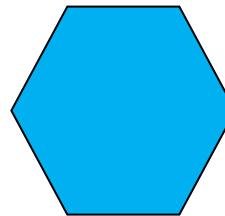
Structuring Elements

A **structuring element** is a shape mask used in the basic morphological operations.

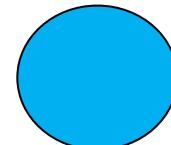
They can be any shape and size that is digitally representable, and each has an **origin**.



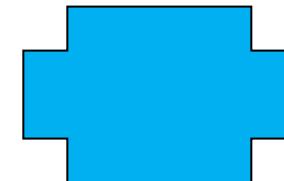
box



hexagon



disk



other



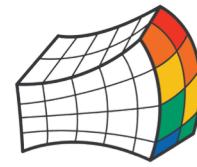
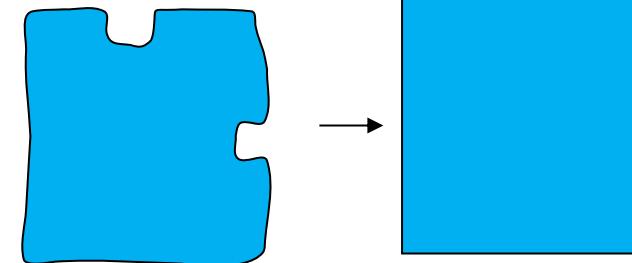
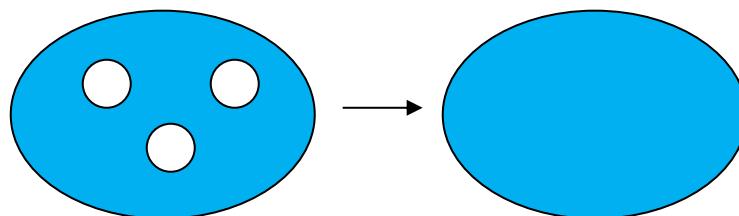
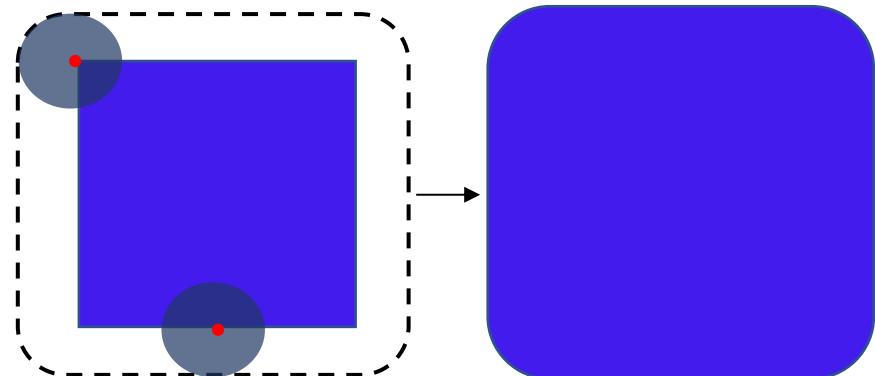
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Dilation

Dilation **expands** the connected sets of 1s of a binary image.

It can be used for

1. growing features
2. filling holes and gaps



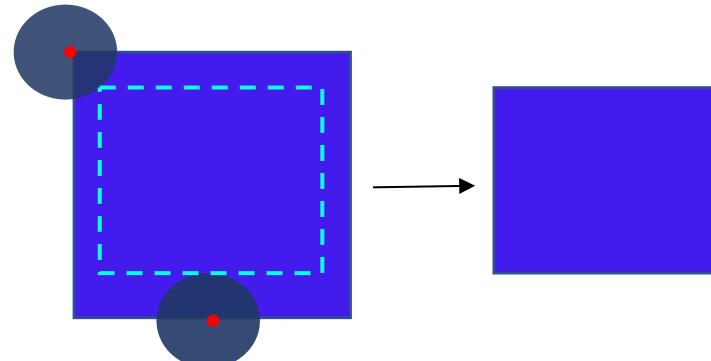
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Erosion

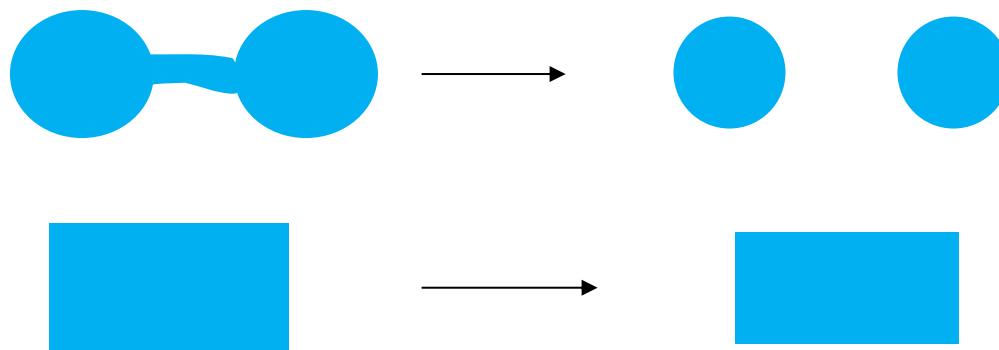
Erosion **shrinks** the connected sets of 1s of a binary image.

It can be used for

1. shrinking features



2. Removing bridges, branches and small protrusions



Segment Editor Tools

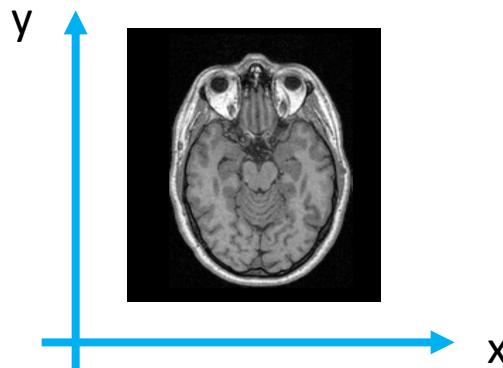
The image shows the 3DSlicer software interface. At the top left is the 3DSlicer logo. Below it is a toolbar with various icons: None, Paint, Draw, Erase, Level tracing, Grow from seeds, Fill between slices, Threshold, Margin, Hollow, Smoothing (which is highlighted with a red box), Scissors, Islands, Logical operators, Draw tube, Fast Marching, Flood filling, Local Threshold, Mask volume, Split volume, Surface cut, and Watershed. Below the toolbar is a section titled "Effects" containing the same set of tools. A red arrow points from the "Smoothing" button in the toolbar to the "Smoothing" section in the effects panel. The "Smoothing" section contains the following text: "Make segment boundaries smoother... [Show details.](#)". It includes a dropdown menu for "Smoothing method" set to "Opening (remove extrusions)", a "Kernel size" input field set to "3.00mm" which also shows "3x3x3 pixels" below it, an "Apply" button, and "Undo" and "Redo" buttons at the bottom.



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Image Registration

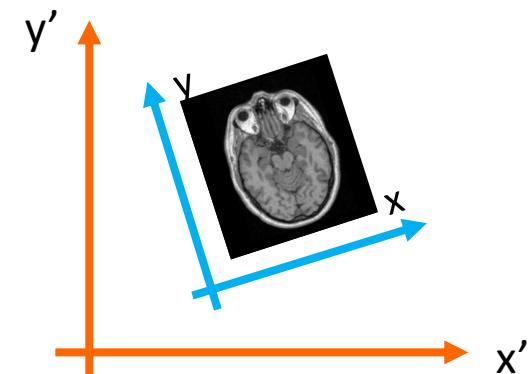
- Registration can be used to obtain a correspondence between images such that a change in measured dimensions can be quantified.
- The **moving** image will be resampled into the **fixed** image coordinate system



Physical coordinates of
fixed image



Space Transform



Physical coordinates of
moving image

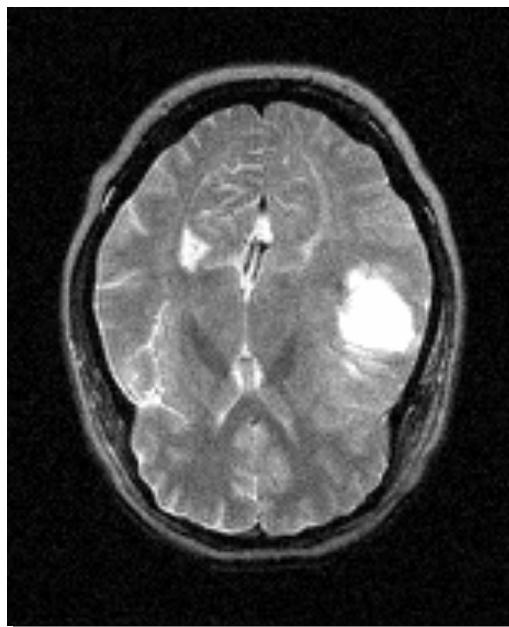
- The space transformation can be rigid or non-rigid (more on this later)



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Multimodal registration

MRI-T2



PET



Space Transform

256 x 256 pixels

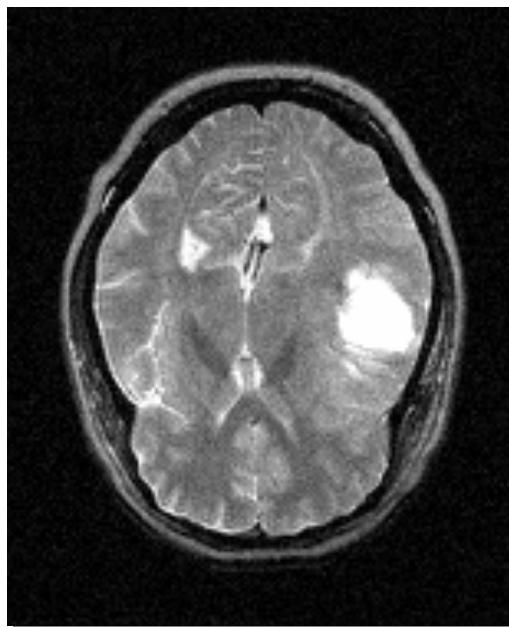
128 x 128 pixels

Images from the project: "Retrospective Image Registration Evaluation",
NIH, Project No. 8R01EB002124-03, Principal Investigator, J. Michael Fitzpatrick, Vanderbilt University, Nashville, TN.

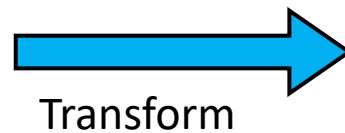


Multimodal registration

MRI-T2



256 x 256 pixels



PET



128 x 128 pixels

**Do not register images in pixel space
Pixel spacing needs to be specified**

Images from the project: "Retrospective Image Registration Evaluation",
NIH, Project No. 8R01EB002124-03, Principal Investigator, J. Michael Fitzpatrick, Vanderbilt University, Nashville,
TN.

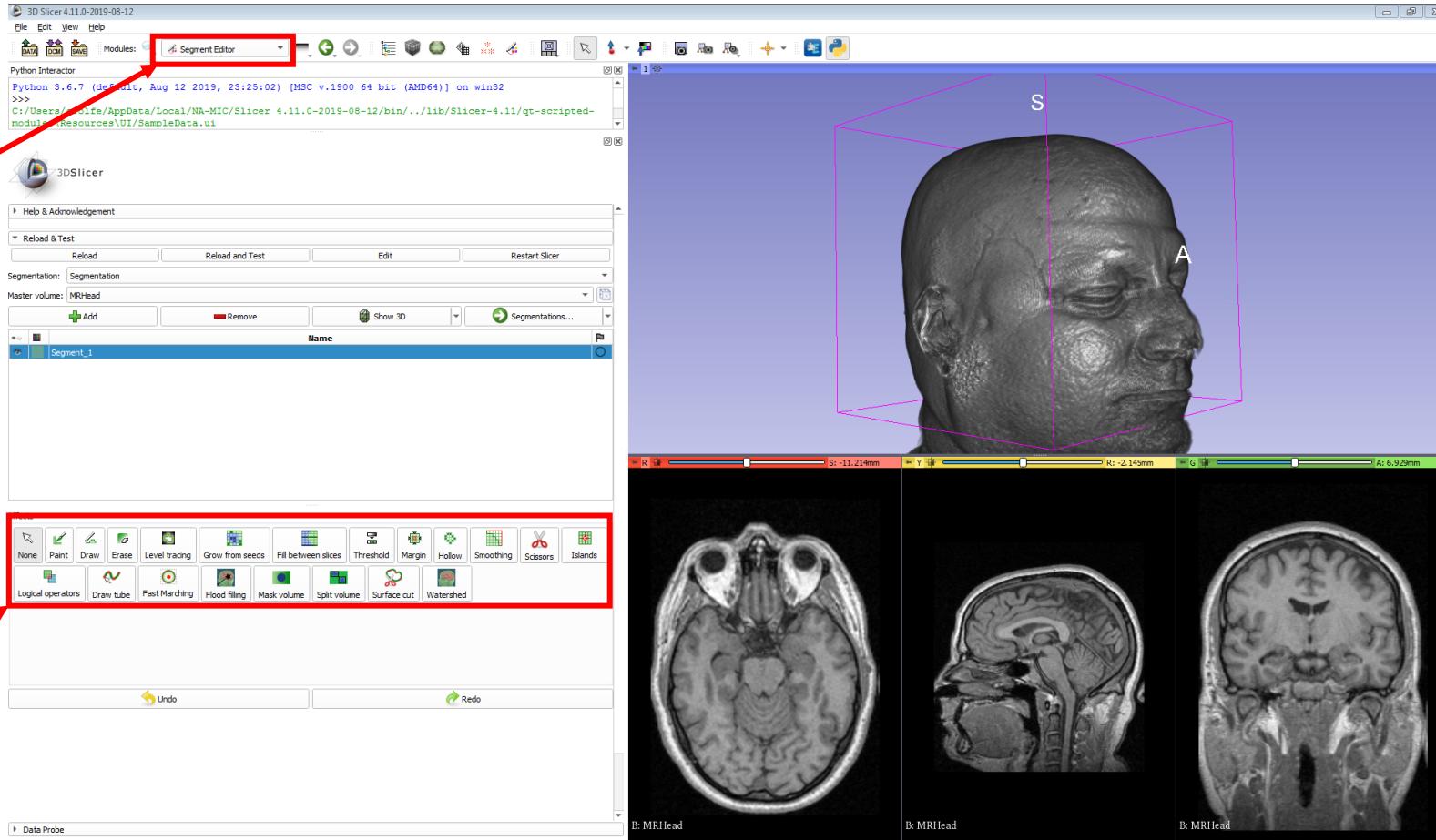


Segmentation

- Dividing an image into connected regions based on the content of the image
- Regions of an image segmentation should be uniform and homogenous with respect to some characteristic, such as gray tone, color or texture and should differ significantly with respect to adjacent regions
- Techniques include
 - Thresholding
 - Grow from seeds
 - Watershed filter
 - Fast marching filter

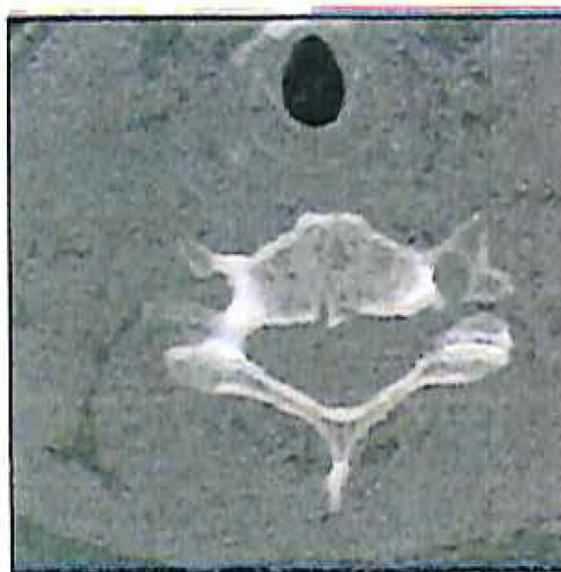


Segmentation tools available in 3D Slicer



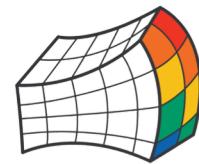
Thresholding

- Assigning labels to pixel intensity ranges
- Can be static or dynamic
- Static: known value ranges for types of tissue in CT scans



● air ● fat ● water ○ bone

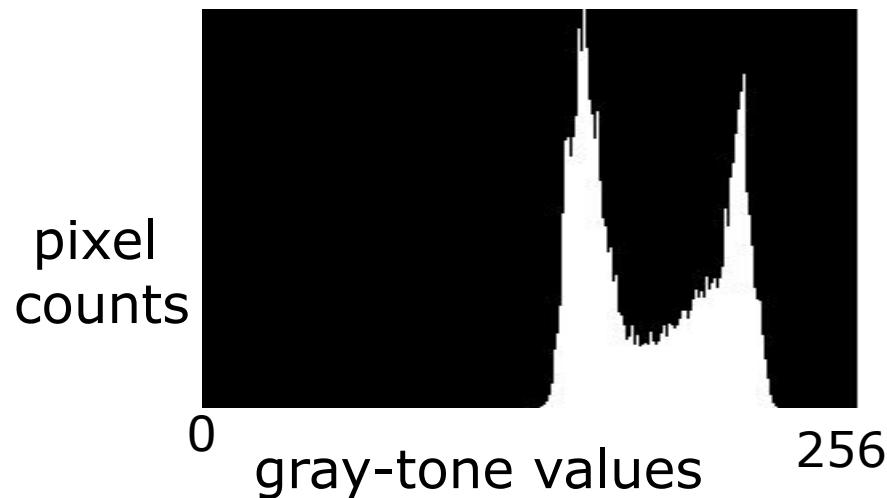
Segmentation in CT
relying on
Hounsfield Units
(HU) which define
a window of values
for each tissue type



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Histogram-Directed Thresholding

How can we use a histogram to separate an image into 2 (or several) different regions?

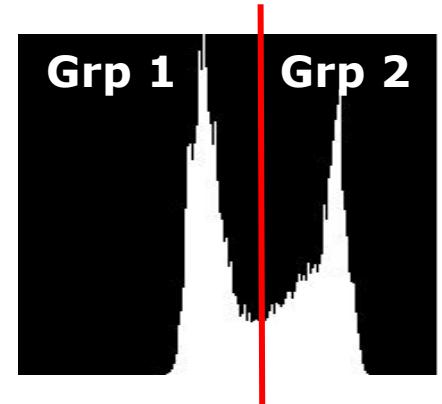


Is there a single clear threshold? 2? 3?



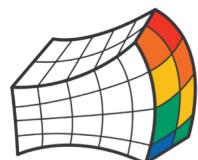
Automatic Thresholding: Otsu's Method

Assumption: the histogram is bimodal



Method: find the threshold t that minimizes the weighted sum of within-group variances for the two groups that result from separating the gray tones at value t .

Note: In practice, this operator works very well for true bimodal distributions and not too badly for others.



Thresholding Example



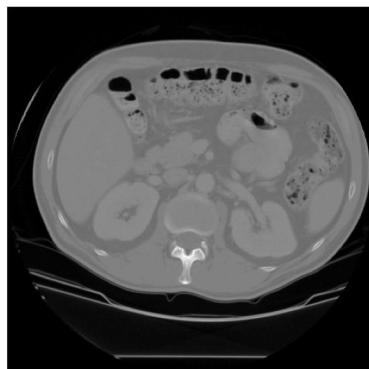
original gray tone image



Binary image after
threshold is applied

Connected Components Labeling

- Identify and then analyze each **connected set of pixels**.
- The connected components operation takes in a binary image and produces a **labeled image** in which each pixel has the integer label of either the background (0) or a component.



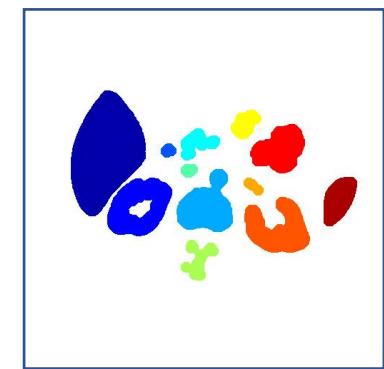
original
grayscale image



binary image
after threshold
applied



binary image
after
morphology



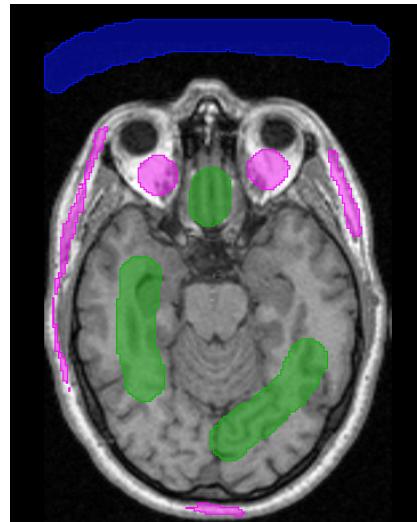
connected
components



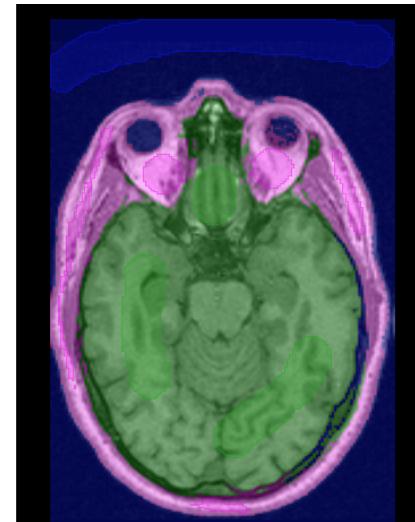
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Grow from seeds

- Region growing techniques start with one pixel of a potential region and try to grow it by adding adjacent pixels till the pixels being compared are too dissimilar
- Can include a priori knowledge of the scene by taking a set of seed pixels can be chosen from the image
- A statistical tests used to decide which pixels can be added to a region



User provided
seeds

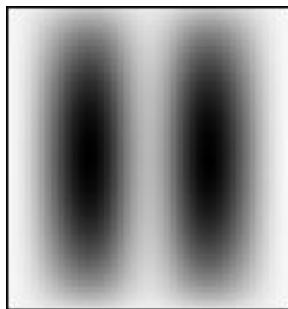


Segmentation
grown from seeds



Watershed filtering

- The watershed transform treats a 2D image like a surface
- Catchment basins are identified at regional minimums
- The basins are “flooded” until the different water sources meet, determining the watershed lines between regions



Gray scale image

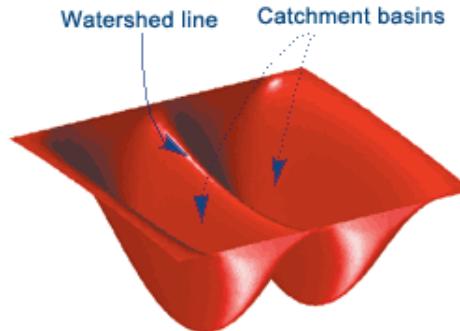
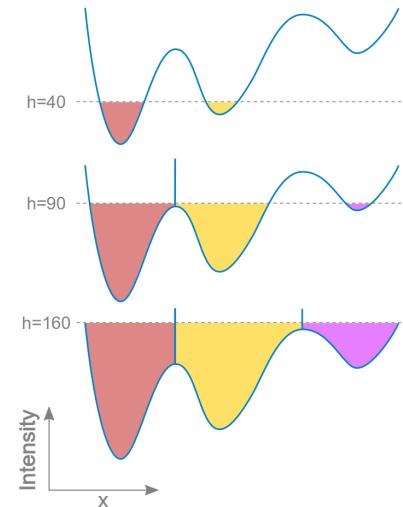


Image visualized as a surface where bright areas are “high” and dark are “low”



Progressive watershed “flooding” in 1D



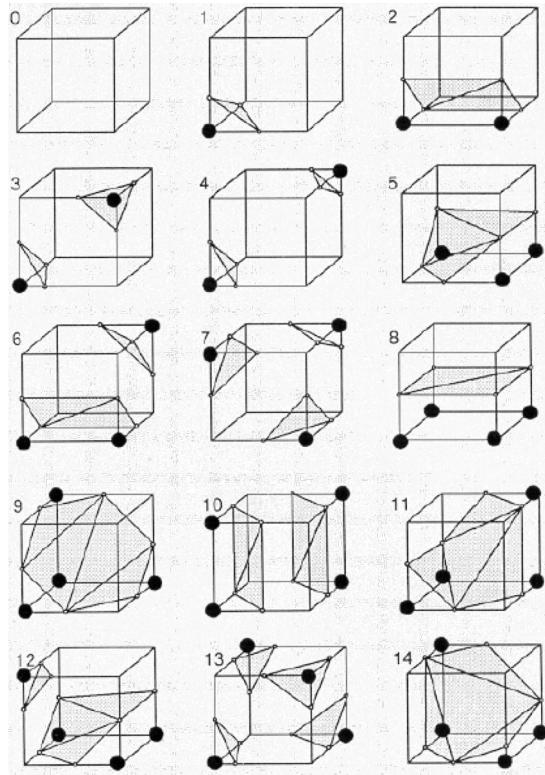
Visualization

- All transforms that optimize the output of the image to create a realistic depiction of 3D data
- Surface-based
 - Fast marching filter
 - Surface rendering
- Direct volume visualization
 - Ray casting

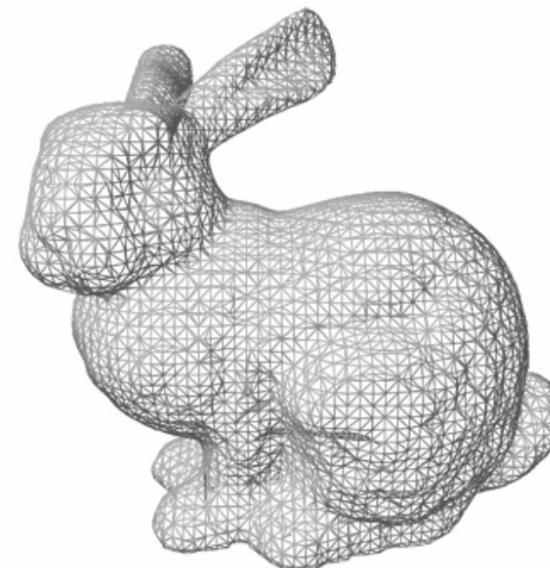


Fast marching filter

- Developed to reconstruct surfaces from medical images
- Each voxel is considered as a point, instead of a 3D voxel
- Create a cube with 8 pixels on adjacent slices. Move the cube to each point in the image to determine if the vertices are “in” or “out”



- 15 distinct topologies can be stored in a lookup table for efficiency



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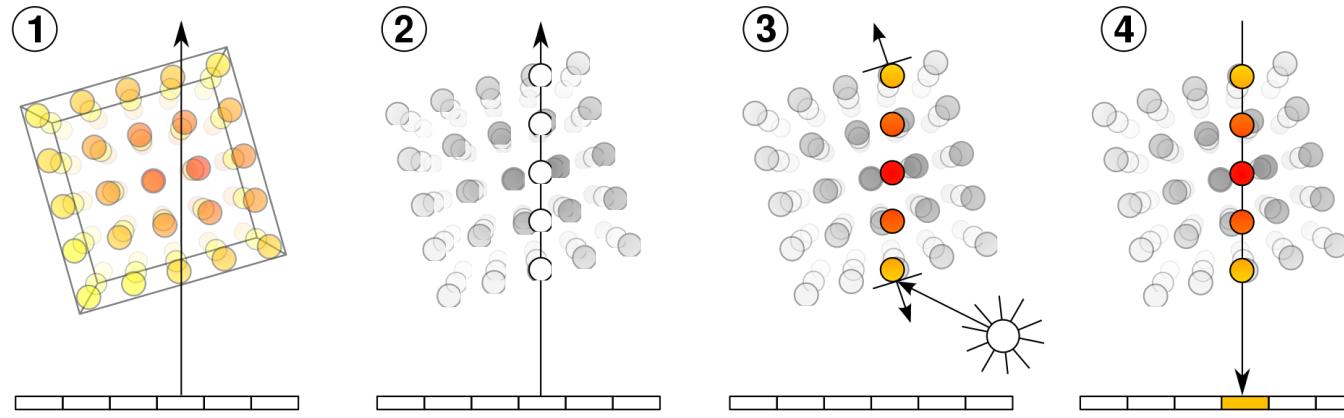
Surface rendering

- Create photo-realistic representations of volume surfaces
- Lighting modeled by constant ambient light overlapped with reflections based on the material properties of the surface
- Takes into account translucency, surface texture, and reflections



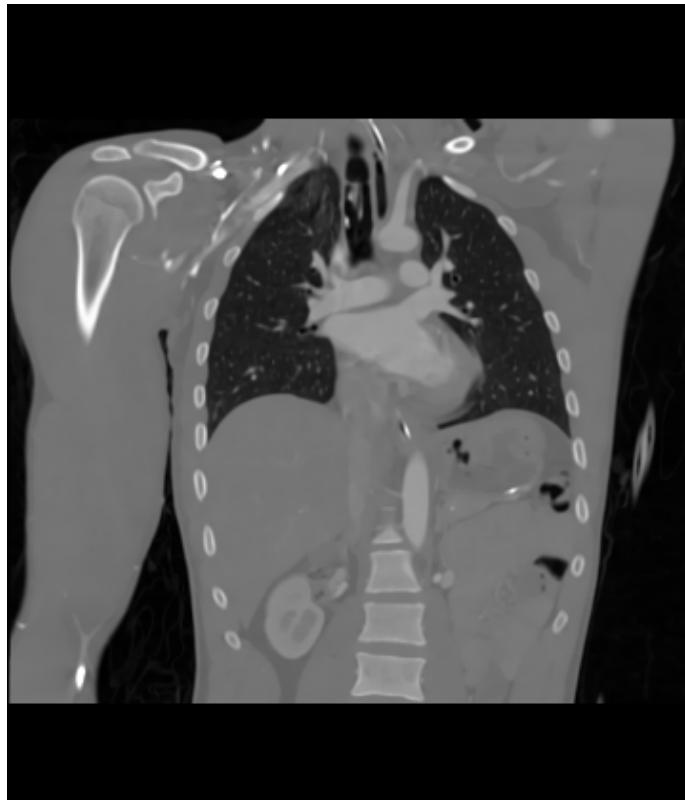
Volume rendering: Ray casting

- Direct volume visualization does not rely on a preliminary calculation of the object surface or segmentation
- Visualization based directly on voxel data
 1. Volume is processed along an imaginary light ray
 2. Parameters are extracted from voxel intensity along the rays and
 3. A transfer function is applied that incorporates material properties and illumination
 4. The final value is applied as color or gray values at the corresponding position on the viewing plane

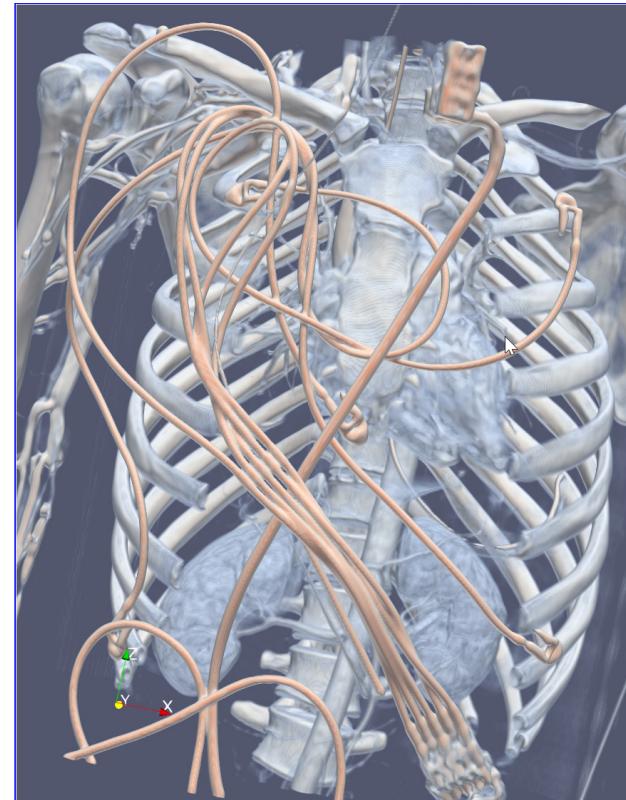


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GPU Ray casting



Coronal slice of 3D CTA
image



3D volume rendering using
ray casting



Resources

Free online texts

Deserno, Thomas Martin. "Biomedical image processing." (2011). Available at [this URL](#)

Shapiro and Stockman, Computer Vision, Prentice-Hall, 2001. Original chapters available at [this URL](#)

Szeliski, Richard. Computer vision: algorithms and applications. Springer Science & Business Media, 2010. Available at [this URL](#)

Online lectures

Noah Snavely's [CS5670 - Introduction to Computer Vision class at Cornell Tech \(Spring 2019\)](#)

Ioannis Gkioulekas's [16-385 Computer Vision class at CMU \(Spring 2019\)](#)

Coordinate systems

Chand John of Stanford created a [detailed powerpoint presentation about the way coordinates are handled in Slicer](#)

Rendering

Udupa, Jayaram K., Hsiu-Mei Hung, and Keh-Shih Chuang. "Surface and volume rendering in three-dimensional imaging: a comparison." Journal of digital Imaging 4.3 (1991): 159.



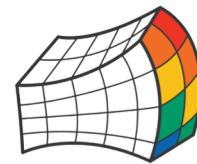
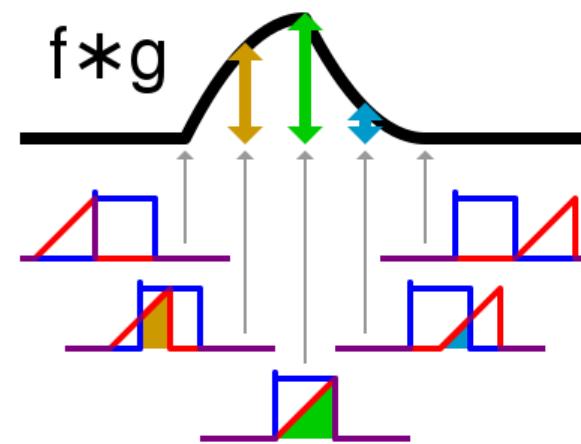
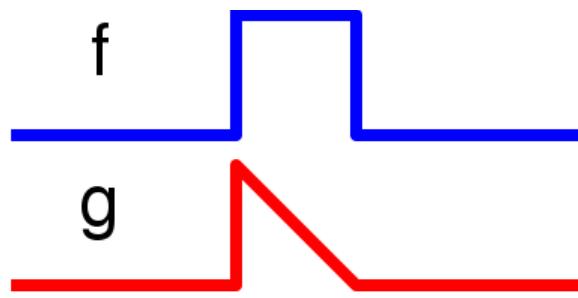
Questions?



Convolution in 1D

$$(f * g)(x) = \int_{-\infty}^{\infty} f(y)g(x - y)dy$$

filtered signal filter input signal notice the flip



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Convolution

- Filters that use a linear combination of pixels in a spatial neighborhood are often defined as convolution with a template, or “kernel”
- The weights of the template are determined by the filter’s kernel and determine the effect of the filter
- The kernel is shifted to each pixel location

From the previous mean filter example, the kernel is:

$$f(.,.) = \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

