Online, 12-15 novembre 2021

vm • EN

Aggiornamento della macchina virtuale (vm)

Georgio Audritto is updating the OII virtual machine. It contains N programs, numbered from 0 to N-1: the version of the i-th one is currently A_i . The sequence A_i is nondecreasing (i.e. $A_i \leq A_{i+1}$ for each $0 \leq i \leq N-2$).



Figure 1: Georgio while he is updating the virtual machine

For each update, Georgio chooses a program i and updates it by B_i versions (so A_i increases by B_i). The same program can be updated multiple times. Moreover:

- Georgio can't update the program number N-1.
- The *i*-th program depends on all the previous ones, so it can't have a lower version than the programs with lower index (for backward compatibility). In other words, after each update, the sequence A_i must be nondecreasing ($A_i \leq A_{i+1}$ must hold for each $0 \leq i \leq N-2$). Note that the order of the programs doesn't change after an update.

What's the maximum number of updates that Georgio can make?

Implementation

You should submit a single file, with a .cpp extension.

Among the attachments in this task you will find a template vm.cpp with a sample implementation.

You will have to implement the following function:

C++ | long long aggiorna(int N, vector<int> A, vector<int> B);

- The integer N represents the number of programs in the virtual machine.
- The vector A contains the initial version of each program. In particular, for each $0 \le i \le N-1$, A_i is the version of the *i*-th program.

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• The vector B specifies how the programs are updated. In particular, for each $0 \le i \le N-2$, A_i increases by B_i after an update of the i-th program.

The function aggiorna must return the maximum number of updates that Georgio can make.

Grader di prova

Among this task's attachments you will find a simplified version of the grader used during the evaluation, which you can use to test your solutions locally. The sample grader reads data from stdin, calls the functions that you should implement and writes back on stdout using the following format.

The input file consists of 3 lines, containing:

- Line 1: the integer N.
- Line 2: the N integers A_0, \ldots, A_{N-1} .
- Line 3: the N-1 integers B_0, \ldots, B_{N-2} .

The output file consists of a single line, containing the value returned by aggiorna.

Constraints

- $2 \le N \le 2 \cdot 10^5$.
- $1 < A_i, B_i < 10^9$.
- $A_i \leq A_{i+1}$ for each $0 \leq i \leq N-2$.

Scoring

Your program will be tested against several test cases grouped in subtasks. In order to obtain the score of a subtask, your program needs to correctly solve all of its test cases.

- Subtask 1 [0 points]: Examples.
- Subtask 2 [12 points]: $B_i = 1$
- Subtask 3 [20 points]: $N \le 500, A_i \le 200$
- Subtask 4 [22 points]: $A_i \le 200$
- Subtask 5 [19 points]: $N = 2 \cdot 10^5$, the input is chosen uniformly randomly among all the valid inputs.
- Subtask 6 [27 points]: No additional limitations.

Examples

stdin	stdout
6 2 7 11 14 18 25 8 4 6 3 4	7
8 3 27 86 95 419 852 1473 6461 100 100 100 1000 1000 10000	0

Explanations

In the **first example**, Georgio can make the following updates:

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- Update of the program 3: the versions become [2, 7, 11, 17, 18, 25];
- Update of the program 2: the versions become [2, 7, 17, 17, 18, 25];
- Update of the program 1: the versions become [2, 11, 17, 17, 18, 25];
- Update of the program 0: the versions become [10, 11, 17, 17, 18, 25];
- Update of the program 1: the versions become [10, 15, 17, 17, 18, 25];
- Update of the program 4: the versions become [10, 15, 17, 17, 22, 25];
- Update of the program 3: the versions become [10, 15, 17, 20, 22, 25].

7 updates have been made: it can be shown that it's the maximum possible for this input.

In the **second example** Georgio can't update any program.

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