

# Task: NAD

## Transmitters



XXIII OI, Stage I. Source file nad.\* Available memory: 256 MB.

19.10–16.11.2015

Byteasar has become the new head of a historic salt mine near Bytown. To increase its popularity with the tourists, he has decided to have wireless Internet set up in the mine's corridors.

The mine consists of  $n$  chambers connected by  $n - 1$  corridors. Each chamber can be reached from every other using the corridors. Byteasar wants to have the wi-fi transmitters installed in the chambers so that Internet is available in every corridor of the mine. The signal in the corridor linking chambers  $a$  and  $b$  will be sufficiently strong if at least one of the following conditions holds:

- there is a transmitter in chamber  $a$  or chamber  $b$ , or
- inside the chambers that can be reached from chamber  $a$  or  $b$  using at most one corridor, there is a total of at least two transmitters.

Byteasar wonders how many wi-fi transmitters are required to provide sufficiently strong signal in all the corridors. Each chamber can have an arbitrary number of transmitters installed.

## Input

The first line of the standard input contains a positive integer  $n$  that specifies the number of chambers in the mine. These chambers are numbered from 1 to  $n$ .

The following  $n - 1$  lines describe the mine's corridors. Each such line contains two integers  $a$  and  $b$  ( $1 \leq a, b \leq n$ ,  $a \neq b$ ), separated by a single space, which indicate that the chambers no.  $a$  and  $b$  are directly linked by a corridor.

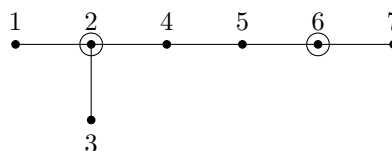
## Output

The first and only line of the standard output should contain a single integer: the minimum number of transmitters that Byteasar has to deploy.

## Example

For the input data:

```
7
1 2
2 3
2 4
4 5
5 6
6 7
```

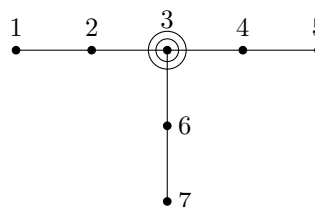


the correct result is:

2

whereas for the following input data

```
7
1 2
2 3
4 3
5 4
6 3
7 6
```



the correct result is:

2

**Explanation of the example:** In the first example, it is sufficient to install one transmitter in each of the chambers no. 2 and 6, whereas in the second one it is sufficient to install two transmitters in the chamber no. 3.

### Sample Grading Tests:

**1ocen:**  $n = 16$ . Chamber no.  $i$  is linked with chamber no.  $\lfloor i/2 \rfloor$  for  $2 \leq i \leq n$ .

**2ocen:**  $n = 303$ . Chamber no. 2 is linked with chambers no. 1 and 3. Each of the chambers no. 1, 2, 3 is also linked with a hundred additional chambers. The optimal solution is installing two transmitters in chamber no. 2.

**3ocen:**  $n = 200\,000$ . The chamber no.  $i$  and  $i + 1$  are linked by a corridor for  $1 \leq i \leq n - 1$ .

## Grading

The set of tests consists of the following subsets. Within each subset, there may be several test groups.

Subset	Property	Score
1	$n \leq 10$	15
2	$n \leq 500$	20
3	$n \leq 200\,000$ , at most three corridors are incident on each chamber	25
4	$n \leq 200\,000$	40