## Problem A. Fraction

Input file: standard input
Output file: standard output

Time limit: 0.5 seconds Memory limit: 512 megabytes

Petya is a big fan of mathematics, especially its part related to fractions. Recently he learned that a fraction  $\frac{a}{b}$  is called *proper* iff its numerator is smaller than its denominator (a < b) and that the fraction is called *irreducible* if its numerator and its denominator are coprime (they do not have positive common divisors except 1).

During his free time, Petya thinks about proper irreducible fractions and converts them to decimals using the calculator. One day he mistakenly pressed addition button (+) instead of division button  $(\div)$  and got sum of numerator and denominator that was equal to n instead of the expected decimal notation.

Petya wanted to restore the original fraction, but soon he realized that it might not be done uniquely. That's why he decided to determine maximum possible proper irreducible fraction  $\frac{a}{b}$  such that sum of its numerator and denominator equals n. Help Petya deal with this problem.

#### Input

In the only line of input there is an integer n ( $3 \le n \le 10^{18}$ ), the sum of numerator and denominator of the fraction

#### Output

Output two space-separated positive integers a and b, numerator and denominator of the maximum possible proper irreducible fraction satisfying the given sum.

## **Examples**

standard input	standard output
3	1 2
4	1 3
12	5 7

#### Note

There are 4 test groups. In this problem all tests are scored **separately**, each test (except sample tests) is worth 4 points.

Group Points		Additional constraints	Comment	
Group	1 Ollius	n	Comment	
0	0	_	Sample tests	
1	20	$n \le 100$		
2	20	$n \le 100000$		
3	40	$n \le 10^9$		
4	20	_		

# Problem B. Jury Meeting

Input file: standard input
Output file: standard output

Time limit: 1 second Memory limit: 512 megabytes

Country of Metropolia is holding Olympiad of Metropolises soon. It mean that all jury members of the olympiad should meet together in Metropolis (the capital of the country) for the problem preparation process.

There are n+1 cities consecutively numbered from 0 to n. City 0 is Metropolis that is the meeting point for all jury members. For each city from 1 to n there is exactly one jury member living there. Olympiad preparation is a long and demanding process that requires k days of work. For all of these k days each of the n jury members should be present in Metropolis to be able to work on problems.

You know the flight schedule in the country (jury members consider themselves important enough to only use flights for transportation). All flights in Metropolia are either going to Metropolis or out of Metropolis. There are no night flights in Metropolia, or in the other words, plane always takes off at the same day it arrives. On his arrival day and departure day jury member is not able to discuss the olympiad.

Gather everybody for k days in the capital is a hard objective, doing that while spending the minimum possible money is even harder. Nevertheless, your task is to arrange the cheapest way to bring all of the jury members to Metrpolis, so that they can work together for k days and then send them back to their home cities. Cost of the arrangement is defined as a total cost of tickets for all used flights. It is allowed for jury member to stay in Metropolis for more than k days.

#### Input

The first line of input contains three integers n, m and k  $(1 \le n \le 10^5, 0 \le m \le 10^5, 1 \le k \le 10^6)$ .

The *i*-th of the following m lines contains the description of the *i*-th flight defined by four integers  $d_i$ ,  $f_i$ ,  $t_i$  and  $c_i$  ( $1 \le d_i \le 10^6$ ,  $0 \le f_i \le n$ ,  $0 \le t_i \le n$ ,  $1 \le c_i \le 10^6$ , exactly one of  $f_i$  and  $t_i$  equals zero), the day of departure (and arrival), the departure city, the arrival city and the ticket cost.

## Output

Output the only integer that is the minimum cost of gathering all jury members in city 0 for k days and then sending them back to their home cities.

If it is impossible to gather every body in Metropolis for k days and then send them back to their home cities, output "-1" (without the quotes).

# **Examples**

standard input	standard output
2 6 5	24500
1 1 0 5000	
3 2 0 5500	
2 2 0 6000	
15 0 2 9000	
9 0 1 7000	
8 0 2 6500	
2 4 5	-1
1 2 0 5000	
2 1 0 4500	
2 1 0 3000	
8 0 1 6000	

#### Note

The optimal way to gather everybody in Metropolis in the first sample test is to use flights that take place on days 1, 2, 8 and 9. The only alternative option is to send jury member from second city back home on day 15, that would cost 2500 more.

In the second sample it is impossible to send jury member from city 2 back home from Metropolis.

## **Scoring**

Tests in this problem are divided into three groups. For each of the groups you earn points only if your solution passes all tests in this group and all tests in all **previous** groups.

Croup	Points	Additional constraints	Comment	
Group Points	1 OHIGS	n,m	Comment	
0	0	_	Sample tests	
1	20	$n, m \le 10$		
2	30	$n,m \le 1000$		
3	50	_		

# Problem C. Michael and Charging Stations

Input file: standard input
Output file: standard output

Time limit: 1 second Memory limit: 512 megabytes

Michael has just bought a new electric car for moving across city. Michael does not like to overwork, so each day he drives to only one of two his jobs.

Michael's day starts from charging his electric car for getting to the work and back. He spends 1000 burles on charge if he goes to the first job, and 2000 burles if he goes to the second job.

On a charging station he uses there is a loyalty program that involves bonus cards. Bonus card may have some non-negative amount of bonus burles. Each time customer is going to buy something for the price of x burles, he is allowed to pay an amount of y ( $0 \le y \le x$ ) burles that does not exceed the bonus card balance with bonus burles. In this case he pays x-y burles with cash, and the balance on the bonus card is decreased by y bonus burles.

If customer pays whole price with cash (i.e., y = 0) then 10% of price is returned back to the bonus card. This means that bonus card balance increases by  $\frac{x}{10}$  bonus burles. Initially the bonus card balance is equal to 0 bonus burles.

Michael has planned next n days and he knows how much does the charge cost on each of those days. Help Michael determine the minimum amount of burles in cash he has to spend with optimal use of bonus card. Assume that Michael is able to cover any part of the price with cash in any day. It is not necessary to spend all bonus burles at the end of the given period.

#### Input

The first line of input contains a single integer n ( $1 \le n \le 300\,000$ ), the number of days Michael has planned.

Next line contains n integers  $a_1, a_2, \ldots, a_n$  ( $a_i = 1000$  or  $a_i = 2000$ ) with  $a_i$  denoting the charging cost at the day i.

## Output

Output the minimum amount of burles Michael has to spend.

## **Examples**

standard input	standard output
3	3700
1000 2000 1000	
6	10000
2000 2000 2000 2000 2000 1000	

#### Note

In the first sample case the most optimal way for Michael is to pay for the first two days spending 3000 burles and get 300 bonus burles as return. After that he is able to pay only 700 burles for the third days, covering the rest of the price with bonus burles.

In the second sample case the most optimal way for Michael is to pay the whole price for the first five days, getting 1000 bonus burles as return and being able to use them on the last day without paying anything in cash.

# **Scoring**

Tests for this problem are divided into four groups. For each of the groups you earn points only if your

### Olympiad of Metropolises, day 1 [en] Moscow, September 5th, 2017

solution passes all tests in this group and all tests in all of the **previous** groups.

Group	Points	Additional constraints	Comment
Group	1 011100	n	Commone
0	0	_	Sample tests
1	30	$n \le 20$	_
2	30	$n \le 1000$	_
3	40	_	_

## Problem D. Lada Malina

Input file: standard input
Output file: standard output

Time limit: 4 seconds Memory limit: 256 megabytes

After long-term research and lots of experiments leading Megapolian automobile manufacturer «AutoVoz» released a brand new car model named «Lada Malina». One of the most impressive features of «Lada Malina» is its highly efficient environment-friendly engines.

Consider car as a point in Oxy plane. Car is equipped with k engines numbered from 1 to k. Each engine is defined by its velocity vector whose coordinates are  $(vx_i, vy_i)$  measured in distance units per day. An engine may be turned on at any level  $w_i$ , that is a real number between -1 and +1 (inclusive) that result in a term of  $(w_i \cdot vx_i, w_i \cdot vy_i)$  in the final car velocity. Namely, the final car velocity is equal to

$$(w_1 \cdot vx_1 + w_2 \cdot vx_2 + \ldots + w_k \cdot vx_k, w_1 \cdot vy_1 + w_2 \cdot vy_2 + \ldots + w_k \cdot vy_k)$$

Formally, if car moves with constant values of  $w_i$  during the whole day then its x-coordinate will change by the first component of an expression above, and its y-coordinate will change by the second component of an expression above. For example, if all  $w_i$  are equal to zero, the car won't move, and if all  $w_i$  are equal to zero except  $w_1 = 1$ , then car will move with the velocity of the first engine.

There are n factories in Megapolia, i-th of them is located in  $(fx_i, fy_i)$ . On the i-th factory there are  $a_i$  cars «Lada Malina» that are ready for operation.

As an attempt to increase sales of a new car, «AutoVoz» is going to hold an international exposition of cars. There are q options of exposition location and time, in the i-th of them exposition will happen in a point with coordinates  $(px_i, py_i)$  in  $t_i$  days.

Of course, at the «AutoVoz» is going to bring as much new cars from factories as possible to the place of exposition. Cars are going to be moved by enabling their engines on some certain levels, such that at the beginning of an exposition car gets exactly to the exposition location.

However, for some of the options it may be impossible to bring cars from some of the factories to the exposition location by the moment of an exposition. Your task is to determine for each of the options of exposition location and time how many cars will be able to get there by the beginning of an exposition.

#### Input

The first line of input contains three integers k, n, q ( $2 \le k \le 10$ ,  $1 \le n \le 10^5$ ,  $1 \le q \le 10^5$ ), the number of engines of «Lada Malina», number of factories producing «Lada Malina» and number of options of an exposition time and location respectively.

The following k lines contain the descriptions of «Lada Malina» engines. The i-th of them contains two integers  $vx_i$ ,  $vy_i$  ( $-1000 \le vx_i$ ,  $vy_i \le 1000$ ) defining the velocity vector of the i-th engine. Velocity vector can't be zero, i.e. at least one of  $vx_i$  and  $vy_i$  is not equal to zero. It is guaranteed that no two velosity vectors are collinear (parallel).

Next n lines contain the descriptions of factories. The i-th of them contains two integers  $fx_i$ ,  $fy_i$ ,  $a_i$   $(-10^9 \le fx_i, fy_i \le 10^9, 1 \le a_i \le 10^9)$  defining the coordinates of the i-th factory location and the number of cars that are located there.

The following q lines contain the descriptions of the car exposition. The i-th of them contains three integers  $px_i$ ,  $py_i$ ,  $t_i$  ( $-10^9 \le px_i$ ,  $py_i \le 10^9$ ,  $1 \le t_i \le 10^5$ ) defining the coordinates of the exposition location and the number of days till the exposition start in the i-th option.

## Output

For each possible option of the exposition output the number of cars that will be able to get to the exposition location by the moment of its beginning.

## **Examples**

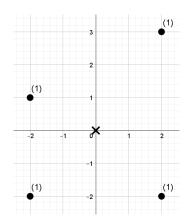
standard input	standard output
2 4 1	3
1 1	
-1 1	
2 3 1	
2 -2 1	
-2 1 1	
-2 -2 1	
0 0 2	
3 4 3	4
2 0	9
-1 1	0
-1 -2	
-3 0 6	
1 -2 1	
-3 -7 3	
3 2 2	
-1 -4 1	
0 4 2	
6 0 1	

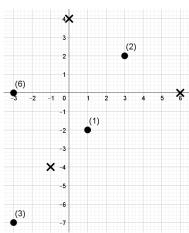
## Note

Images describing sample tests are given below. Exposition options are denoted with crosses, factories are denoted with points. Each factory is labeled with a number of cars that it has.

First sample test explanation:

- Car from the first factory is not able to get to the exposition location in time.
- Car from the second factory can get to the exposition in time if we set  $w_1 = 0$ ,  $w_2 = 1$ .
- Car from the third factory can get to the exposition in time if we set  $w_1 = \frac{1}{4}$ ,  $w_2 = \frac{3}{4}$ .
- Car from the fourth factory can get to the exposition in time if we set  $w_1 = 1$ ,  $w_2 = 0$ .





# Scoring

Tests for this problem are divided into six groups. For each of the groups you earn points only if your solution passes all tests in this group and all tests in some of the previous groups.

Croup	Points	Additional constraint		Required	Commont
Group	Pollits	n,q	k	groups	Comment
0	0	_	_	_	Sample tests
1	15	$n, q \le 1000$	k=2	_	$vx_1 = 1, vy_1 = 1, vx_2 = -1, vy_2 = 1$
2	15	$n, q \le 1000$	k=2	1	
3	20	$n, q \le 1000$	_	0 - 2	
4	15	_	k=2	1	$vx_1 = 1, vy_1 = 1, vx_2 = -1, vy_2 = 1$
5	15	_	k=2	1, 2, 4	
6	20	_	_	0-5	