# Epistemology of BTC

This notebook serves to analyze best approaches to explaining BTC.

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## Raw data

This data comes from the file “btc-epistemology.xlsx”. Just copy the range that includes the subjects column and the prerequisite “1” marks.

In[34]:=
```
exceldata = "block
    1        1    1                                  1

block reward    1        1
    1    1               1        1    1

blockchain    1            1
    1                        1

block time    1
    1    1

change
    1                                        1    1    1    1

change address
    1                                             1    1    1            1

coinbase tx    1    1
    1            1    1    1    1            1

halving        1        1
    1            1        1

hashing
    1

issuance        1    1    1            1
    1               1           1        1

mempool    1        1
```

```
    1                              1

mining    1    1    1                1
    1        1        1    1    1                1    1

mining difficulty    1            1
    1                    1    1

mining diff adj                1
    1            1    1        1

proof of work            1
    1            1    1

receive
    address
                 1            1

satoshi
         1

transaction    1                1
    1                    1                    1    1        1

tx fee
    1        1    1

transactions
    1
    1            1

utxo             1        1
    1    1    1
";

rawdata = ImportString[
  StringReplace[
   StringReplace[
    StringReplace[
     StringReplace[
      StringReplace[exceldata, {
        "\t\n" → ", 0\n"
        , "\t" → ", "
       }
      ]
      , {
       ", ," → ", 0,"
```

```
      }]
     , {
      ", ," → ", 0,"
     }]
    , {",  " → ", 0"}
   ]
   , "\n\n" → "\n"
  ]
  , "CSV"
 ]
```

Out[35]=

```
{{block, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0},
 {block reward, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 1, 0},
 {blockchain, 1, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0},
 {block time, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0},
 {change, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 0},
 {change address, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 1},
 {coinbase tx, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1},
 {halving, 0, 1, 0, 1, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0},
 {hashing, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0},
 {issuance, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 0, 0},
 {mempool, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0},
 {mining, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0},
 {mining difficulty, 1, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0},
 {mining diff adj, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0},
 {proof of work, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0},
 {receive address, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1},
 {satoshi, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0},
 {transaction, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 1, 0, 0},
 {tx fee, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0},
 {transactions, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1},
 {utxo, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0}}
```

In[36]:=
```
subjects = rawdata[[All, 1]];
data =  rawdata[[All, 2 ;;]];
```

In[38]:=
```
literals =
  Sort[Flatten[List[subjects[[#[[1]]]] → subjects[[#[[2]]]]] & /@ Position[data, 1]]];
literals // Length
```

Out[39]=

```
100
```

In[40]:=
```
Column[literals]
```

Out[40]=

```
block → hashing
block → mempool
block → mining
block → transactions
blockchain → block
```

blockchain → block time
blockchain → hashing
blockchain → proof of work
block reward → block
block reward → blockchain
block reward → mining
block reward → mining difficulty
block reward → satoshi
block reward → transactions
block reward → tx fee
block time → block
block time → mining
block time → mining difficulty
change → change address
change → receive address
change → satoshi
change → transaction
change → tx fee
change address → change
change address → receive address
change address → satoshi
change address → transaction
change address → utxo
coinbase tx → block
coinbase tx → block reward
coinbase tx → mining
coinbase tx → proof of work
coinbase tx → receive address
coinbase tx → satoshi
coinbase tx → transaction
coinbase tx → utxo
halving → block reward
halving → block time
halving → coinbase tx
halving → issuance
halving → mining
hashing → proof of work
issuance → blockchain
issuance → block reward
issuance → block time
issuance → coinbase tx
issuance → halving
issuance → mining
issuance → proof of work
issuance → satoshi
mempool → block
mempool → blockchain
mempool → mining
mempool → tx fee
mining → block
mining → blockchain
mining → block reward
mining → coinbase tx
mining → hashing

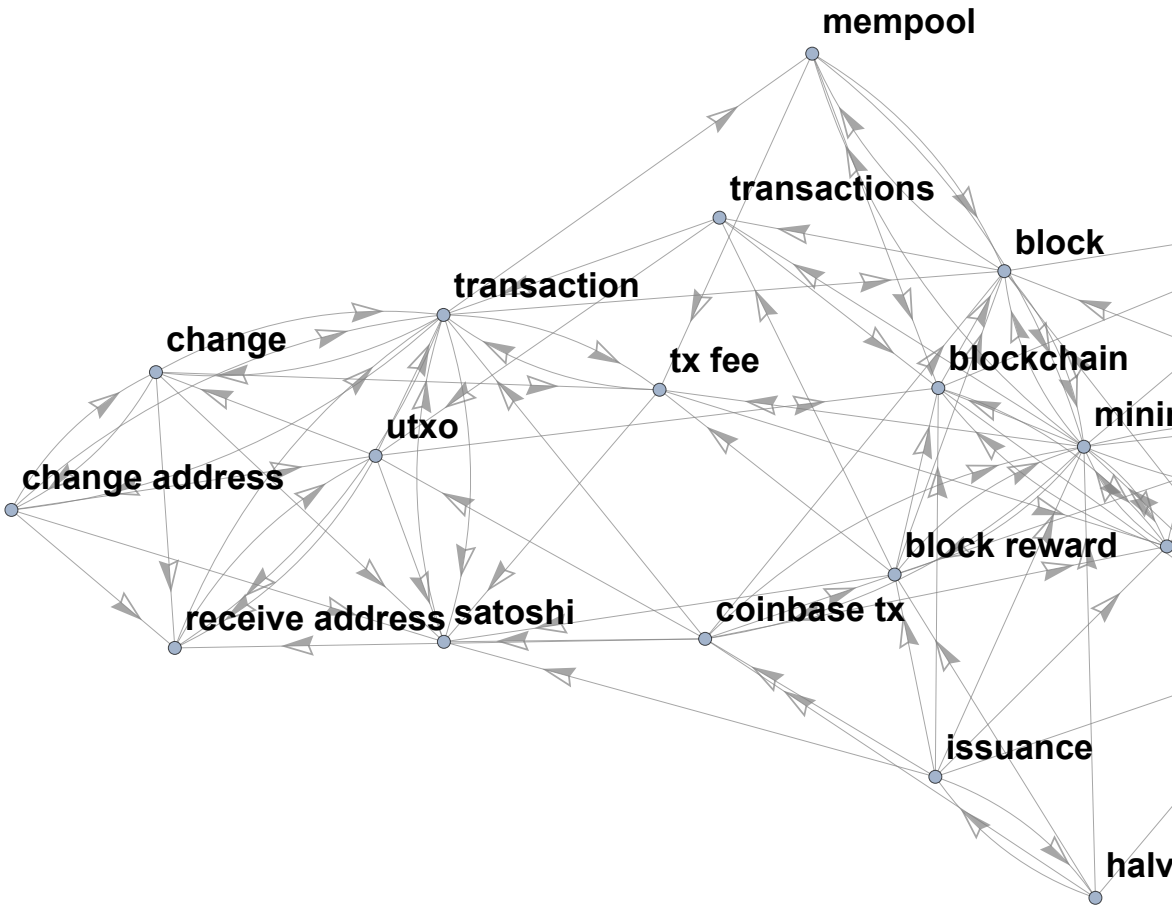
```
mining → mempool
mining → mining diff adj
mining → mining difficulty
mining → proof of work
mining → transactions
mining → tx fee
mining diff adj → block time
mining diff adj → hashing
mining diff adj → mining
mining diff adj → mining difficulty
mining diff adj → proof of work
mining difficulty → block
mining difficulty → block time
mining difficulty → hashing
mining difficulty → mining diff adj
mining difficulty → proof of work
proof of work → blockchain
proof of work → hashing
proof of work → mining
proof of work → mining difficulty
receive address → transaction
receive address → utxo
satoshi → transaction
transaction → block
transaction → change
transaction → change address
transaction → mempool
transaction → receive address
transaction → satoshi
transaction → tx fee
transactions → blockchain
transactions → transaction
transactions → utxo
tx fee → proof of work
tx fee → satoshi
tx fee → transaction
utxo → blockchain
utxo → change
utxo → receive address
utxo → satoshi
utxo → transaction
```

In[41]:=
```
vertices = VertexList[literals]
```

Out[41]=
```
{block, hashing, mempool, mining, transactions, blockchain,
 block time, proof of work, block reward, mining difficulty,
 satoshi, tx fee, change, change address, receive address,
 transaction, utxo, coinbase tx, halving, issuance, mining diff adj}
```

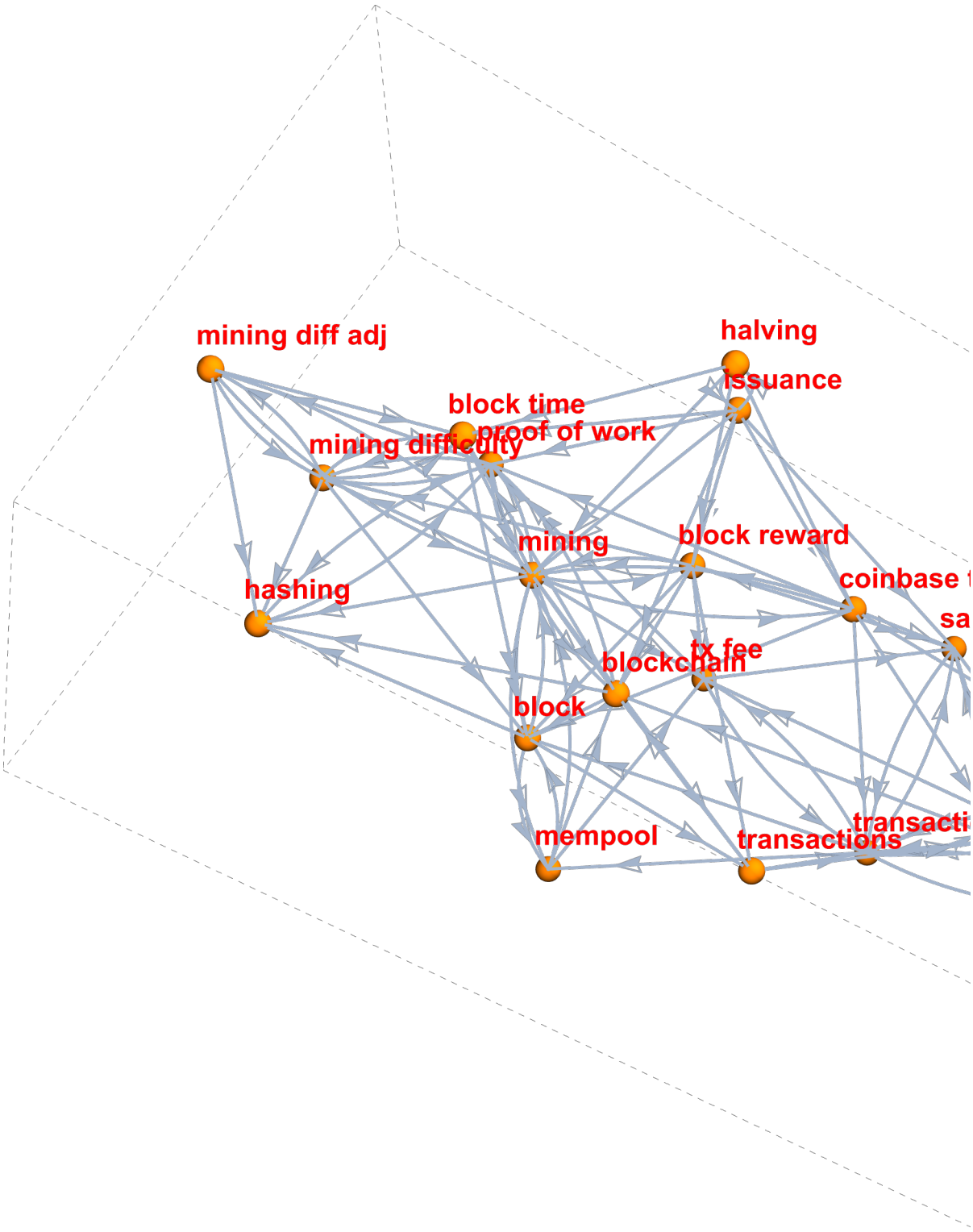
In[42]:=
```
twoD = Graph[
  literals
  , VertexSize → Small
  , VertexLabels → "Name"
  , VertexLabelStyle → Directive[Black, 18, Bold]
  , EdgeStyle → Directive[Gray]
  , EdgeShapeFunction → {{"CarvedArrow", "ArrowSize" → .02}}
 ]
```

Out[42]=




In[43]:=
```
threeD = Graph3D[
  literals
  , Boxed → True
  , BoxStyle → Directive[Dashed]
  , VertexLabels → "Name"
  , VertexLabelStyle → Directive[Red, 18, Bold]
  , VertexSize → 0.2
  , VertexStyle → Orange
  , EdgeStyle → Directive[Thick]
  , EdgeShapeFunction → {{"CarvedArrow", "ArrowSize" → .02}}
 ]
```

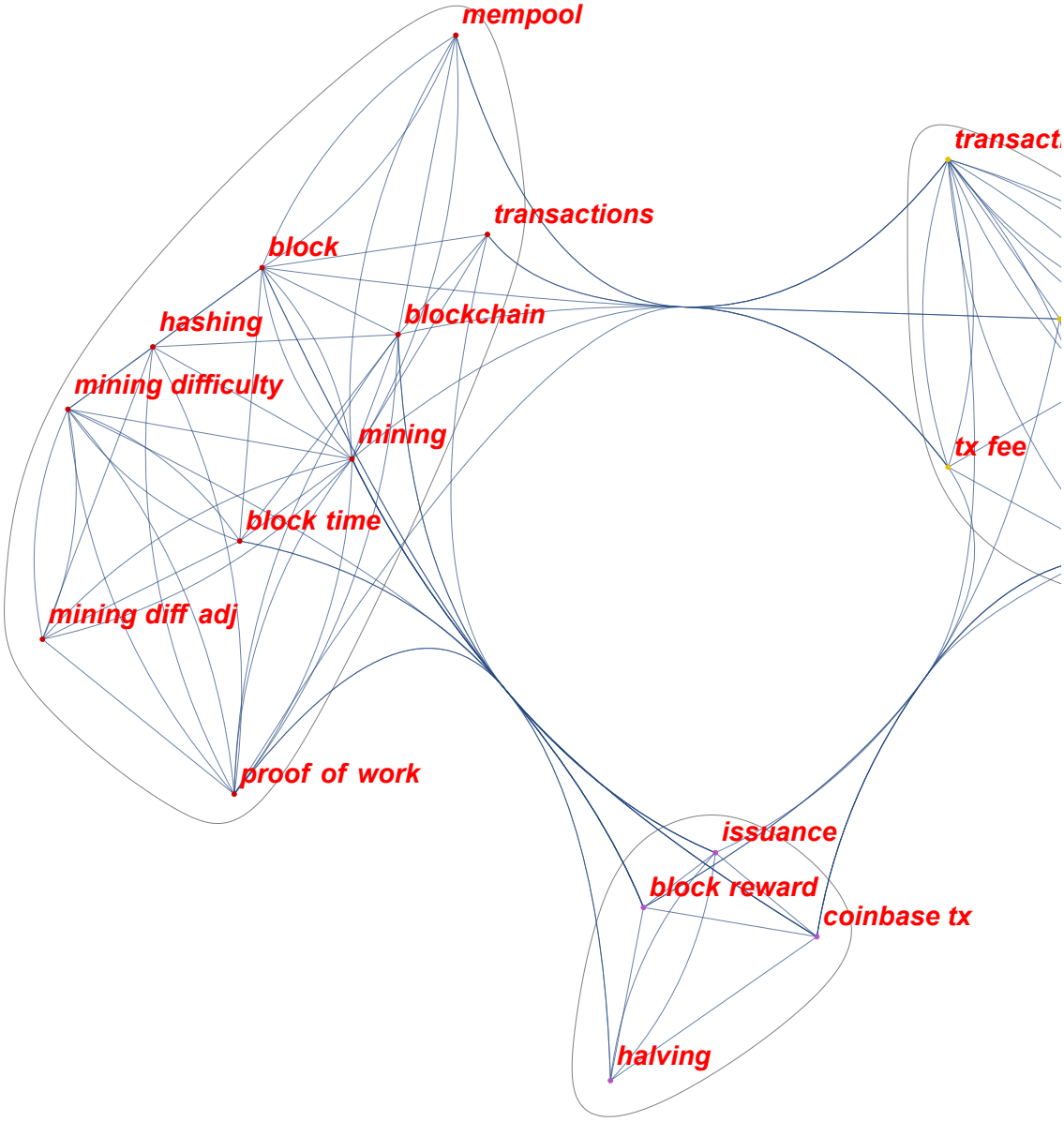
Out[43]=


mining diff adj
halving
issuance
block time
proof of work
mining difficulty
mining
block reward
hashing
coinbase
sa
tx fee
blockchain
block
mempool
transactions
transacti

# Community Graph

In[44]:=
```
CommunityGraphPlot[
 literals
 , ImageSize → 900
 , ImageMargins → 20
 , VertexSize → 0.05
 ,  VertexLabels → "Name"
 , CommunityBoundaryStyle → Automatic
 , VertexLabelStyle → Directive[Red, Italic, Bold, 15]
 (*,EdgeShapeFunction→{{"CarvedArrow","ArrowSize"→.01}}*)
]
```

Out[44]=

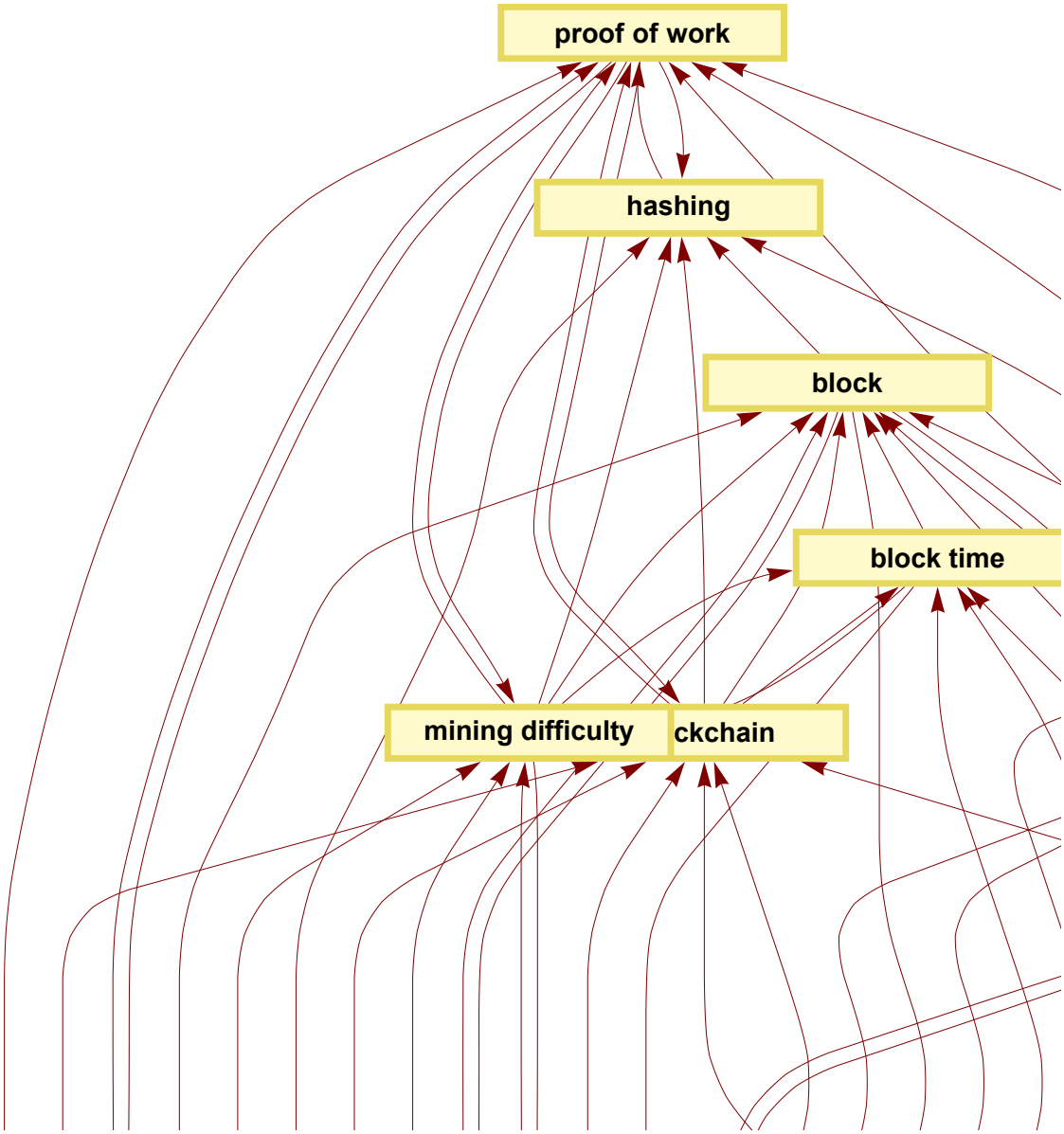


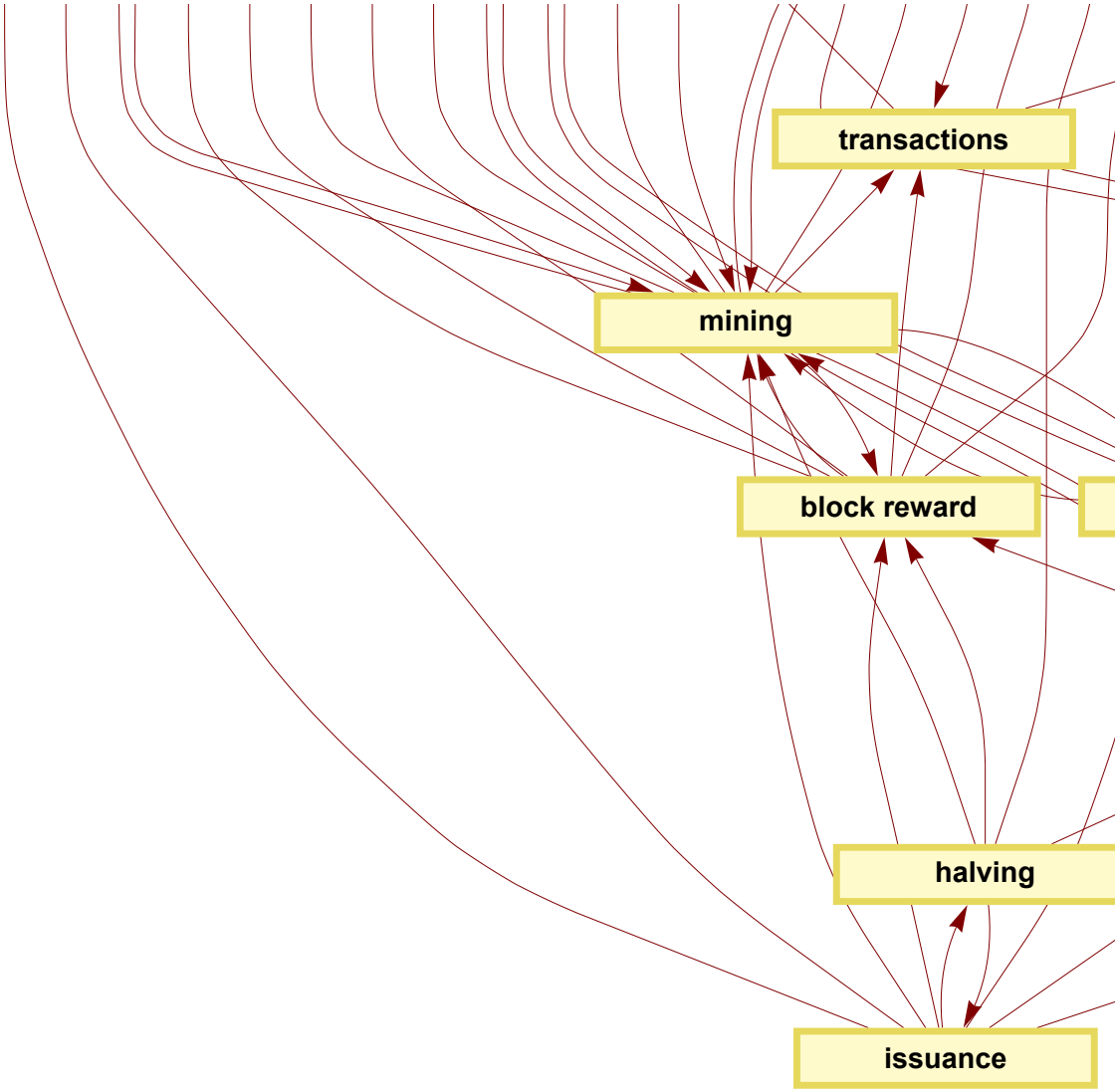

# Layered Graph

In[45]:=

In[46]:=
```
LayeredGraphPlot[
 literals
 , Bottom
 , ImageSize → 1200
 , ImageMargins → 20
 , VertexSize → {2.75, .5}
 , AspectRatio → 1
 , VertexLabelStyle → Directive[Bold, 15]
 (*,VertexSize→0.05
 , VertexLabels→"Name"
 ,EdgeShapeFunction→{{"CarvedArrow","ArrowSize"→.02}}
 *)
 , PlotTheme → "ClassicDiagram"
]
```

Out[46]=






In[47]:=
```
ReverseSortBy[
 Table[{vertices[[x]], VertexDegree[literals][[x]]}, {x, 1, Length[vertices]}], Last]
```

Out[47]=
```
{{mining, 20}, {transaction, 15}, {proof of work, 12}, {block, 12},
 {coinbase tx, 11}, {block reward, 11}, {blockchain, 11}, {mining difficulty, 10},
 {utxo, 9}, {satoshi, 9}, {issuance, 9}, {tx fee, 8}, {change, 8},
 {block time, 8}, {receive address, 7}, {mining diff adj, 7}, {mempool, 7},
 {hashing, 7}, {change address, 7}, {transactions, 6}, {halving, 6}}
```

# Scoring prerequisites and complexities

## Prerequisites Scores

In[48]:=
```
prerequisites = AssociationThread @@ (ReverseSortBy[
        Table[{
          vertices⟦x⟧
          , VertexInDegree[literals]⟦x⟧}
         , {x, 1, Length[vertices]
         }]
        , Last]
       // Transpose
   );
prerequisites // Dataset[
    #
    , ItemStyle → {Black}
    , HeaderStyle → Bold
    , HeaderBackground → LightYellow
    , MaxItems → (vertices // Length)
   ] &
```

Out[49]=

| | |
|---|---|
| **mining** | 9 |
| **transaction** | 8 |
| **satoshi** | 8 |
| **proof of work** | 8 |
| **block** | 8 |
| **blockchain** | 7 |
| **hashing** | 6 |
| **tx fee** | 5 |
| **receive address** | 5 |
| **mining difficulty** | 5 |
| **block time** | 5 |
| **utxo** | 4 |
| **block reward** | 4 |
| **transactions** | 3 |
| **mempool** | 3 |
| **coinbase tx** | 3 |
| **change** | 3 |
| **mining diff adj** | 2 |
| **change address** | 2 |
| **issuance** | 1 |
| **halving** | 1 |

## Complexity Scores

In[50]:=
```
complexity = AssociationThread @@ (ReverseSortBy[
       Table[{
         vertices[[x]]
         , VertexOutDegree[literals][[x]]}
        , {x, 1, Length[vertices]}]
       , Last
      ]
      // Transpose
   );
complexity // Dataset[#, ItemStyle → {Black}, HeaderStyle → Bold,
   HeaderBackground → LightYellow, MaxItems → (vertices // Length)] &
```

Out[51]=

| | |
|---|---|
| **mining** | 11 |
| **issuance** | 8 |
| **coinbase tx** | 8 |
| **transaction** | 7 |
| **block reward** | 7 |
| **utxo** | 5 |
| **mining difficulty** | 5 |
| **mining diff adj** | 5 |
| **halving** | 5 |
| **change address** | 5 |
| **change** | 5 |
| **proof of work** | 4 |
| **mempool** | 4 |
| **blockchain** | 4 |
| **block** | 4 |
| **tx fee** | 3 |
| **transactions** | 3 |
| **block time** | 3 |
| **receive address** | 2 |
| **satoshi** | 1 |
| **hashing** | 1 |

## Prerequisite minus Complexity Scores

In[52]:=
```
ReverseSort[Merge[{prerequisites, -complexity}, Total]] //
 Dataset[#, ItemStyle → {Black}, HeaderStyle → Bold,
   HeaderBackground → LightYellow, MaxItems → (vertices // Length)] &
```

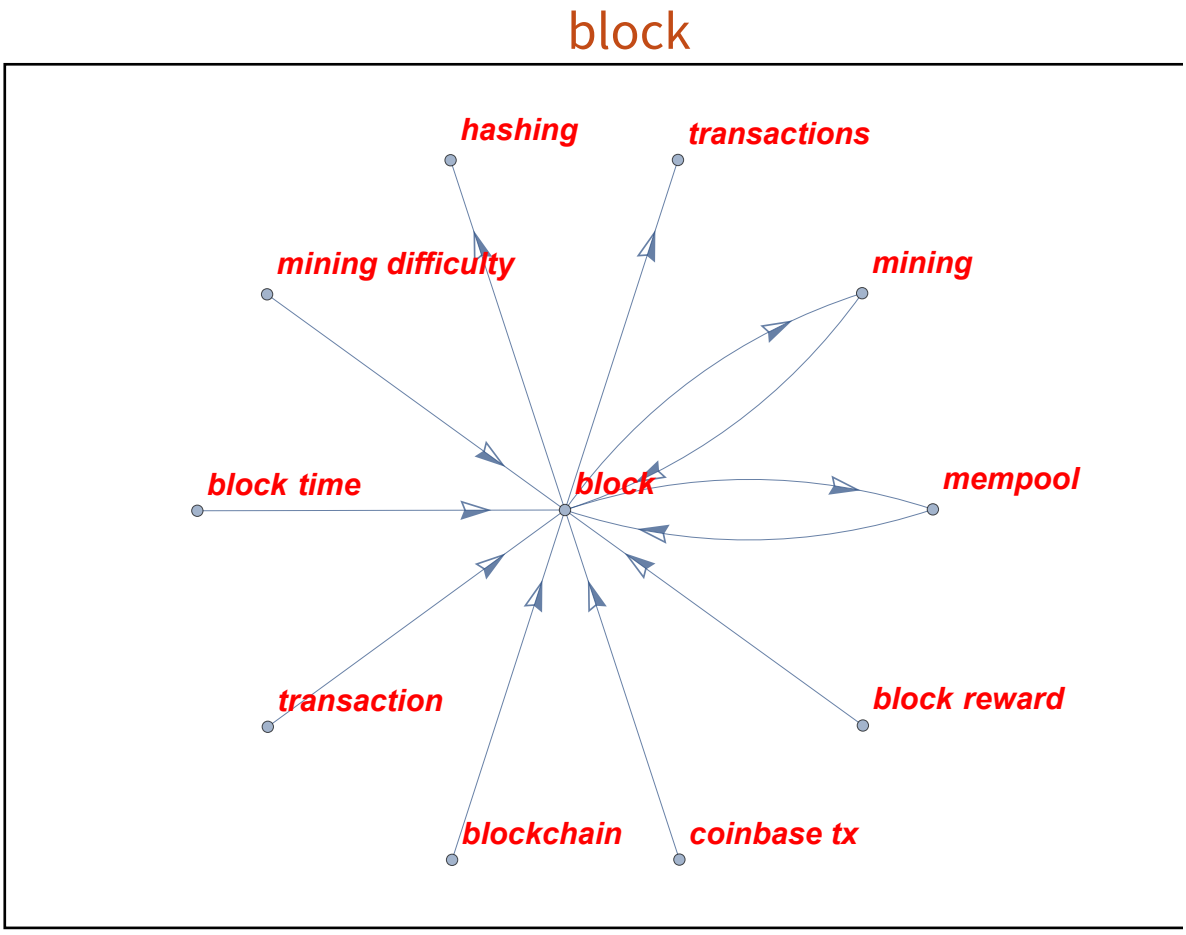
Out[52]=

| | |
|---|---|
| **satoshi** | 7 |
| **hashing** | 5 |
| **block** | 4 |
| **proof of work** | 4 |
| **receive address** | 3 |
| **blockchain** | 3 |
| **block time** | 2 |
| **tx fee** | 2 |
| **transaction** | 1 |
| **transactions** | 0 |
| **mining difficulty** | 0 |
| **mempool** | −1 |
| **utxo** | −1 |
| **change** | −2 |
| **mining** | −2 |
| **change address** | −3 |
| **mining diff adj** | −3 |
| **block reward** | −3 |
| **halving** | −4 |
| **coinbase tx** | −5 |
| **issuance** | −7 |

# Vertex views

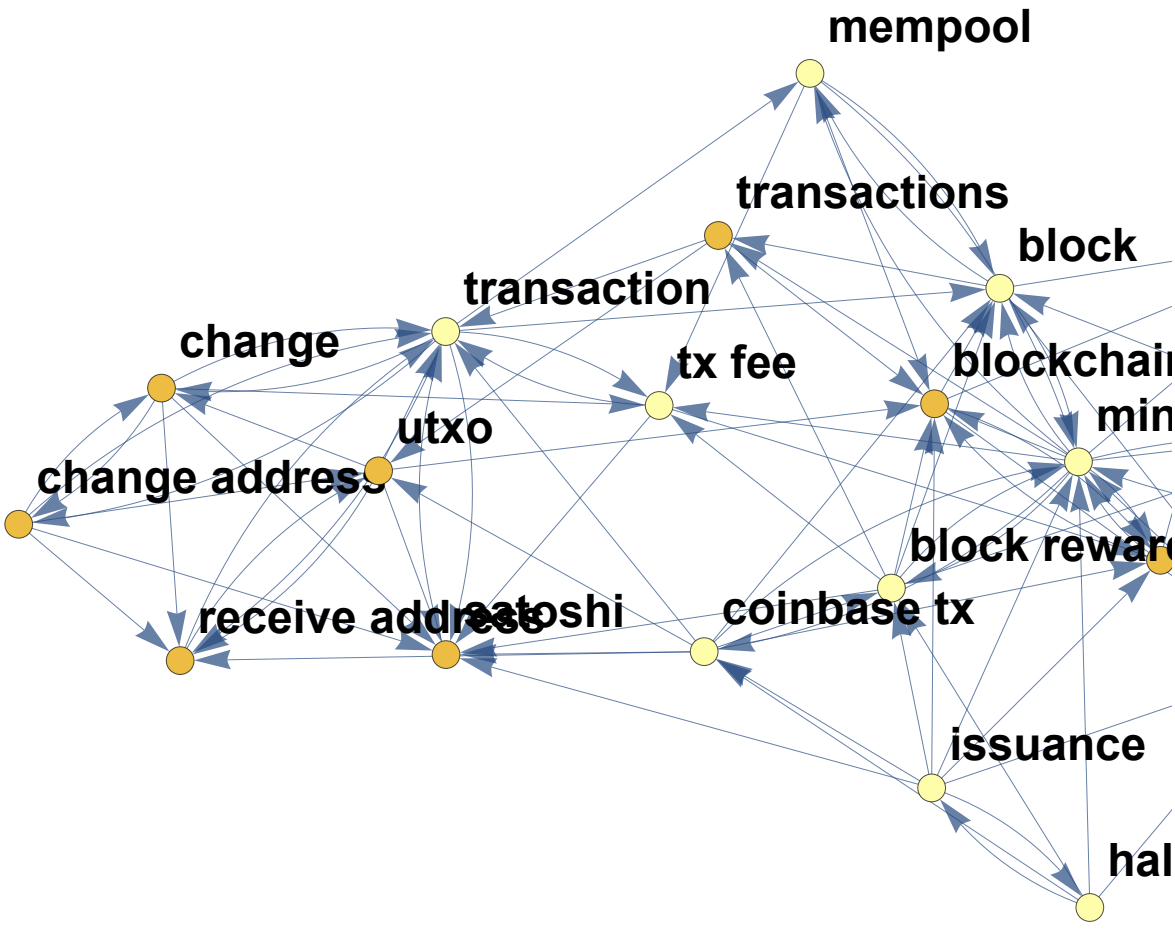
In[68]:=
```
Table[
 Labeled[
  Framed[
   Graph[
    Select[literals, #[[1]] == x || #[[2]] == x &]
    , ImageSize → {600, 400}
    , ImageMargins → 20
    , VertexSize → 0.05
    , VertexLabels → "Name"
    , VertexLabelStyle → Directive[Red, Italic, Bold, 16]
    , EdgeShapeFunction → {{"CarvedArrow", "ArrowSize" → .04}}
   ]
  ]
  , x
  , Top
  , LabelStyle → "Section"
 ]
 , {x, vertices}
]
```

Out[68]=



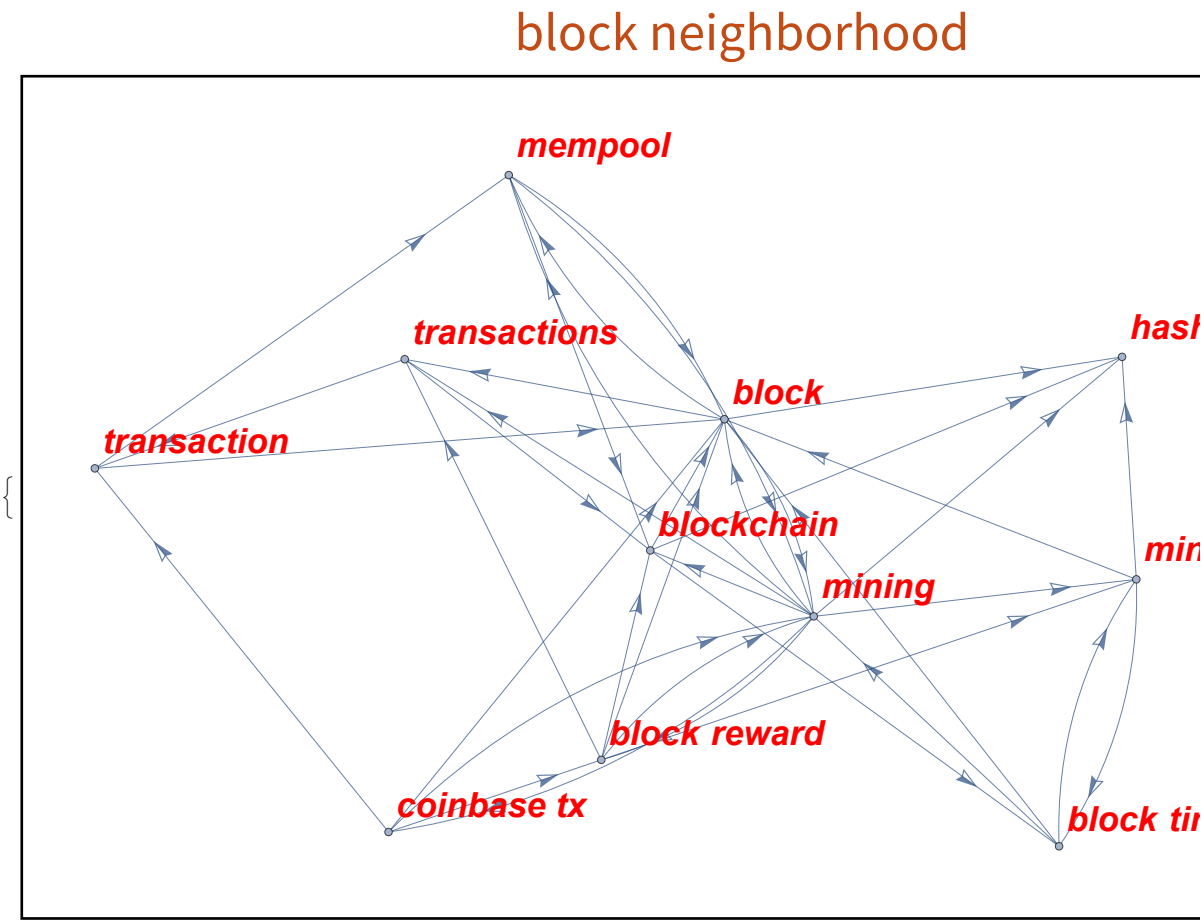
In[54]:=
```
literals // Length
```
Out[54]=
```
100
```

In[55]:=
```
ve = Table[VertexEccentricity[literals, v], {v, vertices}];
HighlightGraph[literals, Table[
  Style[v, ColorData["TemperatureMap", ve[[VertexIndex[literals, v]]] / Max[ve]]],
  {v, vertices}], VertexLabels → "Name",
 VertexLabelStyle → Directive[Black, 24, Bold]]
```
Out[56]=



In[57]:=
```
Table[
 Labeled[
  Framed[
   NeighborhoodGraph[
    literals
    , x
    , ImageSize → 700
    , ImageMargins → 20
    , VertexSize → 0.05
    , VertexLabels → "Name"
    , VertexLabelStyle → Directive[Red, Italic, Bold, 18]
    , EdgeShapeFunction → {{"CarvedArrow", "ArrowSize" → .02}}
   ]
  ]
  , StringJoin[x, " neighborhood"]
  , Top
  , LabelStyle → "Section"
 ]
 , {x, vertices // Sort}
]
```

Out[57]=



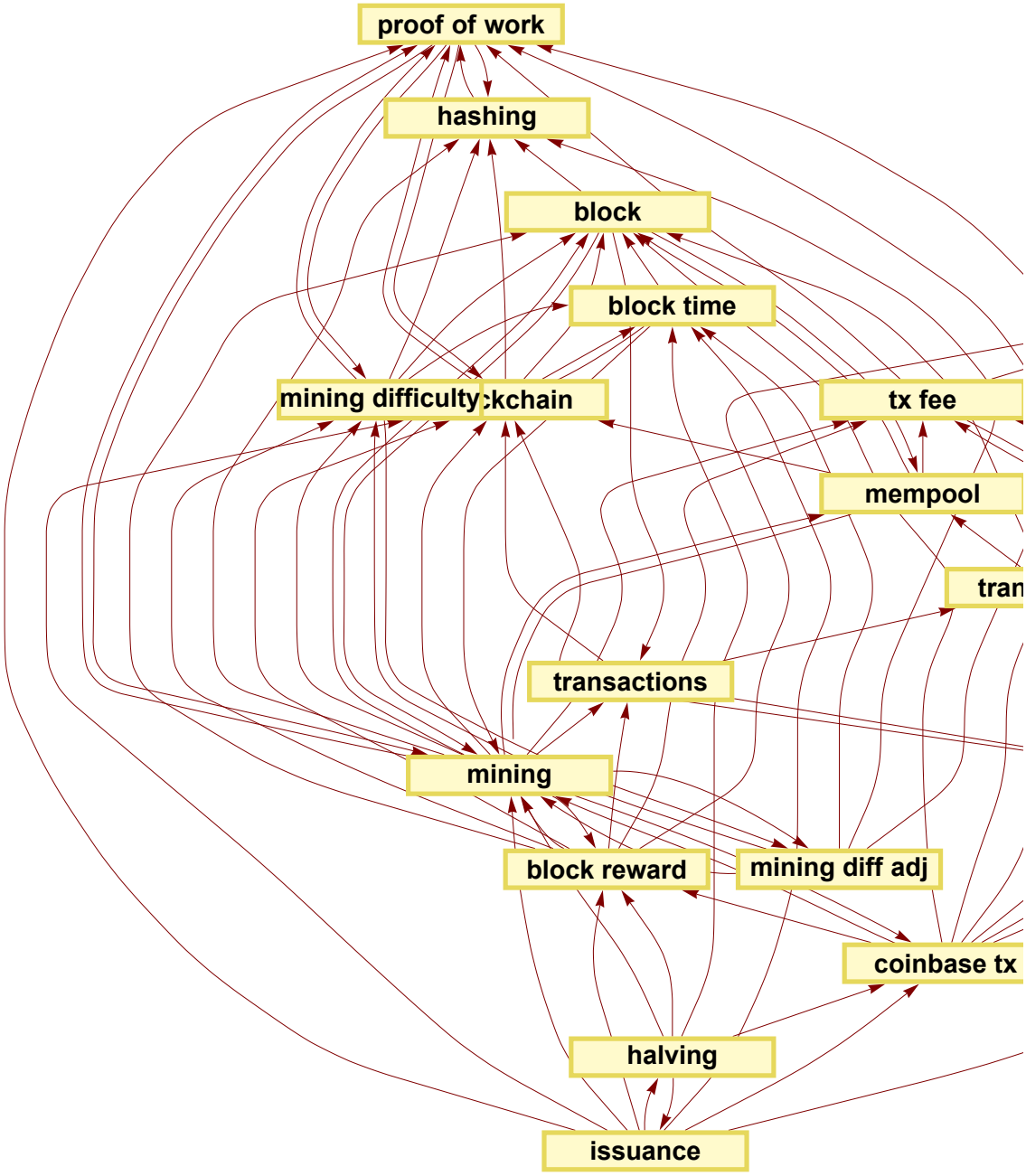

In[58]:=
```
AssociationThread[VertexList[literals], VertexDegree[literals]] // ReverseSort
```

Out[58]=

```
⟨| mining → 20, transaction → 15, proof of work → 12,
 block → 12, coinbase tx → 11, block reward → 11, blockchain → 11,
 mining difficulty → 10, issuance → 9, utxo → 9, satoshi → 9, change → 8,
 tx fee → 8, block time → 8, mining diff adj → 7, receive address → 7,
 change address → 7, mempool → 7, hashing → 7, halving → 6, transactions → 6 |⟩
```

In[33]:=
```
LayeredGraphPlot[
 literals
 , Bottom
 , ImageSize → 900
 , ImageMargins → 20
 , VertexSize → {2.75, .5}
 , AspectRatio → 0.75
 , VertexLabelStyle → Directive[Bold, 15]
 (*,VertexSize→0.05
 , VertexLabels→"Name"
 ,EdgeShapeFunction→{{"CarvedArrow","ArrowSize"→.02}}
 *)
 , PlotTheme → "ClassicDiagram"
]
```

Out[33]=


proof of work
hashing
block
block time
mining difficulty
ckchain
tx fee
mempool
tran
transactions
mining
block reward
mining diff adj
coinbase tx
halving
issuance