MODULE *syncCon*1

EXTENDS *Integers*, *Sequences*, *FiniteSets*, *TLC*

CONSTANTS N, $FAILNUM$

ASSUME $N \leq 5 \land 0 \leq FAILNUM \land FAILNUM \leq 4$

$Nodes \triangleq 1 \,..\, N$

```
--algorithm syncCon1
{ variable FailNum = FAILNUM,
           up = [n ∈ Nodes ↦ TRUE];
           pt = [n ∈ Nodes ↦ 0];
           t = [n ∈ Nodes ↦ FALSE];
           d = [n ∈ Nodes ↦ -1];
           mb = [n ∈ Nodes ↦ {}];
  define {
    SetMin(S) ≜ CHOOSE i ∈ S : ∀ j ∈ S : i ≤ j
  }
  macro MayBeFail( ) {
    if ( FailNum > 0 ∧ up[self] ) {
        either {
                 up[self] := FALSE;
                 FailNum := FailNum - 1;
                 }
        or skip;
    } ;
  }

  fair process ( n ∈ Nodes )
  variable v = 0, pv = 0, Q = {};
  {
  P: if ( up[self] ) {
       v := self;
       Q := Nodes;

  PS:    while ( up[self] ∧ Q ≠ {} ) {
           with ( p ∈ Q ) {
              Node can fail here, such that up[self] will be set to False
              A process can fail anytime during the broadcast
             MayBeFail();
              Pop process p from Q
             Q := Q \ {p};
             if ( up[self] ) {
                 mb[p] := mb[p] ∪ {v};     Broadcast value of self to each process if self is up
              }
           } ;
         } ;
```

```
            A node may fail after broadcast
            MayBeFail() ;

            Increase the number of rounds that are completed if the node is up
            if ( up[self] ) {
                pt[self] := pt[self] + 1 ;
            } ;

            To await, a process must be up and every other process should be on the same round
            Wait for others to move to next round
            If the node is down, exit.
PR:         await (up[self] = FALSE ∨ (up[self] ∧ (∀ i ∈ Nodes : IF up[i] THEN pt[i] = pt[self] ELSE TRUE))) ;

            Terminate and compute decision if the node is up
            if ( up[self] ) {
                d[self] := SetMin(mb[self]) ;
                t[self] := TRUE ;
            }
        } ;
    }
}
```

BEGIN TRANSLATION

VARIABLES $FailNum$, up, pt, t, d, mb, pc

define statement

$SetMin(S) \triangleq$ CHOOSE $i \in S : \forall\, j \in S : i \leq j$

VARIABLES v, pv, Q

$vars \triangleq \langle FailNum,\ up,\ pt,\ t,\ d,\ mb,\ pc,\ v,\ pv,\ Q \rangle$

$ProcSet \triangleq (Nodes)$

$Init \triangleq$ Global variables

$\land\ FailNum = FAILNUM$
$\land\ up = [n \in Nodes \mapsto \text{TRUE}]$
$\land\ pt = [n \in Nodes \mapsto 0]$
$\land\ t = [n \in Nodes \mapsto \text{FALSE}]$
$\land\ d = [n \in Nodes \mapsto -1]$
$\land\ mb = [n \in Nodes \mapsto \{\}]$

Process n

$\land\ v = [self \in Nodes \mapsto 0]$
$\land\ pv = [self \in Nodes \mapsto 0]$
$\land\ Q = [self \in Nodes \mapsto \{\}]$
$\land\ pc = [self \in ProcSet \mapsto \text{“P”}]$

$P(self) \triangleq \land\ pc[self] = \text{“P”}$

$\land$ IF $up[self]$
THEN $\land\ v' = [v$ EXCEPT $![self] = self]$
$\land\ Q' = [Q$ EXCEPT $![self] = Nodes]$
$\land\ pc' = [pc$ EXCEPT $![self] = \text{“PS”}]$
ELSE $\land\ pc' = [pc$ EXCEPT $![self] = \text{“Done”}]$
$\land\ \text{UNCHANGED}\ \langle v,\ Q\rangle$
$\land$ UNCHANGED $\langle FailNum,\ up,\ pt,\ t,\ d,\ mb,\ pv\rangle$

$PS(self) \triangleq$ $\land\ pc[self] = \text{“PS”}$
$\land$ IF $up[self] \land Q[self] \neq \{\}$
THEN $\land \exists\, p \in Q[self]:$
$\land$ IF $FailNum > 0 \land up[self]$
THEN $\land\ \lor\ \land\ up' = [up$ EXCEPT $![self] = \text{FALSE}]$
$\land\ FailNum' = FailNum - 1$
$\lor\ \land$ TRUE
$\land$ UNCHANGED $\langle FailNum,\ up\rangle$
ELSE $\land$ TRUE
$\land$ UNCHANGED $\langle FailNum,\ up\rangle$
$\land\ Q' = [Q$ EXCEPT $![self] = Q[self] \setminus \{p\}]$
$\land$ IF $up'[self]$
THEN $\land\ mb' = [mb$ EXCEPT $![p] = mb[p] \cup \{v[self]\}]$
ELSE $\land$ TRUE
$\land\ mb' = mb$
$\land\ pc' = [pc$ EXCEPT $![self] = \text{“PS”}]$
$\land\ pt' = pt$
ELSE $\land$ IF $FailNum > 0 \land up[self]$
THEN $\land\ \lor\ \land\ up' = [up$ EXCEPT $![self] = \text{FALSE}]$
$\land\ FailNum' = FailNum - 1$
$\lor\ \land$ TRUE
$\land$ UNCHANGED $\langle FailNum,\ up\rangle$
ELSE $\land$ TRUE
$\land$ UNCHANGED $\langle FailNum,\ up\rangle$
$\land$ IF $up'[self]$
THEN $\land\ pt' = [pt$ EXCEPT $![self] = pt[self] + 1]$
ELSE $\land$ TRUE
$\land\ pt' = pt$
$\land\ pc' = [pc$ EXCEPT $![self] = \text{“PR”}]$
$\land$ UNCHANGED $\langle mb,\ Q\rangle$
$\land$ UNCHANGED $\langle t,\ d,\ v,\ pv\rangle$

$PR(self) \triangleq$ $\land\ pc[self] = \text{“PR”}$
$\land\ (up[self] = \text{FALSE} \lor (up[self] \land (\forall\, i \in Nodes : \text{IF}\ up[i]\ \text{THEN}\ pt[i] = pt[self]\ \text{ELSE}\ \text{TRUE})))$
$\land$ IF $up[self]$
THEN $\land\ d' = [d$ EXCEPT $![self] = SetMin(mb[self])]$
$\land\ t' = [t$ EXCEPT $![self] = \text{TRUE}]$

$$
\begin{array}{l}
\quad \text{ELSE} \quad \land \text{TRUE} \\
\qquad\qquad \land \text{UNCHANGED } \langle t,\ d \rangle \\
\land\ pc' = [pc \text{ EXCEPT } ![self] = \text{“Done”}] \\
\land \text{UNCHANGED } \langle FailNum,\ up,\ pt,\ mb,\ v,\ pv,\ Q \rangle
\end{array}
$$

$$n(self) \triangleq P(self) \lor PS(self) \lor PR(self)$$

$$
\begin{array}{l}
Next \triangleq (\exists\, self \in Nodes : n(self)) \\
\qquad \lor \quad \text{Disjunct to prevent deadlock on termination} \\
\qquad\quad ((\forall\, self \in ProcSet : pc[self] = \text{“Done”}) \land \text{UNCHANGED } vars)
\end{array}
$$

$$
\begin{array}{l}
Spec \triangleq \land\ Init \land \Box[Next]_{vars} \\
\qquad\quad \land \forall\, self \in Nodes : \mathrm{WF}_{vars}(n(self))
\end{array}
$$

Agreement invariant
The nodes that have terminated (up nodes) have the same decision values

$$Agreement \triangleq \forall\, i \in Nodes : \forall\, j \in Nodes : \text{IF } t[i] \land t[j] \text{ THEN } d[i] = d[j] \text{ ELSE TRUE}$$

Termination property
If the node is up, it has terminated (its t is TRUE) otherwise it has not terminated

$$Termination \triangleq \Diamond(\forall\, i \in Nodes : \text{IF } up[i] \text{ THEN } t[i] = \text{TRUE ELSE } t[i] = \text{FALSE})$$

END TRANSLATION

END TRANSLATION

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Explanation: Agreement Property: The nodes that have terminated (up nodes) have the same decision values

- The agreement property is satisfied when $FAILNUM = 0$

We take 3 *Nodes* in the system and check for $FAILNUM = 1$ ie 1 node crashes out of the 3 nodes. In this scenario the final state at which the *Agreement* Invariant is violated is:

$\land\ FailNum = 0$
$\land\ Q = \langle \{3\},\ \{\},\ \{\} \rangle$
$\land\ d = \langle -1,\ 1,\ 2 \rangle$
$\land\ mb = \langle \{2,\ 3\},\ \{1,\ 2,\ 3\},\ \{2,\ 3\} \rangle$
$\land\ pc = \langle \text{“PS”},\ \text{“Done”},\ \text{“Done”} \rangle$
$\land\ pt = \langle 0,\ 1,\ 1 \rangle$
$\land\ pv = \langle 0,\ 0,\ 0 \rangle$
$\land\ t = \langle \text{FALSE},\ \text{TRUE},\ \text{TRUE} \rangle$
$\land\ up = \langle \text{FALSE},\ \text{TRUE},\ \text{TRUE} \rangle$
$\land\ v = \langle 1,\ 2,\ 3 \rangle$

1. In this scenario, when Node 1 fails, it was able to broadcast its value to Node 2 but not to Node 3.
2. Node 2 *terminates*(t = TRUE) with minimum value 1, which was sent by Node 1 (its decision is 1).
3. Node 3 *terminates*(t = TRUE) with minimum value 2 (its decision is 2).
4. Since both have different decision values at termination, it violates the *Agreement* property.
5. Note that Node 1 fails, and we do not set its $t[1]$ to TRUE. It remains FALSE as initially set. The decision of the crashed node is not taken into consideration.

Nodes: 3 and Crash: 2

$\wedge\ FailNum = 1$
$\wedge\ Q = \langle\{3\},\ \{\},\ \{\}\rangle$
$\wedge\ d = \langle -1,\ 1,\ 2\rangle$
$\wedge\ mb = \langle\{2,\ 3\},\ \{1,\ 2,\ 3\},\ \{2,\ 3\}\rangle$
$\wedge\ pc = \langle$"PS", "Done", "Done"$\rangle$
$\wedge\ pt = \langle 0,\ 1,\ 1\rangle$
$\wedge\ pv = \langle 0,\ 0,\ 0\rangle$
$\wedge\ t = \langle$FALSE, TRUE, TRUE$\rangle$
$\wedge\ up = \langle$FALSE, TRUE, TRUE$\rangle$
$\wedge\ v = \langle 1,\ 2,\ 3\rangle$