

Exercise1 Solution

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PartA - 1

Attached at the end of the exercise

PartA - 3

Homography with perfect matches:

```
[[ -1.12313781e-03 -1.64757662e-04  9.99919585e-01]
 [ -1.05117244e-05 -1.05462483e-03  1.25622164e-02]
 [ -2.96940746e-07 -4.35706348e-08 -7.82907867e-04]]
```

PartA2 - 6

The problem with forward mapping is that there are some pixels in the dest image that do not have a source pixel mapped to them. So there are some black pixels in the forward mapping.

PartA2 - 7

We got a different result compared to section 6 because there are outlier matching points in the matches.mat file. So the calculated homography is not correct.

PartB - 10

The number of iterations to achieve an accuracy p is

$k = \ln(1 - p) / \ln(1 - w^n)$ where n is the number of points sufficient to compute the model (which is 4 for homography)

$w=0.8$, $n=4$

For $p=90\%$, $k=5$

For $p=99\%$, $k=9$

To cover all the cases 30 *choose* 4 iterations is needed which is 27405

PartB - 12

The calculated ransac homography:

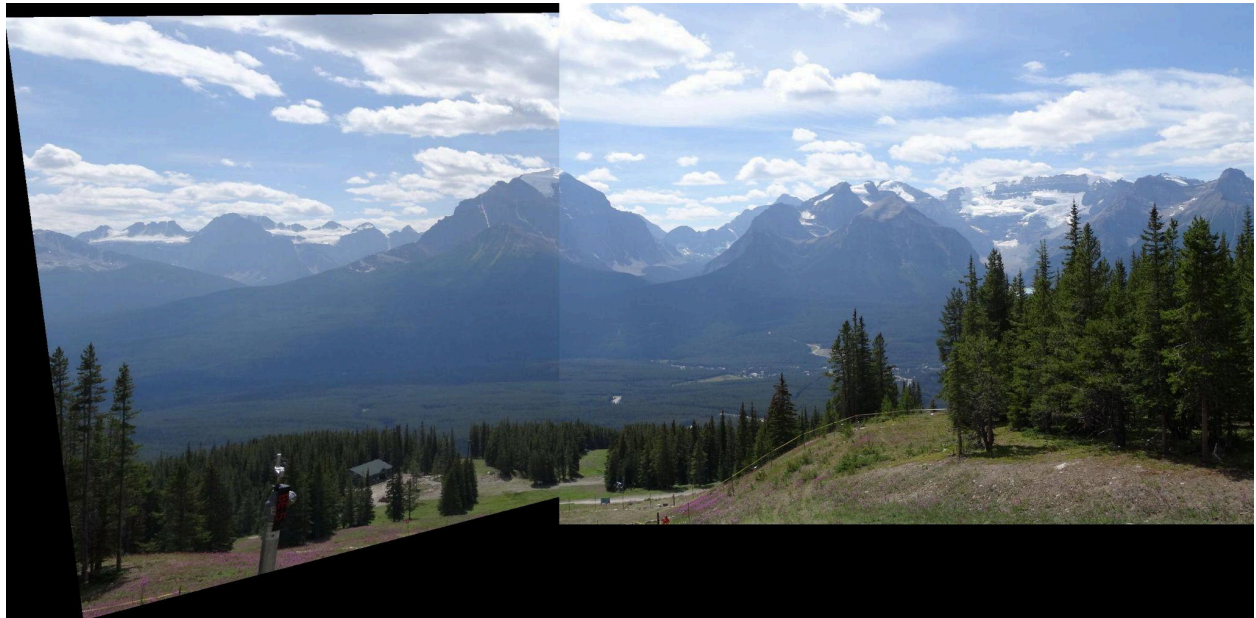
```
[[ 1.12313781e-03  1.64757662e-04 -9.99919585e-01]  
 [ 1.05117245e-05  1.05462483e-03 -1.25622165e-02]  
 [ 2.96940746e-07  4.35706350e-08  7.82907867e-04]]
```

Is identical to the homography calculated using perfect matches in section5.

The homography accuracy is 80%, it makes sense because 80% is the inliers present

Part C

My beautiful panorama:



My images

Panorama



Part1A

$$Ax = b$$

PART A

7

A - Homography

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = \begin{pmatrix} b_1 \\ b_2 \\ 1 \end{pmatrix}$$

due to homogeneous coordinates

$$b_1 = \frac{a_{11}x + a_{12}y + a_{13}}{a_{31}x + a_{32}y + a_{33}} \quad \bigg/ \quad a_{31}x + a_{32}y + a_{33}$$

$$b_2 = \frac{a_{21}x + a_{22}y + a_{23}}{a_{31}x + a_{32}y + a_{33}}$$

$$b_1 \cdot (a_{31}x + a_{32}y + a_{33}) = a_{11}x + a_{12}y + a_{13}$$

$$b_2 \cdot (a_{31}x + a_{32}y + a_{33}) = a_{21}x + a_{22}y + a_{23}$$

Lets put it in matrix form.

$$\begin{pmatrix} x & y & 1 & 0 & 0 & 0 & -b_1x & -b_1y & -b_1 \\ 0 & 0 & 0 & x & y & 1 & -b_2x & -b_2y & -b_2 \end{pmatrix} \begin{pmatrix} a_{11} \\ a_{12} \\ a_{13} \\ a_{21} \\ a_{22} \\ a_{23} \\ a_{31} \\ a_{32} \\ a_{33} \end{pmatrix} = 0$$

Each matching point generates 2 equations.

~~we~~ we will have $2M$ equations where M is the matching point number we can rewrite the systems like

$$M a = 0$$

where a is the vector $\begin{pmatrix} a_{11} \\ \vdots \\ a_{33} \end{pmatrix}$ and M is the system of equations

we don't want a to be the trivial solution
So we set $\|a\|^2 = 1$ and we can do that
because we know a up to a factor

~~because~~ and we want $Ma = 0$ so we can
define the following func to minimize:
 $\min \|Ma\|^2 \quad \|a\|^2$ and the minimum will be

as close to $Ma = 0$ as we can get

So we can define a loss function:

$$L = \|Ma\|^2 - \lambda (\|a\|^2 - 1) \\ = a^T M^T M a - \lambda (a^T a - 1)$$

L derivative
and compare to 0

$$2 M^T M a - \lambda a = 0 \rightarrow \boxed{M^T M a = \lambda a}$$

So we need to find the smallest
eigen value of $M^T M$ and the eigen
vector a .