

Electric Field Definition:

An electric field is a region of space in which an electric charge “feels” a force.

Electric field strength can be calculated using the equation:

$$E = \frac{F}{Q}$$

Where:

E = electric field strength (N/C)

F = electrostatic force on the charge (N)

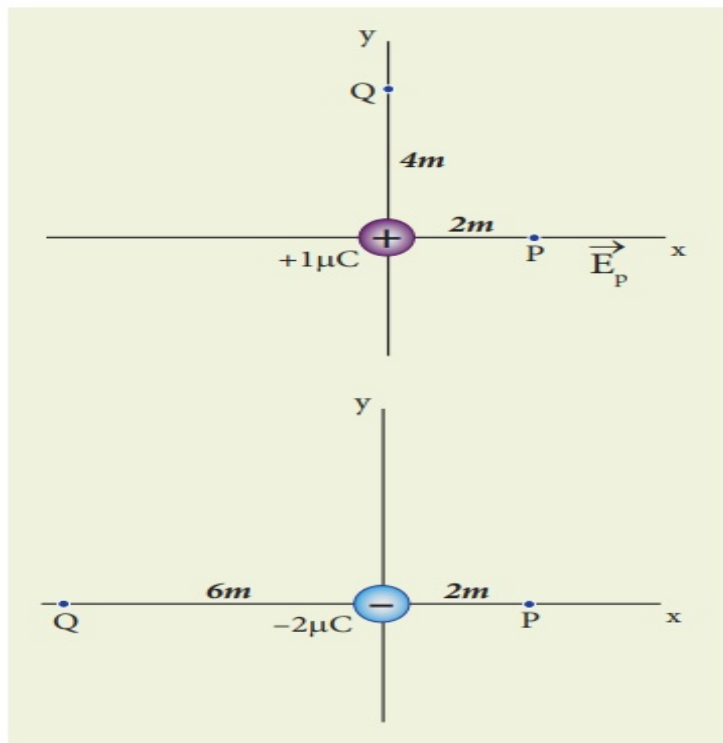
Q = charge (C)

EXAMPLE-1

Calculate the electric field at points P, Q for the following two cases, as shown in the figure.

(a) A positive point charge $+1\ \mu\text{C}$ is placed at the origin

(b) A negative point charge $-2\ \mu\text{C}$ is placed at the origin



Solution

Case (a)

The magnitude of the electric field at point P is

$$E_p = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} = \frac{9 \times 10^9 \times 1 \times 10^{-6}}{4} \\ = 2.25 \times 10^3 \text{ NC}^{-1}$$

Since the source charge is positive, the electric field points away from the charge. So the electric field at the point P is given by

$$\vec{E}_p = 2.25 \times 10^3 \text{ NC}^{-1} \hat{i}$$

For the point Q

$$|\vec{E}_Q| = \frac{9 \times 10^9 \times 1 \times 10^{-6}}{16} = 0.56 \times 10^3 \text{ NC}^{-1}$$

$$\text{Hence } \vec{E}_Q = 0.56 \times 10^3 \hat{j}$$

Case (b)

The magnitude of the electric field at point P

$$|\vec{E}_p| = \frac{kq}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} = \frac{9 \times 10^9 \times 2 \times 10^{-6}}{4} \\ = 4.5 \times 10^3 \text{ N C}^{-1}$$

Since the source charge is negative, the electric field points towards the charge. So the electric field at the point P is given by

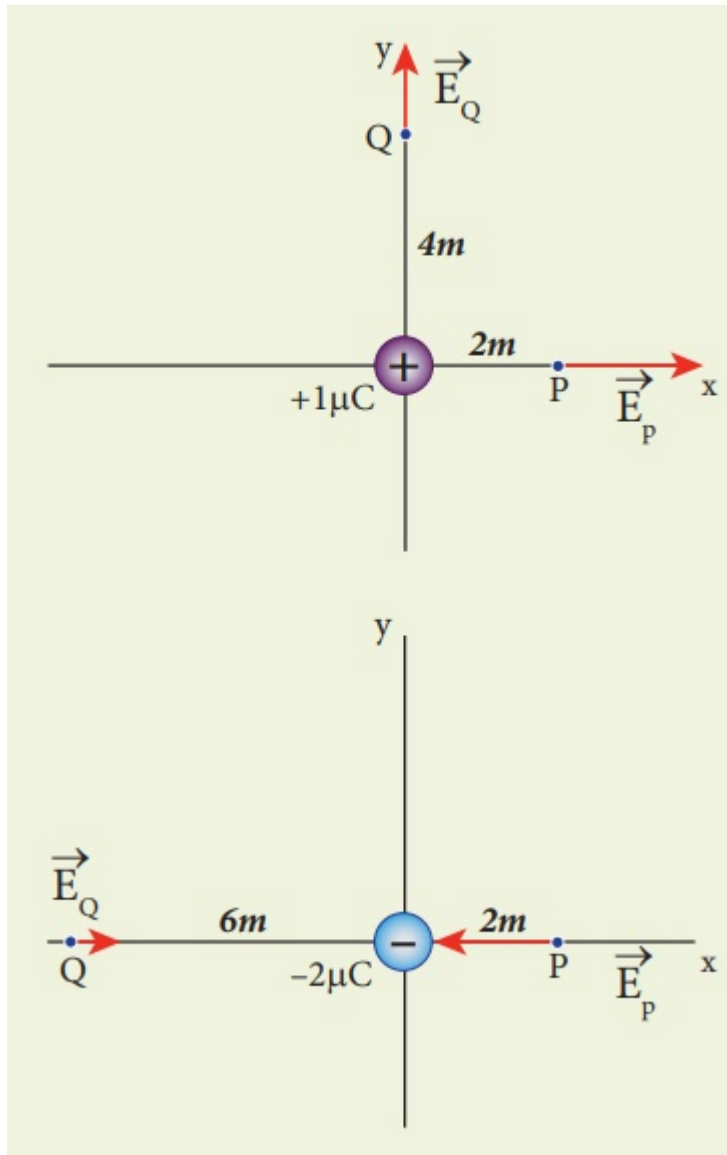
$$\vec{E}_p = -4.5 \times 10^3 \hat{i} \text{ NC}^{-1}$$

$$\text{For the point Q, } |\vec{E}_Q| = \frac{9 \times 10^9 \times 2 \times 10^{-6}}{36}$$

$$= 0.5 \times 10^3 \text{ N C}^{-1}$$

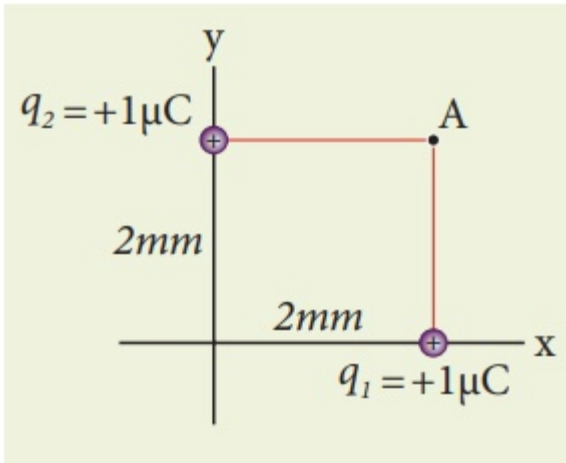
$$\vec{E}_R = 0.56 \times 10^3 \hat{i} \text{ NC}^{-1}$$

At the point Q the electric field is directed along the positive x-axis.



EXAMPLE-2

Consider the charge configuration as shown in the figure. Calculate the electric field at point A. If an electron is placed at points A, what is the acceleration experienced by this electron? (Mass of the electron = 9.1×10^{-31} kg and charge of electron = -1.6×10^{-19} C)



Solution

By using superposition principle, the net electric field at point A is

$$\vec{E}_A = \frac{1}{4\pi\epsilon_0} \frac{q_1}{r_{1A}^2} \hat{r}_{1A} + \frac{1}{4\pi\epsilon_0} \frac{q_2}{r_{2A}^2} \hat{r}_{2A},$$

where r_{1A} and r_{2A} are the distances of point A from the two charges respectively.

$$\begin{aligned} \vec{E}_A &= \frac{9 \times 10^9 \times 1 \times 10^{-6}}{(2 \times 10^{-3})^2} (\hat{j}) + \frac{9 \times 10^9 \times 1 \times 10^{-6}}{(2 \times 10^{-3})^2} (\hat{i}) \\ &= 2.25 \times 10^9 \hat{j} + 2.25 \times 10^9 \hat{i} = 2.25 \times 10^9 (\hat{i} + \hat{j}) \end{aligned}$$

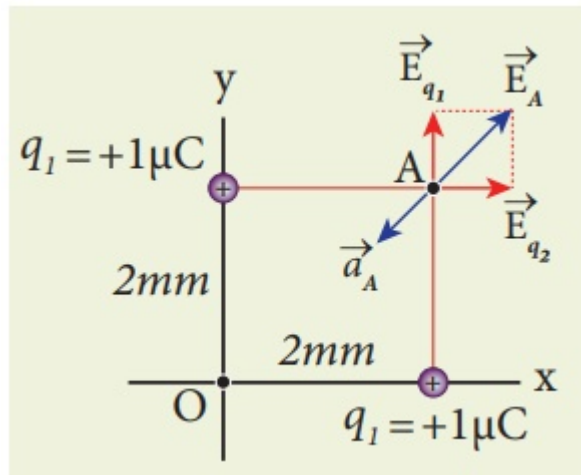
The magnitude of electric field

$$\begin{aligned} |\vec{E}_A| &= \sqrt{(2.25 \times 10^9)^2 + (2.25 \times 10^9)^2} \\ &= 2.25 \times \sqrt{2} \times 10^9 \text{ NC}^{-1} \end{aligned}$$

The direction of \vec{E}_A is given by

$$\frac{\vec{E}_A}{|\vec{E}_A|} = \frac{2.25 \times 10^9 (\hat{i} + \hat{j})}{2.25 \times \sqrt{2} \times 10^9} = \frac{(\hat{i} + \hat{j})}{\sqrt{2}},$$

which is the unit vector along OA as shown in the figure.



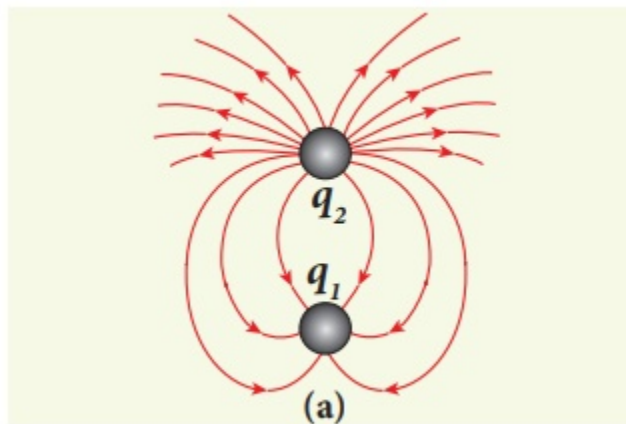
The acceleration experienced by an electron placed at point A is

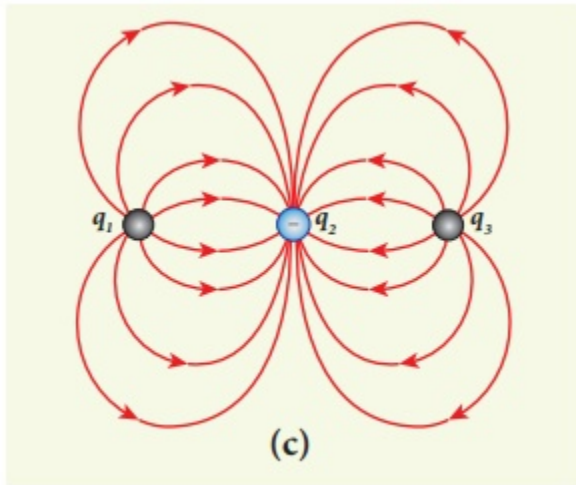
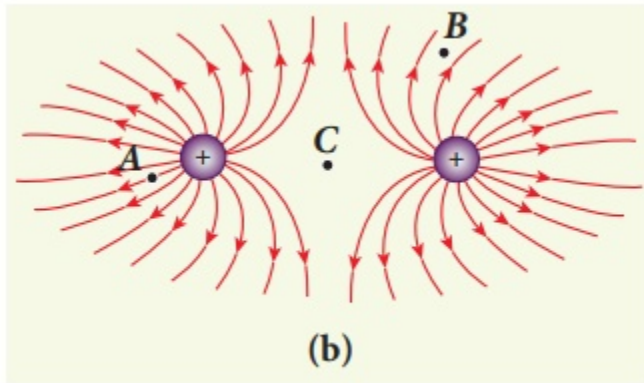
$$\begin{aligned}\vec{a}_A &= \frac{\vec{F}}{m} = \frac{q\vec{E}_A}{m} \\ &= \frac{(-1.6 \times 10^{-19}) \times (2.25 \times 10^9)(\hat{i} + \hat{j})}{9.1 \times 10^{-31}} \\ &= -3.95 \times 10^{20}(\hat{i} + \hat{j}) \text{ N}\end{aligned}$$

The electron is accelerated in a direction exactly opposite to \vec{E}_A .

EXAMPLE -3

The following pictures depict electric field lines for various charge configurations.





- (i) In figure (a) identify the signs of two charges and find the ratio $|q_1 / q_2|$
- (ii) In figure (b), calculate the ratio of two positive charges and identify the strength of the electric field at three points A, B, and C
- (iii) Figure (c) represents the electric field lines for three charges. If $q_2 = -20 \text{ nC}$, then calculate the values of q_1 and q_3

Solution

- (i) The electric field lines start at q_2 and end at q_1 . In figure (a), q_2 is positive and q_1 is negative. The number of lines starting from q_2 is 18 and number of the lines ending at q_1 is 6. So q_2 has greater magnitude. The ratio of $|q_1 / q_2| = N_1 / N_2 = 6/18 = 1/3$. It implies that $|q_2| = 3|q_1|$
- (ii) In figure (b), the number of field lines emanating from both positive charges are equal ($N=18$). So the charges are equal. At point A, the electric field lines are denser compared to the lines at point B. So the electric field at point A is greater in magnitude compared to the field at point B. Further, no electric field line passes through C, which implies that the resultant electric field at C due to these two charges is zero.

(iii) In the figure (c), the electric field lines start at q_1 and q_3 and end at q_2 . This implies that q_1 and q_3 are positive charges. The ratio of the number of field lines is $|q_1 / q_2| = 8/16 = |q_3 / q_2| = 1/2$, implying that q_1 and q_3 are half of the magnitude of q_2 . So $q_1 = q_3 = +10 \text{ nC}$.

s around a uniform spherical conductor are identical to those on a point charge