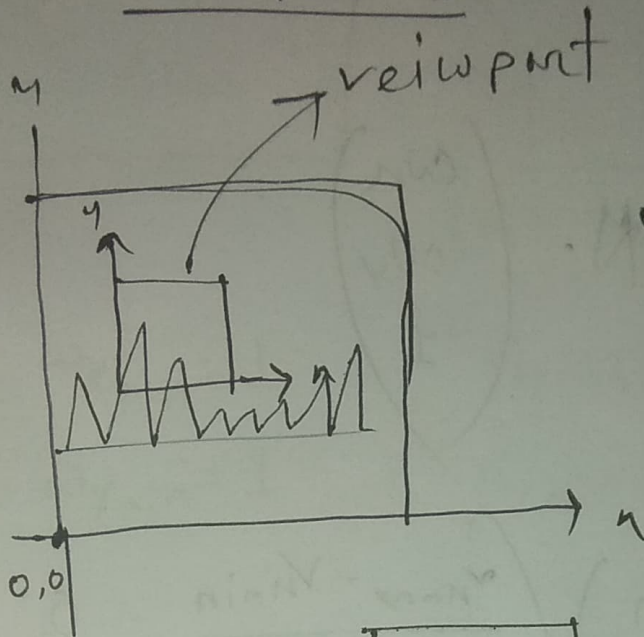


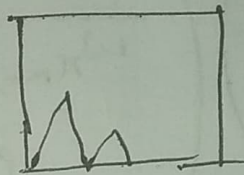
CG

13.09.122

# chapter 5

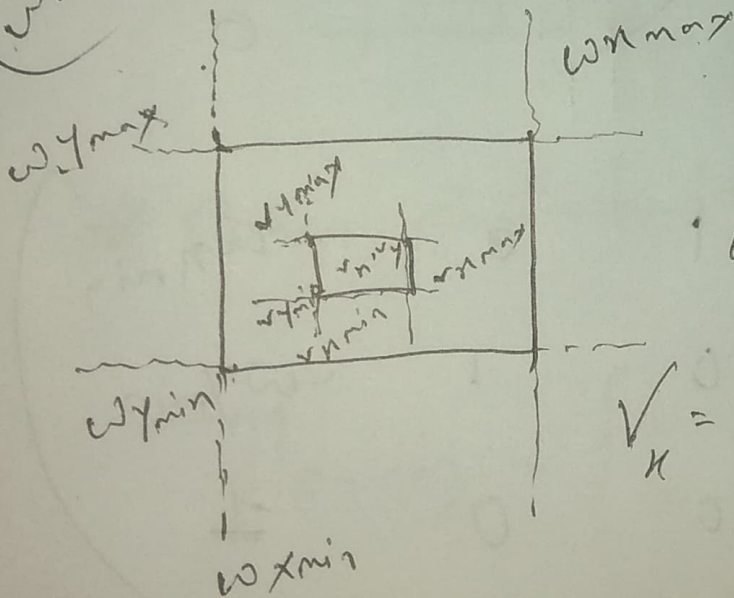


window to  
viewport  
mapping



wsc (world coordinate system)

$(w_x, w_y)$



$$\frac{w_x - w_{xmin}}{w_{xmax} - w_{xmin}} = \frac{v_x - v_{xmin}}{v_{xmax} - v_{xmin}}$$

$$v_x = \frac{w_x - w_{xmin}}{w_{xmax} - w_{xmin}} (v_{xmax} - v_{xmin}) + v_{xmin}$$

$$v_y = \frac{w_y - w_{ymin}}{w_{ymax} - w_{ymin}} (v_{ymax} - v_{ymin}) + v_{ymin}$$

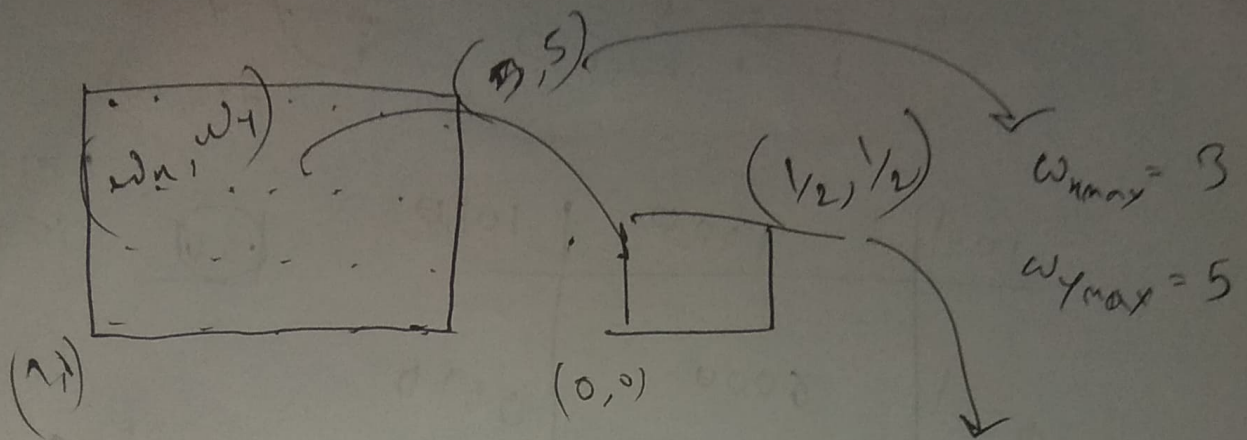
# Viewport transformation Matrix

$$\begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = N \cdot \begin{pmatrix} wx \\ wy \\ 1 \end{pmatrix}$$

$$N = \begin{pmatrix} 1 & 0 & x_{min} \\ 0 & 1 & y_{min} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \frac{x_{max} - x_{min}}{w_{xmax} - w_{xmin}} & 0 & 0 \\ 0 & \frac{y_{max} - y_{min}}{w_{ymax} - w_{ymin}} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & -w_{xmin} \\ 0 & 1 & -w_{ymin} \\ 0 & 0 & 1 \end{pmatrix}$$





$$w_{x\min} = 1$$

$$w_{y\min} = 1$$

$$v_{x\min} = 0$$

$$v_{y\min} = 0$$

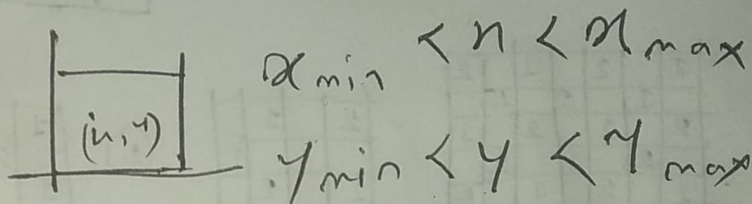
$$v_{x\max} = \frac{1}{2}$$

$$v_{y\max} = \frac{1}{2}$$

$$w_{\max} = 3$$

$$w_{y\max} = 5$$

# Point clipping



# Cohen Sutherland

$$\text{sign}(a) = \begin{cases} 1 & ; +ve \\ 0 & ; -ve \end{cases}$$

$$\text{Bit 1} = \text{sign}(y - y_{\max})$$

$$\text{Bit 2} = \text{sign}(y_{\min} - y)$$

$$\text{Bit 3} = \text{sign}(x - x_{\max})$$

$$\text{Bit 4} = \text{sign}(x_{\min} - x)$$

5 5 5 5 5 5

~~7 7 7~~

$(A+2) \times 2$

2x15

30

15 15

1001	1000	1010
0001	0000	0010
0101	0100	0110

region  
code

$$\begin{pmatrix} v_x \\ v_y \\ 1 \end{pmatrix} = N \cdot \begin{pmatrix} \omega_x \\ \omega_y \\ 1 \end{pmatrix}$$

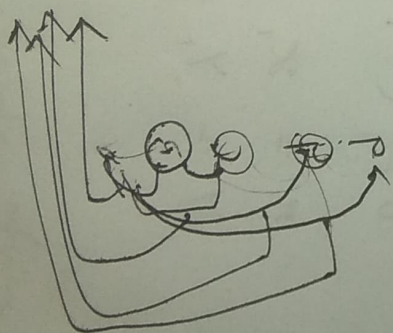
$$N = \begin{pmatrix} 1 & 0 & v_{x_{min}} \\ 0 & 1 & v_{y_{min}} \\ 0 & 0 & 1 \end{pmatrix}$$

$$\frac{v_{x_{max}} - v_{x_{min}}}{\omega_{x_{max}} - \omega_{x_{min}}}$$

$$\frac{v_{y_{max}} - v_{y_{min}}}{\omega_{y_{max}} - \omega_{y_{min}}}$$

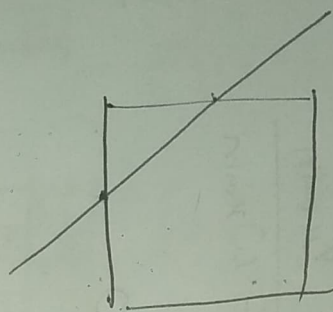
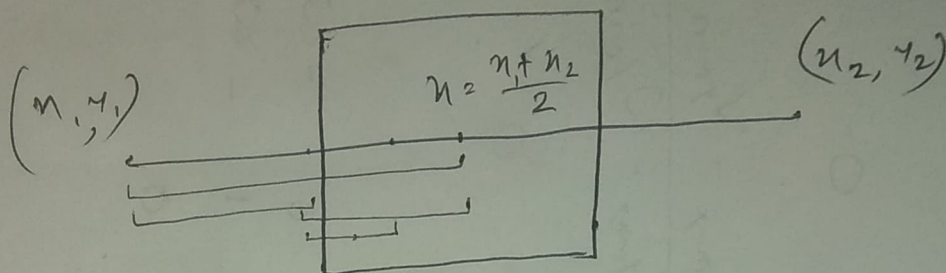
$$\begin{pmatrix} 1 & 0 & -\omega_{x_{min}} \\ 0 & 1 & -\omega_{y_{min}} \\ 0 & 0 & 1 \end{pmatrix}$$

270  
35.29  
13.33





## # Mid point subdivision algo

\* Iterative algo:

## # Liang - Barsky Algorithm

$$u = \{u_1, u_2\}$$

$$x = x_1 + \Delta x \cdot u$$

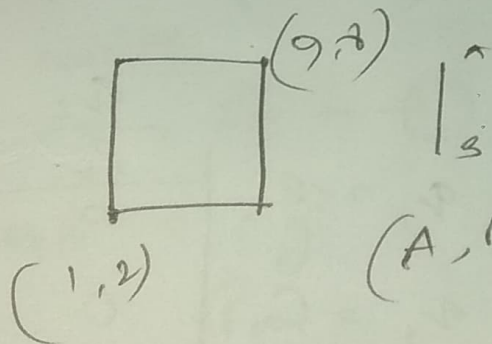
$$y = y_1 + \Delta y \cdot u$$

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$P_k$	$q_k$
$P_1 = -\Delta x$	$q_1 = x_1 - x_{\min}$ (left)
$P_2 = \Delta x$	$q_2 = x_{\max} - x_1$ (right)
$P_3 = -\Delta y$	$q_3 = y_1 - y_{\min}$ (bottom)
$P_4 = \Delta y$	$q_4 = y_{\max} - y_1$ (top)

$P_k = 0 \rightarrow$  Parallel

$P_k < 0 \rightarrow \text{not } \geq q_k$



$$(A, B) = (11, 6), (11, 10)$$

$$P_2 = \Delta x$$

$$= 0$$

$$q_2 = 9 - 11$$

$$= -2$$

For  $q_2 < 0$

(A, B) line is outside from

2

$$P_1, P_2 < 0$$

$$P_3, P_4 > 0$$

$$\rightarrow U_1 = \min\left(1, \frac{a_1}{P_1}, \frac{a_2}{P_2}\right)$$

$$\rightarrow U_2 = \max\left(1, \frac{a_3}{P_3}, \frac{a_4}{P_4}\right)$$

$$U_1 < U_2 \text{ visible}$$

$$U_1 > U_2 \text{ invisible}$$

$$C, D = (3, 7), (3, 10)$$

$P_k$	$a_k$	$\frac{a_k}{P_k}$
$P_1 = 0$	$a_1 = 2$	0
$P_2 = 0$	$a_2 = 0$	0
$P_3 = -3$	$a_3 = 5$	$-5/3$
$P_4 = 3$	$a_4 = 1$	$1/3$

$$U_1 = \min(1, -5/3) = -5/3$$

$$U_2 = \max(0, 1/3) = 1/3$$