

1383.  $\sqrt[3]{\sin x^3}$ .

$$\sin t = 0 + t + 0 - \frac{t^3}{3!} + 0 + \frac{t^5}{5!} + 0 + \underline{O}(t^7)$$

$$\sin x^3 = x^3 - \frac{x^9}{3!} + \frac{x^{15}}{5!} + \underline{O}(x^{21})$$

$$\sqrt[3]{\sin x^3} = \sqrt[3]{x^3 - \frac{x^9}{3!} + \frac{x^{15}}{5!} + \underline{O}(x^{21})} = x \sqrt[3]{1 - \frac{x^6}{3!} + \frac{x^{12}}{5!} + \underline{O}(x^{18})}$$

$$\sqrt[3]{1+t} = 1 + \frac{1}{3}t - \frac{1}{9}t^2 + \underline{O}(t^3)$$

$$\text{h.e. } x \sqrt[3]{1 + \left(-\frac{x^6}{3!} + \frac{x^{12}}{5!} + \underline{O}(x^{18})\right)} =$$

$$= x \left( 1 + \frac{1}{3} \left( -\frac{x^6}{3!} + \frac{x^{12}}{5!} + \underline{O}(x^{18}) \right) - \frac{1}{9} \left( -\frac{x^6}{3!} + \frac{x^{12}}{5!} + \underline{O}(x^{18}) \right)^2 + \underline{O}(x^{18}) \right) =$$

$$= x \left( 1 - \frac{x^6}{18} + \frac{x^{12}}{360} - \frac{x^{12}}{324} + \underline{O}(x^{18}) \right) = \underline{x - \frac{x^7}{18} - \frac{x^{13}}{3240} + \underline{O}(x^{19})}$$

1384.  $\ln \cos x$ .

$$\cos x = 1 - \frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \underline{O}(x^8)$$

$$\ln \cos x = \ln \left( 1 - \frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \underline{O}(x^8) \right)$$

$$\ln(1+t) = t - \frac{t^2}{2} + \frac{t^3}{3} + \underline{O}(t^4)$$

$$\ln \left( 1 - \frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \underline{O}(x^8) \right) =$$

$$= -\frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \underline{O}(x^8) - \frac{1}{2} \left( -\frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \underline{O}(x^8) \right)^2 + \frac{1}{3} \left( -\frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} + \underline{O}(x^8) \right)^3 + \underline{O}(x^8)$$

$$= -\frac{x^2}{2} + \frac{x^4}{4!} - \frac{x^6}{6!} - \frac{1}{2} \left( \frac{x^4}{4} - \frac{x^6}{24} \right) + \frac{1}{3} \left( -\frac{x^6}{8} \right) + \underline{O}(x^8) =$$

$$= \underline{-\frac{x^2}{2} - \frac{x^4}{12} - \frac{x^6}{45} + \underline{O}(x^8)}$$

1385.  $\sin(\sin x)$ ,  $\sin x = x - \frac{x^3}{3!} + \underline{O}(x^5)$

$$\sin(\sin x) = \sin \left( x - \frac{x^3}{3!} + \underline{O}(x^5) \right) =$$

$$= x - \frac{x^3}{3!} + \underline{O}(x^5) - \frac{1}{3!} \left( x - \frac{x^3}{3!} + \underline{O}(x^5) \right)^3 + \underline{O}(x^5) =$$

$$= x - \frac{x^3}{3!} - \frac{x^3}{3!} + \underline{O}(x^5) = \underline{x - \frac{x^3}{3} + \underline{O}(x^5)}$$