

Figure 5.1 AES Encryption Process

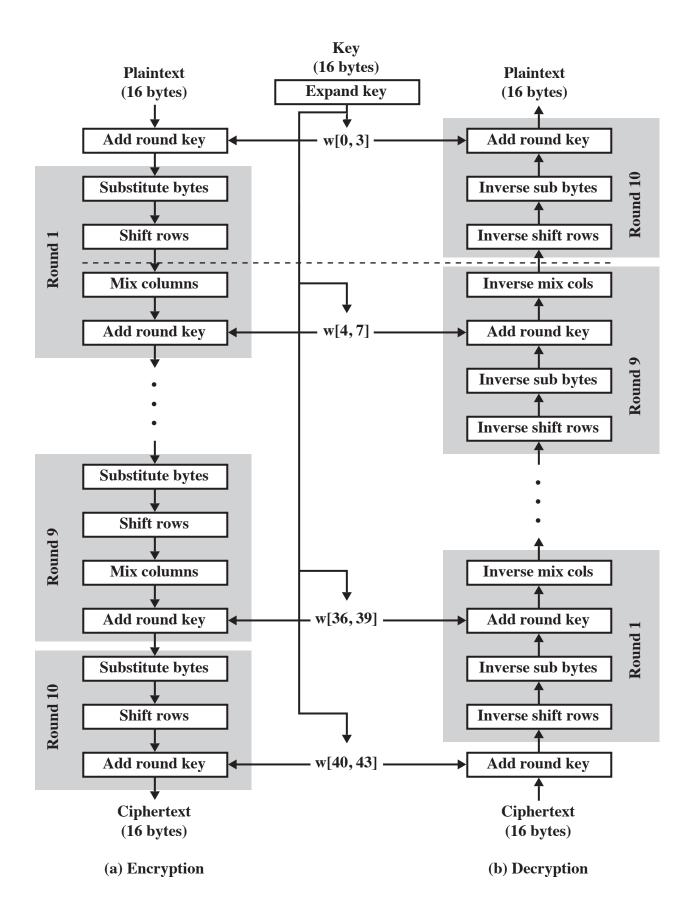


Figure 5.3 AES Encryption and Decryption

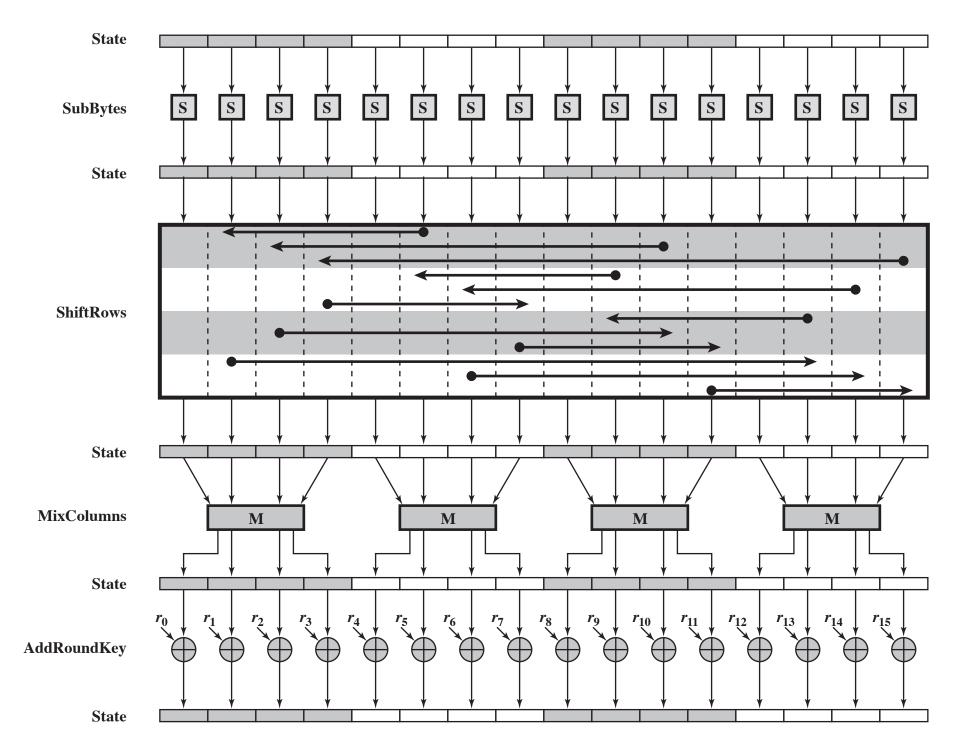
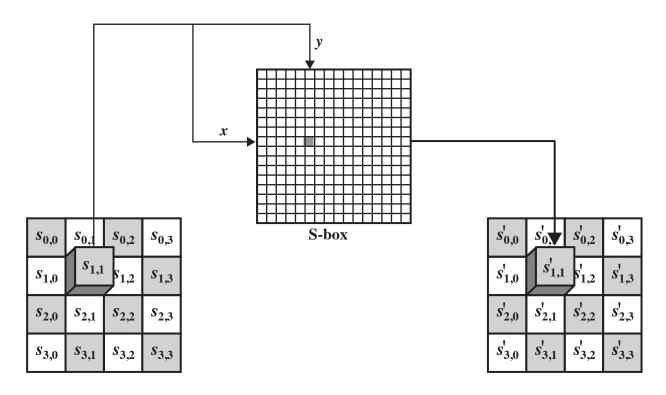
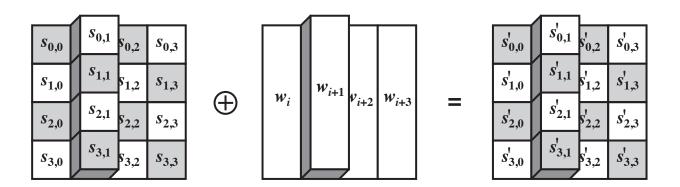


Figure 5.4 AES Encryption Round

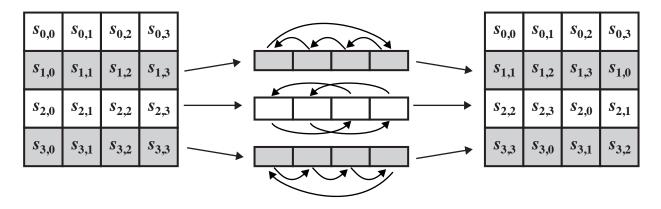


(a) Substitute byte transformation

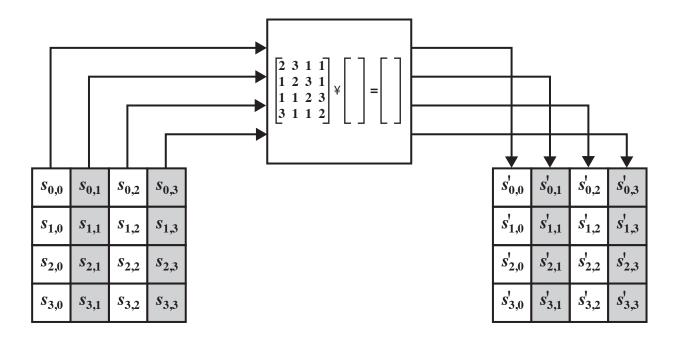


(b) Add round key Transformation

Figure 5.5 AES Byte-Level Operations



(a) Shift row transformation



(b) Mix column transformation

Figure 5.7 AES Row and Column Operations

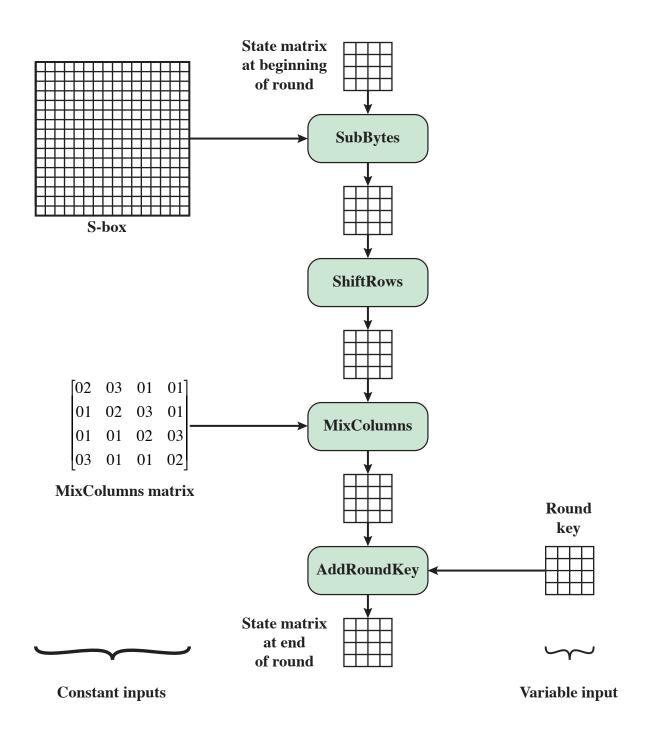


Figure 5.8 Inputs for Single AES Round

Table 5.1 AES Parameters

Key Size (words/bytes/bits)	4/16/128	6/24/192	8/32/256
Plaintext Block Size (words/bytes/bits)	4/16/128	4/16/128	4/16/128
Number of Rounds	10	12	14
Round Key Size (words/bytes/bits)	4/16/128	4/16/128	4/16/128
Expanded Key Size (words/bytes)	44/176	52/208	60/240

Table 5.2 AES S-Boxes

(a) S-box

			y														
		0	1	2	3	4	5	6	7	8	9	A	В	С	D	Е	F
	0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
	1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
	2	В7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
	3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
	4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	В3	29	E3	2F	84
	5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
	6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
x	7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
	8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
	9	60	81	4F	DC	22	2A	90	88	46	EE	В8	14	DE	5E	0B	DB
	A	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
	В	E7	C8	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
	C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
	D	70	3E	B5	66	48	03	F6	0E	61	35	57	В9	86	C1	1D	9E
	Е	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
	F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	В0	54	BB	16

(b) Inverse S-box

			y														
		0	1	2	3	4	5	6	7	8	9	A	В	С	D	Е	F
	0	52	09	6A	D5	30	36	A5	38	BF	40	A3	9E	81	F3	D7	FB
	1	7C	E3	39	82	9B	2F	FF	87	34	8E	43	44	C4	DE	E9	СВ
	2	54	7B	94	32	A6	C2	23	3D	EE	4C	95	0B	42	FA	C3	4E
	3	08	2E	A1	66	28	D9	24	B2	76	5B	A2	49	6D	8B	D1	25
	4	72	F8	F6	64	86	68	98	16	D4	A4	5C	CC	5D	65	В6	92
	5	6C	70	48	50	FD	ED	В9	DA	5E	15	46	57	A7	8D	9D	84
	6	90	D8	AB	00	8C	BC	D3	0A	F7	E4	58	05	B8	В3	45	06
x	7	D0	2C	1E	8F	CA	3F	0F	02	C1	AF	BD	03	01	13	8A	6B
A	8	3A	91	11	41	4F	67	DC	EA	97	F2	CF	CE	F0	B4	E6	73
	9	96	AC	74	22	E7	AD	35	85	E2	F9	37	E8	1C	75	DF	6E
	A	47	F1	1A	71	1D	29	C5	89	6F	В7	62	0E	AA	18	BE	1B
	В	FC	56	3E	4B	C6	D2	79	20	9A	DB	C0	FE	78	CD	5A	F4
	С	1F	DD	A8	33	88	07	C7	31	B1	12	10	59	27	80	EC	5F
	D	60	51	7F	A9	19	B5	4A	0D	2D	E5	7A	9F	93	C9	9C	EF
	Е	A0	E0	3B	4D	AE	2A	F5	В0	C8	EB	BB	3C	83	53	99	61
	F	17	2B	04	7E	BA	77	D6	26	E1	69	14	63	55	21	0C	7D

Table 5.3 Key Expansion for AES Example

Key Words	Auxiliary Function
w0 = 0f 15 71 c9	RotWord(w3)= 7f 67 98 af = x1
w1 = 47 d9 e8 59	SubWord(x1) = d2 85 46 79 = y1
w2 = 0c b7 ad	Rcon(1)= 01 00 00 00
w3 = af 7f 67 98	$y1 \oplus Rcon(1) = d3 85 46 79 = z1$
$w4 = w0 \oplus z1 = dc \ 90 \ 37 \ b0$	RotWord(w7) = 81 15 a7 38 = $x2$
$w5 = w4 \oplus w1 = 9b \ 49 \ df \ e9$	SubWord(x4) = 0c 59 5c 07 = y2
$w6 = w5 \oplus w2 = 97 \text{ fe } 72 \text{ 3f}$	Rcon(2) = 02 00 00 00
w7 = w6 \oplus w3 = 38 81 15 a7	$y2 \oplus Rcon(2) = 0e 59 5c 07 = z2$
$w8 = w4 \oplus z2 = d2 c9 6b b7$	RotWord(w11)= ff d3 c6 e6 = $x3$
$w9 = w8 \oplus w5 = 49 \ 80 \ b4 \ 5e$	SubWord(x2) = $16 66 b4 8e = y3$
$w10 = w9 \oplus w6 = de 7e c6 61$	Rcon(3) = 04 00 00 00
$w11 = w10 \oplus w7 = e6 \text{ ff d3 c6}$	y3 \(\phi\) Rcon(3)= 12 66 b4 8e = z3
$w12 = w8 \oplus z3 = c0 \text{ af df } 39$	RotWord(w15) = ae 7e c0 b1 = $x4$
$w13 = w12 \oplus w9 = 89 2f 6b 67$	SubWord(x3)= e4 f3 ba c8 = y4
$w14 = w13 \oplus w10 = 57 51 ad 06$	Rcon(4) = 08 00 00 00
$w15 = w14 \oplus w11 = b1$ ae 7e c0	$y4 \oplus Rcon(4) = ec f3 ba c8 = 4$
$w16 = w12 \oplus z4 = 2c \ 5c \ 65 \ f1$	RotWord(w19) = 8c dd 50 43 = $x5$
$w17 = w16 \oplus w13 = a5 73 0e 96$	SubWord($x4$) = 64 c1 53 1a = y5
$w18 = w17 \oplus w14 = f2 22 a3 90$	Rcon(5) = 10 00 00 00
w19 = w18 \oplus w15 = 43 8c dd 50	$y5 \oplus Rcon(5) = 74 c1 53 1a = z5$
$w20 = w16 \oplus z5 = 58 9d 36 eb$	RotWord(w23) = $40 \ 46 \ bd \ 4c = x6$
$w21 = w20 \oplus w17 = fd ee 38 7d$	SubWord(x5) = 09 5a 7a 29 = y6
$w22 = w21 \oplus w18 = 0f cc 9b ed$	Rcon(6) = 20 00 00 00
$w23 = w22 \oplus w19 = 4c \ 40 \ 46 \ bd$	y6 \(\phi\) Rcon(6)= 29 5a 7a 29 = z6
$w24 = w20 \oplus z6 = 71 c7 4c c2$	RotWord(w27) = a5 a9 ef cf = $x7$
$w25 = w24 \oplus w21 = 8c \ 29 \ 74 \ bf$	SubWord(x6) = 06 d3 df 8a = y7
$w26 = w25 \oplus w22 = 83 \text{ e5 ef } 52$	Rcon(7) = 40 00 00 00
w27 = w26	y7 ⊕ Rcon(7)= 46 d3 df 8a = z7
$w28 = w24 \oplus z7 = 37 14 93 48$	RotWord(w31) = 7d a1 4a f7 = x8
$w29 = w28 \oplus w25 = bb \ 3d \ e7 \ f7$	SubWord(x7) = ff 32 d6 68 = y8
w30 = w29 ⊕ w26 = 38 d8 08 a5	Rcon(8) = 80 00 00 00
w31 = w30	$y8 \oplus Rcon(8) = 7f 32 d6 68 = z8$
$w32 = w28 \oplus z8 = 48 \ 26 \ 45 \ 20$	RotWord(w35) = be 0b 38 3c = $x9$
$w33 = w32 \oplus w29 = f3 \text{ 1b a2 d7}$	SubWord(x8)= ae 2b 07 eb = y9
$w34 = w33 \oplus w30 = cb c3 aa 72$	Rcon(9) = 1B 00 00 00 $y9 \oplus Rcon(9) = b5 2b 07 eb = z9$
$w35 = w34 \oplus w32 = 3c \text{ be 0b } 38$	
$w36 = w32 \oplus z9 = fd \ 0d \ 42 \ cb$	RotWord(w39) = 6b 41 56 f9 = x10
w37 = w36 ⊕ w33 = 0e 16 e0 1c	SubWord(x9)= 7f 83 b1 99 = y10 Rcon(10)= 36 00 00 00
$w38 = w37 \oplus w34 = c5 d5 4a 6e$	$y10 \oplus Rcon(10) = 49 \ 83 \ b1 \ 99 = z10$
$w39 = w38 \oplus w35 = f9 \ 6b \ 41 \ 56$	110 @ Redf(10) 49 03 B1 33 - 210
$w40 = w36 \oplus z10 = b4 \ 8e \ f3 \ 52$ $w41 = w40 \oplus w37 = ba \ 98 \ 13 \ 4e$	
$w41 = w40 \oplus w37 = ba 98 13 4e$ $w42 = w41 \oplus w38 = 7f 4d 59 20$	
$w43 = w42 \oplus w39 = 86 \ 26 \ 18 \ 76$	

Table 5.4 AES Example

Start of round	After	After	After	Round Key
	SubBytes	ShiftRows	MixColumns	·
01 89 fe 76	· ·			0f 47 0c af
23 ab dc 54				15 d9 b7 7f
45 cd ba 32				71 e8 ad 67
67 ef 98 10				c9 59 d6 98
0e ce f2 d9	ab 8b 89 35	ab 8b 89 35	b9 94 57 75	dc 9b 97 38
36 72 6b 2b	05 40 7f f1	40 7f f1 05	e4 8e 16 51	90 49 fe 81
34 25 17 55	18 3f f0 fc	f0 fc 18 3f	47 20 9a 3f	37 df 72 15
ae b6 4e 88	e4 4e 2f c4	c4 e4 4e 2f	c5 d6 f5 3b	b0 e9 3f a7
65 Of c0 4d	4d 76 ba e3	4d 76 ba e3	8e 22 db 12	d2 49 de e6
74 c7 e8 d0	92 c6 9b 70	c6 9b 70 92	b2 f2 dc 92	c9 80 7e ff
70 ff e8 2a	51 16 9b e5	9b e5 51 16	df 80 f7 c1	6b b4 c6 d3
75 3f ca 9c	9d 75 74 de	de 9d 75 74	2d c5 1e 52	b7 5e 61 c6
5c 6b 05 f4	4a 7f 6b bf	4a 7f 6b bf	b1 c1 0b cc	c0 89 57 b1
7b 72 a2 6d	21 40 3a 3c	40 3a 3c 21	ba f3 8b 07	af 2f 51 ae
b4 34 31 12	8d 18 c7 c9	c7 c9 8d 18	f9 1f 6a c3	df 6b ad 7e
9a 9b 7f 94	b8 14 d2 22	22 b8 14 d2	1d 19 24 5c	39 67 06 c0
71 48 5c 7d	a3 52 4a ff	a3 52 4a ff	d4 11 fe 0f	2c a5 f2 43
15 dc da a9	59 86 57 d3	86 57 d3 59	3b 44 06 73	5c 73 22 8c
26 74 c7 bd	f7 92 c6 7a	c6 7a f7 92	cb ab 62 37	65 0e a3 dd
24 7e 22 9c	36 f3 93 de	de 36 f3 93	19 b7 07 ec	f1 96 90 50
f8 b4 0c 4c	41 8d fe 29	41 8d fe 29	2a 47 c4 48	58 fd 0f 4c
67 37 24 ff	85 9a 36 16	9a 36 16 85	83 e8 18 ba	9d ee cc 40
ae a5 c1 ea	e4 06 78 87	78 87 e4 06	84 18 27 23	36 38 9b 46
e8 21 97 bc	9b fd 88 65 40 f4 1f f2	65 9b fd 88 40 f4 1f f2	eb 10 0a f3 7b 05 42 4a	eb 7d ed bd 71 8c 83 cf
72 ba cb 04 1e 06 d4 fa	40 f4 1f f2 72 6f 48 2d	40 f4 1f f2 6f 48 2d 72		71 8c 83 cf c7 29 e5 a5
1e 06 d4 fa b2 20 bc 65	37 b7 65 4d	65 4d 37 b7	1e d0 20 40 94 83 18 52	4c 74 ef a9
00 6d e7 4e	63 3c 94 2f	2f 63 3c 94	94 c4 43 fb	c2 bf 52 ef
00 0d e7 4e	67 a7 78 97	67 a7 78 97	ec 1a c0 80	37 bb 38 f7
d9 f9 c5 e5	35 99 a6 d9	99 a6 d9 35	0c 50 53 c7	14 3d d8 7d
d8 f7 f7 fb	61 68 68 0f	68 Of 61 68	3b d7 00 ef	93 e7 08 a1
56 7b 11 14	b1 21 82 fa	fa b1 21 82	b7 22 72 e0	48 f7 a5 4a
db a1 f8 77	b9 32 41 f5	b9 32 41 f5	b1 1a 44 17	48 f3 cb 3c
18 6d 8b ba	ad 3c 3d f4	3c 3d f4 ad	3d 2f ec b6	26 1b c3 be
a8 30 08 4e	c2 04 30 2f	30 2f c2 04	0a 6b 2f 42	45 a2 aa 0b
ff d5 d7 aa	16 03 0e ac	ac 16 03 0e	9f 68 f3 b1	20 d7 72 38
f9 e9 8f 2b	99 1e 73 f1	99 1e 73 f1	31 30 3a c2	fd 0e c5 f9
1b 34 2f 08	af 18 15 30	18 15 30 af	ac 71 8c c4	0d 16 d5 6b
4f c9 85 49	84 dd 97 3b	97 3b 84 dd	46 65 48 eb	42 e0 4a 41
bf bf 81 89	08 08 0c a7	a7 08 08 0c	6a 1c 31 62	cb 1c 6e 56
cc 3e ff 3b	4b b2 16 e2	4b b2 16 e2	4b 86 8a 36	b4 8e f3 52
a1 67 59 af	32 85 cb 79	85 cb 79 32	b1 cb 27 5a	ba 98 13 4e
04 85 02 aa	f2 97 77 ac	77 ac f2 97	fb f2 f2 af	7f 4d 59 20
al 00 5f 34	32 63 cf 18	18 32 63 cf	cc 5a 5b cf	86 26 18 76
ff 08 69 64				
0b 53 34 14				
84 bf ab 8f				
4a 7c 43 b9				

 Table 5.5 Avalanche Effect in AES: Change in Plaintext

Round		Number of Bits that Differ
	0123456789abcdeffedcba9876543210	1
	0023456789abcdeffedcba9876543210	1
0	0e3634aece7225b6f26b174ed92b5588	1
O	0f3634aece7225b6f26b174ed92b5588	1
1	657470750fc7ff3fc0e8e8ca4dd02a9c	20
1	c4a9ad090fc7ff3fc0e8e8ca4dd02a9c	20
2	5c7bb49a6b72349b05a2317ff46d1294	58
2	fe2ae569f7ee8bb8c1f5a2bb37ef53d5	50
3	7115262448dc747e5cdac7227da9bd9c	59
<i>J</i>	ec093dfb7c45343d689017507d485e62	37
4	f867aee8b437a5210c24c1974cffeabc	61
т	43efdb697244df808e8d9364ee0ae6f5	O1
5	721eb200ba06206dcbd4bce704fa654e	68
3	7b28a5d5ed643287e006c099bb375302	00
6	0ad9d85689f9f77bc1c5f71185e5fb14	64
Ü	3bc2d8b6798d8ac4fe36a1d891ac181a	04
7	db18a8ffa16d30d5f88b08d777ba4eaa	67
1	9fb8b5452023c70280e5c4bb9e555a4b	O7
8	f91b4fbfe934c9bf8f2f85812b084989	65
O	20264e1126b219aef7feb3f9b2d6de40	0.5
9	cca104a13e678500ff59025f3bafaa34	61
9	b56a0341b2290ba7dfdfbddcd8578205	01
10	ff0b844a0853bf7c6934ab4364148fb9	58
10	612b89398d0600cde116227ce72433f0	30

Table 5.6 Avalanche Effect in AES: Change in Key

Round		Number of Bits that Differ
	0123456789abcdeffedcba9876543210	0
	0123456789abcdeffedcba9876543210	O
0	0e3634aece7225b6f26b174ed92b5588	1
O	0f3634aece7225b6f26b174ed92b5588	1
1	657470750fc7ff3fc0e8e8ca4dd02a9c	22
1	c5a9ad090ec7ff3fc1e8e8ca4cd02a9c	22
2	5c7bb49a6b72349b05a2317ff46d1294	58
2	90905fa9563356d15f3760f3b8259985	50
3	7115262448dc747e5cdac7227da9bd9c	67
<i>J</i>	18aeb7aa794b3b66629448d575c7cebf	O7
4	f867aee8b437a5210c24c1974cffeabc	63
7	f81015f993c978a876ae017cb49e7eec	03
5	721eb200ba06206dcbd4bce704fa654e	81
3	5955c91b4e769f3cb4a94768e98d5267	01
6	0ad9d85689f9f77bc1c5f71185e5fb14	70
0	dc60a24d137662181e45b8d3726b2920	70
7	db18a8ffa16d30d5f88b08d777ba4eaa	74
1	fe8343b8f88bef66cab7e977d005a03c	7-
8	f91b4fbfe934c9bf8f2f85812b084989	67
O	da7dad581d1725c5b72fa0f9d9d1366a	07
9	cca104a13e678500ff59025f3bafaa34	59
9	0ccb4c66bbfd912f4b511d72996345e0	39
10	ff0b844a0853bf7c6934ab4364148fb9	53
10	fc8923ee501a7d207ab670686839996b	33

Table 5.7 S-AES S-Boxes

		j							
		00	01	10	11				
i	00	9	4	A	В				
	01	D	1	8	5				
	10	6	2	0	3				
	11	С	Е	F	7				

		j							
		00	01	10	11				
i	00	A	5	9	В				
	01	1	7	8	F				
	10	6	0	2	3				
	11	C	4	D	Е				

(a) S-Box

(b) Inverse S-Box

Note: hexadecimal numbers in shaded boxes; binary numbers in unshaded boxes.