

# 数据隐私方法伦理和实践

## *Methodology, Ethics and Practice of Data Privacy*

### 隐私保护的应用

#### *Applications*

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# 1. PPML by HE

# **Privacy Preserving Back-Propagation Neural Network Learning Made Practical with Cloud Computing**

Jiawei Yuan, Shucheng Yu  
13'TPDS

## Contribution

- » An efficient and scalable solution that supports collaborative BPN network learning with privacy preservation in the multi-party setting and allows arbitrarily partitioned datasets.

# Main Idea

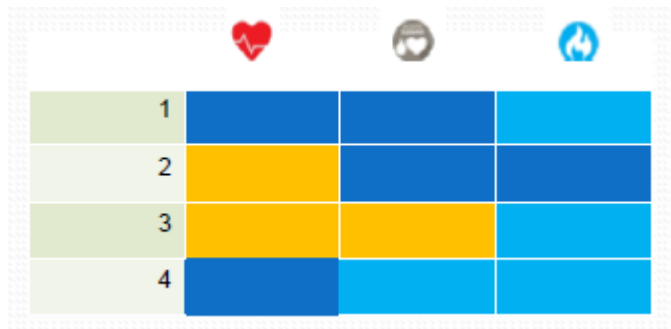
- » Each participant first encrypts her/his private data with the system public key and then uploads the ciphertexts to the cloud
- » Cloud servers then execute most of the operations pertaining to the learning process over the ciphertexts and then return the encrypted results to the participants
- » The participants jointly decrypt the results with which they update their respective weights for the BPN network.
- » Cloud servers learn no privacy data. Though off-loading the computation tasks to the cloud, this scheme is high scalable.




# System Model

- » Trusted authority (TA)
  - Generate and issue encryption/decryption keys
- » Data owners
  - $P_s$  owns a private data set and wants to perform collaborative learning with other data owners
- » Cloud server
  - Execute most of the operations pertaining to the learning

# Data Partition

- » Data is arbitrarily partitioned among multi-parties  $K$
- Assume the aggregated training set  $D$  with  $N$  records in total, each record with  $m$  attributes
  - Each part  $P_s$  holds part of data set without specific order
  - For example (3 parties)



			
1	Blue	Blue	Light Blue
2	Yellow	Blue	Dark Blue
3	Yellow	Yellow	Light Blue
4	Blue	Light Blue	Light Blue

# BGN

Simultaneously supports one multiplication and unlimited number of addition operations.

$$C(m_1\hat{m}_1 + m_2\hat{m}_2 + \cdots + m_i\hat{m}_i)$$

- » Private key:  $SK = q$
- » Public key:  $PK = (n, G, G_1, e, g, h)$ 
  - $e: G \times G \rightarrow G_1$ ; generator:  $g, u$  and set  $h = u^r, q \cdot r = n$
  - Define two cyclic  $G, G_1$  whose order is  $n$  and  $q$
- » Encrypt –  $C = g^m h^r \in G$
- » Decrypt –  $C^q = (g^m h^r)^q = (g^q)^m \bmod n$ 
  - Compute log of  $C^q$  base  $g^q$  (solving discrete logarithm of the ciphertext using Pollard's lambda method)
  - BGN scheme just works with small numbers



# Scheme

1. Each party encrypt her/his input data set by BGN public key and upload the encrypted data to the cloud.
2. The cloud servers performs most of the operations, i.e., **secure scalar product and addition**.
3. As the BGN algorithm just supports one step multiplication over ciphertext, the intermediate results shall be **first securely decrypted and then encrypted** to support consecutive multiplication operations.
4. The decrypted results known to each party cannot be the actual intermediate values. We design a **secret sharing algorithm** that allows the parties to decrypt only the random shares of the intermediate values.
5. **Sigmoid function approximation**.

After the entire process of the privacy preserving learning, all the parties jointly establish a neural network representing the whole data set without disclosing any private data to each other.

# How to apply HE (BGN)



## Parties

- Encrypt her/his data with same public key



## Cloud server

- Encrypt weight with public key
- Compute scalar product on ciphertext,  $\mathcal{C}(L_s)$
- Secure share the  $\mathcal{C}(L_s)$



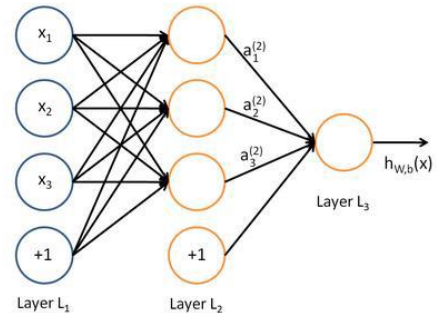
## Parties

- Compute sigmoid function



## Cloud server

- Compute error on ciphertext (true label and output)
- With the help of parties compare error and threshold
- Update weight on ciphertext (true label and output and intermediated result) and Secure share the result



# Cloud Secure Computing

- **Encryption:** Given a message  $M$ , encrypt it as:  $C = g^M h^r \in G, r \xleftarrow{R} Z_n$
- **Secure Scalar Product:** Given the ciphertexts of vector  $(M_{11}, M_{12}, \dots, M_{1v})$  and  $(M_{21}, M_{22}, \dots, M_{2v})$  the cloud computes their scalar products as :

$$C(prod) = h_1^1 * \prod_{i=1}^v e(C_{1i}, C_{2i})$$

where  $h_1 = e(g, h)$ ,  $C_{1i}$  and  $C_{2i}$  are the ciphertexts of message  $M_{1i}$  and  $M_{2i}$  respectively.

- **Secure Addition:** Given the ciphertexts of message  $M_{11}, M_{12}, \dots, M_{1v}$ , the cloud computes their sum as:

$$C(sum) = \prod_{i=1}^v C_i$$

# Cloud Secure Computing

- **Decryption:** without loss of generality, we just demonstrate the decryption of  $C(sum)$  as follows. The cloud broadcasts  $C(sum)$  to each party. On receiving the ciphertext, each party  $P_s$  computes  $C(sum)^{q_{1s}}$  and returns the result to the cloud.

With the results from all the parties, the cloud computes:

$$\prod_{j=1}^Z C(sum)^{q_{1s}} = C(sum)^{q_1}$$

Since  $C(sum) = \prod_{i=1}^v C_i = \prod_{i=1}^v g^{M_i} h^{r_i}$ , we have:

$$C(sum)^{q_1} = (g^{\sum_{i=1}^v M_i} \prod_{i=1}^v h^{r_i})^{q_1} = (g^{q_1})^{\sum_{i=1}^v M_i}$$

Note that  $h^{q_1} = 1$ .  $\sum_{i=1}^v M_i$  can be efficiently solved using Pollard's lambda method[1] given  $g^{q_1}$ . The encrypted scalar product can be decrypted jointly in the similar way.

[1] Katz, Jonathan, et al. *Handbook of applied cryptography*. CRC press, 1996.

# BGN for Large Number

- The Pollard's lambda method is able to decrypt numbers of up to 30-40 bits within a reasonable time slot (e.g., in minutes or hours).
- For larger numbers, let the data holders divide the numbers, if they are large, into several numbers, and the cloud then decrypt the smaller “chunks”.

Let  $V_A = (A_1, A_2, \dots, A_k)$  and  $V_B = (B_1, B_2, \dots, B_k)$  be two vectors, where  $A_i$  and  $B_i$  are  $3d$ -bit numbers for  $1 \leq i \leq k$ . Each number can be represented as

$$A_i = A_{i2} * 2^{2d} + A_{i1} * 2^d + A_{i0},$$

$$B_i = B_{i2} * 2^{2d} + B_{i1} * 2^d + B_{i0}.$$

We can compute the product of  $A_i * B_i$  as follows:

$$\begin{aligned} A_i * B_i &= 2^{4d}(A_{i2} * B_{i2}) + 2^{3d}(A_{i2} * B_{i1} + A_{i1} * B_{i2}) \\ &\quad + 2^{2d}(A_{i2} * B_{i0} + A_{i0} * B_{i2} + A_{i1} * B_{i1}) \\ &\quad + 2^d(A_{i1} * B_{i0} + A_{i0} * B_{i1}) + A_{i0} * B_{i0}. \end{aligned}$$

## Secure Sharing of Sum

Goal- to support consecutive multiplication operations via decryption and re-encryption

- Ciphertext of Sum -  $C(S)$
- Each party  $P_s$  generate a random number  $l_s$ ,
- Encrypt  $l_s$  and send  $C(l_s)$  to cloud
- Cloud obtain  $C(sumL = \sum l_s)$ ,  $C(\bar{L}) = C(sumL - S)$ , decrypt  $C(\bar{L})$  and send  $(l_1 - \bar{L})$  to  $P_1$
- Secure share:  $P_1$  has  $(l_1 - \bar{L})$ , others have  $l_s$

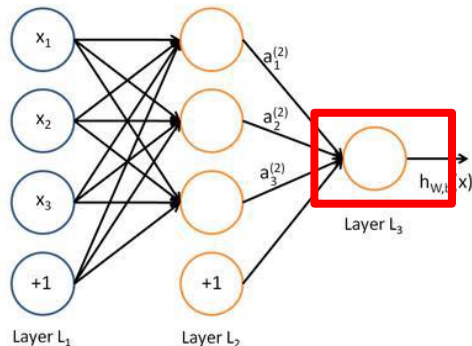
$$C(sumL) = \prod_{s=1}^Z C(L_s) = g_1^{L_1+L_2+\dots+L_Z} h_1^{q_2^{r_s}},$$

# Approximation of Sigmoid Function

- Approximation of activation function using Maclaurin series expansion since BGN encryption does not support exponentiation operation over ciphertext

$$\frac{1}{1+e^{-x}} = \frac{1}{2} + \frac{x}{4} - \frac{x^3}{48} + \frac{x^5}{480} + O(x^6).$$

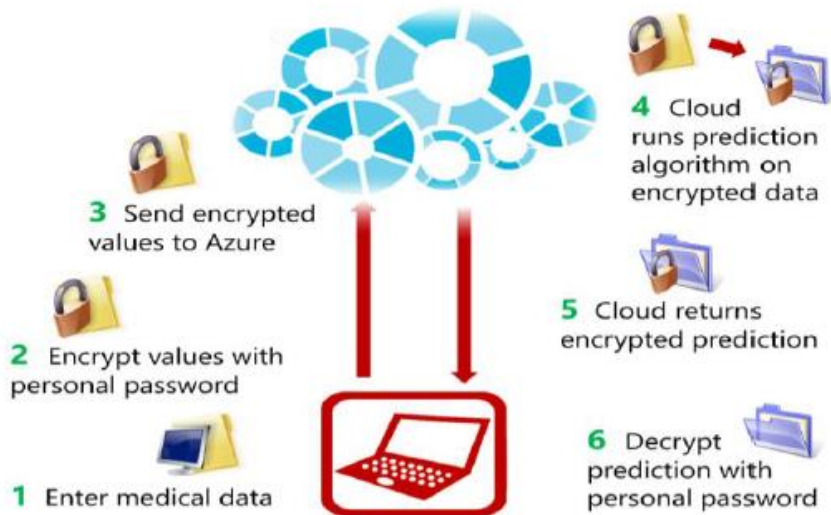
- For  $x^k$  ( $x = \sum x_s$ ), need call k times secure share algorithm



# **CryptoNets: Applying Neural Networks to Encrypted Data with High Throughput and Accuracy**

Nathan Dowlin, Ran Gilad-Bachrach, et.al.  
16'ICML



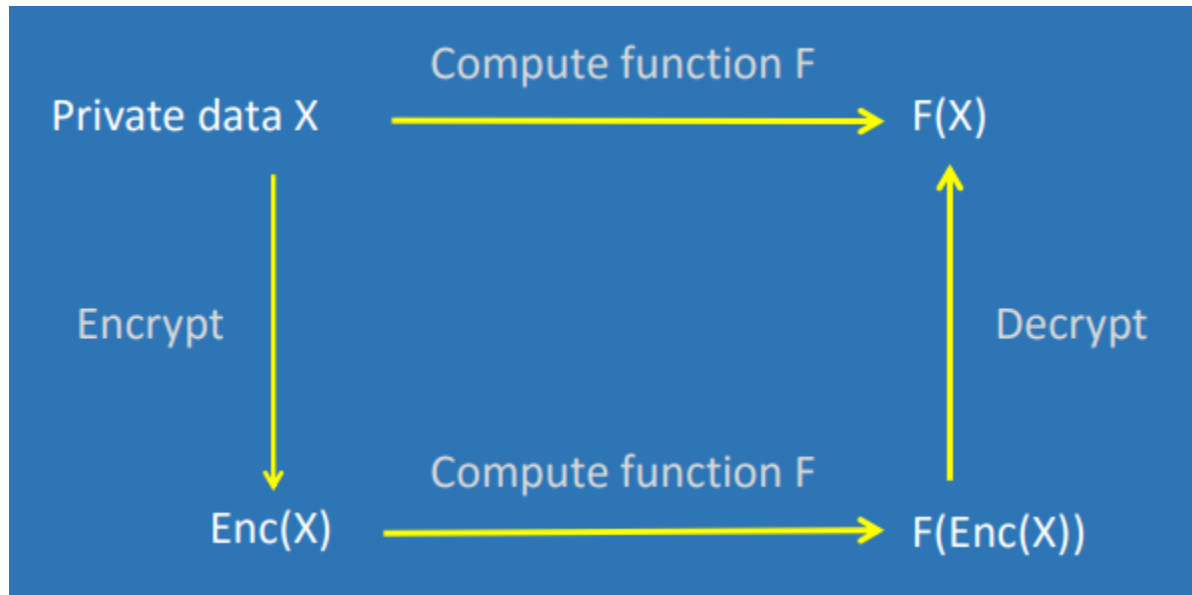


1. Weighted-Sum (convolution layer): a dot product of the weight vector and the vector of values of the feeding layer.
2. Max Pooling: Compute the maximal value of some of the components of the feeding layer.
3. Mean Pooling: Compute the average value of some of the components of the feeding layer.
4. Sigmoid:  $\frac{1}{(1+\exp(-z))}$
5. Rectified Linear:  $\max(0 ; z)$ .

# Homomorphic Encryption

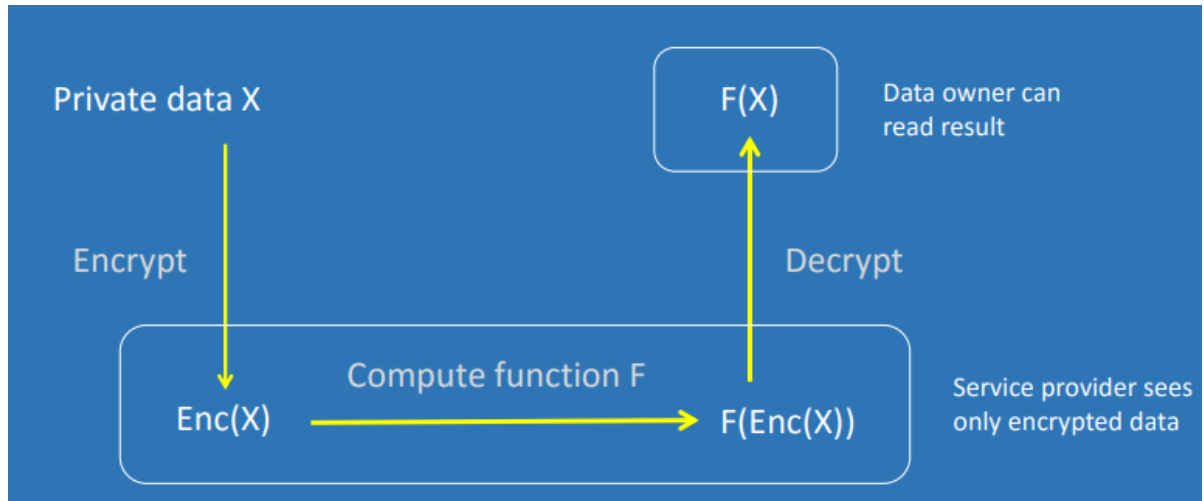
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1.  $F(x)$  is polynomial function



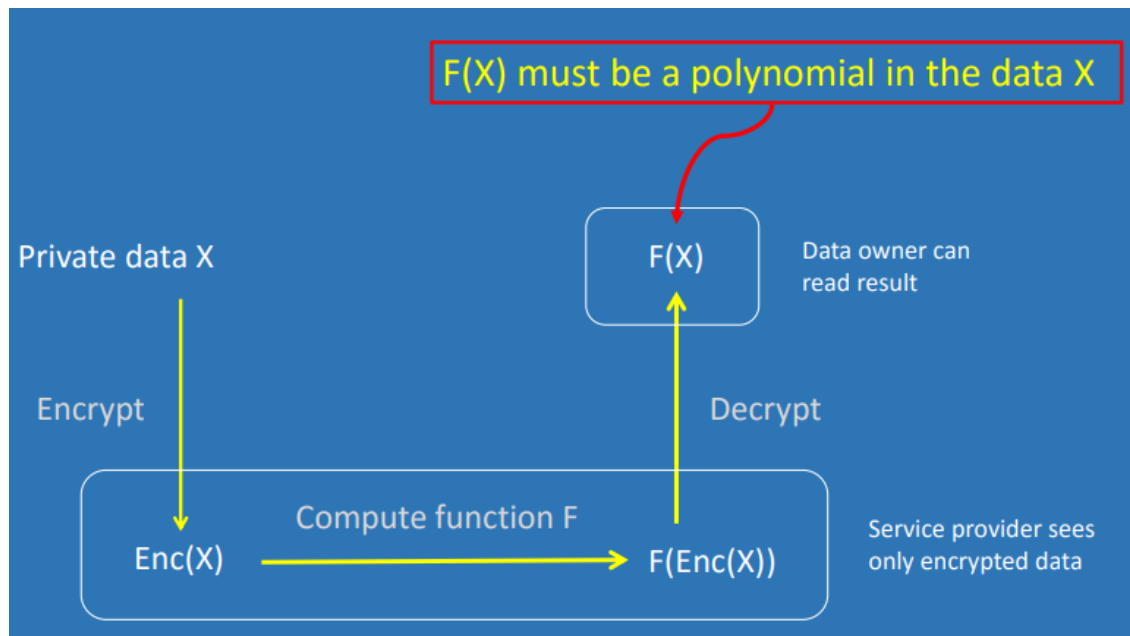
# Homomorphic Encryption

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# Homomorphic Encryption

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- Convert the real number to fixed precision numbers, and then convert them into a polynomial with the coefficients
  - I.e. Conversions as encodings (real number to  $R^n$ ) and decoding ( $R^n$  to real numbers).

$$m = \sum_{i=0}^{n-1} a_i X^i, \text{ with } a_i \text{ is integer}$$

- Levelled homomorphic encryption
  - ‘levelled’ refers to the fact that the homomorphic encryption scheme cannot correctly and securely carry out an arbitrary computation; instead, the scheme can only be used to compute functions up to a certain complexity, or level, that is fixed in advance

Encrypt  $c := \lfloor [q/t] m + e + hs \rfloor_q$

:

Decrypt  $m := \left\lfloor \left[ \frac{t}{q} fc \right] \right\rfloor_t$ .

:

Message- m

Public key - h

Parameters -Others

Ciphertext -c

Private key-f

# Noise & Correctness

## Simple example:

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- Enc( $m$ ):  $m + as + 2e \bmod q$ ,  $q$  is public
- Dec( $c$ ):  $((b \bmod q) * p) \bmod 2 = (b - q \lceil b/q \rceil) p \bmod 2$ 
  - $Bp - asp = (m + 2e) * p \bmod q$
  - Decrypt correctly  $e < \frac{q}{2}$

$p \leftarrow$  private key;

$S \leftarrow$  public key;  $p * s \bmod q = 0$

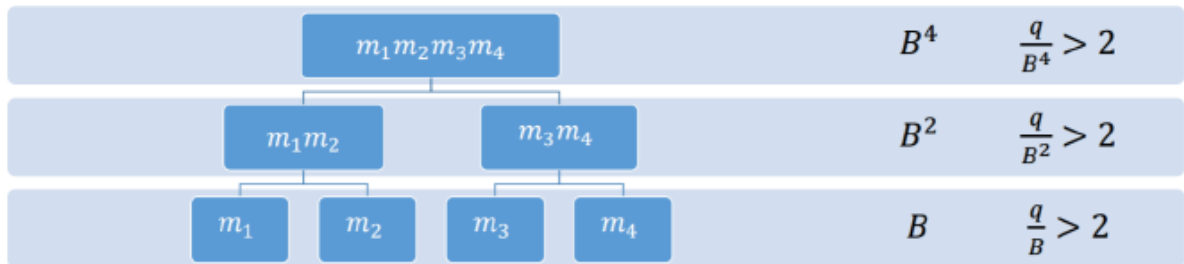
Sample  $a \leftarrow R_q$  uniform;  $e \leftarrow$  error



# Noise Growth

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- Initial noise:  $B$
- Addition: noise add up,  $B \rightarrow 2B$
- Multiplication: noise terms are multiplied,  $B \rightarrow B^2$



- $B^2 \rightarrow B^4, B^4 \rightarrow B^8, \dots, B^{2^{L-1}} \rightarrow B^{2^L}$  (L levels of multiplications)

- For a given  $t$  and  $n$ , the size of the initial noise and a fixed number of levels of multiplications, we can estimate the size of the resulting noise, and we can then **set  $q$  large enough** to allow for correct decryption

# Text Privacy



# Two Kinds of Document Privacy Leakage

## » Authorship attribution

- **writing style** can reveal author identity or other undisclosed personal attributes such as native language, gender or age.

## » Text representation

- User-generated **textual data** not only can reveal the identity of the user but also may contain individual's private information.

# Visual Privacy



# Privacy in Images and Videos

- » Photos or vlogs shared publicly on social platforms may reveal the users'
  - Home location
  - Contact
  - Bank account
  - Family members
  - Other sensitive information

# iPrivacy

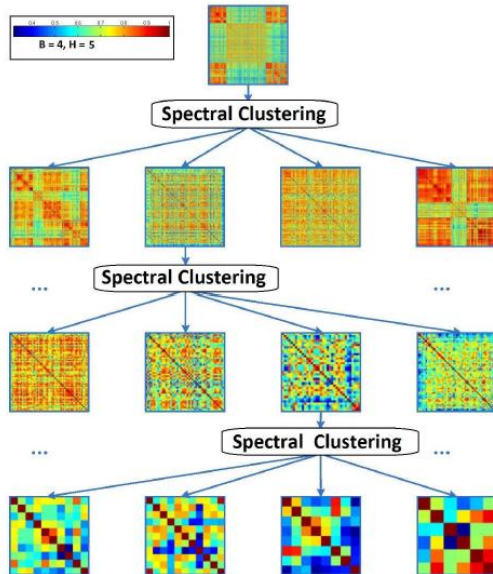
## » Step 1: Deep CNNs

- Semantic image segmentation
- Automatic object-privacy alignment

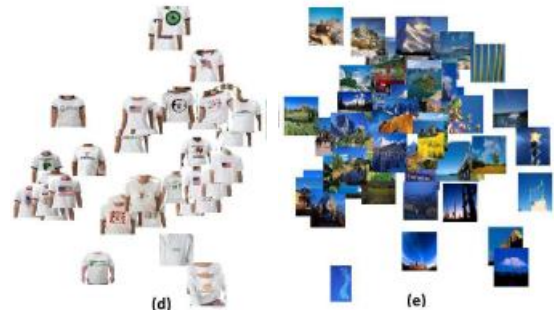


# iPrivacy

## » Step 2: A visual tree



- Organize privacy-sensitive object classes hierarchically in a coarse-to-fine fashion
- Each leaf node: privacy-sensitive object class





# iPrivacy

## » Step 3: Tree classifier

### » Example



Original image



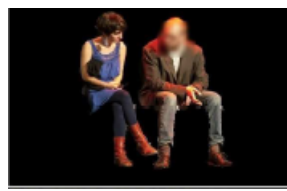
Human region



Detected human objects



Face identification



Face blurring



Shared image

# **What about Video Privacy?**

# Audio Privacy

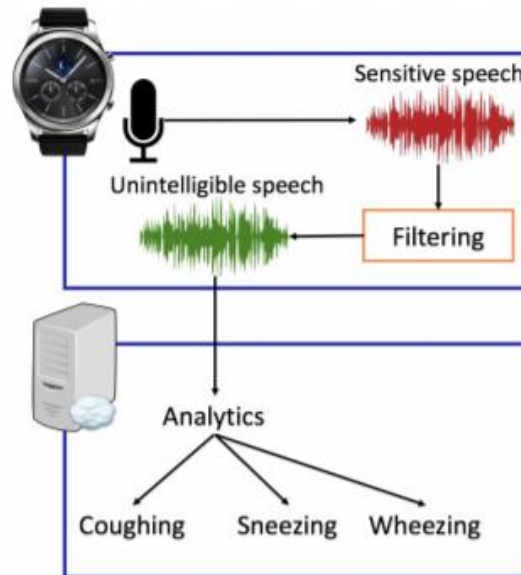


# Privacy Threats in Audio

- » Speech overheard
- » Human gestures/behavior leakage
  - through audio sensing signals
- » Contact-free monitoring of the health conditions of individuals
  - through breathing patterns

# Audio Privacy Protection : Approach 1

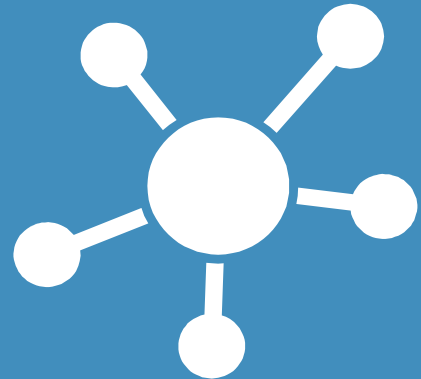
Approach proposed by D. Liaqat et al.



[1] D. Liaqat, E. Nemati, M. Rahman and J. Kuang, "A method for preserving privacy during audio recordings by filtering speech," 2017 IEEE Life Sciences Conference (LSC), Sydney, NSW, 2017, pp. 79-82.

# Social Network Privacy

Social networks describe entities (often people) and the relationships between them.



# Problem Description

- » **Model** we will model a social network as a simple, undirected graph  $G = (V, E)$ .
  - **Nodes** entities, each has a unique name
  - **Edges** connections between entities
  
- » **Goal** to remove information pertaining to individual identities, while retaining the topological structure of the graph. We will refer to this de-identified graph as  $G' = (V', E')$ .

# Location Privacy





## Problem Description

- » Cellular service providers and car companies are able to collect location trace data from many mobile users.
- » The owners of these repositories may wish to publish, distribute, or sell these data to enable a new set of applications called *location-based services* (LBS).

THANKS!

# Any questions?

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