

1. Use the GA to solve the travel salesmen problem with 25 cities. You can assume the missing information.

Solution:

Assumption:

1. Assume the population is  $5 * 4 = 20$ .
2. The reproduction procedure does not have mating but mutation only (To simplify the problem). For each group with 4 possible TSP solutions, the new group is form by the best solution within the group, and 3 new solutions, which are mutated (three types of mutations) from the best solution inside the group.
3. Mutation points are random.
4. There are three types of mutations. The first one is Flip, The second one is Swap and the third type is Slide.
5. Suppose one of the solution is [1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25] and the start point of mutation is 1 and the end point of mutation is 4. Then Flip will produce solution [4 3 2 1 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25]. Swap will produce solution [4 2 3 1 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25]. Slide will produce solution [2 3 4 1 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25].
6. City locations are 2-D only.

The Matlab code is as followed

In genCityLocation.m file:

```
% This function generates the city locations and  
% make sure all the city have different locations [x y]
```

```
function xy = genCityLocation(num_city)  
bound = 2 .* num_city;  
x = randperm(bound, num_city);  
y = randperm(bound, num_city);  
xy = [x' y'];  
end
```

In tsp\_ga1.m file:

```
function [optD optR] = tsp_ga1(xy, times)
```

```
%times = 100;
```

```
%x = randperm(100,25);  
%y = randperm(100,25);  
%xy = [x' y'];
```

```
% Initiate the population
```

```
popSize = 20; % Population size is 20
```

```
groupSize = 4; % Group size is 4
```

```
numCity = 25; % number of different cities is 25
```

```

pop = zeros(popSize, numCity); % A matrix with 20 rows and 25 columns
for i = 1:popSize
    pop(i, :) = randperm(numCity);
end

% Initiate the distance matrix
disMatx = zeros(numCity, numCity);
for j = 1:numCity
    for k = 1:numCity
        disMatx(j, k) = sqrt((xy(j, 1) - xy(k, 1))^2 + (xy(j, 2) - xy(k, 2))^2);
    end
end

% Run the GA
globalMin = Inf; % Global minimum distance
totalDist = zeros(1, popSize); % Total distance for each solution
disHistory = zeros(1, times);
tempPop = zeros(4, numCity);
newPop = zeros(popSize, numCity); % New population after mutations

for t = 1:times
    % Calculate the total distance
    for p = 1:popSize
        d = disMatx(pop(p, numCity), pop(p, 1));
        for q = 2:numCity
            d = d + disMatx(pop(p, q - 1), pop(p, q));
        end
        totalDist(p) = d;
    end

    % Find the best solution in the population
    [minDist index] = min(totalDist);
    disHistory(t) = minDist;
    if minDist < globalMin
        globalMin = minDist;
        optRoute = pop(index, :); % Best solution for now
    end

    % GA operators
    randomOrder = randperm(popSize);
    for p = 4:4:popSize
        group = pop(randomOrder(p - 3:p), :);
        groupDist = totalDist(randomOrder(p - 3:p));
        [groupMinDist groupIndex] = min(groupDist);
        groupOptRoute = group(groupIndex, :); % Get the best solution in one group
        routeInsertionPoints = sort(ceil(numCity*rand(1,2))); % Randomly get the mutation point
        I = routeInsertionPoints(1);
        J = routeInsertionPoints(2);
        for k = 1:4 % Mutate the best and get three new solution
            tempPop(k, :) = groupOptRoute;
            switch k

```

```

        case 2 % Flip
            tempPop(k, 1:J) = tempPop(k, J:-1:1);
        case 3 %Swap
            tempPop(k,[1 J]) = tempPop(k, [J 1]);
        case 4 %Slide
            tempPop(k, 1:J) = tempPop(k, [1+1:J 1]);
        end
    end
    newPop(p-3:p, :) = tempPop;
end
pop = newPop;
end

```

```

% Plot the optRoute
figure('Name', 'TSP_GA Result');
subplot(1, 2, 1);
plot(xy(:,1), xy(:,2), '.');
title('City Locations');
subplot(1, 2, 2);
rte = optRoute([1:numCity 1]);
plot(xy(rte, 1), xy(rte, 2), 'r.-');
title(sprintf('Final Minimum Distance = %1.4f', globalMin));
optD = globalMin;
optR = optRoute;
end

```

In the command line window:

```

xy = genCityLocation(25);
tsp_ga1(xy, 10);
tsp_ga1(xy, 100);
tsp_ga1(xy, 1000);
tsp_ga1(xy, 10000);

```

And the result of each function is shown in Figure 1, 2, 3, 4.

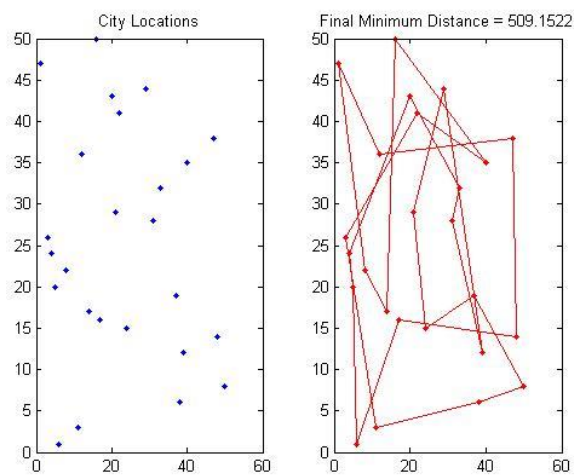


Figure 1: Result with iteration time = 10

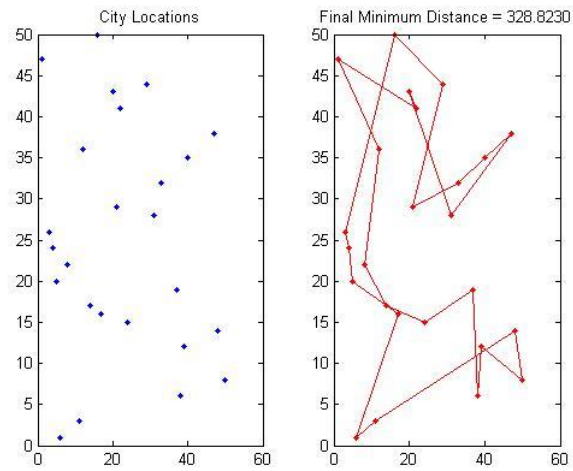


Figure 2: Result with iteration time = 100

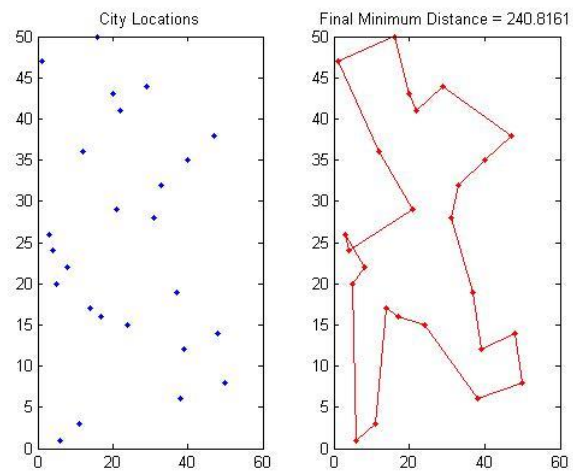


Figure 3: Result with iteration time = 1000

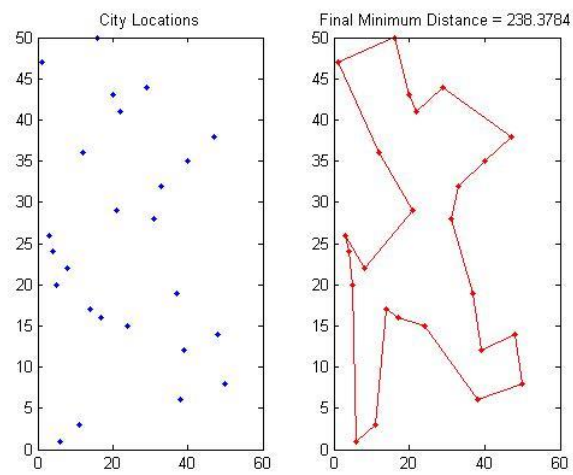


Figure 4: Result with iteration time = 10000