One Loop Matching for Quasi PDF

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January 13, 2020

1 **Diagrams**

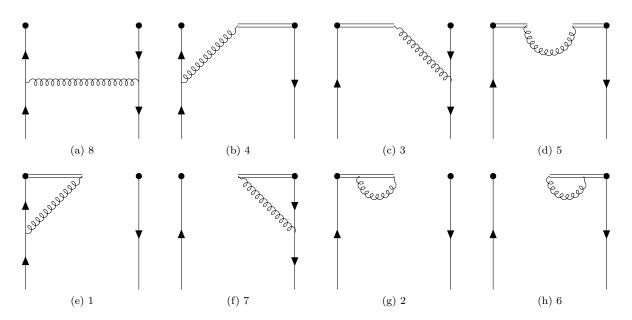


Figure 1: Diagrams of quasi PDF in Feynman gauge.

Analytic Results $\mathbf{2}$

$$\Gamma_{a} = \tilde{q}_{11} = \frac{\alpha_{S}C_{F}}{2\pi} \left\{ \begin{array}{c} (x-1)\ln\frac{x-1}{x} + 1, & x > 1\\ (1-x)\ln\frac{(P^{z})^{2}}{m^{2}} + (1-x)\ln\frac{4x}{1-x} + 1 - \frac{2x}{1-x}, & 0 < x < 1\\ (x-1)\ln\frac{x}{x-1} - 1, & x < 0 \end{array} \right.$$

$$(1)$$

$$\Gamma_{a} = \tilde{q}_{11} = \frac{\alpha_{S}C_{F}}{2\pi} \begin{cases}
(x-1)\ln\frac{x-1}{x} + 1, & x > 1 \\
(1-x)\ln\frac{(P^{z})^{2}}{m^{2}} + (1-x)\ln\frac{4x}{1-x} + 1 - \frac{2x}{1-x}, & 0 < x < 1 \\
(x-1)\ln\frac{x}{x-1} - 1, & x < 0
\end{cases}$$

$$\Gamma_{b} = \tilde{q}_{12} = \frac{\alpha_{S}C_{F}}{2\pi} \begin{cases}
-\frac{2x}{1-x}\ln\frac{x-1}{x} - \frac{1}{1-x}, & x > 1 \\
\frac{2x}{1-x}\ln\frac{(p^{z})^{2}}{m^{2}} + \frac{2x}{1-x}\ln\frac{4x}{1-x} + 1 - \frac{x}{1-x}, & 0 < x < 1 \\
-\frac{2x}{1-x}\ln\frac{x}{x-1} + \frac{1}{1-x}, & x < 0
\end{cases} \tag{2}$$

$$\Gamma_d = \tilde{q}_{13} = \frac{\alpha_S C_F}{2\pi} \begin{cases} \frac{1}{1-x}, & x > 1\\ -\frac{1}{1-x}, & 0 < x < 1\\ -\frac{1}{1-x}, & x < 0 \end{cases}$$
 (3)

Numerical Results (z = 1/4)3

Diagram a/8

```
0.349565 \text{ CV}(1,3) \text{ CV}(2,4/3) - 0.477465 \text{ CV}(1,3) \text{ CV}(2,4/3) \log(s)
```

Diagram b/4

```
0.212207 \text{ CV}(1,3) \text{ CV}(2,4/3) \log(s)-0.273255 \text{ CV}(1,3) \text{ CV}(2,4/3)
```

Diagram c/3

0.212207 CV(1,3) CV(2,4/3) log(s)-0.273255 CV(1,3) CV(2,4/3)

Diagram d/5

(-0.8488263632 +- 0)*CV(1,3)*CV(2,4/3)