Day
A. preparation
Ref. An Intruduction & QFT
M. Peskin & D. Schroeder
Pauli & Divoc motrices
$Q_{i} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, Q_{5} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}, Q_{3} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$
products of sigma matices Titi = Sij + i Eijk Tk
Weyl representation
$X^{\circ} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$, $X^{i} = \begin{pmatrix} 0 & 0^{i} \\ -0^{i} & 0 \end{pmatrix}$, $X^{5} = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$

And: - 6mmm: cation relation

SM Feynman Rules: M. M ig. 8 Pr. Sij /Jz Joseph W igs 8ⁿ T^aj p-mtit Sij - ight Say - 2 (gm - pr) Feynman Gauge & unitary Gauge

0

Physical constants (p) G 2019): $M_{\pm} = 172.9 \pm 0.4 \text{ GeV}$ $M_{W} = 80.379 \pm 0.012 \text{ GeV}$ M_{b} , M_{e} , M_{q} set to 0, ckM to diegonal. Och coupling (\overline{M}_{S} scheme) $\partial_{S}(M) = \frac{9^{2}(M)}{42}$, $\partial_{S}(M_{\pm}) = 0.118 \pm 0.001$

Ew coupling (GF scheme) $G_F = \frac{\sqrt{2}g^2}{8m_w^2} = 1.16638 \times 10^{-5} \text{ GeV}^2$

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B. Top quark decay out LO (total winth) iM = ü(p,) 8 p u(p.) · E (p2) · ig/52 for impolarized top and sum over final state splas, 2/M/2=1.7~[p,8mp. (po+m4).8) PL). Nc · \(\frac{1}{2} \) \(\frac{1} \) \(\frac{1}{2} \) \(\frac{1}{2 re call spin sum for massive vector boson 三1M12= 92 {2Tr[水水。]+ him. Tr[水水。] With a bit calention, $|M|^{\nu} = M_{\nu}^{2} \cdot (1-x) \cdot (1+\frac{1}{2x}) \cdot \frac{9^{2}}{2^{2}}, \quad x = \frac{mw}{mt^{2}}$ With the usual formula for decay width, $|T| = \frac{1}{2m_{\tau}} \cdot \int d|T|^{2} \cdot M|^{\nu}$ $|T| = \frac{1}{2m_{\tau}} \cdot \int d|T|^{2} \cdot M|^{\nu}$

 $= \frac{1}{2m_{+}} \cdot m_{+}^{2} (1-x) \cdot (1+\frac{1}{2x}) \cdot \frac{4m_{+}^{2}G_{F}}{\sqrt{2}} \cdot \frac{1}{8^{2}} \cdot (1-x)$ $= \frac{\sqrt{2} G_{F} m_{+}^{2}}{\sqrt{2}} \cdot m_{+} \cdot (1-x)^{2} (1+\frac{1}{2x})$

numerically. 17 = 1.49 GeV

note when m. >> mn. | x m; due to the longestudinal W/goldstone contribution, e.g.,

 $\frac{1}{|\mathcal{M}_{c}|^{2}} \approx \frac{1}{2} \operatorname{Tr} \left[\frac{\mathcal{K} \mathcal{B}}{\mathcal{A}} \right] \cdot \left(\frac{\mathcal{K} \mathcal{B}}{\mathcal{A}} \right)^{2}$

using $v = \frac{z_{m_n}}{g}$, $|\mathcal{M}_1|^2 \approx m_1^2 \cdot \frac{1}{z_x} \cdot \frac{g^2}{\nu}$.

- - '

Recall authorly width of unstable particles are vather defined as imaginary part of 1PI two-point con. It's with optical theorem.

Im
$$-\frac{1}{2}$$
 $= \frac{1}{2}$ $= \frac{1}{2}$ (unitary condition $|1+i\hat{T}|^2 = |\Rightarrow -i(\hat{T}-\hat{T}^+) = \hat{T}^+\hat{T}|$)
That implies for scalar $p = -\frac{1}{2} \frac{(M(p^2))}{M}$.

For the case of fermion, define
$$-i\hat{Z}(p) = -\frac{1}{2} \frac{(p)}{p_R} + \hat{Z}_-(p)p_L$$
then

$$\Gamma = - \left[\operatorname{Im} \left(\overline{2}_{+}(\beta) + \overline{2}_{-}(\beta) \right) \middle| \beta = m \right],$$

arxiv:0801.0669

alternative way,

p / m p in dimensional regularization

d=4-26 $-i\sum_{k}(p)=m^{2k}\cdot\int\frac{d^{k}k}{(27)^{k}}\cdot(-g^{2}/2)\cdot\frac{1}{(k^{2}-m^{2}w)((k-p)^{2})}$ the Diroc algebra, $=-2(1-t)(\beta-k)-\frac{2p\cdot k}{m_w^2}k+\frac{k^2}{m_w^2}(k+p),$ $\frac{1}{2^{2} \cdot \gamma_{p}} \cdot \left(2 M^{2}\right)^{\epsilon} \cdot \int d^{d}k \cdot \frac{1}{\left(\left|\epsilon^{2} - M N^{2}\right|\right)\left(\left(k - p\right)^{2}\right)} = \beta_{o}\left(p^{2}, M^{2}_{w}, o\right)$ 1 (2/2) 6. [ddk. (k2-mw)((k-p)2) = B. (p2, m2, 0). pm (using Passarino - Vellman nortation that will be introduced later, $V_{\Gamma} = \frac{\Gamma^{2}(1-\epsilon)}{\Gamma(1-2\epsilon)}$)

$$-\frac{m_{N}^{2}}{2b\cdot k\cdot k}\cdot \frac{(k_{1}\cdot m_{N}^{2})((k-b)_{1})}{(k_{1}\cdot m_{N}^{2})((k-b)_{2})} = -(1+\frac{m_{N}^{2}}{b_{2}})\cdot \frac{(k_{1}\cdot m_{N}^{2})((k-b)_{2})}{\sqrt{k}}$$

$$\frac{k^2}{m^2}.(K+p).\frac{1}{(k^2-m^2)((k-p)^2)}$$

$$\left[e \cdot g, \int d^{d}k \cdot \frac{1}{(k-p)^{2}} = 0, \int d^{d}k \frac{k^{2} - m_{v}^{2}}{k^{2} - m_{v}^{2}} = 0\right]$$

thus

using

$$B_{1}(p^{2}, M_{w}^{2}, 0) = \frac{1}{2p^{2}} \cdot A_{0}(m_{w}^{2}) - \frac{1}{2}(H_{p^{2}}^{M_{w}^{2}}) B_{0}(p^{2}, M_{w}^{2}, 0)$$

0,1

Bo
$$(p^2, m_{\tilde{u}}, 0) = \left(\frac{m_{\tilde{u}}^2}{m_{\tilde{u}}^2}\right)^{\epsilon} \left\{ \pm + 2 + \frac{m_{\tilde{u}}^2 - p^2}{p^2} \ln \left(\frac{m_{\tilde{u}}^2 - p^2 - i\epsilon}{m_{\tilde{u}}^2}\right) \right\}$$

One find the imaginary put,

$$Im B_{o}(p^{2}, m_{w}^{2}, o) = \frac{p^{2} - m_{w}^{2}}{p^{2}} \times O(p^{2} - m_{w}^{2})$$

 $findly$.

$$I_{m} \sum_{z} (p) = \frac{1}{162^{2}} \cdot \frac{9^{2}}{2} \cdot \cancel{p} \cdot \left(\frac{m_{w}^{2}}{p^{2}} - \frac{p^{2}}{2m_{w}^{2}} - \frac{1}{2} \right) .$$

$$\left(1 - \frac{m_{w}^{2}}{p^{2}} \right) \times 0 \cdot p^{2} - m_{w}^{2})$$

Proof of optical theory at Feynman diagram level -> Cuthosky rules!!