

$((\lambda x1) (f\ 1\ x1)) + \#t$

Rename bound variables:

$((\lambda x1) (f\ 1\ x1)) + \#t$

Assign type variables:	
expression	variables
$((\lambda x1) (f\ 1\ x1)) + \#t$	T0
$(\lambda x) (f\ 1\ x)$	T1
$(f\ 1\ x)$	T2
f	Tf
1	Tnum1
x	Tx
+	T+
#t	T#t

Construct type equations:	
expression	equation
$((\lambda x1) (f\ 1\ x1)) + \#t$	$T1 = [T+ * T\#t \rightarrow T0]$
$(\lambda x) (f\ 1\ x)$	$T1 = [Tf * Tx \rightarrow T2]$
$(f\ 1\ x)$	$Tf = [Tnum1 * Tx \rightarrow T2]$
1	$Tnum1 = \text{Number}$
+	$T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}]$
#t	$T\#t = \text{Boolean}$

Solving equations:	
equation	substitution
1 $T1 = [T+ * T\#t \rightarrow T0]$	
2 $T1 = [Tf * Tx \rightarrow T2]$	
3 $Tf = [Tnum1 * Tx \rightarrow T2]$	
4 $Tnum1 = \text{Number}$	
5 $T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}]$	
6 $T\#t = \text{Boolean}$	

$(T1 = [T+ * T\#t \rightarrow T0]) \circ \text{Substitution} = (T1 = [T+ * T\#t \rightarrow T0])$

equation	substitution
2 $T1 = [Tf * Tx \rightarrow T2]$	$\{ T1 := [T+ * T\#t \rightarrow T0] \}$
3 $Tf = [Tnum1 * Tx \rightarrow T2]$	
4 $Tnum1 = \text{Number}$	
5 $T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}]$	
6 $T\#t = \text{Boolean}$	

$(T1 = [Tf * Tnum1 * Tx \rightarrow]) \circ \text{Substitution} = ([T+ * T\#t \rightarrow T0] = [Tf * Tx \rightarrow T2])$

equation	substitution
3 $Tf = [Tnum1 * Tx \rightarrow T2]$	$\{ T1 := [T+ * T\#t \rightarrow T0] \}$
4 $Tnum1 = \text{Number}$	
5 $T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}]$	
6 $T\#t = \text{Boolean}$	
7 $Tf = T+$	
8 $Tx = T\#t$	
9 $T2 = T0$	

$(Tf = [Tnum1 * Tx \rightarrow T2]) \circ \text{Substitution} = \text{Substitution} \circ (Tf = [Tnum1 * Tx \rightarrow T2])$

equation	substitution
4 $Tnum1 = \text{Number}$	$\{ T1 := [T+ * T\#t \rightarrow T0], Tf := [Tnum1 * Tx \rightarrow T2] \}$
5 $T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}]$	
6 $T\#t = \text{Boolean}$	
7 $Tf = T+$	
8 $Tx = T\#t$	
9 $T2 = T0$	

$(Tnum1 = \text{Number}) \circ \text{Substitution} = \text{Substitution} \circ (Tnum1 = \text{Number})$

equation	substitution
5 $T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}]$	$\{ T1 := [T+ * T\#t \rightarrow T0], Tf := [\text{Number} * Tx \rightarrow T2], Tnum1 = \text{Number} \}$
6 $T\#t = \text{Boolean}$	
7 $Tf = T+$	
8 $Tx = T\#t$	
9 $T2 = T0$	

$(T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}]) \circ \text{Substitution} = \text{Substitution} \circ (T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}])$

equation	substitution
6 $T\#t = \text{Boolean}$	$\{ T1 := [[\text{Number} * \text{Number} \rightarrow \text{Number}] * T\#t \rightarrow T0], Tf := [\text{Number} * Tx \rightarrow T2], Tnum1 = \text{Number}, T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}] \}$
7 $Tf = T+$	
8 $Tx = T\#t$	
9 $T2 = T0$	

$(T\#t = \text{Boolean}) \circ \text{Substitution} = \text{Substitution} \circ (T\#t = \text{Boolean})$

equation	substitution
7 $Tf = T+$	$\{ T1 := [[\text{Number} * \text{Number} \rightarrow \text{Number}] * \text{Boolean} \rightarrow T0], Tf := [\text{Number} * Tx \rightarrow T2], T+ = [\text{Number} * \text{Number} \rightarrow \text{Number}], T\#t = \text{Boolean} \}$
8 $Tx = T\#t$	
9 $T2 = T0$	

$$(Tf = T+) \circ \text{Substitution} = \text{Substitution} \circ (Tf = T+)$$

	equation	substitution
8	$Tx = T\#t$	$\{ T1 := [(Number * Number \rightarrow Number) * Boolean \rightarrow T0], Tf := [Number * Tx \rightarrow T2], T+ = [Number * Number \rightarrow Number], T\#t = Boolean \}$
9	$T2 = T0$	
10	$Tx = Number$	
11	$T2 = Number$	

$$(Tx = T\#t) \circ \text{Substitution} = \text{Substitution} \circ (Tx = T\#t)$$

	equation	substitution
9	$T2 = T0$	$\{ T1 := [(Number * Number \rightarrow Number) * Boolean \rightarrow T0], Tf := [Number * T\#t \rightarrow T2], T+ = [Number * Number \rightarrow Number], T\#t = Boolean, Tx = T\#t \}$
10	$Tx = Number$	
11	$T2 = Number$	

$$(T2 = T0) \circ \text{Substitution} = \text{Substitution} \circ (T2 = T0)$$

	equation	substitution
10	$Tx = Number$	$\{ T1 := [(Number * Number \rightarrow Number) * Boolean \rightarrow T0], Tf := [Number * T\#t \rightarrow T0], T+ = [Number * Number \rightarrow Number], T\#t = Boolean, Tx = T\#t \}$
11	$T2 = Number$	

$$(Tx = Number) \circ \text{Substitution} = \text{Substitution} \circ (Tx = Number)$$

now we got $Tx = Boolean$ and $Tx = Number$ so we can say that the expression is not well-typed