10) Testing Hypotheses

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December 2019

Reference

Tables, Graphics, and Figures from

Computational and Inferential Thinking: The Foundations of Data Science

Adhikari & DeNero (2019): Ch 11 Testing **Hypotheses**

https://www.inferentialthinking.com/

US Supreme Court, 1965: Swain vs Alabama

26% of the eligible jurors were black in Talladega County in Alabama

Swain's trial: 8 blacks among the 100 selected for the jury panel

No black man was selected for the trial jury

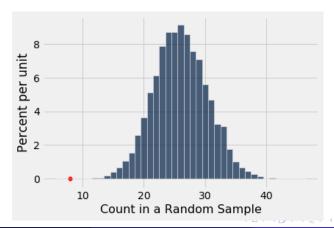
```
from datascience import *
eligible_population = [0.26, 0.74]
sample_proportions(100, eligible_population)
```

array([0.25, 0.75])

```
(100 * sample proportions(100, eligible population)).item(0)
                         24.0
def one simulated count():
    return (100 * sample proportions(100,
             eligible population)).item(∅)
counts = make array()
import numpy as np
repetitions = 10000
for i in np.arange(repetitions):
    counts = np.append(counts, one simulated count())
```

Comparing the Prediction and the Data

```
Table().with_column(
    'Count in a Random Sample', counts
).hist(bins = np.arange(5.5, 46.6, 1))
plots.scatter(8, 0, color='red', s=30);
```



Plants should bear purple or white flowers at random, in the ratio 3:1

```
def distance from 75(p):
    return abs(100*p - 75)
model proportions = [0.75, 0.25]
def one_simulated_distance():
    proportion purple in sample = sample proportions(929,
                               model proportions).item(∅)
    return distance from 75(proportion purple in sample)
distances = make array()
repetitions = 10000
for i in np.arange(repetitions):
   distances = np.append(distances, one_simulated_distance())
```

Purple-flowering Statistic

Mendel recorded:

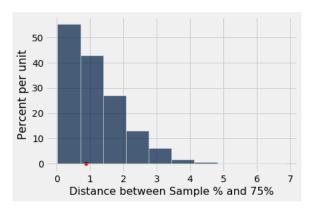
705 / 929 0.7588805166846071 =
$$75.88\%$$

sample percent of purple-flowering plants - 75

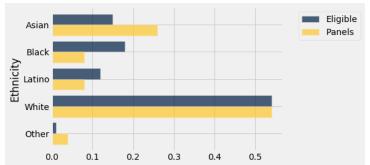
$$0.8880516684607045 = 0.88\%$$

Comparing the Prediction and the Data

```
Table().with_column(
    'Distance between Sample % and 75%', distances
).hist()
plots.scatter(observed_statistic, 0, color='red', s=30);
```



Jury Selection in Alameda County in 2010 among 1,453 People



Comparison with Panels Selected at Random

Ethnicity	Eligible	Panels	Random Sample
Asian	0.15	0.26	0.163799
Black	0.18	0.08	0.194769
Latino	0.12	0.08	0.128011
White	0.54	0.54	0.501721
Other	0.01	0.04	0.0116999

The Distance between Two Distributions

Ethnicity	Eligible	Panels	Difference	Absolute Difference
Asian	0.15	0.26	0.11	0.11
Black	0.18	0.08	-0.1	0.1
Latino	0.12	0.08	-0.04	0.04
White	0.54	0.54	0	0
Other	0.01	0.04	0.03	0.03

Simulating One Value of the Statistic

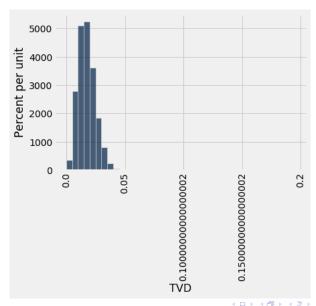
jury with diffs.column('Absolute Difference').sum() / 2

```
0.14
def total variation distance(distribution 1, distribution 2):
    return sum(np.abs(distribution 1 - distribution 2)) / 2
total variation distance(jury.column('Panels'), jury.column('Eligible'))
                               0.14
sample distribution = sample proportions(1453, eligible population)
total variation distance(sample distribution, eligible population)
```

0.0364280798348245

5,000 Simulations

```
def one simulated tvd():
    sample distribution = sample proportions(1453,
                              eligible population)
    return total variation distance(sample distribution,
                                   eligible population)
tvds = make array()
repetitions = 5000
for i in np.arange(repetitions):
    tvds = np.append(tvds, one simulated tvd())
```



Berkeley Statistics Class

350 students was divided into 12 discussion sections (n)

$$H_0: \mu_3 = \mu_n \text{ vs } H_A: \mu_3 \neq \mu_n$$

```
path_data = 'https://github.com/data-8/textbook/raw/gh-pages/data/'
scores = Table.read_table(path_data + 'scores_by_section.csv')
```

section_averages = scores.group('Section', np.average)

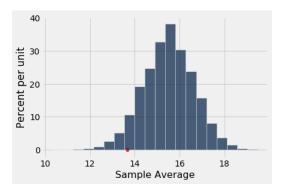
Section	Midterm	average
1		15.5938
2		15.125
3		13.6667

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Simulating a Statistic 10,000

27 randomly selected scores

```
averages_tbl = Table().with_column('Sample Average', sample_averages)
averages_tbl.hist(bins=20)
observed_statistic = 13.667
plots.scatter(observed_statistic, 0, color='red', s=30);
```



np.count_nonzero(sample_averages <= observed_statistic) / repetitions</pre>

0.0553

Simulating a Statistic 50,000

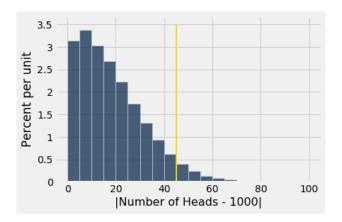
$$H_0: p = \frac{1}{2}$$
 (coin is fair) vs $H_A: p \neq \frac{1}{2}$

test statistic $= \mid$ number of heads $-1000 \mid$

```
fair_coin = [1, 0]
def one_simulated_statistic():
    number_of_heads = sum(np.random.choice(fair_coin, 2000))
    return abs(number_of_heads - 1000)

statistics = make_array()
for i in np.arange(50000):
    statistics = np.append(statistics, one_simulated_statistic())
```

```
results = Table().with_column('|Number of Heads - 1000|', statistics)
results.hist(bins = np.arange(0, 101, 5))
plots.plot([45, 45], [0, 0.035], color='gold', lw=2);
```



The area to the right of 45 is about 5%