



A Spherical Hidden Markov Model for Semantics-Rich Human Mobility Modeling

Wanzheng Zhu (WZ)*, Chao Zhang*, Shuochao Yao, Xiaobin Gao, Jiawei Han

University of Illinois, at Urbana-Champaign

wz6@illinois.edu

Human Mobility Modeling – Problem Description

Input

Human Trace Data: *Twitter*



Time

Fri Aug 01 00:00:30 CDT 2014



Location

33.982552, -118.309053



Text

absolutely_loved guardian_galaxyI
absolutely loved Guardians of the Galaxy 😊

Output

Mobility Modeling

Pattern Discovery

- Understanding Human Movement
- Next Location Prediction
- Traffic Scheduling
- Urban Planning
- Activity Recommendation

What & **When** are people's activities at different regions?

How & **Why** do people move from one region to another?

Human Mobility Modeling – Related Works

Pattern-based Methods

Discovering specific mobility patterns that occur frequently

- Frequent Sequential Patterns
- Co-location Patterns
- Periodic Patterns

Model-based Methods

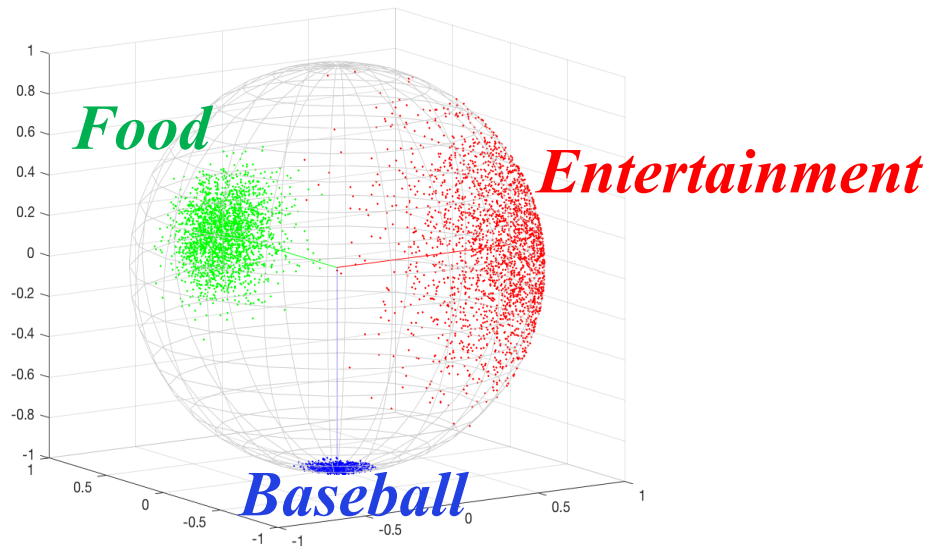
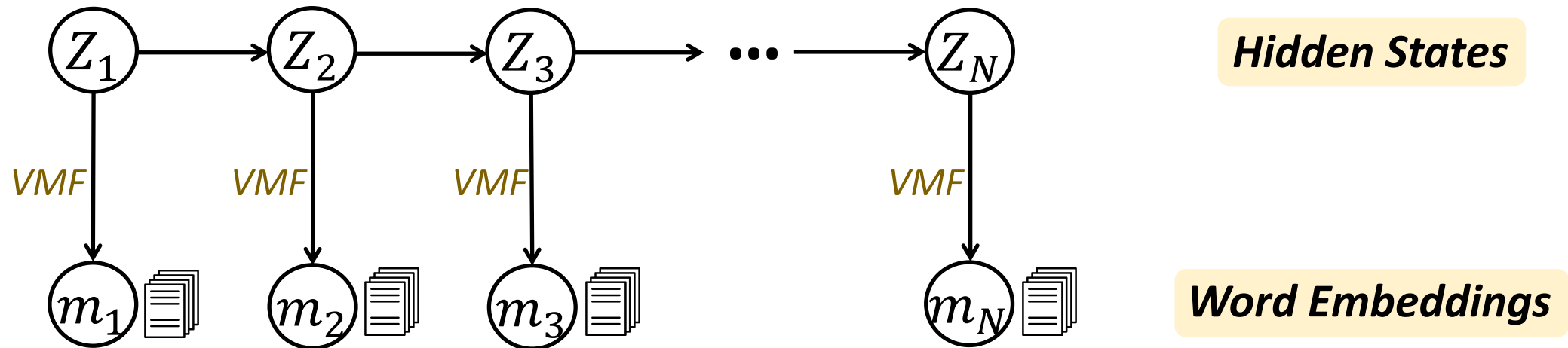
Statistical models – fitting data into the model.

- Hidden Markov Models
- Continuous-time Random-walk Models
- Periodicity Underlying Human Movement

Most previous works do NOT consider **TEXT** information!

Previous *State-of-the-art* work: GMove (Zhang *et al.* 2016a)

Model Description (HMM + VMF)

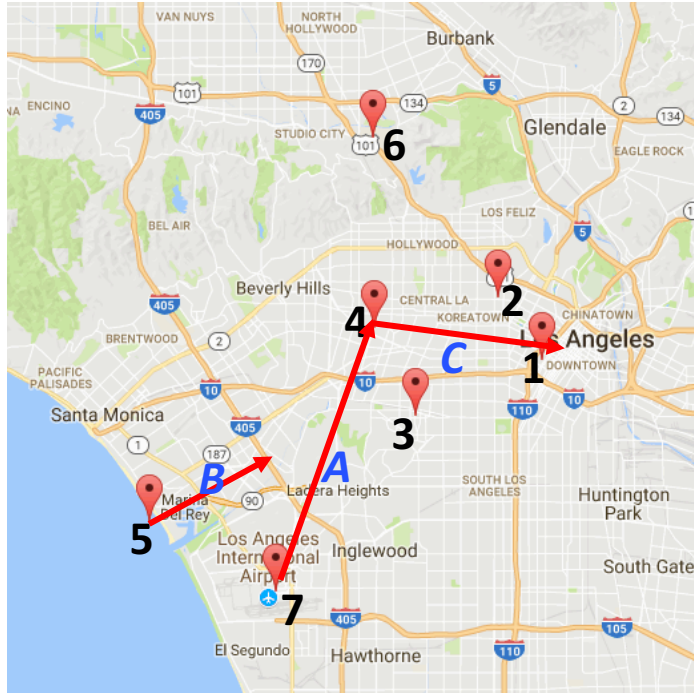


The vMF Distribution

Intuition:

- Word embeddings are on the surface of a **unit hypersphere**
- ***The Von Mises-Fisher (vMF) distribution*** is well suited for *unit-length* directional data with different *concentration* levels.

Interesting States



State 1: Basketball	State 2: Baseball	State 3: General Sports	State 4: Restaurant/ Food	State 5: Beach	State 6: Universal Studios	State 7: Airport
lakers	homeruns	cfbplayoff	osteriamamm a	monica	universal	internati onal
grizzlies	dodgers	oilers	island's	beachselfie	waterworld	angeles
celtics	giants	2-May	hotwings	zoltar	hhn2014	los
nba	162	jets	jicama	beach	hollywoodh orrornights	airport
bryant	sfvspit	preseason	flore	fishbarmb	universalcit ywalk	lax

Dataset: ~30K Tweets in LA, from Aug/01/2014 to Nov/30/2014

Interesting Patterns:

- **A:** LA Airport/Flights → Restaurants in LA
- **B:** Beach Activities → Leisure Activities
- **C:** Food → Concert/ Show

The vMF Distribution – Parameter Inference



How to update the HMM parameters?

M-step of the EM algorithm:

$$\theta := \operatorname{argmax}_{\theta} \sum_i \sum_{z_i} Q_i(z_i) \log p(\mathbf{m}_i, \mathbf{z}_i | \theta)$$

- Very complicated math expression

$$f_p(\mathbf{x}; \boldsymbol{\mu}, \boldsymbol{\kappa}) = \frac{\boldsymbol{\kappa}^{p/2-1}}{(2\pi)^{p/2} I_{p/2-1}(\boldsymbol{\kappa})} \exp(\boldsymbol{\kappa} \boldsymbol{\mu}^T \mathbf{x})$$

Modified Bessel Function: $I_{p/2-1} = \left[\sum_{m=0}^{\infty} \frac{1}{m! \Gamma(m+p/2)} \left(\frac{x}{2} \right)^{2m+p/2-1} \right]$

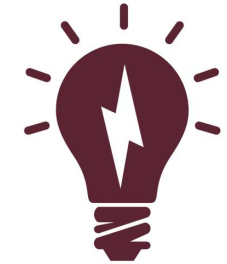
Gamma function

Theoretical Contribution of the vMF distribution

There is ***no closed form solution*** for updating κ in the M-step.

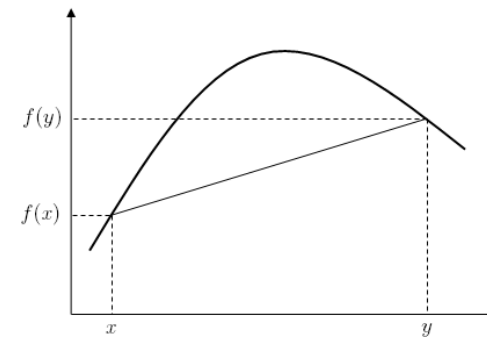
Existence: There exists ***one unique*** κ to maximize the M-step.

- By ***the intermediate value theorem***



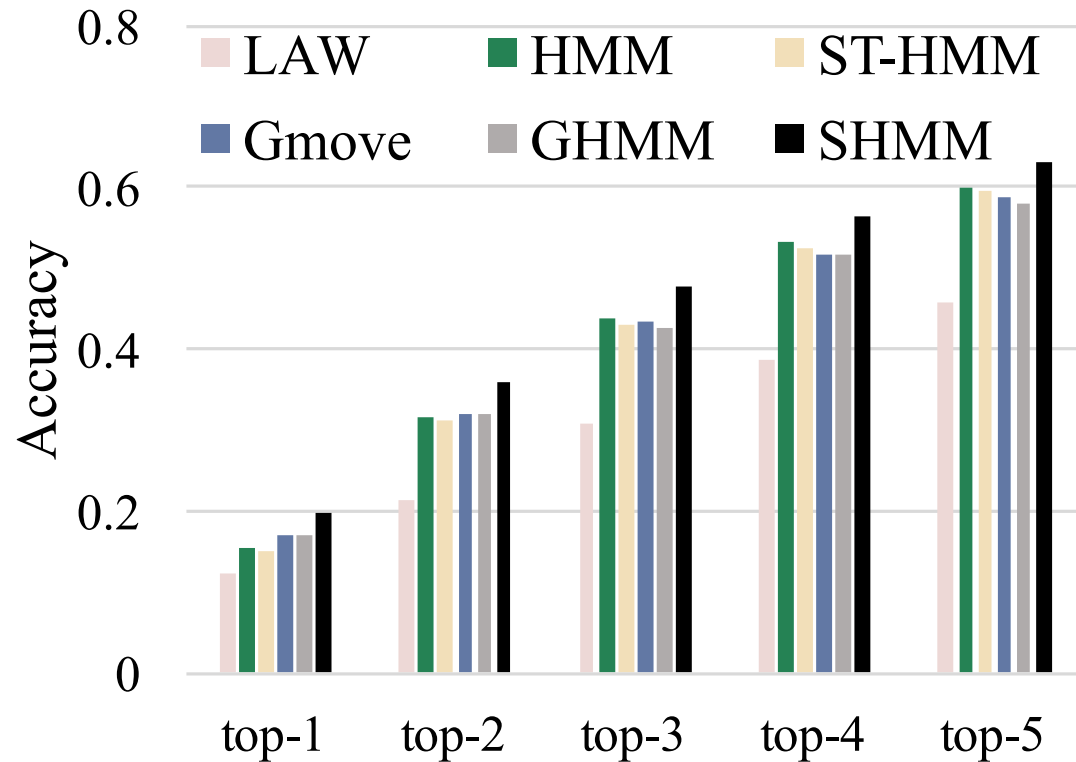
Feasibility: ***Newton's method*** is guaranteed to converge to the optimal κ .

- By its ***concavity*** property
- Quadratic convergence rate

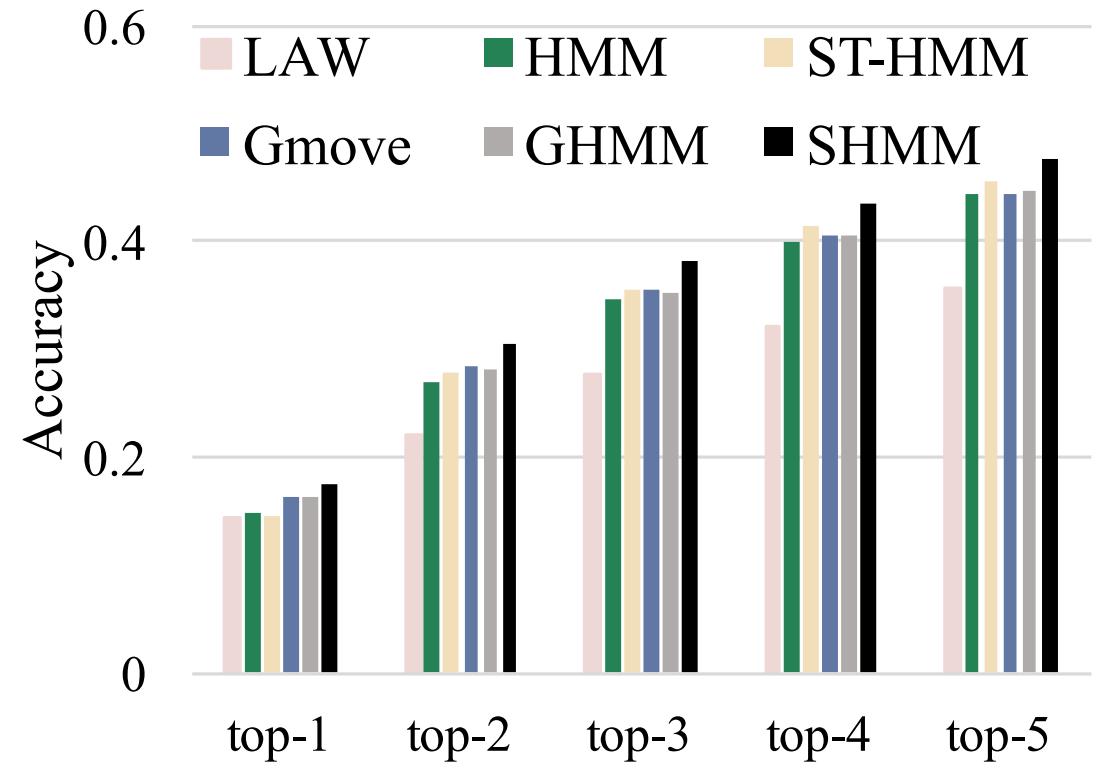


Simulation: Synthetic data

Results – Next Location Prediction



Dataset: ~30k Tweets in LA, from Aug/01/2014 to Nov/30/2014



Dataset: ~42k Tweets in NYC, from Aug/01/2014 to Nov/30/2014

Accuracy Improvement: ~3.2%

Contributions and Conclusion

Model

HMM + VMF



Mobility
Modeling



Downstream
Applications

Semantics

Interpretable

Theory

Existence



Feasibility

HMM + VMF

EM + VMF

Thank you!

A Spherical Hidden Markov Model for Semantics- Rich Human Mobility Modeling

Wanzheng Zhu (WZ)

wz6@illinois.edu

Code & Data & Paper & Presentation:

<https://github.com/WanzhengZhu/SHMM>