

# 成像算法基础

滤波

# 滤波卷积

滤波>卷积

17	24	12	28	31	36
21	5	7	29	18	36
4	6	13	12	15	14
16	18	21	13	15	11
22	22	31	24	26	36

# 卷积

<del>1</del> <sup>9</sup> 7	<del>2</del> <sup>8</sup> 4	<del>1</del> <sup>7</sup> 2	28	31	36
<del>2</del> <sup>4</sup> 1	<del>3</del> <sup>5</sup>	<del>7</del> <sup>6</sup>	29	18	36
<del>1</del> <sup>4</sup>	<del>3</del> <sup>2</sup>	<del>1</del> <sup>3</sup> 3	12	15	14
16	18	21	13	15	11
22	22	31	24	26	36

$9 \times 17 + 8 \times 24 + 7 \times 12 + 4 \times 21 + 5 \times 5 + 6 \times 7 + 1 \times 4$

# 扩展的滤波应用

- 去噪
- 锐化
- Demosaic
- 畸变调整
- 统计
- .....

通过像素及像素周周边值得到新的像素值的操作

# 边界效应

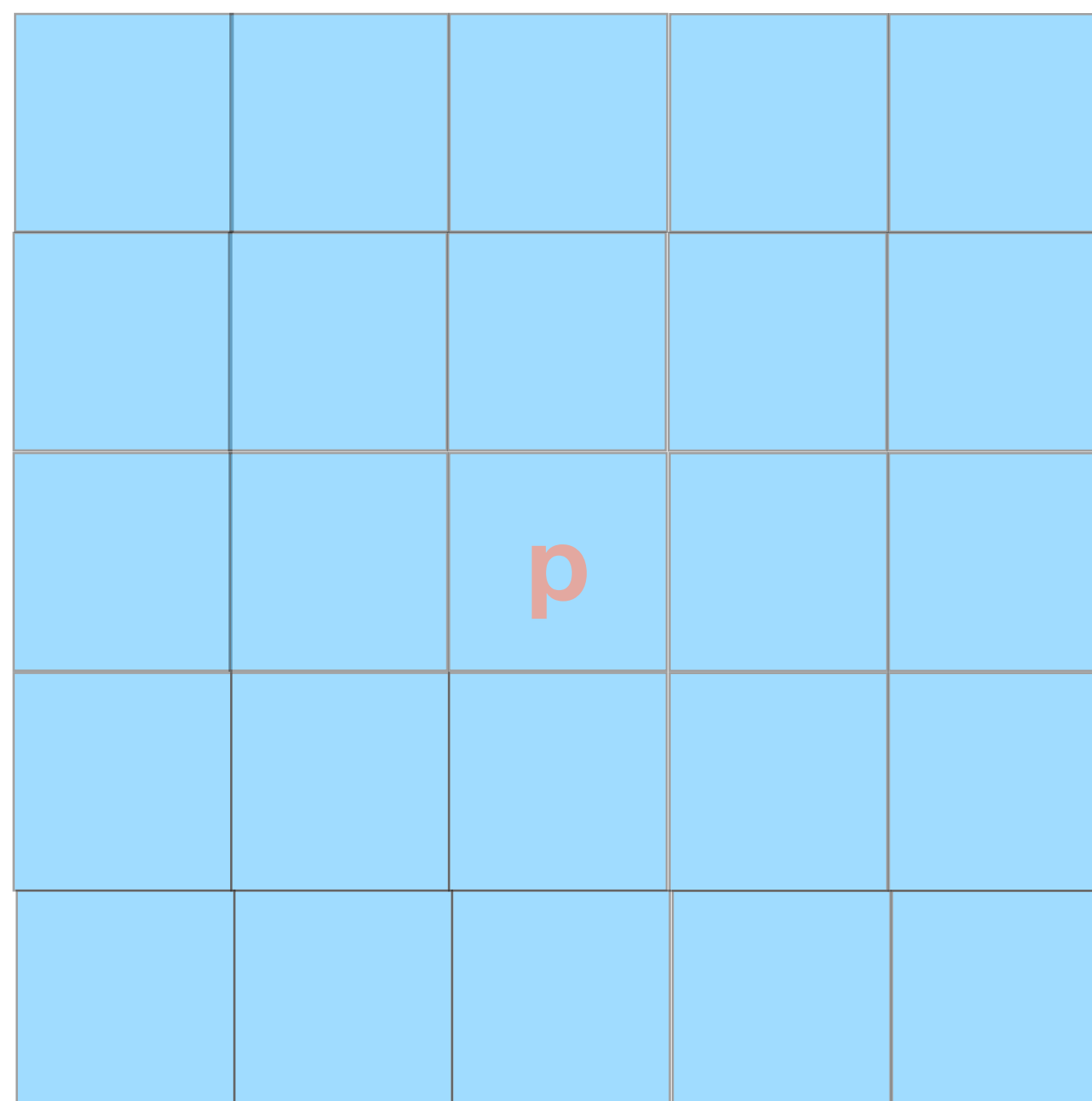
9	<del>17</del> 74	24	12	28	31	36
4	<del>21</del> 5	6	7	29	18	36
1	2	3	13	12	15	14
	16	18	21	13	15	11
	22	22	31	24	26	36

# 均值滤波,中值滤波

所有值和的平均值

可以卷积计算

$$\frac{\sum x_n}{N}$$



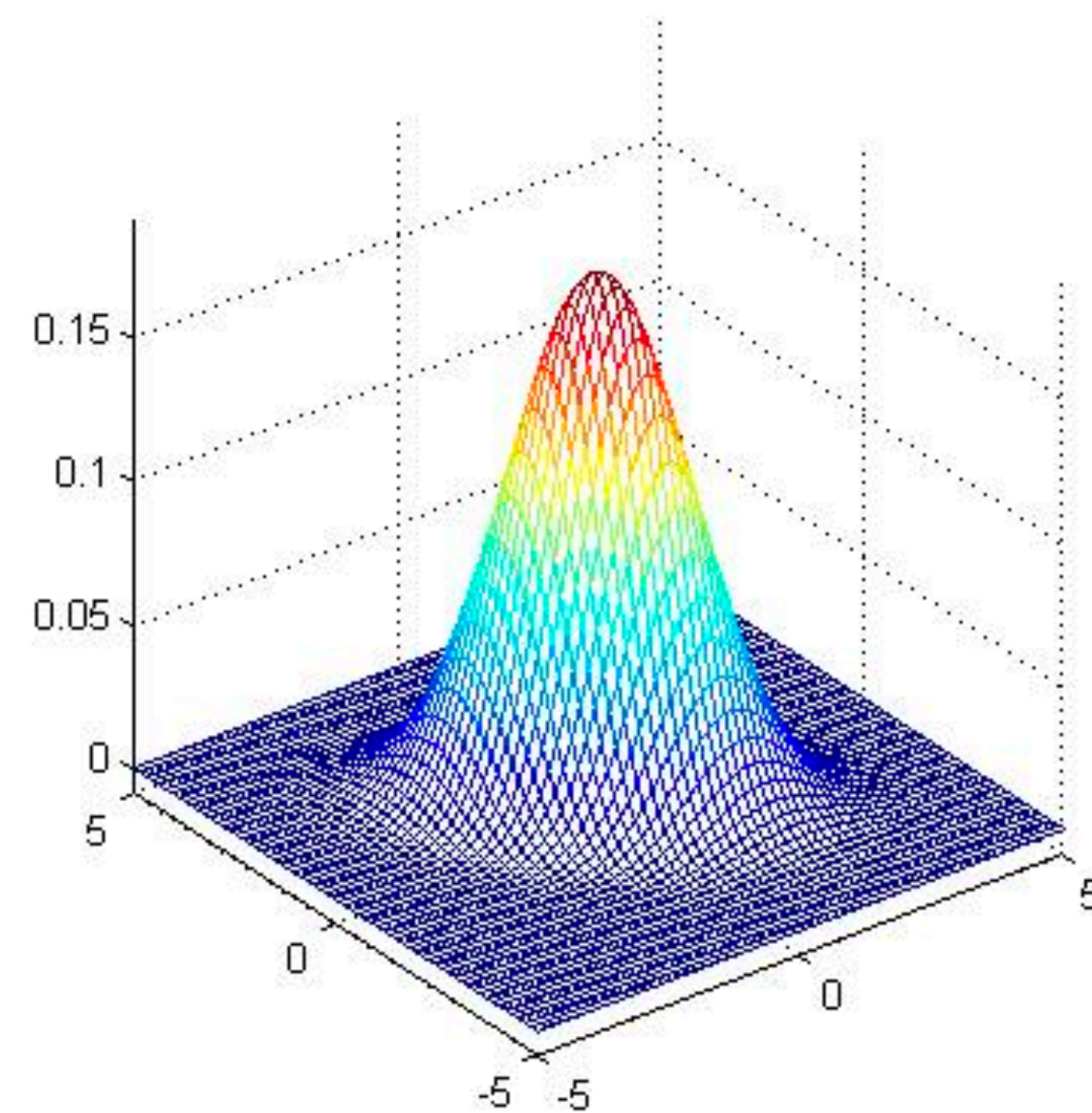
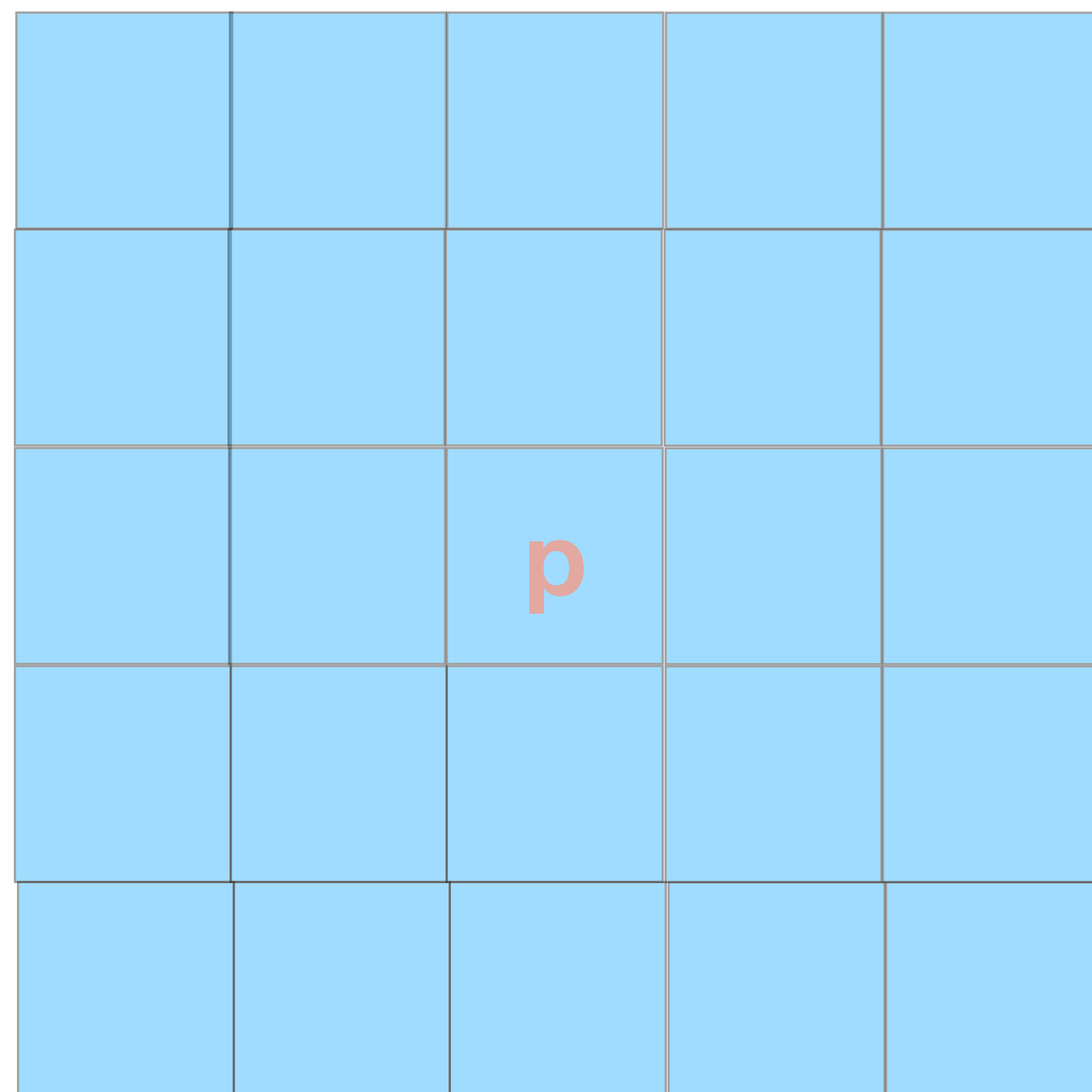
所有值和的中间值

不可以卷积计算

Median(Xn)



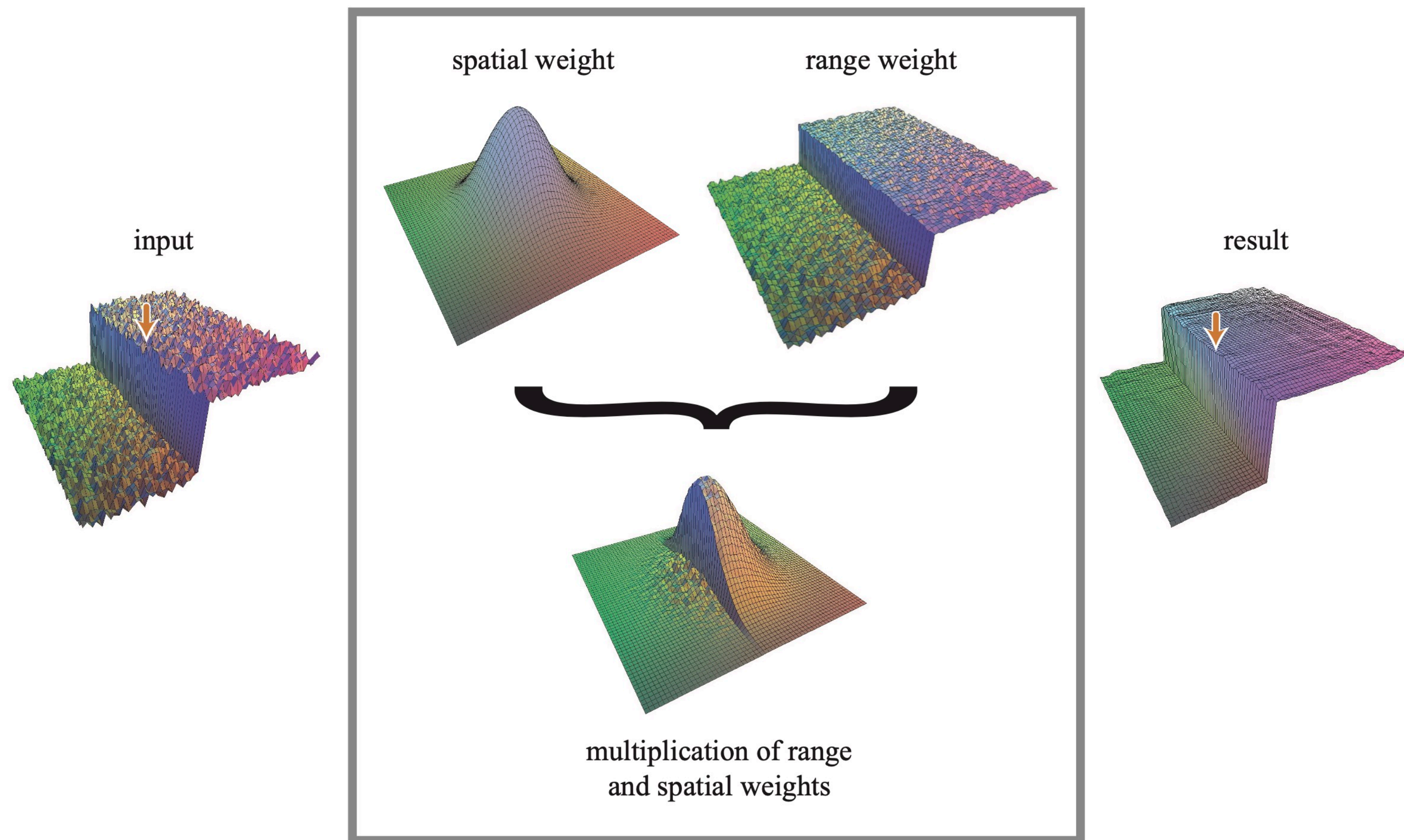
$$\frac{1}{\sqrt{2\Pi}\delta}e^{-\frac{x^2+y^2}{2\delta^2}}$$





# 双边滤波

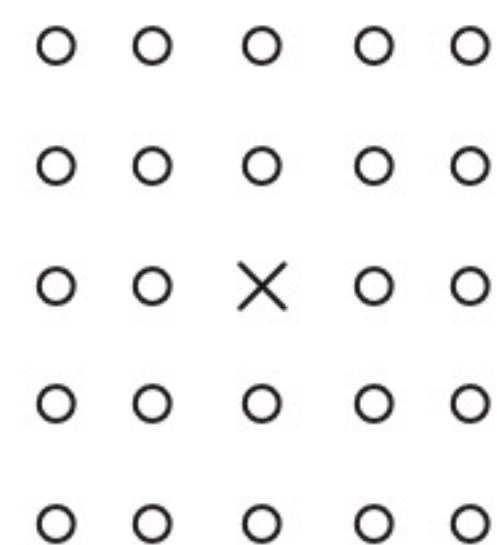
$$BF[I]_{\vec{p}} = \frac{\sum_{\vec{q} \in S} \omega_s(\|\vec{p} - \vec{q}\|) \omega_r(\|I_{\vec{p}} - I_{\vec{q}}\|) I_{\vec{q}}}{\sum_{\vec{q} \in S} \omega_s(\|\vec{p} - \vec{q}\|) \omega_r(\|I_{\vec{p}} - I_{\vec{q}}\|)}$$





# FIR

$$y(m, n) = \sum_{k=-N}^N \sum_{l=-N}^N h(k, l) x(m - k, n - l)$$



$$\begin{bmatrix} 1 & 2 & 1 \\ 2 & \boxed{4} & 2 \\ 1 & 2 & 1 \end{bmatrix} \cdot \frac{1}{16}$$

0 0 0 0 0 0 0		0 0 0 0 0 0 0
0 0 0 0 0 0 0		0 0 0 0 0 0 0
0 0 0 0 0 0 0		0 0 1 3 4 4 3
0 0 0 16 16 16 16	⇒	0 0 3 9 12 12 9
0 0 0 16 16 16 16		0 0 4 12 16 16 12
0 0 0 16 16 16 16		0 0 4 12 16 16 12
0 0 0 16 16 16 16		0 0 3 9 12 12 9
<u>Input Image</u>		<u>Output Image</u>

# IIR

$$y(m, n) = x(m, n) + ay(m - 1, n) + ay(m, n - 1)$$

$$\begin{array}{cc} \circ & 1/2 \\ \circ \times & 1/2 \times \end{array}$$

0 0 0 0 0 0 0		0 0 0 0 0 0 0
0 0 0 0 0 0 0		0 0 0 0 0 0 0
0 0 0 0 0 0 0		0 0 0 0 0 0 0
0 0 0 64 0 0 0	$\Rightarrow$	0 0 0 64 32 16 8
0 0 0 0 0 0 0		0 0 0 32 32 24 16
0 0 0 0 0 0 0		0 0 0 16 24 24 20
0 0 0 0 0 0 0		0 0 0 8 16 20 20
$\underbrace{\hspace{1.5cm}}$		$\underbrace{\hspace{1.5cm}}$
Input Image		Output Image

# API的选择

- Scipy
- Opencv
- Skimage
- .....

# Scipy中的滤波

`gaussian_filter(input, sigma[, order, ...])` Multidimensional Gaussian filter.  
`gaussian_filter1d(input, sigma[, axis, ...])` One-dimensional Gaussian filter.  
`gaussian_gradient_magnitude(input, sigma[, ...])` Multidimensional gradient magnitude using Gaussian derivatives.  
`gaussian_laplace(input, sigma[, output, ...])` Multidimensional Laplace filter using gaussian second derivatives.  
`generic_filter(input, function[, size, ...])` Calculate a multi-dimensional filter using the given function.  
`generic_filter1d(input, function, filter_size)` Calculate a one-dimensional filter along the given axis.  
`generic_gradient_magnitude(input, derivative)` Gradient magnitude using a provided gradient function.  
`generic_laplace(input, derivative2[, ...])` N-dimensional Laplace filter using a provided second derivative function.  
`laplace(input[, output, mode, cval])` N-dimensional Laplace filter based on approximate second derivatives.  
`maximum_filter(input[, size, footprint, ...])` Calculate a multi-dimensional maximum filter.  
`maximum_filter1d(input, size[, axis, ...])` Calculate a one-dimensional maximum filter along the given axis.  
`median_filter(input[, size, footprint, ...])` Calculate a multidimensional median filter.  
`minimum_filter(input[, size, footprint, ...])` Calculate a multi-dimensional minimum filter.  
`minimum_filter1d(input, size[, axis, ...])` Calculate a one-dimensional minimum filter along the given axis.  
`percentile_filter(input, percentile[, size, ...])` Calculate a multi-dimensional percentile filter.  
`prewitt(input[, axis, output, mode, cval])` Calculate a Prewitt filter.  
`rank_filter(input, rank[, size, footprint, ...])` Calculate a multi-dimensional rank filter.  
`sobel(input[, axis, output, mode, cval])` Calculate a Sobel filter.  
`uniform_filter(input[, size, output, mode, ...])` Multi-dimensional uniform filter.  
`uniform_filter1d(input, size[, axis, ...])` Calculate a one-dimensional uniform filter along the given axis.

.....  
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# Opencv中的滤波

```
cv.blur(src, ksize[, dst[, anchor[, borderType]]])  
cv.bilateralFilter(src, d, sigmaColor, sigmaSpace[, dst[, borderType]])  
cv.dilate(src, kernel[, dst[, anchor[, iterations[, borderType[, borderValue]]]])  
cv.erode(src, kernel[, dst[, anchor[, iterations[, borderType[, borderValue]]]])  
cv.filter2D(src, ddepth, kernel[, dst[, anchor[, delta[, borderType]]]])  
cv.GaussianBlur(src, ksize, sigmaX[, dst[, sigmaY[, borderType]])  
cv.getGaussianKernel(ksize, sigma[, ktype])  
cv.boxFilter(src, ddepth, ksize[, dst[, anchor[, normalize[, borderType]]]])  
.....  
https://docs.opencv.org/4.2.0/d4/d86/  
group\_\_imgproc\_\_filter.html#gad533230ebf2d42509547d514f7d3fbc3
```

# 自己实现的滤波

```
generic_filter(input, function[, size, ...])  
cv.filter2D(src, ddepth, kernel[, dst[, anchor[, delta[, borderType]]])
```

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