# CS 446/ECE 449: Machine Learning

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L29: Q-learning

### Goals of this lecture

- Extending MDPs
- Getting to know Q-learning

# Recap so far: Known MDP

- To compute  $V^*$ ,  $Q^*$ ,  $\pi^*$ : use policy/value iteration or exhaustive
- To evaluate fixed policy  $\pi$ : use policy evaluation

#### But what if:

- Transition probabilities and rewards are not known
- No model available (model free RL)

## Bellman optimality principle:

$$Q^*(s,a) = \sum_{s' \in \mathcal{S}} P(s' \mid s,a) \left[ R(s,a,s') + \max_{a' \in \mathcal{A}_{s'}} Q^*(s',a')) \right]$$

### Idea:

- Run a simulator to collect experience tuples/samples (s, a, r, s')
- Approximate transition probability using samples

# Algorithm sketch for Q-learning:

- Obtain a sample transition (s, a, r, s')
- Obtained sample suggests:

$$Q(s, a) \approx y_{(s, a, r, s')} = r + \max_{a' \in \mathcal{A}_{s'}} Q(s', a')$$

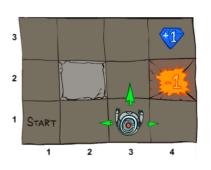
 To account for missing transition probability we keep running average

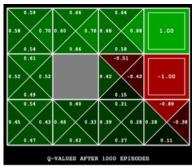
$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + \alpha y_{(s,a,r,s')}$$

## Summary:

- Known MDP
  - ▶ To compute  $V^*$ ,  $Q^*$ ,  $\pi^*$ : use value/policy iteration
  - ▶ To evaluate fixed policy  $\pi$ : use policy evaluation
- Unknown MDP: Model free
  - To compute V\*, Q\*, π\*: use Q-learning
  - ▶ To evaluate fixed policy  $\pi$ : use value learning

# Our current Q-learning works fine in case we have a tabular environment:

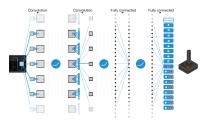




# How to use this idea for playing Atari games?

- What are the actions?
- What are the rewards?
- What are the states?

How about  $Q_{\theta}(s, a)$  as a neural net which takes images as input and produces a number for each of the possible actions?



# Deep Q-learning algorithm (Deep Q-networks (DQN)):

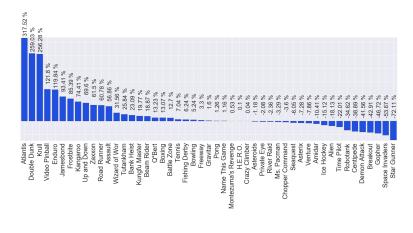
Given dataset  $\mathcal{D} = \{(s_j, a_j, r_j, s_{j+1})\}$ :

- Sample minibatch  $\mathcal{B} \subseteq \mathcal{D}$
- Compute target  $y_j = r_j + \gamma \max_a Q_{\theta^-}(s_{j+1}, a) \quad \forall j \in \mathcal{B}$
- Use stochastic (semi-)gradient descent to optimize w.r.t. parameters  $\theta$

$$\min_{\theta} \sum_{(s_j, a_j, r_i, s_{j+1}) \in \mathcal{B}} \left( Q_{\theta}(s_j, a_j) - y_j \right)^2$$

• Perform  $\epsilon$ -greedy action and augment  $\mathcal D$ 

### Results:



### Quiz:

- What differentiates RL from supervised learning?
- What is a MDP?
- What to do if no transition probabilities are available?

## Important topics of this lecture

- Getting a feeling for reinforcement learning
- Understanding how to use reinforcement learning

### What's next:

Policy Gradient Methods