

# Left Factoring

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- ❑ If two alternatives of a production begin with the same string , then the grammar is not LL(1)
  - ❑ Example:  $S \rightarrow OS1 \mid O1$  is not LL(1)
- ❑ In left factoring it is not clear which two alternative productions to use to expand a non-terminal S
- ❑ General method:  
 $A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$

The equivalent non left-factored grammar is

$$\begin{aligned} A &\rightarrow \alpha A', \\ A' &\rightarrow \beta_1 \mid \beta_2 \end{aligned}$$

# Eliminating Left Factoring Example

## □ Example 1

$$\begin{aligned} S &\rightarrow iEtS \mid iEtSeS \mid a \\ E &\rightarrow b \end{aligned}$$

The equivalent non left factored grammar is

$$\begin{aligned} S &\rightarrow iEtSS' \mid a \\ S' &\rightarrow eS \mid \epsilon \\ E &\rightarrow b \end{aligned}$$

## □ Example 2

$$S \rightarrow bSSaaS \mid bSSaSb \mid bSb \mid a$$

## □ Eliminate the common prefix $bS$

$$S \rightarrow bSS' \mid a$$
$$S' \rightarrow SaaS \mid SaSb \mid b$$

Again, this is a grammar with common prefixes.

## □ Eliminate the common prefix $Sa$ from the second grammar

$$S \rightarrow bSS' \mid a$$
$$S' \rightarrow SaA \mid b$$
$$A \rightarrow aS \mid Sb$$