

# Type Systems

# Semantic Analysis

What can we do with semantic information for identifier x

- What kind of value is stored in x?
- How big is x?
- Who is responsible for allocating space for x?
- Who is responsible for initializing x?
- How long must the value of x be kept?
- If x is a procedure, what kinds of arguments does it take and
- What kind of return value does it have?
- Storage layout for local names

# Introduction

- A source program should follow both the syntactic and semantic rules of the source language.
- Some rules can be checked statically during compile time and other rules can only be checked dynamically during runtime.
- Static checking includes the syntax checks performed by the parser and semantic checks such as type checks, flow-of control checks, uniqueness checks, and name-related checks.
- Here we focus on type checking.

# Type Checking

- **Problem:** Verify that a type of a construct matches that expected by its context.
- **Examples:**
  - $\square$  mod requires integer operands (PASCAL)
  - $\square$  \* (dereferencing) – applied to a pointer
  - $\square$  a[i] – indexing applied to an array
  - $\square$  f(a1, a2, ..., an) – function applied to correct arguments.
- **Information gathered by a type checker:**
  - $\square$  Needed during code generation.

# Use of Type

- Virtually all high-level programming languages associate types with values.
- Types often provide an implicit context for operations.
  - In C the expression  $x + y$  will use integer addition if  $x$  and  $y$  are int's, and floating-point addition if  $x$  and  $y$  are float's.
- Types can catch programming errors at compile time by making sure operators are applied to semantically valid operands.
  - For example, a Java compiler will report an error if  $x$  and  $y$  are String's in the expression  $x * y$

# Types

- Basic types are atomic types that have no internal structure as far as the programmer is concerned. Type →
  - They include types like integer, real, boolean, and character.
  - Subrange types like 1..10 in Pascal and enumerated types like (violet, indigo, blue, green, yellow, orange, red) are also basic types.
- Constructed types include arrays, records, sets, and structures constructed from the basic types and/or other constructed types.
  - Pointers and functions are also constructed types.

```
int | float | char | ...  
| void  
| error  
| name  
| variable  
| array( size, Type)  
| record( (name, Type)*)  
| pointer( Type)  
| tuple((Type)*)  
| fcn( Type, Type) (Type → Type)
```

Basic Types

Structured Types

# Type Expressions

- **Type Expressions** denote the type of a language construct.
  - It is either a basic type or formed from other type expressions by applying an operator called a **type constructor**.
    - Example: a function from an integer to an integer.
    - A type constructor applied to a type expression is a type expression.
- Here we use type expressions formed from the following rules:
  - A basic type is a type expression. Other basic type expressions are **type-error** to signal the presence of a type error and **void** to signal the absence of a value.
  - If a type expression has a name then the name is also a type expression.

# Type Constructors -

$\text{char name}[5]$  {id.type = array(I, T)}  
 $\uparrow$   $\uparrow$   
 $T$   $I$   
 $\rightarrow T_1 \times T_2 = \underline{T_1 \times T_2}$   $\rightarrow$  function {.....}  
 $\text{int sum(int a, int b)}$   
 $\text{id.type = fn(int x int, int)}$

- Arrays. If **T** is a type expression and **I** is the type expression of an index set then **array(I, T)** denotes an *array of elements of type T*.
- Products. If **T1** and **T2** are type expressions, then their Cartesian product, **T1 x T2**, is a type expression.
  - For example if the arguments of a function are two reals followed by an integer then the type expression for the arguments is: **real x real x integer**.
- Records. The fields in a record (or structure) have names which should be included in the type expression of the record. The type expression of a record with n fields is:

**record(F<sub>1</sub> x F<sub>2</sub> x ... x F<sub>n</sub>)**

where if the *name of field i* is *name<sub>i</sub>* and the type expression of field i is *T<sub>i</sub>* then *F<sub>i</sub>* is:

(name<sub>i</sub> x T<sub>i</sub>).

struct student  
 {  
 int no  
 char name[5]  
 float gpa;  
 };

id.type =  
record((no, int) x  
(name, array(5, char)  
(gpa, float))



# Type Constructors

*int \*a; // id.type = pointer(int)  
char \*c; // id.type = pointer(char)*

- *Pointers.*

- If T is a type expression then pointer (T) denotes a pointer to an object of type T.

- *Functions.*

- A function maps elements from its domain to its range.

- The type expression for a function is: D --> R where

D is the type expression for the domain of the function and R is the type expression for the range of the function.

- For example, the type expression of the mod operator in Pascal is:

integer x integer --> integer

because it divides an integer by an integer and returns the integer remainder.

The type expression for the domain of a function with no arguments is void and the type expression for the range of a function with no returned value is void:

e.g., void --> void

is the type expression for a procedure with no arguments and no returned value.

*( fcn(D, R)*

# A Simple Typed Language

*a, b: int*

Program → Declaration; Statement

Declaration → Declaration; Declaration

| id: Type

Statement → Statement; Statement

| id := Expression ✓

| if Expression then Statement ✓

| while Expression do Statement ✓

Expression → literal | num | id

| Expression mod Expression

| E[E] | E ↑ | E (E) → function call



array  
access

pointer

# Type Checking Expressions

- $E \rightarrow \text{int\_const} \quad \{ E.\text{type} = \text{int} \}$
- $E \rightarrow \text{float\_const} \quad \{ E.\text{type} = \text{float} \}$
- $\left\{ \begin{array}{l} E \rightarrow \text{id} \quad \{ E.\text{type} = \text{sym\_lookup}(\text{id.entry}, \text{type}) \} \\ E \rightarrow E_1 + E_2 \quad \{ E.\text{type} = \text{if } E_1.\text{type} \notin \{\text{int}, \text{float}\} \mid \\ \quad E_2.\text{type} \notin \{\text{int}, \text{float}\} \\ \quad \text{then error} \\ \text{else if } E_1.\text{type} == E_2.\text{type} == \text{int} \\ \quad \text{then int} \\ \quad \text{else float} \} \end{array} \right.$

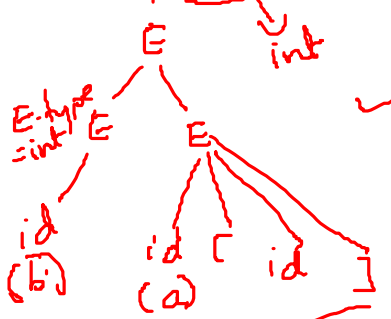
E  
|  
id  
|  
ω

# Type Checking Expressions

int a[10]

a[i] + 10;

b = a[i];



int a; id.type = int

$S \rightarrow$  parameter type  
 $T \rightarrow$  return type  
`(int x char x float)` ✓  
void

$E \rightarrow \underline{E_1} [\underline{E_2}]$

$\{E.type = \text{if } E_1.type = \text{array}(S, T) \wedge E_2.type = \text{int} \text{ then } T \text{ else error}\}$

$E \rightarrow \underline{*E_1}$

$\{E.type = \text{if } E_1.type = \text{pointer}(T) \text{ then } T \text{ else error}\}$

$E \rightarrow \&E_1$

$\{E.type = \text{pointer}(E_1.type)\}$

$E \rightarrow \underline{(E_1(E_2))}$

$\{E.type = \text{if } (E_1.type = \text{fcn}(S, T) \wedge E_2.type = S, \text{ then } T \text{ else error})\}$

`Sum(a, b)`  
T

= stud[i]

int \*b; id by pointer (int)  
int a; a.type = int

$\rightarrow a = \underline{*b}$



char \*c; pointer (char)

= \*c + ...

# Type Checking Statements

*void, error*

$S \rightarrow \underline{id} := \underline{E}$

{S.type := if id.type = E.type  
then void else error}

$S \rightarrow \text{if } \underline{E} \text{ then } \underline{S_1}$

{S.type := if E.type = boolean  
then S<sub>1</sub>.type else error}

$S \rightarrow \text{while } E \text{ do } S_1$

{S.type := if E.type = boolean  
then S<sub>1</sub>.type} *else error*

$S \rightarrow \underline{S_1}; \underline{S_2}$

{S.type := if S<sub>1</sub>.type = void ∧  
S<sub>2</sub>.type = void then void else error}

