

Due: 2013/12/20

Homework 11

Problem 1. Find seven points in the plane such that when we connect pairs of points with distance 1, the resulting graph has chromatic number 4.

Problem 2. Given $2n$ points in the plane, n red and n blue. Prove that one can always 1-1 pair the red and blue points such that these n segments do not intersect.

Problem 3. Given a set V of n points in the plane, call a line magic if it contains exactly 3 points in V . Prove that the number of magic lines is at most $n^2/6$.

Problem 4. Given a point set V in the plane, call a line magic if it contains exactly 3 points in V . Let M_n be the maximum number of magic lines over all configuration of n points. Prove a lower bound on the order of M_n as better as you can.