

Exploring a lower resolution physics grid in CAM-SE-CSLAM

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Key Points:

- Unlike the dynamics grid, physics grid control volumes have the same smoothness properties
- Grid imprinting from the spectral-element method is eliminated, even in regions with steep terrain
- The coarser physics grid does not degrade the effective resolution of the model

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Abstract

The effects of using a separate grid for evaluating physical parameterizations (a ‘physics grid’) in global atmospheric models has long been discussed. While very few modeling studies have had the capability to experiment with a separate physics grid, here the implementation of a coarser resolution physics grid into CAM-SE-CSLAM is described. The results of experiments using the lower resolution physics grid are compared to the conventional method in which the physics grid and dynamical core grid coincide. Through dividing the elements of CAM-SE-CSLAM into 2×2 control volumes, each volume has the same smoothness property and eliminates grid imprinting, even in regions with steep topography. The impact of the coarser resolution physics grid on the resolved scales of motion is analyzed across a range of dynamical core grid resolutions. The results demonstrate that the effective resolution of the model is not degraded through the use of a coarser resolution physics grid. Since the physics makes up about half the computational cost of the conventional CAM-SE-CSLAM configuration, the coarser physics grid may allow for significant cost savings with little downside.

1 Introduction

Global atmospheric models fundamentally consist of two components. The dynamical core (*dynamics*), which numerically integrate the adiabatic equations of motion and tracer advection, and the physical parameterizations (*physics*), which compute the effects of diabatic and subgrid-scale processes (e.g., radiative transfer and moist convection) on the grid-scale. More out of convenience than anything else, the physics are evaluated on the dynamics grid, i.e., the physics grid and dynamics grid coincide. From linear stability and accuracy analysis of numerical methods, it is a common result that the shortest simulated wavelengths are not accurately represented by the dynamical core. Additionally, simulated downscale cascades result in an unrealistic collection of energy and/or enstrophy near the truncation scale, which may be observed from kinetic energy spectra in model simulations [Skamarock, 2011]. Some form of dissipation must be incorporated into models to mitigate these numerical artifacts near the grid scale [Jablonowski and Williamson, 2011]. This numerical dissipation has no physical analogy [although see Grinstein *et al.*, 2007], and the grid-scale is therefore contaminated by numerous un-physical processes. The under-resolved nature of the grid-scale led Lander and Hoskins [1997] to speculate whether the physics should be evaluated on a grid that is more reflective of the scales actually resolved by the dynamical core.

Exploring the impact of different physics grid resolutions have so far been limited to models employing the spectral transform method [Lander and Hoskins, 1997; Williamson, 1999; Wedi, 2014]. Lander and Hoskins [1997] argue that passing under-resolved states to the physics may be especially problematic in spectral transform models, since the physics are evaluated on a latitude-longitude transform grid, and contains more degrees of freedom than the spectral representation to prevent aliasing of quadratic quantities. However, Lander and Hoskins [1997] find that the spectral truncation of the physics tendencies damps errors that may result from passing an under-resolved state to the physics, although the extent to which these errors may still be present in the model is difficult to address.

Another class of spectral-transform models evaluate the quadratic terms using semi-Lagrangian methods, which are implicitly diffusive, relaxing constraints on the resolution of the transform grid. Wedi [2014] experimented with different transform grid resolutions and concluded that the standard high resolution quadratic grid actually improves forecast skill over the use of a lower-resolution transform grid. They suggest that increasing the resolution of the transform grid simulates a kind of sub-grid variability on the spectral state, which is thought to be under-represented in global atmospheric models [Shutts, 2005]. This is in principle the purpose of “super-parameterization,” in which a cloud re-

solving model is embedded in each grid cell to approximate sub-grid variability, and improves both diurnal and sub-seasonal variability in the model [Randall *et al.*, 2003].

After the physics tendencies are transformed into spectral space, the tendencies may be truncated at any particular wave number. Williamson [1999] conducted a pair of convergence tests using a global spectral transform model; a conventional convergence test and one in which the spectral truncation of the physics tendencies is held fixed and the resolution of the dynamical core increased. In contrast to the realistic weather forecasts of Wedi [2014], Williamson [1999] run their model to equilibrium in an idealized climate configuration. When the physics and dynamics resolutions increase together, as in more typical convergence studies, the strength of the Hadley Cell increases monotonically with resolution. This sensitivity of Hadley Cell strength to horizontal resolution is a common result of global models at hydrostatic resolutions [see Herrington and Reed, 2017, and references therein]. But with the truncation wave number of physics tendencies held fixed, the Hadley Cell showed very little sensitivity to dynamical core resolution, resembling the solution for which the dynamics truncation wave number is equal to that of the lower resolution physics.

Herrington and Reed [2017] speculate that the results of Williamson [1999] indicate that the scales of motion resolved by the dynamical core are aliased to the lower resolution physics. It may be worth considering that if the resolution of the dynamics is reduced in response to a coarser physics grid, then the dynamics may be no better resolved on the coarser physics grid, compared with the conventional method of evaluating the physics and dynamics at the same resolution. The results of Williamson [1999] and Wedi [2014] do not provide evidence that a lower resolution physics grid reduces computational errors in spectral transform models, but again, this is a difficult problem to address, and seldom discussed in either study.

Global spectral transform models, while remarkably efficient at small processor counts, do not scale well on massively parallel systems. High-order Galerkin methods are becoming increasingly popular in climate and weather applications due to their high-parallel efficiency, high-processor efficiency, high-order accuracy (for smooth problems), and geometric flexibility facilitating mesh-refinement applications. High resolution climate simulations with NCAR’s Community Atmosphere Model [CAM; Neale *et al.*, 2012] are typically performed using a continuous Galerkin dynamical core referred to as CAM-SE [CAM Spectral Elements; Taylor *et al.*, 2008; Dennis *et al.*, 2012; Lauritzen *et al.*, 2018]. CAM-SE may be optionally coupled to a conservative, semi-Lagrangian tracer advection scheme for accelerated multi-tracer transport [CAM-SE-CSLAM; Lauritzen *et al.*, 2017]. Tracer advection then evolves on an entirely separate, finite-volume grid which contains the same degrees of freedom as CAM-SE’s quadrature node grid.

Element-based Galerkin methods are susceptible to grid-imprinting, and may need be considered when contemplating a particular physics grid [Herrington *et al.*, 2018, hereafter referred to as H18]. Grid imprinting manifests at the element boundaries, since the global basis is least smooth (C^0 ; all derivatives are discontinuous) for quadrature nodes lying on the element boundaries, and the gradients (e.g., the pressure gradient) are systematically tighter producing local extremes. Through computing the physics tendencies at the nodal points, element boundary extrema is also observed in the physics tendencies.

H18 has shown that through evaluating the physics on the finite-volume tracer advection grid in CAM-SE-CSLAM, element boundary noise is substantially reduced, although still problematic in regions of steep terrain, at low latitudes. Through integrating CAM-SE’s basis functions over the control volumes of the finite-volume grid, element boundary extrema is additionally weighted by the C^∞ solutions (i.e., the basis representation is infinitely smooth and all derivatives are continuous) that characterize the interior of the element, and the state is smoother. Additionally, in defining an area averaged state, the finite-volume physics grid is made consistent with assumptions inherent to the physics,

and is more appropriate for coupling to other model components (e.g., the land model), which is typically performed using finite-volume based mapping algorithms.

The finite-volume grid of H18 is found through dividing the elements of CAM-SE’s gnomonic cubed-sphere grid with equally spaced, equi-angular coordinate lines parallel to the equi-angular element boundaries, such that there are 3×3 control volumes per element (hereafter referred to as *pg3*; see Figure 1b). While a 3×3 physics grid was chosen in order to have the same degrees of freedom as the dynamical core, the control volumes encompass a region of the element in which their proximity to the element boundaries are not equal. Therefore, not every control volume in an element has the same smoothness properties. This may be avoided through defining a physics grid in which the elements are instead divided into 2×2 control volumes (hereafter referred to as *pg2*; see Figure 1a). The control volumes of the *pg2* grid all have the same proximity to the element boundaries, and should mitigate the element boundary noise that remains in the *pg3* grid, and shown in H18.

In this study, we test the hypothesis that the coarser, *pg2* physics grid is effective at reducing spurious noise at element boundaries, particularly over regions of rough topography. In addition, the recent trend towards running models at ever higher resolutions is an almost prohibitive computational burden. As the physics are responsible for over half of the computational cost in CAM-SE [Lauritzen *et al.*, 2018], the improvement in computational performance using a coarser resolution physics grid is potentially significant. However, any advantages of using a coarser physics grid need be weighed against any potential reduction in simulation quality, e.g., possible aliasing of the resolved scales of motion by the coarser grid, as suggested by the results of Williamson [1999]. Section 2 describes the implementation of the *pg2* grid into CAM-SE-CSLAM. Section 3 provides the results of idealized model configurations to identify any changes in grid imprinting, or in the overall solution, compared with the *pg3* configuration. Section 4 provides a discussion of the results and conclusions.

2 Methods

Separating dynamics, tracer and physics grids introduces the added complexity of having to map the state from dynamics and tracer grids to the physics grid; and mapping physics tracer tendencies back to the tracer grid and physics tendencies needed by the dynamical core to the dynamics grid. The dynamics grid refers to the Gauss-Lobatto-Legendre (GLL) quadrature nodes by the spectral-element method to solve the momentum equations for the momentum vector (u, v) , thermodynamics equation for temperature (T) , continuity equation for dry air (p) , and continuity equations for water vapor and condensates thermodynamically active [see, e.g., Lauritzen *et al.*, 2018, for details]. By tracer grid we refer to the *pg3* grid on which CSLAM performs tracer transport of water vapor, condensates and other tracers. The GLL value for water vapor and condensates is overwritten by the CSLAM values every physics time-step so that the spectral-element advection of water species does not become decoupled from the the CSLAM advection of the same water species. Mapping velocity components, dry air mass and temperature from the GLL grid to the *pg2* grid is done by using the internal degree 3 Lagrange basis functions in CAM-SE [as described in Herrington *et al.*, 2018, for *pg3*; exactly the same methods can be used for *pg2*].

As compared to the *pg3* configuration, the extra complication of the *pg2* setup is that tracer state needs to be mapped from the tracer grid to the physics grid and tracer tendencies need to be mapped from the physics grid to CSLAM grid. In order to describe the algorithm some notation needs to be introduced.

The mapping algorithm is applied to each element Ω (with spherical area $\Delta\Omega$) so without loss of generality consider one element. Let $\Delta A_k^{(pg)}$ and $\Delta A_\ell^{(nc)}$ be the spherical

area of the physics grid cell $A_k^{(pg)}$ and CSLAM control volume $A_\ell^{(nc)}$, respectively. The physics grid cells and CSLAM cells respectively span the element without gaps or overlaps

$$\cup_{k=1}^{pg^2} A_k^{(pg)} = \Omega \text{ and } A_k^{(pg)} \cap A_\ell^{(pg)} = \emptyset \quad \forall k \neq \ell, \quad (1)$$

$$\cup_{k=1}^{nc^2} A_k^{(nc)} = \Omega \text{ and } A_k^{(nc)} \cap A_\ell^{(nc)} = \emptyset \quad \forall k \neq \ell. \quad (2)$$

The overlap areas between the k -th physics grid cell and CSLAM cells is denoted

$$A_{k\ell} = A_k^{(pg)} \cap A_\ell^{(nc)}, \quad (3)$$

so that

$$A_k^{(pg)} = \cup_{\ell=1}^{nc^2} A_{k\ell}. \quad (4)$$

This overlap grid is also referred to as an exchange grid.

2.1 Mapping tracers from CSLAM to pg

For mapping tracer state from the CSLAM grid to any physics grid can be done using existing CSLAM technology, i.e. do a high-order shape-preserving reconstruction of mixing ratio and dry air mass inside each CSLAM control volume and integrate those reconstruction functions over the overlap areas [Lauritzen *et al.*, 2010; Nair and Lauritzen, 2010]. This algorithm retains the properties of CSLAM: inherent mass-conservation, mixing ratio shape-preservation and linear-correlation preservation.

In mathematical terms, the dry pressure level thickness integrated over the k 'th physics grid cell is given by

$$\overline{\Delta p}_k^{(pg)} = \sum_{\ell=1}^{nc^2} \langle \Delta p \rangle_{k\ell}, \quad (5)$$

where $\langle \Delta p \rangle_{k\ell}$ is the integral over the high-order reconstruction of Δp over the overlap area $A_{k\ell}$ divided by the area of the overlap

$$\langle \Delta p \rangle_{k\ell} = \frac{1}{\delta A_{k\ell}} \int_{A_{k\ell}} \left[\sum_{i+j \leq 2} C_\ell^{(ij)} x^i y^j \right] dA, \quad (6)$$

where the reconstruction coefficients $C_\ell^{(ij)}$ in CSLAM cell ℓ are computed from the cell average pressure level thicknesses on the CSLAM grid $\Delta p^{(nc)}$ and the numerical integration over overlap areas is done by line-integral quadrature. The details are given in Lauritzen *et al.* [2010] and not repeated here.

The tracer mass per unit area on the physics grid is given by

$$\overline{m\Delta p}_k^{(pg)} = \sum_{\ell=1}^{nc^2} \langle m\Delta p \rangle_{k\ell}, \quad (7)$$

where $\langle m\Delta p \rangle_{k\ell}$ is the integral over the high-order reconstruction of Δp and m combined using the approach outlined in Appendix B of Nair and Lauritzen [2010] over the overlap area $A_{k\ell}$

$$\langle m\Delta p \rangle_{k\ell} = \frac{1}{\delta A_{k\ell}} \int_{A_{k\ell}} \left[\overline{\Delta p}_\ell^{(nc)} \sum_{i+j \leq 2} c_\ell^{(ij)} x^i y^j + \overline{m}_\ell^{(nc)} \sum_{i+j \leq 2} \tilde{C}_\ell^{(ij)} x^i y^j \right] dA, \quad (8)$$

where $\tilde{C}_\ell^{(00)} = C_\ell^{(00)} - \overline{\Delta p}_\ell^{(nc)}$ and $\tilde{C}_\ell^{(ij)} = C_\ell^{(ij)}$ for $i, j > 0$. The mixing ratio on the physics grid is then

$$\overline{m}_k^{(pg)} = \frac{\overline{m\Delta p}_k^{(pg)}}{\overline{\Delta p}_k^{(pg)}}. \quad (9)$$

The tendencies from the parameterizations are computed on the physics grid. The tracer tendency in physics grid cell k is denoted $f_k^{(pg)}$. The problem is how to map $f_k^{(pg)}$ to the CSLAM control volumes $f_\ell^{(nc)}$ satisfying the following constraints:

1. Local mass-conservation

$$f_k^{(pg)} \Delta p_k^{(pg)} = \cup_{\ell=1}^{nc^2} \Delta A_{k\ell} \Delta p_\ell^{(nc)} f_\ell^{(nc)}, \quad (10)$$

where $\Delta p_k^{(pg)}$ is the pressure level thickness in physics grid cell k and similarly for $\Delta p^{(nc)}$.

2. **Shape-preservation in mixing ratio:** The tendencies mapped to the CSLAM grid should not produce values smaller than the updated physics grid mixing ratios, $m_k^{(pg)} + \Delta t f_k^{(pg)}$, or values smaller than the existing CSLAM mixing ratios [revise for whatever code works best]

$$m^{(min)} = \min \left(m_k^{(pg)} + \Delta t f_k^{(pg)}, \left\{ m_\ell^{(nc)} | \ell = 1, nc^2 \right\} \right), \quad (11)$$

where Δt is the physics time-step. Similarly for maxima

$$m_k^{(max)} = \max \left(m_k^{(pg)} + \Delta t f_k^{(pg)}, \left\{ m_{k\ell}^{(nc)} | \ell = 1, nc^2 \right\} \right), \quad (12)$$

3. **Linear correlation preservation:** The physics forcing must not disrupt linear tracer correlation between species on the CSLAM grid [see, e.g., *Lauritzen and Thuburn, 2012*].
4. **Consistency:** A constant mixing ratio tendency, $cnst$, on the physics grid, $f_k^{(pg)} = cnst \forall k$, must result in the same (constant) forcing on the CSLAM grid, $f_\ell^{(nc)} = f_k^{(pg)} = cnst \forall \ell$.

To motivate the algorithm that will simultaneously satisfy 1-4 it is informative to discuss how ‘standard’ mapping algorithms will violate one or more of the constraints:

- **Conservative remapping:** Assume that one remaps the mass-tendencies in exactly the same way as the mapping of mixing ratio state from the CSLAM grid to the physics grid described in section ?? . That is, replace m with f and map from physics grid to the CSLAM grid instead of the other way around. The mapped mass-tendency is $\overline{f \Delta p_k^{(pg)}}$ and due to the properties of the mapping algorithm the mass-tendency is conserved, linear correlation between mass-tendencies are conserved and shape in mass-tendency is preserved.

That said, this approach is problematic. The issue is that the dry pressure level thickness mapped from pg to nc , call it $\overline{\Delta p^{(nc)}}$, differs from $\overline{\Delta p^{(nc)}}$. During physics-dynamics coupling the dry pressure level thickness should remain constant. So when converting the mass-tendencies to mixing ratio tendencies through, e.g.,

$$\overline{m_k^{(pg)}} = \frac{\overline{f \Delta p_k^{(pg)}}}{\overline{\Delta p_k^{(pg)}}}, \quad (13)$$

a constant mixing ratio tendency is not conserved since $\overline{\Delta p_k^{(pg)}} \neq \overline{\Delta p_k^{(pg)}}$. Basically the constant tendency will map to a field representing the spurious discrepancy between $\overline{\Delta p_k^{(pg)}}$ and $\overline{\Delta p_k^{(pg)}}$. A constant tendency can be preserved by using

$$\overline{m_k^{(pg)}} = \frac{\overline{f \Delta p_k^{(pg)}}}{\overline{\Delta p_k^{(pg)}}}, \quad (14)$$

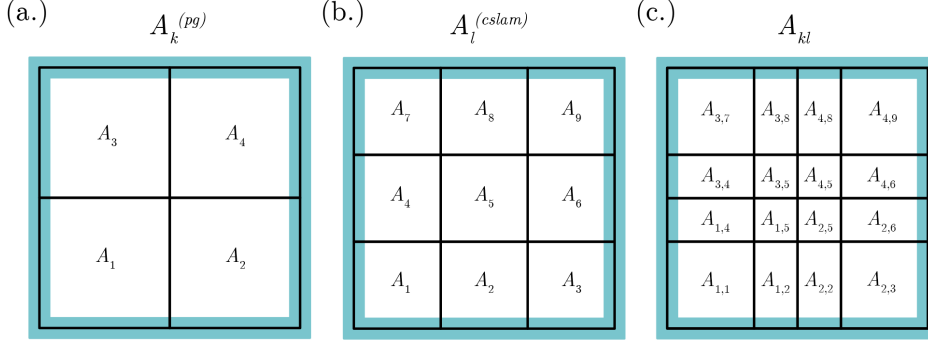


Figure 1. Indice notation for (a) the $pg2$ grid, (b) the $pg3$ grid and (c) their exchange grid. **Peter - do you think you will use this figure?**

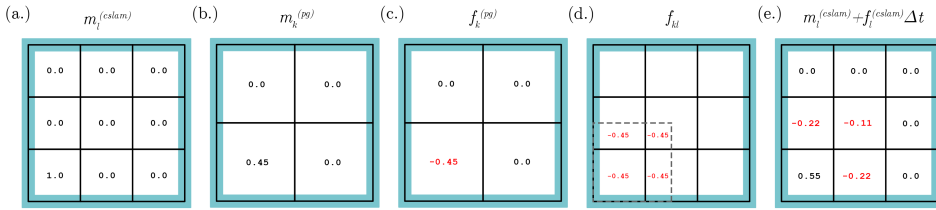


Figure 2. Make captions stand-alone while being concise

instead, but now mass-conservation is lost since $\widetilde{\Delta p_k^{(pg)}} \neq \overline{\Delta p_k^{(pg)}}$. This issue is similar to the mass-wind inconsistency found in specified dynamics applications [e.g. ?].

Even if one could derive a reversible map for mapping Δp from physics grid to the CSLAM grid there could still be problems with driving mixing ratios negative on the CSLAM grid (we refer to this as the ‘negativity problem’). This problem is depicted schematically in Figure 2. Consider a single element of CSLAM control volumes, containing only a single cell with mixing ratio 1.0, and 0.0 everywhere else (m_l ; Figure 2a). Assume that the mixing ratios mapped to the $pg2$ grid (m_k ; Figure 2b) results in a negative tracer tendency from the physics (f_k ; Figure 2c). The non-zero values of the tendencies for $pg2$ areas overlapping CSLAM grid cells originally containing a mixing ratio of zero ($f_{k,l}$; Figure 2d), are driven negative by the mapped tendency (Figure 2e).

- Interpolation: Traditional Lagrange interpolate of the mixing ratio tendency would preserve a constant and could be made shape-preserving using *ad hoc* filters [e.g. ?] but will not inherently preserve mass tendency and suffers from the ‘negativity problem’ described above.

As illustrated above none of the standard interpolation or remapping methods will simultaneously satisfy 1-4.

2.2 Algorithm

mention that the reason we map tendency and not state is to avoid spurious tendencies solely due to interpolation errors, i.e. zero tendency on physics grid would transform into tendencies on the CSLAM grid. Define the $\Delta m_{k\ell}$ is the amount of mixing ratio that can be removed without producing new extrema in $m_{k\ell}$

$$\Delta m_{k\ell} = \bar{m}_{k\ell} - m^{(min)}, \quad (15)$$

where $\bar{m}_{k\ell}$ has been computed using higher-order mapping mention why the problem is well-posed Describe algorithm here

Peter - I think the results of the terminator tests should be mentioned here. We could just put in a sentence saying it passes. But I'm assuming that if we don't use the algorithm that weights the tendency by the amount of available mixing ratio, it will fail. If that's the case, we could just do a two panel plot showing the iCLy at day 15 for with and without the algorithm.

2.3 Model Configurations

Two model configurations using the Community Earth System Model, version 2.1 (CESM2.1; <https://doi.org/10.5065/D67H1H0V>) are chosen to carry out the objectives discussed in Section 1. To test the hypothesis, that the *pg2* grid reduces spurious grid-noise over mountainous regions, a Held-Suarez configuration [*FHS94* compset; *Held and Suarez*, 1994] modified to include real world topography is analyzed. H18 indicate that this configuration tends to have more grid-noise over steep terrain than in a more complex configuration using CAM, version 6 moist physics [CAM6;], and is therefore a conservative choice for evaluating any change in grid imprinting between *pg3* and *pg2*.

To understand whether the resolved scales of motion are influenced by a coarser resolution physics grid, a suite of aqua-planet simulations [*Neale and Hoskins*, 2000; *Medeiros et al.*, 2016] are carried out over a range of spectral-element grid resolutions, using CAM6 physics (*QPC6* compset). The aqua-planet is an ocean covered planet in perpetual equinox, with fixed, zonally-symmetric sea surface temperatures idealized after present day Earth [*QOBS* in *Neale and Hoskins*, 2000]. While the dynamics time-step, Δt_{dyn} , varies with resolution according to a CFL criterion, there is no established standard for how the physics time-step, Δt_{phys} , should vary across resolutions. This is further complicated by several studies indicating a high sensitivity of solutions to Δt_{phys} in CAM [*Williamson and Olson*, 2003; *Williamson*, 2013; *Wan et al.*, 2015; *Herrington and Reed*, 2018].

Here, a scaling for Δt_{phys} across resolutions is proposed, based on results of the moist bubble test [*Herrington and Reed*, 2018] using CAM-SE-CSLAM and detailed in Appendix A: . The basis for the scaling is to alleviate truncation errors that arise in the moist bubble test when Δt_{phys} is too large. The scaling is linear in grid-spacing,

$$\Delta t_{phys} = \Delta t_{phys,0} \times \frac{N_e}{N_{e,0}} s, \quad (16)$$

where $\Delta t_{phys,0}$ is taken to be the standard 1800s used in CAM-SE-CSLAM at low resolution, $N_{e,0} = 30$ (equivalent to a dynamics grid-spacing of 111.2km). N_e refers to the horizontal resolution of the grid; each of the six panels of the cubed-sphere are divided into $N_e \times N_e$ elements. Throughout the paper, spectral-element grid resolutions are denoted by an *ne* followed by the quantity N_e , e.g., *ne30*.

The only other parameter varied across resolutions modulates the strength of explicit numerical dissipation. The spectral element method is not implicitly diffusive, so fourth-order hyper-viscosity operators are applied to the state to suppress numerical artifacts. The

scaling of the hyper-viscosity coefficients, ν , across resolutions is defined as,

$$\nu_T = \nu_{vor} = 0.30 \times \left(\frac{30}{N_e} 1.1 \times 10^5 \right)^3 \frac{m^4}{s}, \quad (17)$$

$$\nu_p = \nu_{div} = 0.751 \times \left(\frac{30}{N_e} 1.1 \times 10^5 \right)^3 \frac{m^4}{s}, \quad (18)$$

where subscripts T , vor , p , div refer to state variables the operators are applied to, temperature, vorticity, pressure and divergence, respectively. The scaling reduces the coefficient by an order of magnitude for each doubling of the resolution [as in *Lauritzen et al.*, 2018]. No explicit dissipation of tracers (e.g., water vapor) is required since the semi-Lagrangian numerics in CSLAM are diffusive.

3 Results

3.1 Held-Suarez with Topography

Flow over topography can result in significant grid imprinting using the spectral element method [*Lauritzen et al.*, 2015, H18]. Figure 3 shows the results of the Held-Suarez with topography simulations. The middle panel is the vertical pressure velocity, ω , averaged over two years, over the Andes and Himalayan region at two different levels in the mid-troposphere, using the *ne30pg3* grid. The fields are displayed as a raster plot on the physics grid, so that individual extrema, which characterize the flow over the Andes between about $10^\circ - 20^\circ$ S, may be identified as spurious. Near the foot of the Himalayas, between about $20^\circ - 30^\circ$ N, there are parallel stripes of extrema aligned with the mountain front that appear to be spurious $2\Delta x$ oscillations.

As discussed in H18, grid imprinting over mountainous terrain tends to occur in regions of weak gravitational stability, causing extrema to extend through the full depth of the troposphere as resolved updrafts and downdrafts. Thus, grid imprinting over mountains may be alleviated through increasing the divergence damping in the model. Figure 3 (right panel) repeats the *ne30pg3* simulation through increasing ν_{div} by an order of magnitude. The spurious noise over the Andes and the Himalayas are damped, and grid point extrema tend to diffuse into neighboring grid cells. The wavenumber-power spectrum of the kinetic energy due to divergent flow (Figure 4) confirms that divergent modes are damped at higher wavenumbers (greater than 30), by about an order of magnitude relative to the default *ne30pg3* simulation.

The ω field of the *ne30pg2* simulation is provided in Figure 3 (left panel). Grid cell extrema over the Andes is less prevalent than in the *ne30pg3* simulation, as seen by the reduction in large magnitude ω (e.g., red grid cells). The spurious oscillations at the foot of the Himalayas appear to have been entirely eliminated. This improvement in grid imprinting is due to the consistent smoothing properties of the control volumes in the *pg2* grid compared with the *pg3* grid discussed in Section 1, and these results are consistent with our hypothesis. The divergent modes are marginally damped relative to *ne30pg3* for wavenumbers greater than about 50, but are an order of magnitude larger than in the enhanced divergence damping *ne30pg3* run (Figure 4). From a model development standpoint, the *pg2* configuration is preferable to placing additional constraints on ν_{div} in a *pg3* configuration, since this coefficient is one of only a handful of free parameters available to tune CAM-SE.

3.2 Aqua-planets

The Tropical regions are very sensitive to horizontal resolution, primarily due to the scale dependence of resolved updrafts and downdrafts at hydrostatic scales [*Herrington and Reed*, 2017, 2018]. The vertical velocity of updrafts and downdrafts is related to the horizontal length scales of buoyancy the model is able to support. This can be demon-

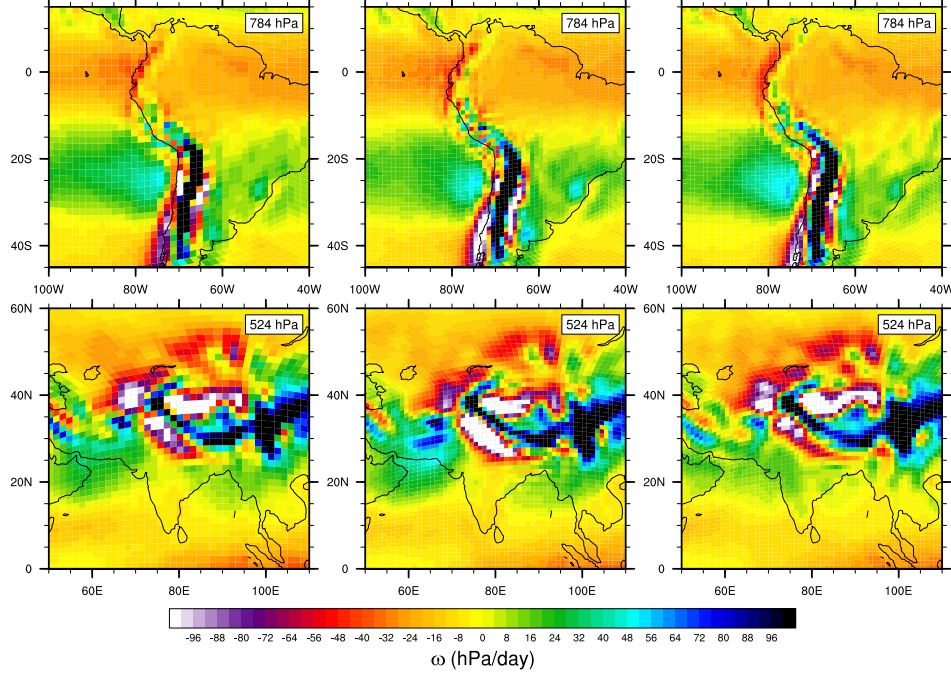


Figure 3. Mean ω at two model levels in the middle troposphere, in a Held-Suarez configuration outfitted with real world topography. (Left) *ne30pg2* (Middle) *ne30pg3* and (Right) *ne30pg3* with the divergence damping coefficient, ν_{div} , increased by an order of magnitude. The ω fields are computed from a two-year simulation. The data are presented on a raster plot in order to identify individual grid cells

strated through a scale analysis of the Poisson equation [Jeevanjee and Romps, 2016] valid for hydrostatic scales, showing that the ratio of the scale of ω at two resolutions, due to their respective buoyancies is,

$$\frac{\omega_{\Delta x_1}}{\omega_{\Delta x_2}} = \frac{D_{\Delta x_2}}{D_{\Delta x_1}}, \quad (19)$$

where $D_{\Delta x}$ is a characteristic buoyancy horizontal length scale for grid-spacing Δx (hereafter referred to as the *forcing scale*), and it is presumed that the magnitude of the buoyancy and the vertical scale of the buoyancy is unchanged or compensating across the two resolutions. Equation 15 indicates that the magnitude of the vertical velocity scales like the inverse of the forcing scale, which was verified in a simple moist bubble configuration using CAM-SE and the CAM finite-volume dynamical core [Herrington and Reed, 2018] and using CAM-SE-CSLAM (Appendix A:). It is by no means trivial that equation 15 holds for the moist bubble test, since the scaling is derived from the dry anelastic equations.

In aqua-planet simulations using CAM-SE, the forcing scale is grid-limited, varying with resolution in the range of five to ten times the grid-spacing [Herrington and Reed, 2018]. From equation 15, this grid-dependence explains why the updrafts and downdrafts are so sensitive to horizontal resolution. A grid-limited forcing scale is analogous to an effective resolution, which is the characteristic length scale below which the solution becomes contaminated by numerical artifacts, and the features are overly damped due to numerical dissipation. The effective resolution may be inferred from kinetic energy spectra as the wavenumber where the slope of the spectrum becomes steeper than the observationally determined slope [Skamarock, 2011]. In the CESM2 release of CAM-SE, this crite-

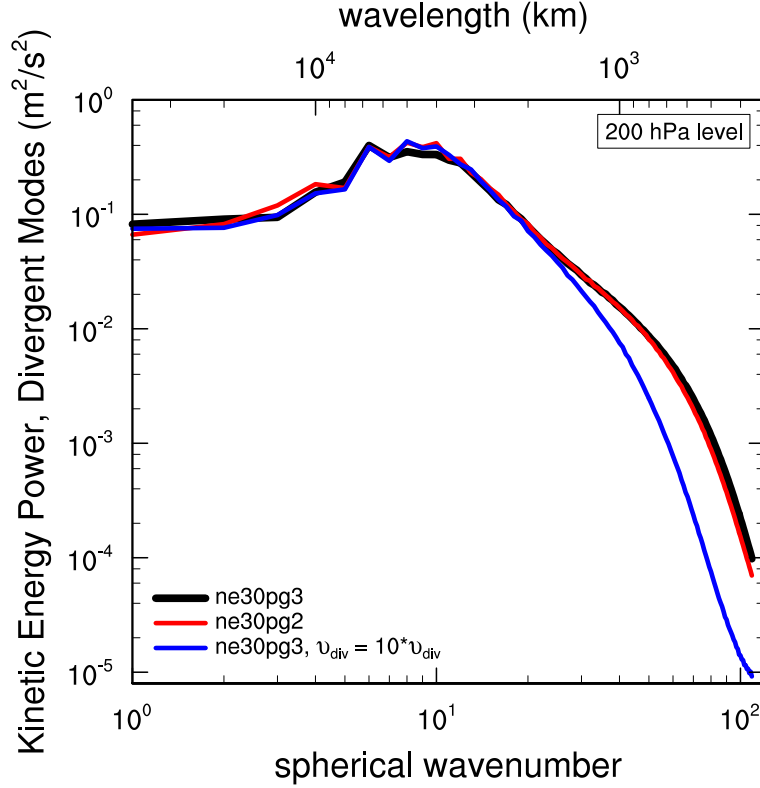


Figure 4. Kinetic energy power spectrum arising from divergent modes in *ne30pg3*, *ne30pg2* and *ne30pg3* with the divergence damping coefficient, v_{div} , increased by an order of magnitude, in the Held-Suarez with topography simulations. Spectra computed from five months of six-hourly winds.

tion occurs near wavenumber 60 [see Figure 6 in *Lauritzen et al.*, 2018], a length scale of about six times the grid spacing and overlapping with the estimated forcing scale.

When the physics and dynamics grids are of different resolutions, which grid determines the models characteristic forcing scale? The remainder of section 3 attempts to address this question using spectral element grids at low resolution (Section 3.2.1), high resolution (Section 3.2.2) and across all resolutions typical of present day climate models (Section 3.2.3).

3.2.1 Low Resolution

The question posed above may be addressed through comparing *ne30pg2*, where $\Delta x_{phys} = 166.8\text{km}$, $\frac{3}{2}$ times larger than the dynamics grid spacing, $\Delta x_{dyn} = 111.2\text{km}$, to a simulation where both are equal to the physics grid spacing, $\Delta x_{dyn} = \Delta x_{phys} = 166.8\text{km}$ (*ne20pg3*), and another simulation where both are equal to the dynamics grid spacing, $\Delta x_{dyn} = \Delta x_{phys} = 111.2\text{km}$ (*ne30pg3*). The resolvable scales in the *ne30pg2* solution are expected to be bounded by the *ne20pg3* and *ne30pg3* solutions. Although according to equation 12, Δt_{phys} for *ne20* grids should be different from *ne30* grids, here it is set to the *ne30* value (see Table 1) in order to reduce the differences between the three configurations, and justified because lower resolution runs aren't very sensitive to this range of Δt_{phys} (Figure A.2).

Table 1. Δx and Δt for the physics and dynamics in the low resolution simulations

Grid name	Δx_{dyn}	Δt_{dyn}	Δx_{phys}	Δt_{phys}
ne20pg3	166.8km	300s	166.8km	1800s
ne30pg2	111.2km	300s	166.8km	1800s
ne30pg3	111.2km	300s	111.2km	1800s

Figure 5 is a snapshot of the ω field in the Inter-Tropical Convergence Zone (ITCZ) in the pressure-longitude plane, in the three simulations. The ω field is overlain with the $\pm 15K/day$ contour of the physics temperature tendencies (black), which are primarily due to stratiform cloud formation. Since the component of ω due to buoyancy is determined by the physics temperature tendencies mapped to the GLL grid, the tendencies and ω are shown on the *GLL* grid, $f_T^{(gll)}$ and ω_{gll} , respectively. The white contour is intended to outline regions where the deep convection scheme is fairly active, set to the $0.0075kg/m^2/s$ value of the convective mass fluxes (note the convective mass fluxes have not been mapped to the *GLL* grid, and are instead shown on the *pg* grid). The figure indicates that large regions of the ITCZ are comprised of upward ω that balance the warming due to compensating subsidence produced by the deep convection scheme. Much larger magnitude ω are comprised of resolved updrafts driven by the buoyancy of stratiform clouds, and resolved downdrafts due to evaporation of condensates produced by overlying clouds [Herrington and Reed, 2018]. These large buoyancy stratiform clouds tend to form in the middle-to-upper troposphere due to detrainment of moisture from the deep convection scheme [Zhang and McFarlane, 1995].

It is not obvious from the snapshots in Figure 5 whether the characteristic length scale of the stratiform clouds, assumed here to be equal to the forcing scale, is any different across the three simulations. Analogous to determining the effective resolution [Skamarock, 2011], the forcing scale may be inferred from the wave-number power spectrum of $f_T^{(gll)}$ as the maximum wavenumber prior to the steep, un-physical decline in power that characterizes the near-grid scale (hereafter $f_T^{(gll)}$ is referred to as the *forcing*). The wave-number power spectrum of the forcing in the middle-to-upper troposphere is shown in Figure 6a. Unlike kinetic energy spectra, the decline in forcing with wave-number is more gradual, making it difficult to determine a characteristic forcing scale from the spectra. However, it is clear that the slope of the *ne20pg3* spectrum begins to steepen at smaller wavenumbers than in the *ne30pg3* spectra. Additionally, the *ne30pg2* spectra is remarkably similar to the *ne30pg3* spectra, for all wavenumbers. These spectra indicate that the characteristic forcing scale in the *ne30pg2* and *ne30pg3* simulations are similar, and that both are smaller than the *ne20pg3* forcing scale. From equation 15, it is expected that the magnitude of the vertical motion is greater in both the *ne30pg2* and *ne30pg3* simulations.

The probability density function (PDF) of upward ω_{gll} everywhere in the simulations is shown in Figure 6b. Large magnitude ω_{gll} are more frequent in the *ne30pg2* run, compared to *ne20pg3*, and the PDF is actually more similar to the *ne30pg3* distribution, consistent with their similar forcing scales. This may be further illustrated through scaling the PDF's,

$$P_s(\omega) = \alpha \times P(\omega/\alpha), \quad (20)$$

where $P_s(\omega)$ is the scaled PDF of ω and α is the ratio of ω to ω_{target} , the ω associated with the target grid resolution, Δx_{target} . Making the assumption that the forcing scale is linear in Δx , then from equation 15, $\alpha = \Delta x_{target}/\Delta x$. The target resolution is taken here to be equal to the *ne30pg3* grid resolution.

If the forcing scale of *ne30pg2* is in fact determined by Δx_{phys} , then one sets $\Delta x = \Delta x_{phys}$ in α . This scaled PDF, however, severely overestimates the frequency of upward

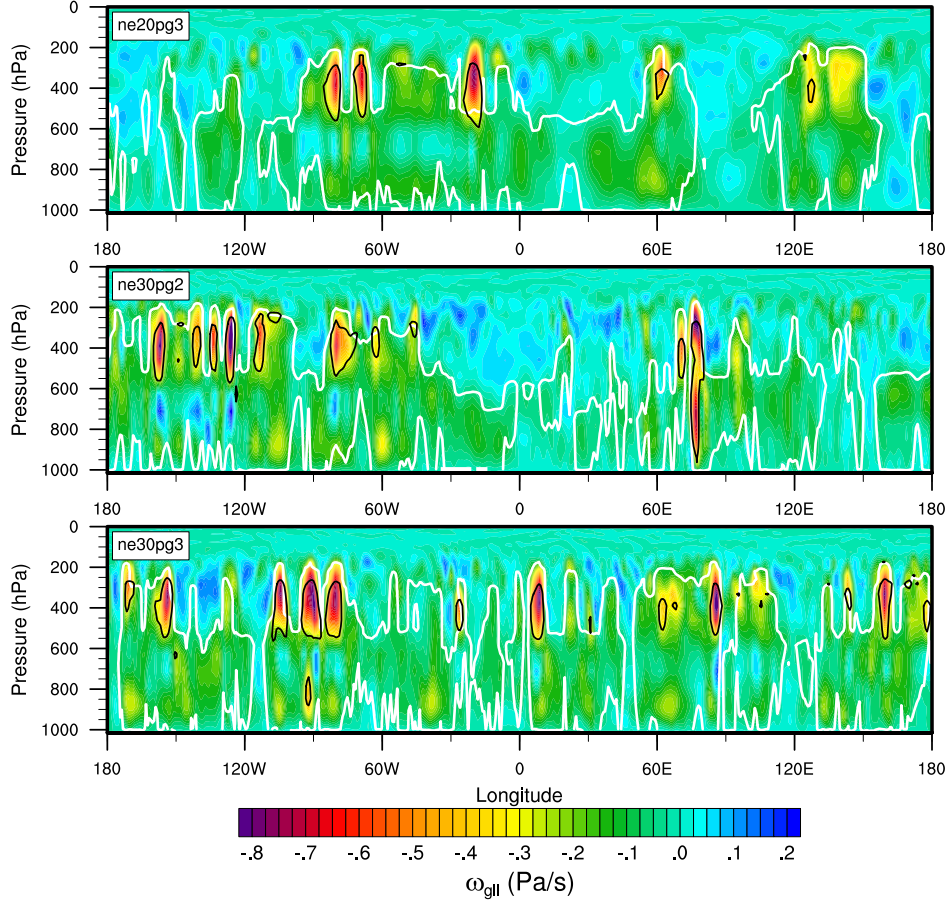


Figure 5. Snapshots in the longitude-pressure plane of ω_{gll} through the ITCZ region in the *ne20pg3*, *ne30pg2* and *ne30pg3* configurations. Black is the $\pm 15K/day$ contour of the physics tendencies, and the white contour is the $0.0075 kg/m^2/s$ contour of the parameterized deep convective mass fluxes.

ω of the target resolution, *ne30pg3* (Figure 6c). It is clear from the similarity of the unscaled PDF's of *ne30pg2* and *ne30pg3* (Figure 6b), and their forcing spectra (Figure 6a), that the forcing scale is determined by Δx_{dyn} , rather than Δx_{phys} . And one can be reasonably confident in the linear framework used to approximate α - the scaled *ne20pg3* PDF fits the *ne30pg3* distribution quite well. It then follows that the forcing scale of *ne20* simulations is about $\frac{3}{2}$ times that of *ne30* simulations, the ratio of their grid spacings.

There are two reasons the *pg2* forcing scale is determined by the *GLL* grid. The first being that the hyper-viscosity coefficients are a function of the *GLL* grid resolution (equation 14). The fourth-order hyper-viscosity is very scale-selective, targeting near grid-scale features more so than, e.g., a second-order operator. Despite this scale-selectiveness, the difference in Δx_{phys} between *pg2* and *pg3* are small enough that the hyper-viscous smoothing render this distinction somewhat ambiguous, and the forcing scale is not all that sensitive to the coarser physics. This is illustrated through increasing ν in *ne30pg2* to *ne20* values, which causes the forcing to steepen at lower wavenumbers compared with the standard *ne30pg2* run (not shown). However, the forcing still steepens at higher wavenumbers than in the *ne20pg3* run (not shown), and so hyper-viscosity alone does not determine the forcing scale in *pg2*. In Appendix B: , it is demonstrated that an additional fac-

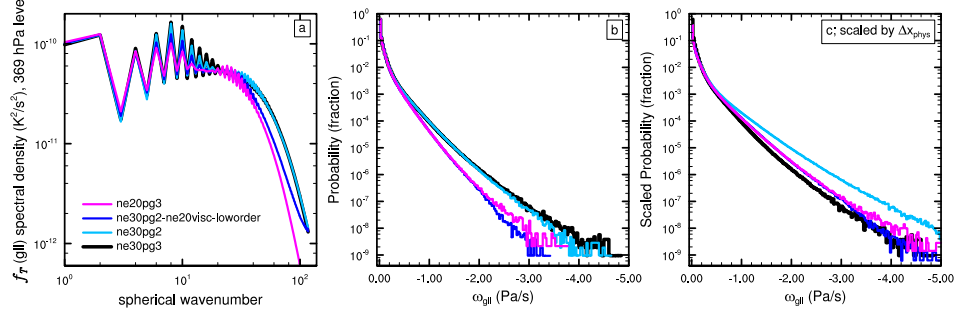


Figure 6. (Left) Wavenumber-power spectrum of the temperature tendencies from the moist physics, near the 369 hPa level, (Middle) probability density distribution and (Right) the scaled probability density distribution of upward ω everywhere in the model. The scaled distributions are scaled to *ne30pg3* using Δx_{phys} .

Table 2. Δx and Δt for the physics and dynamics in the high resolution simulations

Grid name	Δx_{dyn}	Δt_{dyn}	Δx_{phys}	Δt_{phys}
ne80pg3	41.7km	112.5s	41.7km	625s
ne120pg2	27.8km	75s	41.7km	450s
ne120pg3	27.8km	75s	27.8km	450s

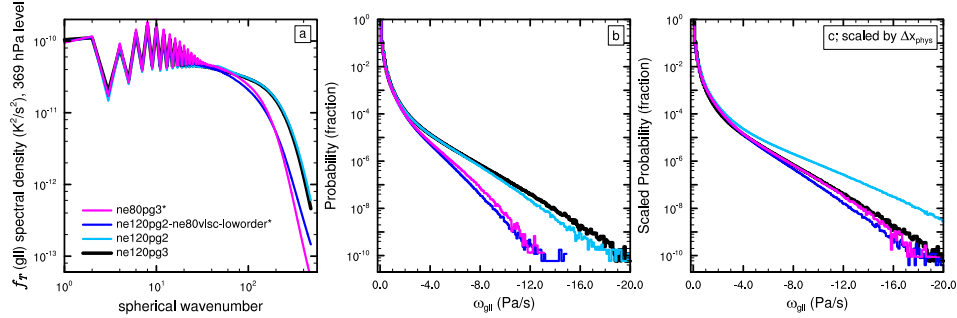


Figure 7. As in Figure 6, but for the high resolution simulations. Asterisks indicate that the physics time-step in these simulations are $\Delta t_{phys} = 675s$, which is larger than that used for the default *ne120* runs (see Table 2). **why is there so many spaces around the equal sign?**

tor is the use of high-order mapping of the forcing from the *pg2* grid, to the *GLL* and *CSLAM* grids. High-order mapping in effect reconstructs scales that are not supported on the *pg2* grid.

The combined effect of these two factors on the forcing scale is illustrated through an *ne30pg2* simulation that uses low-order mapping (see Appendix B:), and with hyper-viscosity coefficients set to *ne20* values (*ne30pg2* – *ne20visc* – *loworder* in Figure 6). The PDF of ω_{gll} and the forcing spectrum more closely resemble the *ne20pg3* run. In this case, the forcing scale is more accurately determined by Δx_{phys} , since the scaled PDF is in fairly good agreement with the *ne30pg3* simulation (Figure 6c).

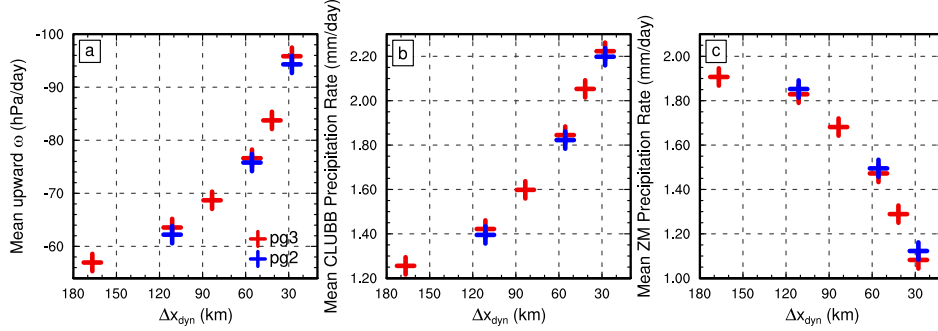


Figure 8. Global mean, time-mean (a) upward ω , (b) CLUBB precipitation rate and (c) parameterized deep convective precipitation rate. All means computed from the final 11 months of one-year simulations, and upward ω is computed using the corresponding 6-hourly output.

3.2.2 High Resolution

3.2.3 Across Resolutions

4 Conclusions

Mitigating grid-imprinting through increasing the divergence damping coefficient an order of magnitude greater than is required for numerical stability is not ideal from a model development perspective. The hyper-viscosity coefficients are one of the only a handful of free-parameters in CAM-SE to tune the kinetic energy spectrum to match observations [Skamarock *et al.*, 2014; Lauritzen *et al.*, 2018].

In sum, at low resolution, the default *pg2* configuration does not degrade the resolution of the model since (1) the *GLL* resolution is unchanged and (2) the high-order mapping is able to reproduce a state similar to what occurs in a *pg3* configuration. Increasing the hyper-viscosity coefficients is akin to reducing the resolution of the *GLL* solution.

A: Defining Δt_{phys} across resolutions

Herrington and Reed [2018] developed a moist bubble test, which indicate that time-truncation errors are large at high resolution (about 50km or less) using more conventional values for the physics time-step. The test may be able to provide incite on a reasonable scaling of Δt_{phys} across resolutions in more complex configurations. In the test a set of non-rotating simulations are initialized with a warm, super-saturated moist bubble, and the grid spacing and bubble radius are simultaneously reduced by the same factor in each run through varying the planetary radius. The test was designed to mimic the reduction in buoyancy length scales that occur when the model resolution is increased in more complex configurations [Hack *et al.*, 2006; Herrington and Reed, 2018].

The moist bubble test is performed with CAM-SE-CSLAM and coupled to the simple condensation routine of Kessler [1969] across five different resolutions (pertaining to the *ne30*, *ne40*, *ne60*, *ne80*, and *ne120* grids). The results are expressed as the minimum ω throughout each one day simulation, and shown in Figure A.1. Two sets of simulations are performed with both *pg3* and *pg2*, one with Δt_{phys} determined by equation 12, and an equivalent set of simulations with $\Delta t_{phys} = 1800s$ for all resolutions.

Since the diameters of the bubbles, D , are set proportional to Δx_{dyn} , Herrington and Reed [2018] has shown that ω converges to the scaling of equation 15 in the limit

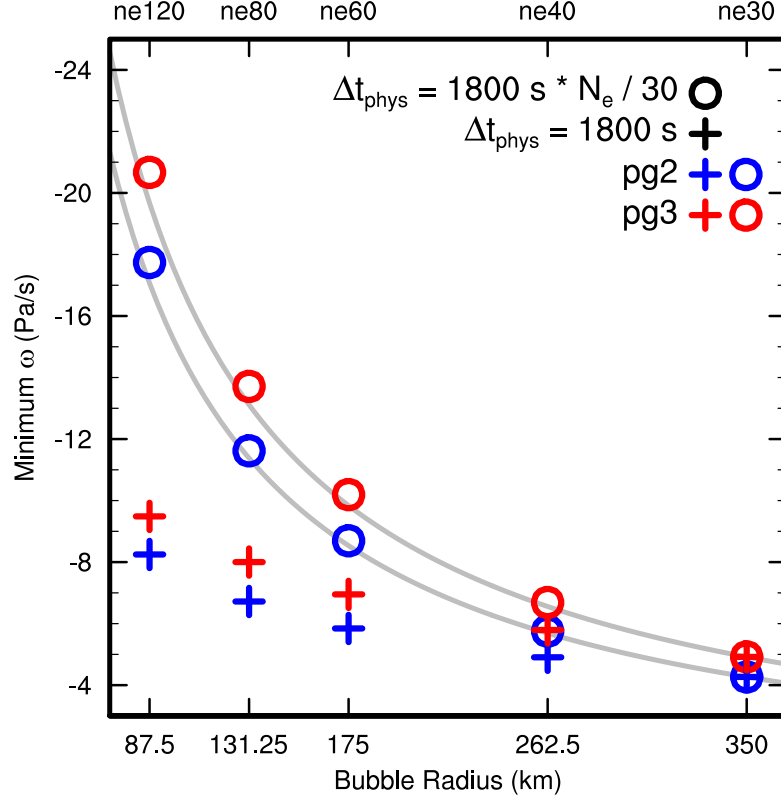


Figure A.1. The magnitude of ω in the *pg3* solutions are systematically larger than the *pg2* solutions, which is primarily a result of the damping effect of integrating the basis functions over a larger control volume.

of small Δt_{phys} , where small Δt_{phys} refers to the CFL limiting time-step used by the dynamics. Equation 15 is overlain as grey lines in Figure A.1, with *ne30* being the reference resolution. The solutions using Δt_{phys} from equation 12 follow the scaling, whereas fixing $\Delta t_{phys} = 1800\text{s}$ across resolutions damps the solution relative to the analytical solution, progressively more so at higher resolutions. If Δt_{phys} is too large, the solution has non-negligible error, which is avoided through scaling Δt_{phys} according to equation 12.

To get a handle on whether the test is useful for understanding more realistic configurations, four aqua-planet simulations are performed using the CAM6 physics package. A pair of *ne30pg2* simulations, one in which Δt_{phys} is set to the appropriate value from equation 12 (1800s), and another where it is set to the Δt_{phys} corresponding to the *ne20* resolution (2700s). Similarly, a pair of *ne120pg2* simulations are performed, one with Δt_{phys} set to the value from equation 12 (450s), and one with Δt_{phys} set to the *ne80* value (625s).

Figure A.2 shows the PDFs of upward ω computed from a year of six-hourly data in the simulations. At lower resolution, Δt_{phys} has only a very small effect on the solution, near the tale-end of the distributions. At high-resolution, values of ω less than about 3Pa/s are more frequent in the small Δt_{phys} run, with the discrepancy growing more for larger magnitudes of ω . The progressively larger errors with increasing resolution also manifests in the moist bubble tests, indicating that truncation errors arising from large Δt_{phys} do exist in more complex configurations.

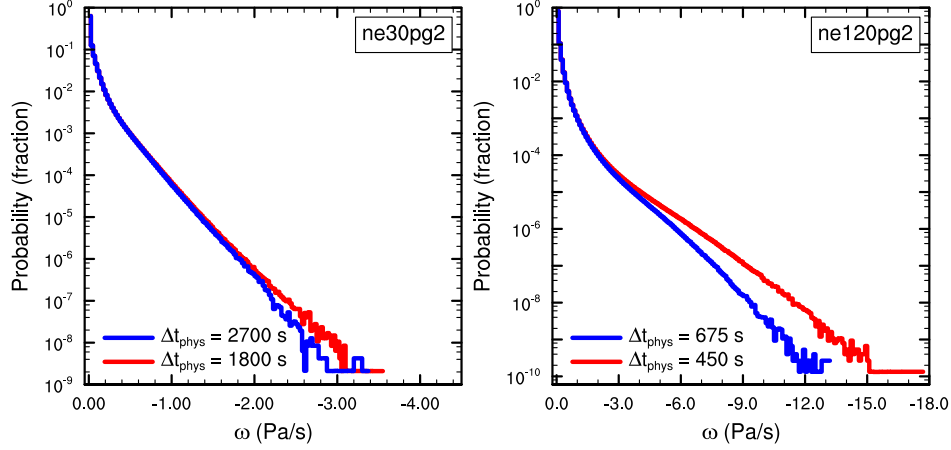


Figure A.2. Probability density distribution of upward ω everywhere in the model in the aqua-planets using the *ne30pg2* grid (Left) and the *ne120pg2* grid (Right). Figure computed for one year of 6-hourly data. The different colors indicate the physics time-steps used in the runs.

B: The impact of high-order mapping to the dynamics grids

Figure B.1a shows a close-up of the wavenumber power spectrum of the forcing on the *pg* grid (dotted), where it is computed, and on the *GLL* grid (solid), where it has been mapped. In *ne30pg3*, the magnitudes are similar on both grids, except the mapping tends to damp the high wavenumbers of the forcing on the *GLL* grid (greater than 60), but these scales are primarily below the effective resolution of the model and should not effect the solution. For *ne30pg2*, the magnitude of the forcing is actually greater after mapping to the *GLL* grid, and more similar to the forcing in the *ne30pg3* simulations. The high-order mapping can therefore replicate the scales of the physics tendencies that occur in the *pg3* simulation, even though the physics are evaluated on a coarser *pg2* grid.

The importance of the high-order mapping can be shown with an additional *ne30pg2* simulation, using low-order mapping (*ne30pg2 – loworder* in Figure B.1). Specifically, low-order mapping refers to piecewise constant mapping from *pg2* to *CSLAM* and bi-linear mapping from *pg2* to *GLL*. The forcing spectrum is now similar on both the *pg2* and *GLL* grids, although the low-order mapping tends to damp the forcing on the *GLL* grid for wavenumbers greater than about 60, scales below than the effective resolution (Figure B.1a). A close up of the PDF of ω_{gll} is provided in Figure B.1b (solid lines). As expected, the frequency of large magnitude ω_{gll} in the low-order run is less compared to the default *ne30pg2* simulation.

The dotted lines in Figure B.1b show the PDF of ω on the *pg* grids. The frequency of large magnitude ω is reduced on the *pg* grids, compared to the state on the *GLL* grids. This is primarily due to the smoothing effect of integrating the nodal point values over control volumes (H18). The larger ω values are even less frequent on the *pg2* grid due to integrating over control volumes $\frac{9}{4}$ times greater than the *pg3* control volumes.

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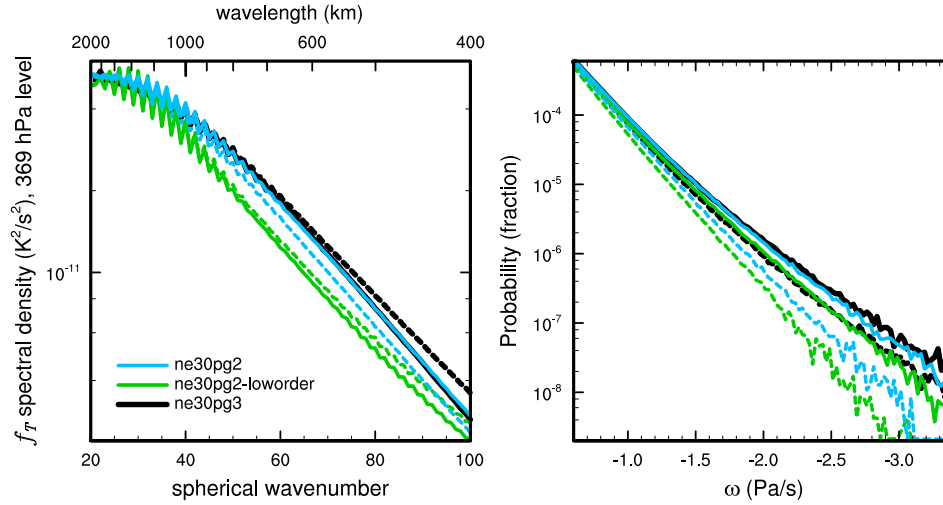


Figure B.1. (Left) Wavenumber-power spectrum of the temperature tendencies from the moist physics, at the 369 hPa level, and (right) probability density distribution of upward ω , everywhere in the model, for three year-long aqua-planet simulations. Solid lines refer to values of on the *GLL* grids, and dashed lines, the fields on the *pg* grids. See text for details regarding the three simulations.

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