

# Arbitrage Betting

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### **Abstract**

This paper produces methodologies and ideas on how to do Arbitrage Betting. Arbitrage Betting is explained from first principles mathematically. Source Code for calculating arbitrage bets is also provided in Python. Pros and Cons of Arbitrage Betting are also discussed. Optimization of Arbitrage Betting is also discussed. Real World problems are solved in this paper.

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# Chapter 1

## Introduction

### 1.1 Introduction to Arbitrage Betting

Betting arbitrage ("sure bets", sports arbitrage) is an example of arbitrage arising on betting markets due to either bookmakers' differing opinions on event outcomes or errors. When conditions allow, by placing one bet per each outcome with different betting companies, the bettor can make a profit regardless of the outcome. Mathematically, arbitrage occurs when there are a set of odds, which represent all mutually exclusive outcomes that cover all state space possibilities (i.e. all outcomes) of an event, whose implied probabilities add up to less than 1. In the bettors' slang an arbitrage is often referred to as an arb; people who take advantage of these arbitrage opportunities are called arbers.

#### 1.1.1 Theory of Arbitrage Betting

Consider the variables for a soccer betting market as follows: Let us suggest that there are there events in a soccer match.

$$P(\text{Home Team Wins}) = p_1$$

$$P(\text{Draw}) = p_2$$

$$P(\text{Away Team Wins}) = p_3$$

When betting a match a *bookmaker* will offer odds for each of the three possible outcomes.

Some examples of odds are as follows:

$$\text{Odds}(\text{Home Team Wins}) = o_1$$

$$\text{Odds}(\text{Draw}) = o_2$$

$$\text{Odds}(\text{Away Team Wins}) = o_3$$

The purpose of Arbitrage Betting is to find a set of odds that will allow us to make a profit regardless of the outcome of the match.

Before we can do this we need to understand the relationship between odds and probabilities. I will explain below how betting odds work.

##### 1.1.1.1 Learning to Bet

**Bet Amount/Punt Amount** When betting on a match you will be asked to place a bet amount.

**Odds** are the ratio of the amount of money that you will win to the amount of money that you bet.

**Probability** is the likelihood of an event occurring.

**Profit** is the amount of money that you will win.

**Return** is the amount of money that you will win plus the amount of money that you bet.

**Example: There is a soccer match between Manchester United vs Everton.**

The odds for Manchester United to win are 1.5.  
The odds for a draw are 3.5.  
The odds for Everton to win are 5.

Now the ratio of the amount of money that you will win to the amount of money that you bet is as follows:

**Manchester United to win** = 1.5  
**Draw** = 3.5  
**Everton to win** = 5

You may be wondering how the odds are calculated.

The bookmaker will calculate the odds based on the probability of the event occurring. For interest sake Manchester United compared to Everton, Manchester United is the favourite to win. Everton is the underdog. The bookmaker will calculate the odds based on the probability of the event occurring. The bookmaker will calculate the probability of the event occurring by looking at the history of the teams. There are many factors that the bookmaker will take into account. Different bookmakers will have different odds for the same match. This is where we will take advantage later in our paper to do Arbitrage Betting.

Lets take a bet for Manchester United to win.

**Bet Amount** = R100  
**P(Manchester United to win)** = 1.5

Our profit is calculated as follows:

Profit = (Bet Amount  $\times$  P(Manchester United to win)) – Bet Amount  
Profit = ( $R100 \times 1.5$ ) – R100  
Profit = R50

Return = Bet Amount + Profit  
Return = R100 + R50  
Return = R150

As you can see we have made a profit of R50.  
If we bet R100 on Manchester United to win we will win R150.

But what happens if Everton wins?  
We will have a loss of R100.

Even a draw will result in a loss of R100.

This is why we need to find a set of odds that will allow us to make a profit regardless of the outcome of the match. This is when we will use Arbitrage Betting.

### 1.1.1.2 Betting on all the Outcomes

As we have seen above, we can make a profit by betting on Manchester United to win.

Let us see what happens if we bet on all the outcomes.  
We will bet R100 on Manchester United to win, R100 on a draw and R100 on Everton to win in total

our investment is R300.

Case 1: Manchester United wins.

$$\text{Winning} = \text{Bet Amount} \times P(\text{Manchester United to win})$$

$$\text{Winning} = R100 \times 1.5$$

$$\text{Winning} = R150$$

$$\text{Return} = \text{Bet Amount} + \text{Winning}$$

$$\text{Return} = R100 + R150$$

$$\text{Return} = R250$$

$$\text{Profit/Loss} = \text{Return} - \text{TotalInvestment}$$

$$\text{Profit/Loss} = R250 - R300$$

$$\text{Loss} = -R50$$

Case 2: Draw.

$$\text{Winning} = \text{Bet Amount} \times P(\text{Draw})$$

$$\text{Winning} = R100 \times 3.5$$

$$\text{Winning} = R350$$

$$\text{Return} = \text{Bet Amount} + \text{Winning}$$

$$\text{Return} = R100 + R350$$

$$\text{Return} = R450$$

$$\text{Profit/Loss} = \text{Return} - \text{TotalInvestment}$$

$$\text{Profit/Loss} = R450 - R300$$

$$\text{Profit} = R150$$

Case 3: Everton wins.

$$\text{Winning} = \text{Bet Amount} \times P(\text{Everton to win})$$

$$\text{Winning} = R100 \times 5$$

$$\text{Winning} = R500$$

$$\text{Return} = \text{Bet Amount} + \text{Winning}$$

$$\text{Return} = R100 + R500$$

$$\text{Return} = R600$$

$$\text{Profit/Loss} = \text{Return} - \text{TotalInvestment}$$

$$\text{Profit/Loss} = R600 - R300$$

$$\text{Profit} = R300$$

As we can see by doing this there is times where we will make a profit and times where we will make a loss. In reality the odds wont be exactly the same as the ones that we have used in our example. It is more dangerous to bet on all the outcomes because the odds will be different.

There is still risk involved in betting on all the outcomes.

But now i will introduce you to Arbitrage Betting where we will make guaranteed profits.

#### 1.1.1.3 Mathematics of Arbitrage Betting

**Arbitrage Betting** is a betting strategy that allows us to make a profit regardless of the outcome of the match.

In order to do Arbitrage Betting we need to find a set of odds that will allow us to make a profit regardless of the outcome of the match.

$M_n$	$O_1$	$O_2$	$O_3$
$M_1$	1.5	3.5	5
$M_2$	2	3.6	5
$M_3$	1.6	12	0.5

Table 1.1: Table of Odds

### Assumption:

Let us generate 3 superficial game odds with 3 outcomes that can occur in a game. In the matrix we may say that all the odds computed are from the same bookmaker.

The odds are as follows:

Where  $M_n$  is the match number,  $O_1$  is the odds of the first outcome,  $O_2$  is the odds of the second outcome and  $O_3$  is the odds of the third outcome.

### How do we recognise Arbitrage Betting opportunities?

Let us denote  $A_n$  as the arbitrage probability of the  $M_n$ .

If the the sum of the  $A_n$  is  $< 1$  then we have an Arbitrage Betting opportunity.

We can calculate the probability of the  $M_n$  as follows:

$$A_n = \sum_{O_n=1}^{N_O} \frac{1}{O_n} \quad (1.1)$$

Where  $N_O$  is the number of odds in the match and  $O_n$  is the current odds in the loop of the sum.

### Example: Calculating the opportunity of a match

Let us calculate the arbitrage probability of the first match  $M_1$ .

$$\begin{aligned} A_1 &= \sum_{O_1=1}^{N_O} \frac{1}{O_1} \\ A_1 &= \frac{1}{1.5} + \frac{1}{3.5} + \frac{1}{5} \\ A_1 &= 1,15238095 \end{aligned}$$

As we can see in  $A_1$  we do not have an Arbitrage Betting opportunity.

Solving for the other matches we get the following:

$$\begin{aligned} A_2 &= 0.97777778 \\ A_3 &= 2,70833333 \end{aligned}$$

As we can see in  $A_2$  we have an Arbitrage Betting opportunity.

Since we now found an opportunity let us get to work on computing our profit for  $A_2$ .

### Example: Calculating the Arbitrage Statistics for $A_2$

Let us calculate the arbitrage statistics for the second match  $M_2$ .

Given  $A_2 = 0.97777778$

Since we have an Arbitrage Betting opportunity we can calculate the following:

$$Profit = (Investment / ArbitragePercentage) - Investment \quad (1.2)$$

Where *Investment* is the amount of money that we are going to invest in the match.

Let us say that we are going to invest R100 in the match.

$$Profit = (R100/0.97777778) - R100$$

$$Profit = R2.27$$

As we can see we are going to make a profit of R2.27. With zero risk. We bet on all the outcomes and we are guaranteed to make a profit.

Now we need to find the stake for each outcome.

We can calculate the stake for each outcome as follows:

$$Individualbets = (Investment \times IndividualArbitragePercentage) / TotalArbitragePercentage$$

$$S_n = \frac{I \times A_{current}}{A_{total}} \quad (1.3)$$

Where  $S_n$  is the stake for the  $M_n$  at  $O_n$  odds,  $I$  is the investment,  $A_{current}$  is the arbitrage percentage of the current  $O_n$  odd and  $A_{total}$  is the total arbitrage percentage of  $M_n$ .

Let us compute the stake for all the outcomes of  $M_2$ .

$$S_1 = \frac{R100 \times \frac{1}{2}}{0.97777778}$$

$$S_1 = R51.14$$

$$S_2 = \frac{R100 \times \frac{1}{3.6}}{0.97777778}$$

$$S_2 = R38.41$$

$$S_3 = \frac{R100 \times \frac{1}{5}}{0.97777778}$$

$$S_3 = R20.45$$

As we can see we are going to bet R51.14 on the first outcome, R38.41 on the second outcome and R20.45 on the third outcome.

To get a guaranteed profit of R2.27

Our return on investment is as follows:

$$ROI = \frac{Profit}{Investment} \times 100 \quad (1.4)$$

$$ROI = \frac{R2.27}{R100} \times 100$$

$$ROI = 2.27\%$$

Now that you are aware of the concept of Arbitrage Betting, In the real world you get  $O_n$  outcomes and  $M_n$  matches.

The odds are never given like that in the real world by the bookies they are always one step ahead of us.

But i am going to show you how to get the odds in the real world and introduce you to Arbitrage Betting in different bookmakers at once.

You can start looking for opportunities with this current knowledge but further in this paper we will look at how to automate the process of finding Arbitrage Betting opportunities. Talk about issues with the current solutions and how we can improve on them.

Hope you enjoyed my introduction to Arbitrage Betting.



## Chapter 2

# Betting in the Real World

### 2.1 Finding the most Optimized Arbitrage Bet

We have learnt how to find arbitrage bets in the previous section. Now we will learn how to find the most optimized arbitrage bet. This is done by finding the most optimized arbitrage bet in the following way:

We look at  $n$  amount of bookmakers  $B$ . We formulate a matrix of  $O_n$  odds for the same match  $M_n$

$$M_n = \begin{bmatrix} B_1 & B_2 & B_3 & \dots & B_n \\ O_1 & O_1 & O_1 & \dots & O_1 \\ O_2 & O_2 & O_2 & \dots & O_2 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ O_n & O_2 & O_3 & \dots & O_n \end{bmatrix} \quad (2.1)$$

We then find the most optimized arbitrage bet by finding the maximum value for each row in the matrix  $M_n$

Resulting in a matrix of  $O_n$  odds for the same match  $M_n$

$$Opt_n = \begin{bmatrix} B_x & B_y & B_z & \dots & B_p \\ O_1 & O_2 & O_3 & \dots & O_n \end{bmatrix} \quad (2.2)$$

Where  $B_{var}$  is the bookmaker with the highest odds for the match  $M_n$

In theory the more bookmakers we have the more optimized our arbitrage bet will be. The more optimized bet results in yielding a higher profit for the arbitrage bet.

But always remember for it to be an arbitrage bet the  $A_n$  must be less than 1.