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EE379: Control Systems

Lab 7: Performance of systems

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State space, response of systems to various inputs, and interconnections of systems

2 OBJECTIVES

Learn how to compute the transient and steady state characteristics of a system in MATLAB.

3 PERFORMANCE

As you should have studied in the lectures and we also mentioned in earlier lab handouts, the step input is very common in control systems, e.g., if you want the elevator to go from the ground floor to the fourth floor, then the desired behavior is a step of magnitude 4. Therefore, the performance of a control system is often based on the response of the system to a step input. The step response has two categories of performance measures: the performance of transient response and the performance of steady state response. The characteristics of the transient response include the rise time, settling time, peak time and the maximum overshoot. For the steady state we are interested in the steady state error. In this handout we will learn how to calculate these performance measures in MATLAB.

4 STEP RESPONSE CHARACTERISTICS IN MATLAB

You already know that the step response of a system can be found in MATLAB using the function `step()`. The information about the transient response of a system when excited by a step input, can be found by the function `stepinfo()`. There is no function to find the steady state error in response to a step input. However, you can use the code

$$\text{abs}(1-\text{dcgain}(\text{sys}))$$

to find the steady state error for a step input. An example code is given below:



4.1 CODE

```
% Example  
my_tf = tf(1,[1 2]);  
stepinfo(my_tf);  
steady_state_error=abs(1-dcgain(my_tf));
```

4.2 OUTPUT

```
steady_state_error =  
  
0.5000
```

```
RiseTime: 1.0985  
TransientTime: 1.9560  
SettlingTime: 1.9560  
SettlingMin: 0.4523  
SettlingMax: 0.5000  
Overshoot: 0  
Undershoot: 0  
Peak: 0.5000  
PeakTime: 5.2729
```

5 EXERCISE 1

Find the rise time, peak time, peak value, overshoot, settling time and the steady state error for step input of the following systems:

5.1 CODE

```
num1=[2 2];  
dem1=[1 9 20];  
tf1=tf(num1,dem1)  
stepinfo(tf1)  
steadyerror1=abs(1-dcgain(tf1))  
num2=[1 1];  
dem2=[1 12 47 60];  
tf2=tf(num2,dem2);  
stepinfo(tf2);  
steaderror2=abs(1-dcgain(tf2));  
num3=[1];  
dem3=[1 10];
```



```
tf3=tf(num3,dem3);  
stepinfo(tf3);  
steadyerror3=abs(1-dcgain(tf3));
```

5.2 OUTPUT

```
tf1 =  
  
      2 s + 2  
-----  
      s^2 + 9 s + 20  
  
Continuous-time transfer function.
```

```
ans =
```

```
struct with fields:
```

```
      RiseTime: 0.0510  
      TransientTime: 1.5940  
      SettlingTime: 1.5940  
      SettlingMin: 0.0917  
      SettlingMax: 0.1949  
      Overshoot: 94.9219  
      Undershoot: 0  
      Peak: 0.1949  
      PeakTime: 0.2878
```

```
steadyerror1 =
```

```
0.9000
```

```
ans =
```

```
struct with fields:
```

```
      RiseTime: 0.2247  
      TransientTime: 2.2150  
      SettlingTime: 2.2150  
      SettlingMin: 0.0151  
      SettlingMax: 0.0240  
      Overshoot: 43.7489  
      Undershoot: 0  
      Peak: 0.0240  
      PeakTime: 0.6908
```

```
tf2 =  
  
      s + 1  
-----  
      s^3 + 12 s^2 + 47 s + 60  
  
Continuous-time transfer function.
```

```
steaderror2 =
```

```
0.9833
```



```
tf3 =  
  
    1  
    ----  
   s + 10  
  
Continuous-time transfer function.  
  
ans =  
  
    struct with fields:  
  
    RiseTime: 0.2197  
    TransientTime: 0.3912  
    SettlingTime: 0.3912  
    SettlingMin: 0.0905  
    SettlingMax: 0.1000  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 0.1000  
    PeakTime: 1.0546  
  
steadyerror3 =  
  
    0.9000
```

6 EXERCISE 2

$$\frac{p}{s - p}$$

This system has a pole at p , it has no zeros and the gain is equal to the negative of the pole i.e. $-p$. Using Matlab, plot the step response of systems of this form for $p = -1, -2, -5, -10$. Plot all the step responses on a single figure. A sample code is given below.

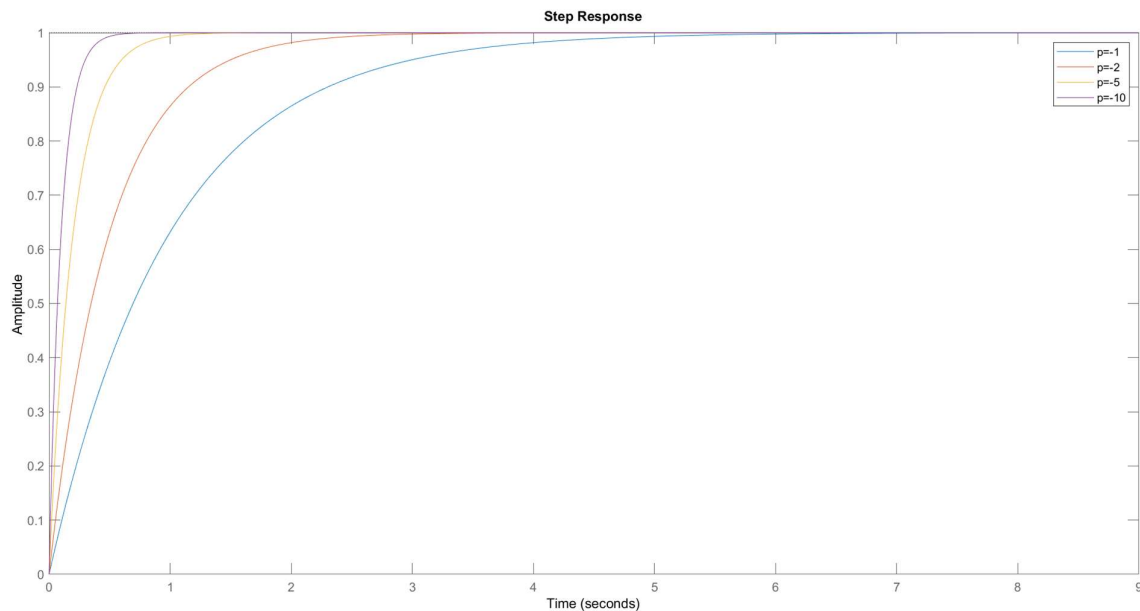
6.1 CODE:

```
clc  
clear  
close  
hold on;  
sys1 = zpk([],-1,1);  
tf1=tf(sys1);  
step(ss(sys1));  
sys2 = zpk([],-2,2);
```



```
tf2=tf(sys2);  
step(ss(sys2));  
sys3 = zpk([],-5,5);  
tf3=tf(sys3);  
step(ss(sys3));  
sys4 = zpk([],-10,10);  
tf4=tf(sys4);  
step(ss(sys4));  
legend('p=-1','p=-2','p=-5','p=-10');  
  
stepinfo(sys1);  
steadyerror1=abs(1-dcgain(tf1));  
stepinfo(sys2);  
steadyerror2=abs(1-dcgain(tf2));  
stepinfo(sys3);  
steadyerror3=abs(1-dcgain(tf3));  
stepinfo(sys4);  
steadyerror4=abs(1-dcgain(tf4));
```

6.2 OUTPUT





ans =

struct with fields:

```
RiseTime: 2.1970
TransientTime: 3.9121
SettlingTime: 3.9121
SettlingMin: 0.9045
SettlingMax: 1.0000
Overshoot: 0
Undershoot: 0
Peak: 1.0000
PeakTime: 10.5458
```

steadyerror1 =

0

ans =

struct with fields:

```
RiseTime: 0.4394
TransientTime: 0.7824
SettlingTime: 0.7824
SettlingMin: 0.9045
SettlingMax: 1.0000
Overshoot: 0
Undershoot: 0
Peak: 1.0000
PeakTime: 2.1092
```

steadyerror3 =

0

ans =

struct with fields:

```
RiseTime: 1.0985
TransientTime: 1.9560
SettlingTime: 1.9560
SettlingMin: 0.9045
SettlingMax: 1.0000
Overshoot: 0
Undershoot: 0
Peak: 1.0000
PeakTime: 5.2729
```

steadyerror2 =

0

ans =

struct with fields:

```
RiseTime: 0.2197
TransientTime: 0.3912
SettlingTime: 0.3912
SettlingMin: 0.9045
SettlingMax: 1.0000
Overshoot: 0
Undershoot: 0
Peak: 1.0000
PeakTime: 1.0546
```

steadyerror4 =

0

6.3 COMMENTS

The introduction of an additional pole into a system leads to a reduction in the speed at which the system responds, the extent of which is contingent on the proximity of the pole to the imaginary $j\omega$ axis.



7 EXERCISE 3:

$$\frac{k}{s - p}$$

Using Matlab, plot the step response of systems of this form for $p = -5$ and $k = 1, 2, 5, 10$. Plot all the step responses on a single figure. For each system also find the values of the various performance characteristics. Comment on the effects of changing the gain.

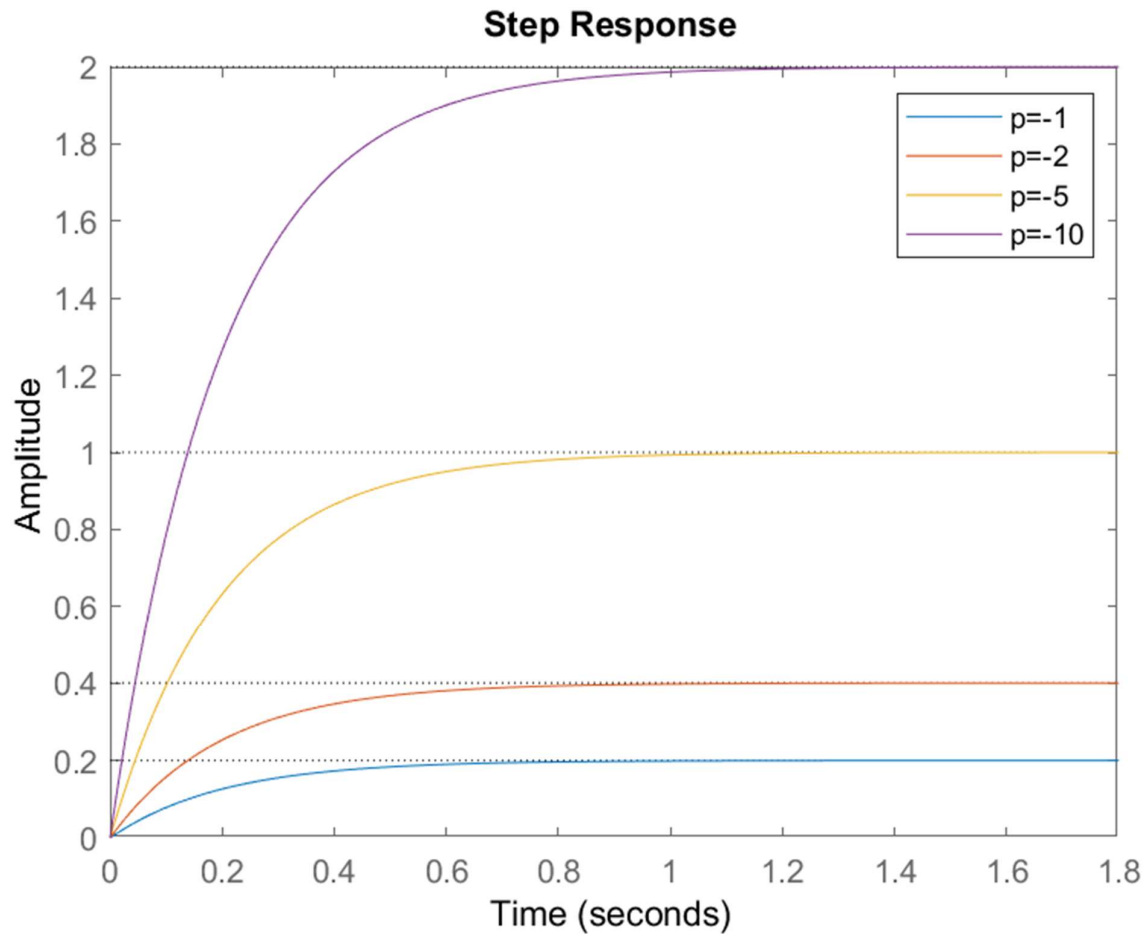
7.1 CODE:

```
clc
clear
close
hold on;
sys1 = zpk([], -5, 1);
tf1=tf(sys1);
step(ss(sys1));
sys2 = zpk([], -5, 2);
tf2=tf(sys2);
step(ss(sys2));
sys3 = zpk([], -5, 5);
tf3=tf(sys3);
step(ss(sys3));
sys4 = zpk([], -5, 10);
tf4=tf(sys4);
step(ss(sys4));
legend('p=-1', 'p=-2', 'p=-5', 'p=-10');

stepinfo(sys1)
steadyerror1=abs(1-dcgain(tf1))
stepinfo(sys2)
steadyerror2=abs(1-dcgain(tf2))
stepinfo(sys3)
steadyerror3=abs(1-dcgain(tf3))
stepinfo(sys4)
steadyerror4=abs(1-dcgain(tf4))
```



7.2 OUTPUT:





```
ans =  
  
struct with fields:  
  
    RiseTime: 0.4394  
    TransientTime: 0.7824  
    SettlingTime: 0.7824  
    SettlingMin: 0.9045  
    SettlingMax: 1.0000  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 1.0000  
    PeakTime: 2.1092  
  
steadyerror3 =  
  
    0  
  
ans =  
  
struct with fields:  
  
    RiseTime: 0.4394  
    TransientTime: 0.7824  
    SettlingTime: 0.7824  
    SettlingMin: 1.8090  
    SettlingMax: 1.9999  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 1.9999  
    PeakTime: 2.1092  
  
steadyerror4 =  
  
    1  
1
```

```
ans =  
  
struct with fields:  
  
    RiseTime: 0.4394  
    TransientTime: 0.7824  
    SettlingTime: 0.7824  
    SettlingMin: 0.1809  
    SettlingMax: 0.2000  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 0.2000  
    PeakTime: 2.1092  
  
steadyerror1 =  
  
    0.8000  
  
ans =  
  
struct with fields:  
  
    RiseTime: 0.4394  
    TransientTime: 0.7824  
    SettlingTime: 0.7824  
    SettlingMin: 0.3618  
    SettlingMax: 0.4000  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 0.4000  
    PeakTime: 2.1092  
  
steadyerror2 =  
  
    0.6000
```

7.3 COMMENTS:

Altering the gain of a system does not affect the overall speed of the system's response; instead, it modifies the ultimate value at which the system stabilizes.



8 EXERCISE 4:

$$\frac{k(s - z)}{s - p}$$

Using Matlab, plot the step response of systems of this form for $z = -5$, $k = 1$ and $p = -1, -2, -5, -10$. Also have a plot for no zero. Plot all the step responses on a single figure. For each system also find the values of the various performance characteristics. Comment on the effects of changing the zeros.

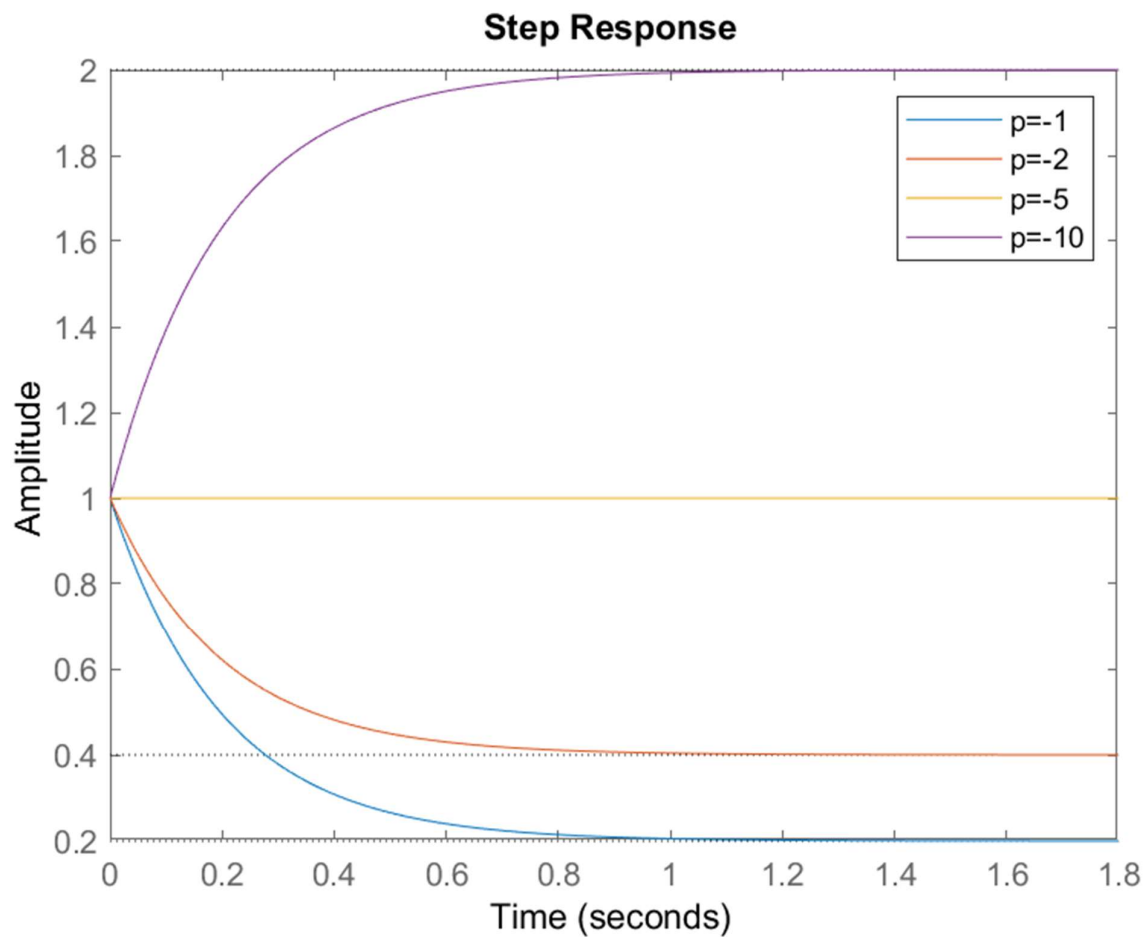
8.1 CODE:

```
clc
clear
close
hold on;
sys1 = zpk(-1,-5,1);
tf1=tf(sys1);
step(ss(sys1));
sys2 = zpk(-2,-5,1);
tf2=tf(sys2);
step(ss(sys2));
sys3 = zpk(-5,-5,1);
tf3=tf(sys3);
step(ss(sys3));
sys4 = zpk(-10,-5,1);
tf4=tf(sys4);
step(ss(sys4));
legend('p=-1','p=-2','p=-5','p=-10');

stepinfo(sys1)
steadyerror1=abs(1-dcgain(tf1))
stepinfo(sys2)
steadyerror2=abs(1-dcgain(tf2))
stepinfo(sys3)
steadyerror3=abs(1-dcgain(tf3))
stepinfo(sys4)
steadyerror4=abs(1-dcgain(tf4))
```



8.2 OUTPUT:





```
ans =  
  
    struct with fields:  
  
        RiseTime: 0  
        TransientTime: 0.7824  
        SettlingTime: 1.0597  
        SettlingMin: 0.2000  
        SettlingMax: 1  
        Overshoot: 400.0000  
        Undershoot: 0  
        Peak: 1  
        PeakTime: 0  
  
steadyerror1 =  
  
    0.8000  
  
ans =  
  
    struct with fields:  
  
        RiseTime: 0  
        TransientTime: 0.7824  
        SettlingTime: 0.8635  
        SettlingMin: 0.4000  
        SettlingMax: 1  
        Overshoot: 150  
        Undershoot: 0  
        Peak: 1  
        PeakTime: 0  
  
steadyerror2 =  
  
    0.6000
```

8.3 COMMENTS:

Incorporating an additional zero in a system amplifies the velocity of the system's response, with the degree of escalation hinging on the proximity of the pole to the imaginary $j\omega$ axis.



9 EXERCISE 5

Use the formulas given above to find the values of the pole of a first order system that would give

- rise times of 0.1, 0.5 and 1
- settling times of 1, 1.5 and 2

9.1 CODE:

```
risetime=[0.1 0.5 1];  
pole=2./risetime;  
settlingtime=[1 1.5 2];  
pole1=4./settlingtime;
```

9.2 OUTPUT:

```
>> pole  
  
pole =  
  
    20     4     2  
  
>> pole1  
  
pole1 =  
  
    4.0000    2.6667    2.0000
```

10 EXERCISE 6:

Find the damping ratio and the natural frequency of the following systems:

$$\frac{5}{s^2 - 4s + 5}, \quad \frac{2}{s^2 - 2s + 2}, \quad \frac{5}{s^2 - 2s + 5}$$



10.1 CODE:

```
tf1=tf(5,[1 -4 5]);  
tf2=tf(2,[1 -2 2]);  
tf3=tf(5,[1 -2 5]);  
damp(tf1)  
damp(tf2)  
damp(tf3)
```

10.2 OUTPUT:

```
>> lab6lcs
```

Pole	Damping	Frequency (rad/seconds)	Time Constant (seconds)
2.00e+00 + 1.00e+00i	-8.94e-01	2.24e+00	-5.00e-01
2.00e+00 - 1.00e+00i	-8.94e-01	2.24e+00	-5.00e-01

Pole	Damping	Frequency (rad/seconds)	Time Constant (seconds)
1.00e+00 + 1.00e+00i	-7.07e-01	1.41e+00	-1.00e+00
1.00e+00 - 1.00e+00i	-7.07e-01	1.41e+00	-1.00e+00

Pole	Damping	Frequency (rad/seconds)	Time Constant (seconds)
1.00e+00 + 2.00e+00i	-4.47e-01	2.24e+00	-1.00e+00
1.00e+00 - 2.00e+00i	-4.47e-01	2.24e+00	-1.00e+00

11 EXERCISE 7:

Write a MATLAB function that takes the damping ratio and natural frequency as arguments and returns a transfer function of the form given in equation (2).

$$\frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$



11.1 OUTPUT

```
>> lab61cs  
What is the b 20  
What is the a 10  
  
Tf =  
  
20/(s^2 + 20*s + 20)
```

11.2 CODE

```
syms s;  
prompt1="What is the b ";  
prompt2="What is the a ";  
b=input(prompt1);  
a=input(prompt2);  
  
Tf=(b)/(s^2+2*s*a+b)
```

12 EXERCISE 8

Write a MATLAB function that takes the damping ratio and natural frequency as arguments and returns a transfer function of the form given in equation (2). Call this function my_second_order_tf.

12.1 CODE:

```
syms s;  
prompt1="What is the natural Frequency ";  
prompt2="What is the Damping Ratio ";  
naturalfrequency=input(prompt1);  
dampingratio=input(prompt2);  
  
Tf=(naturalfrequency^2)/(s^2+2*dampingratio*s*naturalfrequency+naturalfrequency^2)
```



12.2 OUTPUT:

```
>> lab6lcs
What is the natural Frequency 10
What is the Damping Ratio 20

Tf =

100/(s^2 + 400*s + 100)
```

13 EXERCISE: 9

Using the function that you have just created, `my_second_order_tf`, make transfer functions for the following sets of damping ratios and natural frequencies Set 1: $\zeta = 0$, $\omega_n = 1, 2, 5$ (See the note given below) Set 2: $\zeta = 1$, $\omega_n = 1, 2, 5$ Set 3: $\zeta = 0, 0.5, 1, 2$, $\omega_n = 1$ For each set of values plot the step responses on a single figure. For each system also find the values of the various performance characteristic. Comment on the effects of changing the natural frequency and the damping ratio. Classify each of the above systems as undamped, underdamped, critically damped or overdamped.

13.1 CODE:

```
prompt1="What is the natural Frequency ";
prompt2="What is the Damping Ratio ";
naturalfrequency1=input(prompt1);
dampingratio1=input(prompt2);
naturalfrequency2=input(prompt1);
dampingratio2=input(prompt2);
naturalfrequency3=input(prompt1);
dampingratio3=input(prompt2);

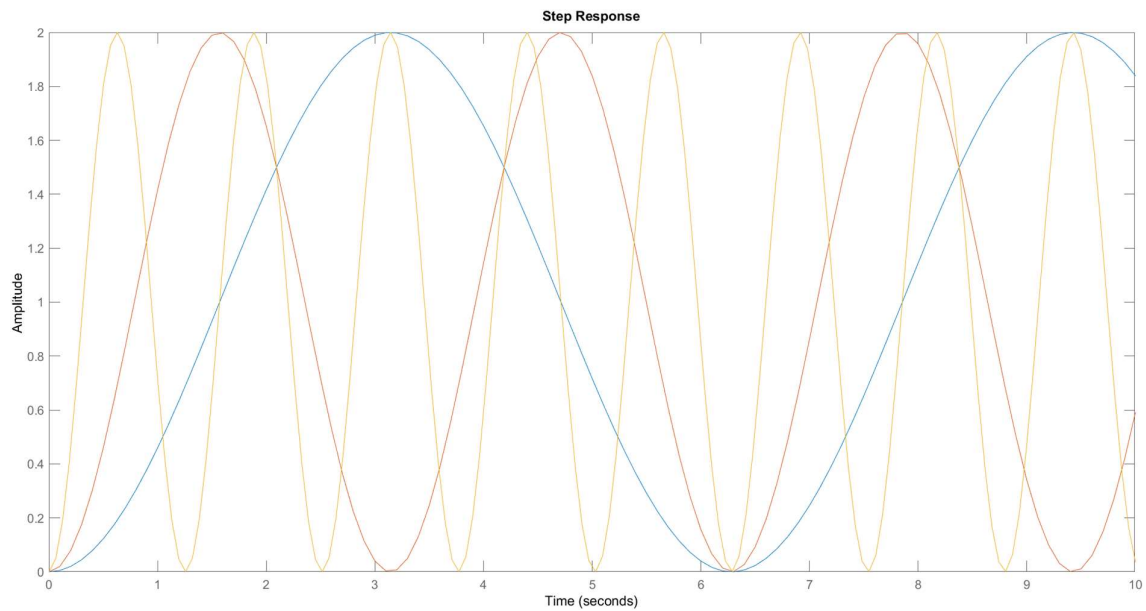
Tf1=tf([naturalfrequency1^2],[1 2*dampingratio1*naturalfrequency1
naturalfrequency1^2]);
Tf2=tf([naturalfrequency2^2],[1 2*dampingratio2*naturalfrequency2
naturalfrequency2^2]);
Tf3=tf([naturalfrequency3^2],[1 2*dampingratio3*naturalfrequency3
naturalfrequency3^2]);
hold on;
step(Tf1,10)
step(Tf2,10)
step(Tf3,10)
```



```
stepinfo(Tf1)  
stepinfo(Tf2)  
stepinfo(Tf3)
```

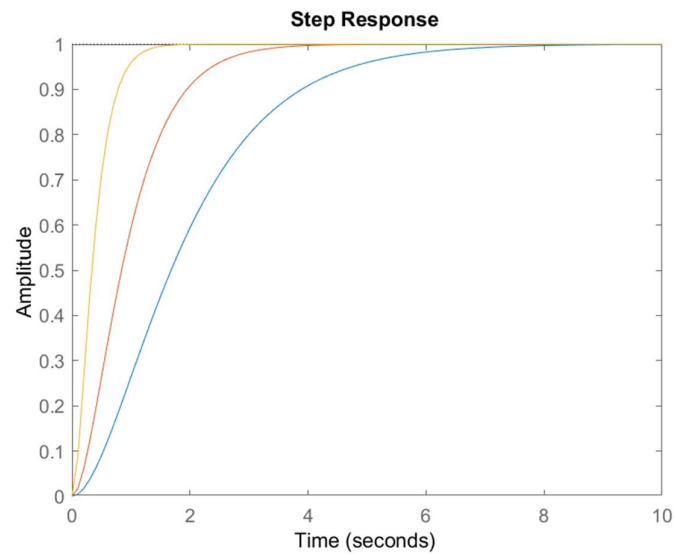
13.2 OUTPUT:

13.2.1 Part 1





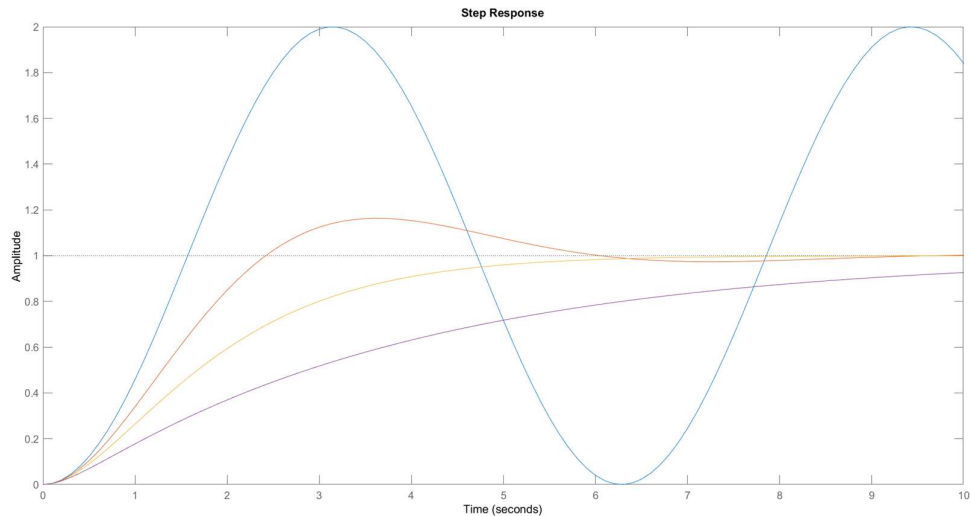
13.2.2 Part 2



```
ans =  
  
struct with fields:  
  
    RiseTime: 3.3579  
    TransientTime: 5.8339  
    SettlingTime: 5.8339  
    SettlingMin: 0.9000  
    SettlingMax: 0.9994  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 0.9994  
    PeakTime: 9.7900  
  
ans =  
  
struct with fields:  
  
    RiseTime: 1.6790  
    TransientTime: 2.9170  
    SettlingTime: 2.9170  
    SettlingMin: 0.9008  
    SettlingMax: 0.9991  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 0.9991  
    PeakTime: 4.6900  
  
ans =  
  
struct with fields:  
  
    RiseTime: 0.6717  
    TransientTime: 1.1668  
    SettlingTime: 1.1668  
    SettlingMin: 0.9008  
    SettlingMax: 0.9999  
    Overshoot: 0  
    Undershoot: 0  
    Peak: 0.9999  
    PeakTime: 2.3900
```



13.2.3 Part 3



ans =

struct with fields:

```
RiseTime: NaN
TransientTime: NaN
SettlingTime: NaN
SettlingMin: NaN
SettlingMax: NaN
Overshoot: NaN
Undershoot: NaN
Peak: Inf
PeakTime: Inf
```

ans =

struct with fields:

```
RiseTime: 1.6390
TransientTime: 8.0759
SettlingTime: 8.0759
SettlingMin: 0.9315
SettlingMax: 1.1629
Overshoot: 16.2929
Undershoot: 0
Peak: 1.1629
PeakTime: 3.5920
```

ans =

struct with fields:

```
RiseTime: 3.3579
TransientTime: 5.8339
SettlingTime: 5.8339
SettlingMin: 0.9000
SettlingMax: 0.9994
Overshoot: 0
Undershoot: 0
Peak: 0.9994
PeakTime: 9.7900
```



14 EXERCISE 10

Using the formulas given above, find the values of damping ratio and natural frequency that result in %OS=10 and $\zeta = 1$.

14.1 CODE:

```
OS=10;  
Ts=.01;  
Zeta = -(log(OS/100))/sqrt((log(OS/100))^2 + pi^2)  
Wn = 4/(Zeta*Ts)
```

14.2 OUTPUT:

```
w_n_ans =  
  
6.7664  
  
>> zeta_ans  
  
zeta_ans =  
  
0.5912
```

15 EXERCISE: 11

For the systems given below, find the natural frequency, the damping ratio and transient characteristics. Also plot their step responses on a single graph.

$$\frac{1}{s^2 + s + 1}, \quad \frac{s + 1}{s^2 + s + 1}$$

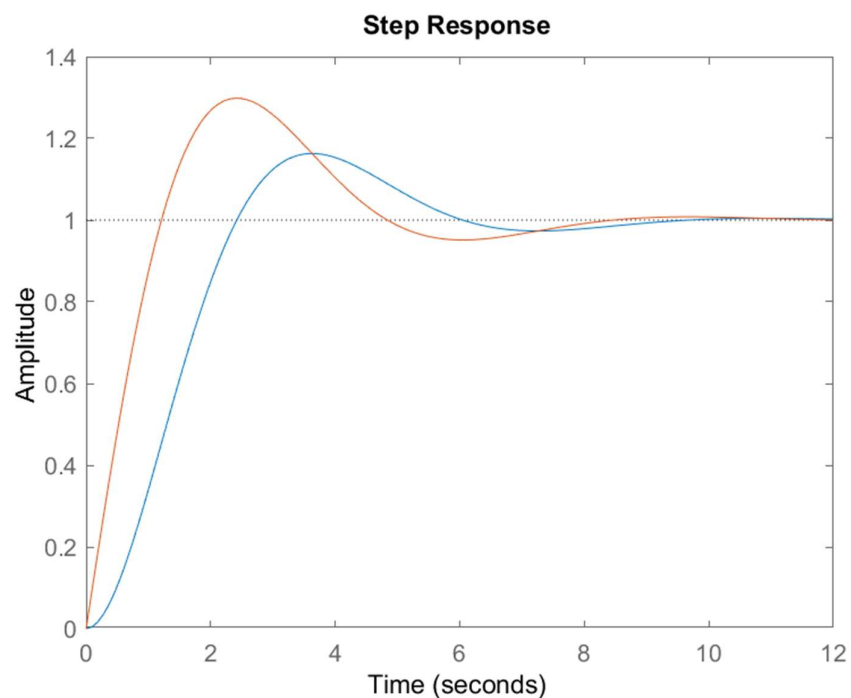
15.1 CODE:

```
num=[1];  
dem=[1 1 1];
```



```
tf1=tf(num,dem);  
hold on;  
damp(tf1);  
step(tf1);  
stepinfo(tf1);  
num1=[1 1];  
dem1=[1 1 1];  
tf2=tf(num1,dem1);  
damp(tf2);  
step(tf2);  
stepinfo(tf2);
```

15.2 OUTPUT



15.3 COMMENTS

Introducing an extra zero to a second-order system engenders a swifter pace at which the step response advances when juxtaposed with the initial system.



16 EXERCISE 12:

For the systems given below, find the natural frequency, the damping ratio and transient characteristics. Also plot their step responses on a single graph.

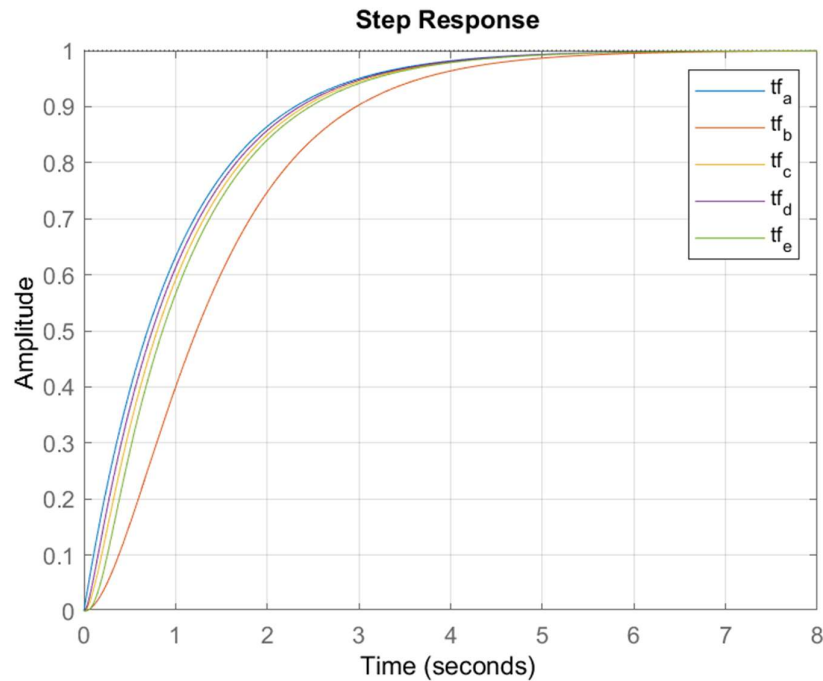
$$\frac{1}{(s+1)}, \quad \frac{2}{(s+1)(s+2)}, \quad \frac{10}{(s+1)(s+10)}, \quad \frac{20}{(s+1)(s+20)}$$

16.1 CODE:

```
tf_a = zpk([], -1, 1);  
tf_b = zpk([], [-1 -2], 2);  
tf_c = zpk([], [-1 -10], 10);  
tf_d = zpk([], [-1 -20], 20);  
tf_e = zpk([], [-1 -10-5*1i -10+5*1i], 125);  
figure  
t = 0:0.01:8;  
hold on  
step(tf_a, t)  
step(tf_b, t)  
step(tf_c, t)  
step(tf_d, t)  
step(tf_e, t)  
grid  
legend('tf_a', 'tf_b', 'tf_c', 'tf_d', 'tf_e')
```



16.2 OUTPUT:



Comments:

The introduction of an additional pole to a first-order system results in a deceleration of the speed at which the step response progresses when compared to the original system.

damp_a:

Pole Damping Frequency Time Constant
(rad/seconds) (seconds)

-1.00e+00 1.00e+00 1.00e+00 1.00e+00

damp_b:

Pole Damping Frequency Time Constant
(rad/seconds) (seconds)

-1.00e+00 1.00e+00 1.00e+00 1.00e+00

-2.00e+00 1.00e+00 2.00e+00 5.00e-01

damp_c:

Pole Damping Frequency Time Constant
(rad/seconds) (seconds)

-1.00e+00 1.00e+00 1.00e+00 1.00e+00

-1.00e+01 1.00e+00 1.00e+01 1.00e-01



damp_d:

Pole Damping Frequency Time Constant
(rad/seconds) (seconds)

-1.00e+00 1.00e+00 1.00e+00 1.00e+00

-2.00e+01 1.00e+00 2.00e+01 5.00e-02

damp_e:

Pole Damping Frequency Time Constant
(rad/seconds) (seconds)

-1.00e+00 1.00e+00 1.00e+00 1.00e+00

-1.00e+01 - 5.00e+00i 8.94e-01 1.12e+01 1.00e-01

-1.00e+01 + 5.00e+00i 8.94e-01 1.12e+01 1.00e-01

step_a:

RiseTime: 2.1970

TransientTime: 3.9121

SettlingTime: 3.9121

SettlingMin: 0.9045

SettlingMax: 1.0000

Overshoot: 0

Undershoot: 0

Peak: 1.0000

PeakTime: 10.5458

step_b:

RiseTime: 2.5901

TransientTime: 4.6002

SettlingTime: 4.6002

SettlingMin: 0.9023

SettlingMax: 0.9992

Overshoot: 0

Undershoot: 0

Peak: 0.9992

PeakTime: 7.7827

step_c:

RiseTime: 2.2150

TransientTime: 4.0174

SettlingTime: 4.0174

SettlingMin: 0.9005

SettlingMax: 0.9993



Overshoot: 0
Undershoot: 0
Peak: 0.9993
PeakTime: 7.3591
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step_d:
RiseTime: 2.2000
TransientTime: 3.9634
SettlingTime: 3.9634
SettlingMin: 0.9040
SettlingMax: 0.9993
Overshoot: 0
Undershoot: 0
Peak: 0.9993
PeakTime: 7.3222
step_e:
RiseTime: 2.2117
TransientTime: 4.0769
SettlingTime: 4.0769
SettlingMin: 0.9001
SettlingMax: 0.9994
Overshoot: 0
Undershoot: 0
Peak: 0.9994
PeakTime: 7.5433

17 EXERCISE 13

For the systems given below, find the natural frequency, the damping ratio and transient characteristics. Also plot their step responses on a single graph.



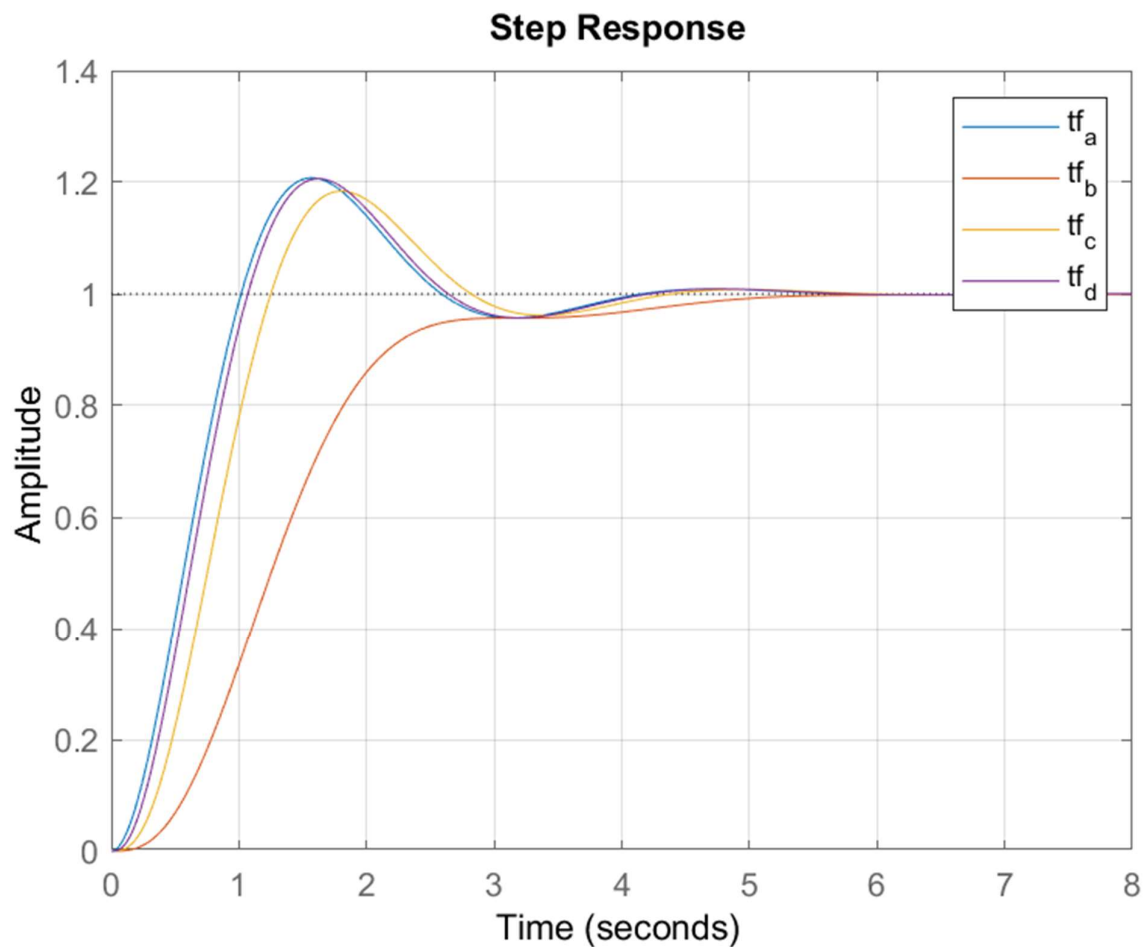
$$\frac{5}{(s+1+2i)(s+1-2i)}$$
$$\frac{5}{(s+1)(s+1+2i)(s+1-2i)}$$
$$\frac{25}{(s+5)(s+1+2i)(s+1-2i)}$$
$$\frac{100}{(s+20)(s+1+2i)(s+1-2i)}$$

17.1 CODE:

```
tf_a = zpk([], [-1-2*i -1+2*i], 5);  
tf_b = zpk([], [-1 -1-2*i -1+2*i], 5);  
tf_c = zpk([], [-5 -1-2*i -1+2*i], 25);  
tf_d = zpk([], [-20 -1-2*i -1+2*i], 100);  
figure  
t = 0:0.01:8;  
hold on  
step(tf_a, t)  
step(tf_b, t)  
step(tf_c, t)  
step(tf_d, t)  
grid  
legend('tf_a', 'tf_b', 'tf_c', 'tf_d')
```



17.2 OUTPUT:



17.3 COMMENTS

Incorporating an extra pole into a second-order system causes a deceleration in the speed at which the step response proceeds in comparison to the initial system.



18 CONCLUSION:

In conclusion, the lab was successful in achieving its objectives of plotting step response of first and second order equations in MATLAB and determining the effect of pole zero locations on step response. The lab also enabled us to find the rise time, transient response, and overshoot for second order systems. Through the experiments conducted, we were able to observe how the placement of poles and zeros in the transfer function of a system can have a significant impact on its step response characteristics, including rise time, settling time, and overshoot. These insights will be invaluable in designing and analyzing control systems in various engineering applications. Overall, this lab provided a comprehensive introduction to the fundamental concepts of system analysis and MATLAB simulation, which will serve as a foundation for further exploration in the field of control systems engineering. In conclusion, the lab was successful in achieving its objectives of plotting step response of first and second order equations in MATLAB and determining the effect of pole zero locations on step response. The lab also enabled us to find the rise time, transient response, and overshoot for second order systems. Through the experiments conducted, we were able to observe how the placement of poles and zeros in the transfer function of a system can have a significant impact on its step response characteristics, including rise time, settling time, and overshoot. These insights will be invaluable in designing and analyzing control systems in various engineering applications. Overall, this lab provided a comprehensive introduction to the fundamental concepts of system analysis and MATLAB simulation, which will serve as a foundation for further exploration in the field of control systems engineering.