from Wyckoff to Quantum ESPRESSO

How to translate a crystallografic structure as given in standard texts (ex. Ralph W.G. Wyckoff, *Crystal Structures*) into the Quantum ESPRESSO input format.

How is a crystal structure defined in QE?

The &SYSTEM namelist (STRUCTURE)

ibrav Bravais-lattice index (NO default, must be specified)

```
0
        read unit cell information from CELL_PARAMETRES card
 1
        cubic P (sc)
        cubic F (fcc)
 3
        cubic I (bcc)
        Hexagonal and Trigonal P
4
5
        Trigonal R
        Tetragonal P (st)
6
7
        Tetragonal I (bct)
8
        Orthorhombic P
9
        Orthorhombic base-centered(bco)
10
        Orthorhombic face-centered
11
        Orthorhombic body-centered
12
        Monoclinic P
13
       Monoclinic base-centered
14
       Triclinic P
```

Crystallographic constants: there are two options

- 1) celldm(i), i=1,2,...,6
- 2) a, b, c, cosab, cosac, cosbc,

```
celldm(1) = a / bohr_radius_angs = alat (internal unit of lenght)
celldm(2) = b / a
celldm(3) = c / a
celldm(4) = cosab
celldm(5) = cosac
celldm(6) = cosbc
```

BEWARE:

```
alat = celldm(1) is the lattice parameter "a" in BOHR
a,b,c are given in ANGSTROM
```

Specify either a,b,c,..., OR celldm but not both. Only crystallographic constants needed for chosen Bravais lattice must be specified; other parameters are IGNORED.

```
c cosab cosac cosbc
                         celldm --> 1 2 3
                                               4
ibrav
                                                           6
 1 cubic P (sc)
                                    *
2 cubic F (fcc)
                                    *
3 cubic I (bcc)
4 Hexagonal and Trigonal P
                                    *
                                          *
5 Trigonal R
                                    *
                                               *
 6 Tetragonal P (st)
 7 Tetragonal I (bct)
                                    *
8 Orthorhombic P
                                          *
                                       *
9 Orthorhombic base-centered(bco)
                                          *
10 Orthorhombic face-centered
                                       *
                                          *
                                    *
11 Orthorhombic body-centered
                                    *
                                          *
12 Monoclinic P
                                       * *
                                    *
                                               *
13 Monoclinic base-centered
                                          *
                                               *
14 Triclinic P
                                    *
                                       *
                                          *
                                               *
```

If ibrav = 0 BL fundamental vectors are read from an optional card CELL_PARAMETERS to be inserted after all needed NAMELISTS.

Where symmetry_class is cubic or hexagonal depending on the expected symmetry of the system w.r.t. the assumed reference system.

If $celldm(1)\neq 0$, lattice vectors are given in these units If celldm(1)=0, lattice vectors are given in BOHR, and the length of the first lattice vector defines alat.

nat INTEGER (NO default, must be specified) number of atoms in the unit cell

ntyp INTEGER (NO default, must be specified) number of types of atoms in the unit cell

nelec REAL

number of electron in the unit cell
Default: the same as ionic charge (neutral cell)

nbnd INTEGER

number of electronic bands to be calculated.

Default: in insulators, nbnd = nelec/2 in metals, 20% more (minimum 4 more)

The ATOMIC_SPECIES card

For each atomic species (ntyp in &SYSTEM namelist) one must specify a label, the atomic mass and the name a PP file.

```
ATOMIC_SPECIES
X(1)     Mass_X(1)     PseudoPot_X(1)
...
X(ntyp) Mass_X(ntyp)     PseudoPot_X(ntyp)
```

The ATOMIC_SPECIES card

For each atomic species (ntyp in &SYSTEM namelist) one must specify a label, the atomic mass and the name a PP file.

```
ATOMIC_SPECIES

X(1) Mass_X(1) PseudoPot_X(1)

...

X(ntyp) Mass_X(ntyp) PseudoPot_X(ntyp)

example

ATOMIC_SPECIES

O 16.00 O.LDA.US.RRKJ3.UPF

C 12.00 C.pz-rrkjus.UPF
```

The ATOMIC_SPECIES card

For each atomic species (ntyp in &SYSTEM namelist) one must specify a label, the atomic mass and the name a PP file.

```
ATOMIC_SPECIES

X(1) Mass_X(1) PseudoPot_X(1)
...

X(ntyp) Mass_X(ntyp) PseudoPot_X(ntyp)

example

ATOMIC_SPECIES

O 16.00 O.LDA.US.RRKJ3.UPF

C 12.00 C.pz-rrkjus.UPF
```

Masses are actually used only if atoms move.

The ATOMIC_POSITIONS card

This card specify the atomic species label and positions of each atom in the unit cell (nat in &SYSTEM namelist).

```
ATOMIC_POSITIONS position_format

X(1) x(1) y(1) z(1)

...

X(nat) x(nat) y(nat) z(nat)
```

where position_format is alat (default), bohr, angstrom or crystal

The ATOMIC_POSITIONS card

This card specify the atomic species label and positions of each atom in the unit cell (nat in &SYSTEM namelist).

```
ATOMIC_POSITIONS position_format

X(1) x(1) y(1) z(1)

...

X(nat) x(nat) y(nat) z(nat)
```

where position_format is alat (default), bohr, angstrom or crystal It is also possible to specify that some coordinates should be kept fixed in relaxation or dynamics.

```
ATOMIC_POSITIONS bohr
C 2.256 0.0 0.0
D 0.0 0.0 0.0 0 0
```

A few examples

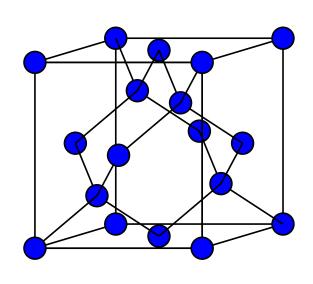
diamond

II,i1: The unit cubes of crystals with the $diamond\ structure$ have eight atoms in the position of O_h^7 (Fd3m):

or more briefly

(8a) 000; 1/4 1/4; F.C.

| Element | Name | a ₀ , A |
|---------|------------|--------------------|
| С | carbon | 3.56679 (20 C) |
| Si | Silicon | 5.43070 (25 C) |
| | | 5.445 (1300 C) |
| Ge | Germanium | 5.65735 (20 C) |
| | | 5.65695 (18 C) |
| lpha-Sn | Tin (gray) | 6.4912 |



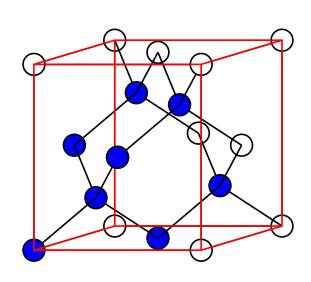
diamond

II,i1: The unit cubes of crystals with the $diamond\ structure$ have eight atoms in the position of O_h^7 (Fd3m):

or more briefly

(8a) 000; 1/4 1/4; F.C.

| Element | Name | a ₀ , A |
|---------|------------|--------------------|
| С | carbon | 3.56679 (20 C) |
| Si | Silicon | 5.43070 (25 C) |
| | | 5.445 (1300 C) |
| Ge | Germanium | 5.65735 (20 C) |
| | | 5.65695 (18 C) |
| lpha-Sn | Tin (gray) | 6.4912 |



```
C: simple cubic \longrightarrow ibrav = 1
    3.56679 A
 &SYSTEM
    ntyp=1, nat=8, ibrav=1, a = 3.56679,
ATOMIC_SPECIES
C 28.086 C.UPF
ATOMIC_POSITIONS
C 0.0 0.0 0.0
C 0.0 0.5 0.5
C 0.5 0.0 0.5
C 0.5 0.5 0.0
C 0.25 0.25 0.25
C 0.25 0.75 0.75
C 0.75 0.25 0.75
C 0.75 0.75 0.25
```

```
C: simple cubic \longrightarrow ibrav = 1
     3.56679 \text{ A} \longrightarrow 6.740259 \text{ bohrs}
 &SYSTEM
    ntyp=1, nat=8, ibrav=1, celldm(1)=6.740259,
ATOMIC_SPECIES
C 28.086 C.UPF
ATOMIC_POSITIONS
C 0.0 0.0 0.0
C 0.0 0.5 0.5
C 0.5 0.0 0.5
C 0.5 0.5 0.0
C 0.25 0.25 0.25
C 0.25 0.75 0.75
C 0.75 0.25 0.75
C 0.75 0.75 0.25
```

```
C: simple cubic \longrightarrow ibrav = 1
     3.56679 \text{ A} \longrightarrow 6.740259 \text{ bohrs}
 &SYSTEM
    ntyp=1, nat=8, ibrav=1, celldm(1)=6.740259,
ATOMIC_SPECIES
C 28.086 C.UPF
ATOMIC_POSITIONS
C 0.0 0.0 0.0
C 0.0 0.5 0.5
C 0.5 0.0 0.5
C 0.5 0.5 0.0
C 0.25 0.25 0.25
C 0.25 0.75 0.75
C 0.75 0.25 0.75
C 0.75 0.75 0.25
```

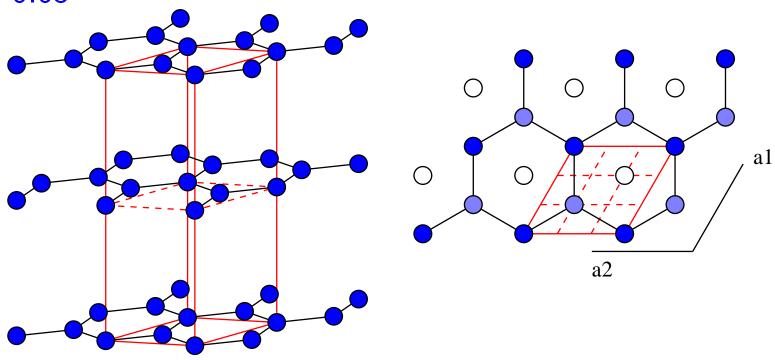
```
C: face centered cubic \longrightarrow ibrav = 2
     3.56679 A \longrightarrow 6.740259 bohrs
 &SYSTEM
    ntyp=1, nat=2, ibrav=2, celldm(1)=6.740259,
ATOMIC_SPECIES
C 28.086 C.UPF
ATOMIC_POSITIONS
C 0.0 0.0 0.0
C 0.25 0.25 0.25
```

graphite

II,i2: The long-familiar form of graphite has an hexagonal unit with $a_0 = 2.456 \text{ A}$, $c_0 = 6.696 \text{ A}$

Its four atoms are in the following two sets of special positions of C_{6v}^4 (C6mc):

(2a) 00u; 0,0,u+1/2 and (2b) 1/3 2/3 v; 2/3, 1/3, v+1/2 where u can be taken as zero; v then is practically zero and cannot exceed 0.05

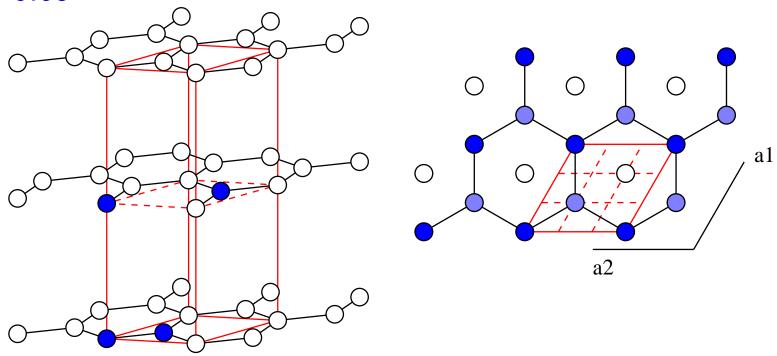


graphite

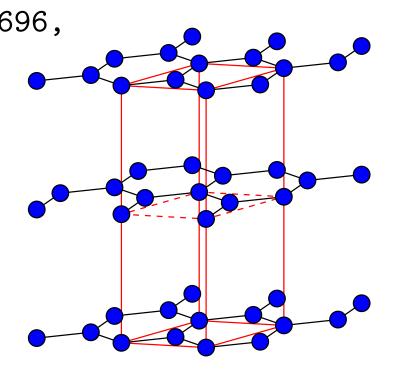
II,i2: The long-familiar form of graphite has an hexagonal unit with $a_0 = 2.456$ A, $c_0 = 6.696$ A

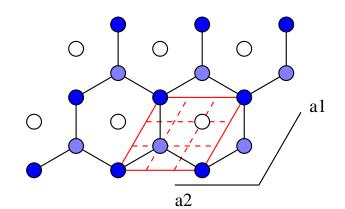
Its four atoms are in the following two sets of special positions of C_{6v}^4 (C6mc):

(2a) 00u; 0,0,u+1/2 and (2b) 1/3 2/3 v; 2/3, 1/3, v+1/2 where u can be taken as zero; v then is practically zero and cannot exceed 0.05



```
hexagonal \longrightarrow ibrav = 4
   a = 2.456 A, c = 6.696 A
   u = v = 0
 &SYSTEM
    ibrav=4, a = 2.456, c = 6.696,
    ntyp=1, nat=4,
ATOMIC_SPECIES
C 28.086 C.UPF
ATOMIC_POSITIONS crystal
C 0.0 0.0 0.0
C 0.333333333 0.66666666 0.0
C 0.0 0.0 0.5
C 0.66666666 0.333333333 0.5
```





```
hexagonal \longrightarrow ibrav = 4
   a = 2.456 \text{ A}, c = 6.696 \text{ A} \longrightarrow a = 4.64117 \text{ bohrs, c/a} = 2.7264
   u = v = 0
 &SYSTEM
    ibrav=4, celldm(1)=4.64117, celldm(3)=2.7264,
    ntyp=1, nat=4,
ATOMIC_SPECIES
C 28.086 C.UPF
ATOMIC_POSITIONS crystal
C 0.0 0.0 0.0
C 0.333333333 0.66666666 0.0
C 0.0 0.0 0.5
C 0.666666666 0.333333333 0.5
```

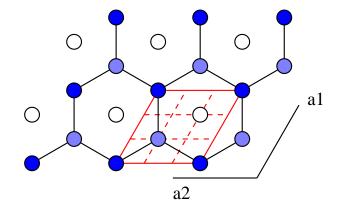
a2

```
hexagonal \longrightarrow ibrav = 4
   a = 2.456 \text{ A}, c = 6.696 \text{ A} \longrightarrow a = 4.64117 \text{ bohrs, c/a} = 2.7264
                                                  0.5 \text{ c/a} = 1.3632
   u = v = 0
  &SYSTEM
     ibrav=4, celldm(1)=4.64117, celldm(3)=2.7264,
     ntyp=1, nat=4,
ATOMIC_SPECIES
C 28.086 C.UPF
ATOMIC_POSITIONS
C 0.0 0.0
                      0.0
```

C 0.0 0.57735027 0.0

C 0.0 0.0 1.3632

C 0.5 0.28867513 1.3632

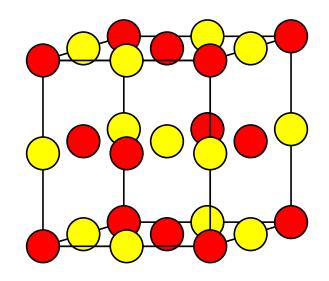


sodium cloride

III, a1: The largest group of RX-type crystals have the structure of $sodium\ cloride$, NaCl. The unit cube of this arrangement contains four molecules with atoms in the positions:

R: (4a) 000; 1/2 1/2 0; 1/2 0 1/2; 0 1/2 1/2, or 000; FC X: (4b) 1/2 1/2; 1/2; 1/2 0 0; 0 1/2 0; 0 0 1/2, or 1/2 1/2; FC

| Crystal | $a_0 \; A$ |
|----------|----------------|
| MgO | 4.21112 (21 C) |
| NaCl | 5.62779 (18 C) |
| NiO | 4.1684 |
| | |

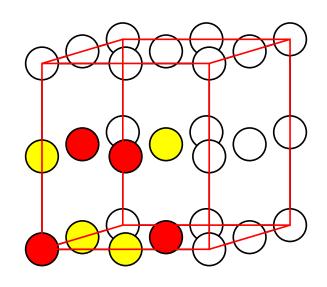


sodium cloride

III, a1: The largest group of RX-type crystals have the structure of $sodium\ cloride$, NaCl. The unit cube of this arrangement contains four molecules with atoms in the positions:

R: (4a) 000; 1/2 1/2 0; 1/2 0 1/2; 0 1/2 1/2, or 000; FC X: (4b) 1/2 1/2; 1/2; 1/2 0 0; 0 1/2 0; 0 0 1/2, or 1/2 1/2; FC

| Crystal | $a_0 A$ |
|----------|----------------|
| MgO | 4.21112 (21 C) |
| NaCl | 5.62779 (18 C) |
| NiO | 4.1684 |
| | |



```
MgO: face centered cubic \longrightarrow ibrav = 2
        4.21112 A \longrightarrow 7.957867 bohrs
 &SYSTEM
    ntyp=2, nat=2, ibrav=2, celldm(1)=7.957867,
ATOMIC_SPECIES
Mg 28.086 Mg.UPF
   16.000 O.UPF
ATOMIC_POSITIONS
Mg 0.0 0.0 0.0
```

```
NiO: face centered cubic \longrightarrow ibrav = 2
        4.1684 \text{ A} \longrightarrow 7.87714 \text{ bohrs}
  &SYSTEM
     ntyp=2, nat=2, ibrav=2, celldm(1)= 7.87714,
ATOMIC_SPECIES
Ni 28.086 Ni.UPF
   16.000 O.UPF
ATOMIC_POSITIONS
```

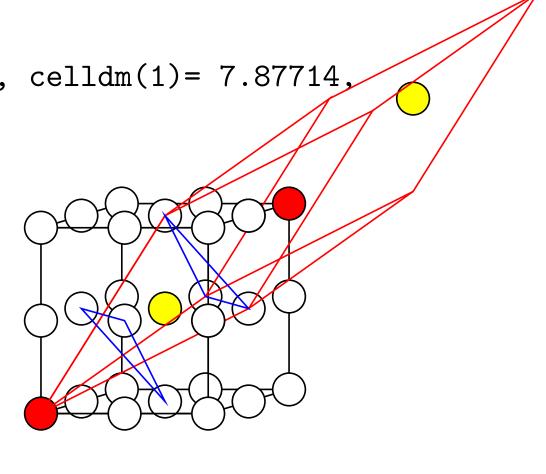
Ni 0.0 0.0 0.0

```
NiO: face centered cubic \longrightarrow ibrav = 2
        4.1684 \text{ A} \longrightarrow 7.87714 \text{ bohrs}
  &SYSTEM
     ntyp=2, nat=2, ibrav=2, celldm(1)= 7.87714,
ATOMIC_SPECIES
Ni 28.086 Ni.UPF
   16.000 O.UPF
ATOMIC_POSITIONS
```

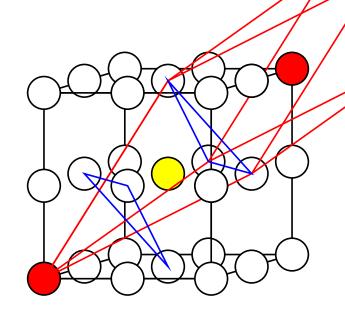
Ni 0.0 0.0 0.0

```
NiO: face centered cubic \longrightarrow ibrav = 2
        4.1684 \text{ A} \longrightarrow 7.87714 \text{ bohrs}
  &SYSTEM
     ntyp=2, nat=2, ibrav=2, celldm(1)= 7.87714,
ATOMIC_SPECIES
Ni 28.086 Ni.UPF
   16.000 O.UPF
ATOMIC_POSITIONS
Ni 0.0 0.0 0.0
```

```
NiO: user supplied lattice \longrightarrow ibrav = 0
       4.1684 \text{ A} \longrightarrow 7.87714 \text{ bohrs}
 &SYSTEM
    ntyp=3, nat=4, ibrav=0, celldm(1)= 7.87714,
CELL_PARAMETERS cubic
1.00 0.50 0.50
0.50 1.00 0.50
0.50 0.50 1.00
ATOMIC_SPECIES
 Ni1 1. Ni.UPF
 Ni2 1. Ni.UPF
 0 1. O.UPF
ATOMIC_POSITIONS crystal
 Ni1 0.0 0.0 0.0
 Ni2 0.5 0.5 0.5
 0 0.25 0.25 0.25
 0 0.75 0.75 0.75
```



```
NiO: rhombohedral lattice \longrightarrow ibrav = 5
       4.1684 \text{ A} \times \sqrt{3/2} = 5.1052265 \text{ A}, \cos(ab) = 5/6
 &SYSTEM
    ntyp=3, nat=4, ibrav=5,
    a = 5.1052265, cosab = 0.83333333,
ATOMIC_SPECIES
 Ni1 1. Ni.UPF
 Ni2 1. Ni.UPF
 0 1. O.UPF
ATOMIC_POSITIONS crystal
 Ni1 0.0 0.0 0.0
 Ni2 0.5 0.5 0.5
 0 0.25 0.25 0.25
```



```
NiO: rhombohedral lattice \longrightarrow ibrav = 5
      4.1684 \text{ A} \times \sqrt{3/2} = 9.64748375 \text{ bohrs, } \cos(ab) = 5/6
 &SYSTEM
   ntyp=3, nat=4, ibrav=5,
    ATOMIC_SPECIES
Ni1 1. Ni.UPF
Ni2 1. Ni.UPF
0 1. O.UPF
ATOMIC_POSITIONS crystal
Ni1 0.0 0.0 0.0
Ni2 0.5 0.5 0.5
0 0.25 0.25 0.25
```

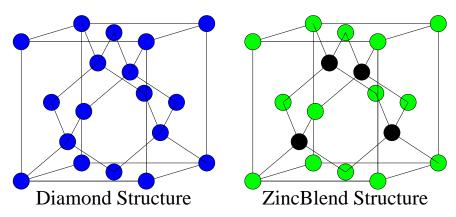
zinc-blend

III, c1: The $zinc\ sulfide$ arrangement, like that of NaCl contains four molecules in its unit cube and is developed on a face-centered lattice. Its atoms have the coordinates (of T_d^2 - $F\bar{4}3m$):

R: (4a) 000; 1/2 1/2 0; 1/2 0 1/2; 0 1/2 1/2, or 000; FC

1/4 1/4 1/4; F.C.

As can be seen each atom has about it four equally distant atoms of the opposite sort arranged at the corners of a regular tetrahedron. If all atoms were alike this would, of course, be the diamond arrangement (II,i1).



```
ZnS: face centered cubic \longrightarrow ibrav = 2
        5.65 \longrightarrow 10.68 \text{ bohrs}
  &SYSTEM
     ntyp=2, nat=2, ibrav=2, celldm(1)=10.68,
ATOMIC_SPECIES
```

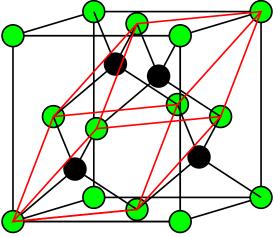
Zn 1. Zn.UPF

S 1. S.UPF

ATOMIC_POSITIONS

Zn 0.0 0.0 0.0

S 0.25 0.25 0.25



```
ZnS: face centered cubic \longrightarrow ibrav = 2 5.65 \longrightarrow 10.68 bohrs &SYSTEM ntyp=2, nat=2, ibrav=2, celldm(1)=10.68, / ... ATOMIC_SPECIES Zn 1. Zn.UPF
```

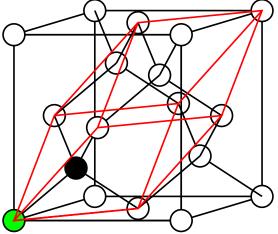
Zn I. Zn.UPi

S 1. S.UPF

ATOMIC_POSITIONS

Zn 0.0 0.0 0.0

S 0.25 0.25 0.25



wurtzite

III,c1: The atoms in the two-molecule hexagonal unit of the zincite, ZnO, arrangement are in the positions:

R: 000. 1/3 2/3 1/2

X: 00u, 1/3 2/3 u+1/2

The axial ratio of crystals with this structure have always been close to c/a=1.63, and the parameter u to 0.375. Under this circumstances each atom has about it a tetrahedron of atoms of the opposite sort just

as in the cubic ZnS arrangement.

| Crystal | a_0 | c_0 | remarks |
|---------|---------|--------|-----------|
| ZnO | 3.24950 | 5.2069 | u = 0.345 |
| ZnS | 3.811 | 6.234 | |
| | | | |
| | | | |

```
ZnO: hexagonal \longrightarrow ibrav = 4
        a = 3.24950 \text{ A}, c = 5.2069 \text{ A} \longrightarrow c/a = 1.60236959
        u = 0.345
  &SYSTEM
    ntyp=2, nat=4, ibrav=4, a = 3.24950, c = 5.2069,
ATOMIC_SPECIES
Zn 1. Zn.UPF
0 1. 0.UPF
ATOMIC_POSITIONS crystal
Zn 0.0 0.0 0.0
```

Zn 0.33333333 0.6666666 0.5

0 0.66666666 0.33333333 0.845

0.00.00345

```
ZnO: hexagonal \longrightarrow ibrav = 4
        a = 3.24950 \text{ A}, c = 5.2069 \text{ A} \longrightarrow c/a = 1.60236959
        u = 0.345
  &SYSTEM
    ntyp=2, nat=4, ibrav=4, a = 3.24950, c = 5.2069,
ATOMIC_SPECIES
Zn 1. Zn.UPF
0 1. 0.UPF
ATOMIC_POSITIONS crystal
Zn 0.0 0.0 0.0
```

Zn 0.33333333 0.6666666 0.5

0 0.66666666 0.33333333 0.845

0.00.00345

```
ZnS: hexagonal \longrightarrow ibrav = 4
       a = 3.811 \text{ A}, c = 6.234 \text{ A} \longrightarrow c/a = 1.63579113
       u = 0.375
 &SYSTEM
    ntyp=2, nat=4, ibrav=4, a = 3.811, c = 6.234,
ATOMIC_SPECIES
Zn 1. Zn.UPF
S 1. S.UPF
ATOMIC_POSITIONS crystal
Zn 0.0 0.0 0.0
Zn 0.33333333 0.6666666 0.5
S 0.0 0.0 0.375
```

S 0.66666666 0.33333333 0.875

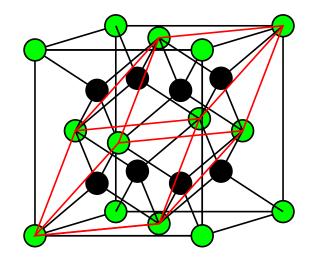
fluorite

IV,a1: Crystals RX₂ in which R is especially big are likely to have the flourite, CaF₂, arrangement. In this grouping each R atom is at the center of eight X atoms situated at the corners of a surrounding cube; and each X atom has about it a tetrahedron of R atoms. The symmstry is cubic with the atoms of its four molecules per unit in the following positions of O_b^5 (Fm3m):

R: (4a) 000; F.C.

X: $(8c) \pm (1/4 \ 1/4 \ 1/4)$; FC

| Crystal | a_0 A | | |
|---------|----------------|--|--|
| CaF_2 | 5.46295 (28 C) | | |
| CeO_2 | 5.4110 (26 C) | | |



```
CaF_2: simple cubic \longrightarrow ibrav = 1
         5.46295 \text{ A} \longrightarrow \text{celldm}(1)=10.32348344 \text{ bohr}
  &SYSTEM
    ntyp=2, nat=12, ibrav=1, celldm(1) = 10.32348344
ATOMIC_SPECIES
Ca 1. Ca.UPF
F 1. F.UPF
ATOMIC_POSITIONS
Ca 0.0 0.0 0.0
Ca 0.0 0.5 0.5
Ca 0.5 0.0 0.5
Ca 0.5 0.5 0.0
F 0.25 0.25 0.25
```

. . .

F -0.25 -0.25 -0.25

```
\begin{array}{ll} \text{CaF}_2\text{:} & \text{face centered cubic} \longrightarrow \text{ibrav} = 2 \\ & 5.46295 \text{ A} \longrightarrow \text{celldm}(1) = 10.32348344 \text{ bohr} \\ & \text{\&SYSTEM} \\ & \text{ntyp=2, nat=3, ibrav=1, celldm}(1) = 10.32348344 \\ & / \\ & \dots \\ & \text{ATOMIC\_SPECIES} \\ & \text{Ca 1. Ca.UPF} \end{array}
```

F 1. F.UPF

ATOMIC_POSITIONS

F 0.25 0.25 0.25

F -0.25 -0.25 -0.25

Ca 0.0 0.0 0.0

lanthanum sesquioxide

V,a1: A number of rate-earth oxides with large metal-to-oxygen separations form hexagonal crystals of which $lanthanum\ sesquioxide$, La₂O₃, is typical. Assumin that the atoms have the dimensions of their ions, these are compounds with r(R)/r(O) greater that 0.87. There is but one molecule in the unit which for La₂O₃ has the cell edges:

$$a_0 = 3.9373 \text{ A}, c_0 = 6.1299 \text{ A}$$

The space group is D_{3d}^3 ($C\bar{3}m$) and the atoms are in the positions:

La: (2d) \pm (1/3 2/3 u) with u =0.245 (from neutron diffraction)

O(1): (1a) 000 and O(2) (2d) with u = 0.645

In this arrangement each lanthanum has four oxygen neighbors at a distance of ca 2.30 A and three more at ca 2.70 A. The oxigen atoms have their usual ionic separation with the closest O-O = ca 2.75 A.

Crystal
$$a_0$$
, A c_0 , A Ce_2O_3 3.888 6.069

```
La_2O_3: hexagonal \longrightarrow ibrav = 4
       a = 3.9373 A, c = 6.1299 A
       u_{La} = 0.245, u_O = 0.645
 &SYSTEM
   ntyp=2, nat=5, ibrav=4, a = 3.9373, c = 6.1299
ATOMIC_SPECIES
La 1. La.UPF
0 1. 0 UPF
ATOMIC_POSITIONS crystal
La 0.33333333 0.6666666 0.245
La -0.33333333 -0.66666666 -0.245
0.0 0.0 0.0
0.33333333 0.6666666 0.645
```

corundum

V,a3: With smaller metallic atoms which make r(R)/r(O) less than 0.60, oxygen ions can approach nearer to a perfect close-packing than is the case with preceding two structures, and such oxides are often found with an arrangement typified by that of *chromium sequioxide*, Cr_2O_3 . Its symmetry is rhombohedral with a unit cell containing two molecules and having the dimensions:

$$a_0 = 5.350 \text{ A}, \ \alpha = 55^{\circ}9'$$

The space group is D_{3d}^6 $(R\bar{3}c)$ and atoms are in the special positions:

Cr: (4c)
$$\pm$$
 (*uuu*); BC. with $u = 0.3475$

O: (6e)
$$\pm (u,1/2-u,1/4; 1/2-u,1/4,u; 1/4,u,1/2-u)$$
 with $u=0.556$

The dimensions of the corresponding hexamolecular cell referred to hexagonal axes are

$$a'_0 = 4.954 \text{ A}, c'_0 = 13.584 \text{ A}.$$

In this cell the atoms have the positions:

Cr:
$$(12c) \pm (00u',0,0,u'+1/2)$$
; rh with $u'=0.3475$

O: (18e)
$$\pm$$
 (v 0 1/4; 0 v 1/4; \bar{v} \bar{v} 1/4); rh with v =0.306

[rh means repeat about $1/3 \ 2/3 \ 2/3 \ and \ 2/3 \ 1/3 \ 1/3$]

| Compound | u=u'(R) | u(O) | v(O) | | |
|-------------------------|---------|------------------------|-------------------------------------|------------------------------|-------------------------------|
| Al_2O_3 | 0.3520 | 0.556 | 0.306 | | |
| $lpha$ -Fe $_2$ O $_3$ | 0.355 | 0.550 | 0.300 | | |
| Ti_2O_3 | 0.3450 | 0.567 | 0.317 | | |
| V_2O_3 | 0.3463 | 0.565 | 0.315 | | |
| | | | | | |
| | | | | | |
| Crystal | | $a_0 \; A$ | α | $a'_0 A$ | c' ₀ A |
| Crystal Al_2O_3 (coru | ndum) | a ₀ A 5.128 | α55° 20' | a' ₀ A 4.76280 | c' ₀ A 13.00320 |
| | • | | | | |
| Al_2O_3 (coru | • | 5.128 | 55° 20' | 4.76280 | 13.00320 |

