1 Nomenclature

1.1 Indices and Sets

 $t \in \mathcal{T}$ Set of hourly time steps: $1, \ldots, T$, where T =number of time periods. Set of machines. $m \in \mathcal{M}$ $m \in \mathcal{P}^+$ Subset of machines producing electrical power. $m \in \mathcal{Q}^+$ Subset of machines producing thermal power. $m \in \mathcal{C}^+$ Subset of machines producing cooling power. $m \in \mathcal{F}$ Subset of machines consuming fuel. $m \in \mathcal{P}^-$ Subset of machines consuming electrical power. $m \in \mathcal{D}$ Subset of machines which can dissipate thermal power to ambient. $es \in \mathcal{E}S$ Set of energy storage technologies. $r \in \mathcal{R}$ Set of renewable technologies. Set of slots: $1, \ldots, N_s$, where $N_s = \text{number of slots}$. $s \in \mathcal{S}$ $v \in \mathcal{V}_m$ Set of vertexes of the performance maps for machine m. Piecewise production cost intervals for machine $m: 1, \ldots, W_m$, where $W_m = \text{number of}$ $w \in \mathcal{W}_m$ sampling sizes.

1.2 Continuous variables

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x_{m,s}^D
                 Size of machine m \in \mathcal{M} installed in slot s \in \mathcal{S} (kW), \in \mathbb{R}.
x_r^D
                  Size of the renewable technology r \in \mathcal{R} (m^2), \in \mathbb{R}.
                  Fuel consumed by machine m \in \mathcal{F} in slot s \in \mathcal{S} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
f_{m,s,t}
Jm,s,t
el_{m,s,t}^{cons}
el_{m,s,t}^{gen}
el_{m,s,t}^{gen}
q_{m,s,t}^{gen}
q_{m,s,t}^{gen}
q_{m,s,t}^{diss}
q_{m,s,t}^{diss}
                  Electric power consumed by machine m \in \mathcal{P}^- in slot s \in \mathcal{S} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
                  Electric power generated by machine m \in \mathcal{P}^+ in slot s \in \mathcal{S} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
                  Electric power generated by renewable technology r \in \mathcal{R} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
                  Thermal power generated by machine m \in \mathcal{Q}^+ in slot s \in \mathcal{S} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
                  Cooling power generated by machine m \in \mathcal{C}^+ in slot s \in \mathcal{S} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
                  Thermal power dissipated by machine m \in \mathcal{D} in slot s \in \mathcal{S} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
                  Useful thermal power generated by machine m \in \mathcal{Q}^+ in slot s \in \mathcal{S} at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
q_{m,s,t}^{us}
el_t^{grid}
                  Electric power exchanged with the grid at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
l_{es,t}^{stor}
                  Energy Level of the energy storage technology es \in \mathcal{E}S at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
l_{es,t}^{charge}
                 Energy input to the energy storage technology es \in \mathcal{E}S at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
l_{es,t}^{disch}
                 Energy output to the energy storage technology es \in \mathcal{E}S at time t \in \mathcal{T} (kWh), \in \mathbb{R}.
                  Convex hull operation control variable associated to vertex v \in \mathcal{V} of the performance map of
\beta_{m,s,t,v}
                 machine m \in \mathcal{M} in site s \in \mathcal{S} at time t \in \mathcal{T} (kW), \in \mathbb{R}.
Linearisation variable associated to the product x_{m,s}^D \cdot z_{m,s,t} of machine m \in \mathcal{M} in site s \in \mathcal{S}
\xi_{m,s,t}
                  at time t \in \mathcal{T} (kW), \in \mathbb{R}.
                 Convex hull operation control variable associated to the cost interval w \in \mathcal{W} of machine
\gamma_{m,s,w}
                  m \in \mathcal{M} in site s \in \mathcal{S} at time t \in \mathcal{T} (-), \in [0, 1].
C_{m,s}^{inv}
                 Investment cost associated to machine m \in \mathcal{M} in site s \in \mathcal{S} (\in), \in \mathbb{R}.
El_{t}^{grid}
                 Revenue from electricity sold to grid at time t \in \mathcal{T} (\in), \in \mathbb{R}.
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1.3 Binary variables

$z_{m,s}^D$	Yes/no installation of machine $m \in \mathcal{M}$ in slot $s \in \mathcal{S}, \in \{0, 1\}$.
$z_{m,s,t}$	On/off status of machine $m \in \mathcal{M}$ in slot $s \in \mathcal{S}$ at time $t \in \mathcal{T}, \in \{0, 1\}$.
$\Delta_{m,s,t}^{on}$	Start-up status of machine $m \in \mathcal{M}$ in slot $s \in \mathcal{S}$ at time $t \in \mathcal{T}$, $\in \{0, 1\}$.
$\Delta_{m,s,t}^{off}$	Shut-down status of machine $m \in \mathcal{M}$ in slot $s \in \mathcal{S}$ at time $t \in \mathcal{T}, \in \{0, 1\}$.

Binary variable to keep into account whether electricity is sold to the grid at time $t \in \mathcal{T}$, s_t

Binary variable to activate the interval $w \in \mathcal{W}$ of the investment cost of machine $m \in \mathcal{M}$ in $b_{m,s,w}$ slot $s \in \mathcal{S}, \in \{0, 1\}.$

$\mathbf{2}$ Model Description

Objective Function 2.1

The objective of the UC problem is to minimize the Total Annual Cost $(TAC = Capex \cdot ccr + Opex)$. The unit commitment problem can then be formulated as:

$$\min \left(\Phi^{TAC} = \Phi^{Capex} \cdot ccr + \Phi^{Opex} \right) \tag{1}$$

where:

$$\Phi^{Capex} = \sum_{s \in \mathcal{S}} \sum_{m \in \mathcal{M}} C_{m,s}^{inv} + \sum_{r \in \mathcal{R}} x_r^D \cdot \hat{c}_r^{inv}$$
(2)

$$\Phi^{Opex} = \sum_{t \in \mathcal{T}} \left(\sum_{m \in \mathcal{F}} \sum_{s \in \mathcal{S}} f_{m,s,t} \cdot \hat{c}_m^{fuel} + \sum_{m \in \mathcal{M}} \sum_{s \in \mathcal{S}} z_{m,s,t} \cdot \hat{c}_m^{O\&M} + \sum_{r \in \mathcal{R}} x_r^D \cdot \hat{c}_r^{O\&M} \right)$$

$$+ \sum_{m \in \mathcal{F}} \sum_{s \in \mathcal{S}} \Delta_{m,s,t}^{on} \cdot \hat{c}_m^{fuel} \cdot SU_m^{cost} + \sum_{m \in \mathcal{P}^-} \sum_{s \in \mathcal{S}} \Delta_{m,s,t}^{on} \cdot \hat{c}_m^{el} \cdot SU_m^{cost} \right)$$

$$(3)$$

2.2**Investment Constraints**

The maximum number of machines that can be installed in a single slot is equal to one, as expressed by (4). If a machine is not installed, it should be always off (5) and finally the constraint (6) imposes a rule on the slots filling order to avoid any symmetry in the MILP formulation.

$$\sum_{m \in \mathcal{M}} z_{m,s}^D \le 1 \tag{4}$$

$$z_{m,s,t} \le z_{m,s}^D$$
 $\forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T}$ (5)

$$z_{m,s+1}^D \le z_{m,s}^D$$
 $\forall s \ge m \quad m \in \mathcal{M} \quad \forall s \in \mathcal{S}$ (6)

The following constraints ensures that the size $x_{m,s,t}^D$ of machine m installed in site s is bounded between the minimum and the maximum available sizes $(\hat{X}_m^{D,max} \text{ and } \hat{X}_m^{D,min})$. The same holds for the total installed area x_r^D of renewable technology r which is limited by the total area available (\hat{A}_r^{max}) .

$$x_{m,s}^{D} \leq z_{m,s}^{D} \cdot \hat{X}_{m}^{D,max} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \qquad (7)$$

$$x_{m,s}^{D} \geq z_{m,s}^{D} \cdot \hat{X}_{m}^{D,min} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \qquad (8)$$

$$z_{m,s}^D \ge z_{m,s}^D \cdot \hat{X}_m^{D,min}$$
 $\forall m \in \mathcal{M} \quad \forall s \in \mathcal{S}$ (8)

$$x_r^D \le \hat{A}_r^{max} \tag{9}$$

In order to include the size effect on the investment costs, a piece-wise approximation of the exponential economy of scale law has been adopted in the MILP formulation. The investment cost function $C_{m,s}^{inv}$ for machine m installed in site s is approximated by the convex combination of the cost function evaluated at the extremes of the piece-wise interval corresponding to the machine size $(C_m^{inv}(X_{m,k}^D))$ and $C_m^{inv}(X_{m,k+1}^D)$. The linearisation bin is activated by the binary variable $b_{m,s,w}$ while the variable $\gamma_{m,s,w} \in [0,1]$ is used to express the convex combination relationship in (14) and (15). At borders of the interpolations intervals $b_{m,s,w}$ takes the value of zero. Constraint (12) imposes that the only $\gamma_{m,s,w}$ values different from zero can be $\gamma_{m,s,k}$ and $\gamma_{m,s,k+1}$. As usual, constraints (11) and (13) are necessary to activate these constrains only if the machines m is installed in site s.

$$b_{m,s,0} = b_{m,s,W_m} = 0 \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad (10)$$

$$\sum_{k \in \mathcal{W}_m} b_{m,s,k} = z_{m,s}^D \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad (11)$$

$$\gamma_{m,s,w} \leq b_{m,s,w-1} + b_{m,s,w} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall w \in \mathcal{W}_m \quad (12)$$

$$\sum_{k \in \mathcal{W}_m} \gamma_{m,s,k} = z_{m,s}^D \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad (13)$$

$$x_{m,s}^D = \sum_{k \in \mathcal{W}_m} \gamma_{m,s,k} \cdot \hat{X}_{m,k}^D \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad (14)$$

$$C_{m,s}^{inv} = \sum_{k \in \mathcal{W}_m} \gamma_{m,s,k} \cdot C_m^{inv}(\hat{X}_{m,k}^D) \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad (15)$$

2.3 Operation Constraints

The electric, heating and cooling energy balances are reported above. Note that the useful heat is defined (18) as the heat which is generated but not dissipated by machine m in site s.

$$el_{m}^{grid} = \sum_{m \in \mathcal{P}^{+}} \sum_{s \in \mathcal{S}} + el_{m,s,t}^{gen} + \sum_{r \in \mathcal{R}} el_{r,t}^{gen} - \sum_{m \in \mathcal{P}^{-}} \sum_{s \in \mathcal{S}} el_{m,s,t}^{cons} - \hat{E}l_{t}^{demand} \qquad \forall t \in \mathcal{T} \qquad (16)$$

$$\sum_{m \in \mathcal{Q}^{+}} \sum_{s \in \mathcal{S}} q_{m,s,t}^{us} + \sum_{es \in \mathcal{E}S} l_{es,t}^{disch} = \sum_{es \in \mathcal{E}S} l_{es,t}^{charge} + \hat{H}_{t}^{demand} \qquad \forall t \in \mathcal{T} \qquad (17)$$

$$q_{m,s,t}^{us} = q_{m,s,t}^{gen} - q_{m,s,t}^{diss} \qquad \forall m \in \mathcal{D} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \qquad (18)$$

$$\sum_{m \in \mathcal{C}^{+}} \sum_{s \in \mathcal{S}} c_{m,s,t}^{gen} = \hat{C}_{t}^{demand} \qquad \forall t \in \mathcal{T} \qquad (19)$$

Even in this case to simulate the part load performance a convex combination is used. In particular the operating point of the machine m in site s at time t is computed as the convex combination of the vertexes of its feasible operational region. Two variable are used to perform the convex combination: $\beta_{m,s,t,v}$ and $\xi_{m,s,t}$ corresponding to $x_{m,s}^D$ when the machine is on. The set of constraints is the follow:

$$\xi_{m,s,t} = \sum_{v \in \mathcal{V}_m} \beta_{m,s,t,v} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (20)$$

$$\xi_{m,s,t} \leq z_{m,s,t} \cdot \hat{X}_m^{D,max} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (21)$$

$$\xi_{m,s,t} \leq x_{m,s}^{D} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (22)$$

$$\xi_{m,s,t} \geq x_{m,s}^{D} - (1 - z_{m,s,t}) \cdot \hat{X}_m^{D,max} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (23)$$

Thanks to the above described formulation, all the variable related to machines inputs and outputs can be defined:

$$f_{m,s,t} = \sum_{v \in \mathcal{V}_m} \beta_{m,s,t,v} \cdot \hat{K}_{m,v}^{IN} \qquad \forall m \in \mathcal{F} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (24)$$

$$el_{m,s,t}^{cons} = \sum_{v \in \mathcal{V}_m} \beta_{m,s,t,v} \cdot \hat{K}_{m,v}^{IN} \qquad \forall m \in \mathcal{P}^- \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (25)$$

$$el_{m,s,t}^{gen} = \sum_{v \in \mathcal{V}_m} \beta_{m,s,t,v} \cdot \left(\hat{K}_{m,v}^{IN} \cdot \hat{K}_m^{IP} + \hat{K}_m^{2P} \right) + \hat{K}_m^{3P} \cdot z_{m,s,t} \qquad \forall m \in \mathcal{P}^+ \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (26)$$

$$q_{m,s,t}^{gen} = \sum_{v \in \mathcal{V}_m} \beta_{m,s,t,v} \cdot \left(\hat{K}_{m,v}^{IN} \cdot \hat{K}_m^{1Q} + \hat{K}_m^{2Q} \right) + \hat{K}_m^{3Q} \cdot z_{m,s,t} \qquad \forall m \in \mathcal{Q}^+ \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (27)$$

$$c_{m,s,t}^{gen} = \sum_{v \in \mathcal{V}_m} \beta_{m,s,t,v} \cdot \left(\hat{K}_{m,v}^{IN} \cdot \hat{K}_m^{1C} + \hat{K}_m^{2C} \right) + \hat{K}_m^{3C} \cdot z_{m,s,t} \qquad \forall m \in \mathcal{C}^+ \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \quad (28)$$

The technical limit regarding the single machine operation has now to be introduced. Fist the max/min energy input depends on the machine size $(\hat{K}_{m,min}^{IN})$ and $\hat{K}_{m,max}^{IN}$:

$$f_{m,s,t} \geq \xi_{m,s,t} \cdot \hat{K}_{m,min}^{IN} \qquad \forall m \in \mathcal{F} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \qquad (29)$$

$$f_{m,s,t} \leq \xi_{m,s,t} \cdot \hat{K}_{m,max}^{IN} \qquad \forall m \in \mathcal{F} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \qquad (30)$$

$$el_{m,s,t}^{cons} \geq \xi_{m,s,t} \cdot \hat{K}_{m,min}^{IN} \qquad \forall m \in \mathcal{F} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \qquad (31)$$

$$el_{m,s,t}^{cons} \leq \xi_{m,s,t} \cdot \hat{K}_{m,max}^{IN} \qquad \forall m \in \mathcal{F} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \qquad (32)$$

Secondly, the constrain on the maximum rump up and rump down limit should be respected, expressed as variation of the energy in input.

$$f_{m,s,t} - f_{m,s,t-1} \leq \hat{f}_{m}^{RU,lim} \qquad \forall m \in \mathcal{F} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T}$$

$$f_{m,s,t-1} - f_{m,s,t} \leq \hat{f}_{m}^{RD,lim} \qquad \forall m \in \mathcal{F} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T}$$

$$el_{m,s,t}^{cons} - el_{m,s,t-1}^{cons} \leq \hat{el}_{m}^{RU,lim} \qquad \forall m \in \mathcal{P}^{-} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T}$$

$$(34)$$

$$\forall m \in \mathcal{P}^{-} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T}$$

$$(35)$$

$$el_{m,s,t-1}^{cons} - el_{m,s,t-1}^{cons} \leq \hat{el}_{m}^{RD,lim} \qquad \forall m \in \mathcal{P}^{-} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T}$$

$$(36)$$

A set of three constraints is used to establish if machine m in slot s has been switched on or off at time t.

$$\Delta_{m,s,t}^{on} \geq (z_{m,s,t} - z_{m,s,t-1}) \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T} \qquad (37)$$

$$\Delta_{m,s,t}^{on} \leq (1 - z_{m,s,t-1}) \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T} \qquad (38)$$

$$\Delta_{m,s,t}^{on} \leq z_{m,s,t} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \qquad (39)$$

$$\Delta_{m,s,t}^{off} \geq (z_{m,s,t-1} - z_{m,s,t}) \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T} \qquad (40)$$

$$\Delta_{m,s,t}^{off} \leq (1 - z_{m,s,t}) \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \in \mathcal{T} \qquad (41)$$

$$\Delta_{m,s,t}^{off} \leq z_{m,s,t-1} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \setminus \{1\} \in \mathcal{T} \qquad (42)$$

These variable are important in order to account for the cost of an extra energy in input when the machines is turned on but mostly to write down constraints (43) and (44) regarding the minimum up and down time respectively.

$$\sum_{i=t-\hat{t}_{min,UT}}^{t} z_{m,s,i} \ge \hat{t}_{min,UT} \cdot \Delta_{m,s,t}^{off} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \ge \hat{t}_{min,UT} \in \mathcal{T}$$

$$\sum_{i=t-\hat{t}_{min,UT}}^{t} z_{m,s,i} \ge \hat{t}_{min,DT} \cdot \Delta_{m,s,t}^{on} \qquad \forall m \in \mathcal{M} \quad \forall s \in \mathcal{S} \quad \forall t \ge \hat{t}_{min,DT} \in \mathcal{T}$$

$$(43)$$

Equation (45) express the storage management constraint which defines, at each time-step, the quantity of energy entering $(l_{es,t}^{charge})$ and exiting $(l_{es,t}^{disch})$ the energy storage system. The level of the energy store in

the storage system should not overcame the maximum storage level (C_{es}^{max}) for each es and also the power input and output should fall into a defined range (46), as stated by equations (47) and (48). Finally the level of the storage is conserved by fixing the storage level at time T to be equal to the storage level at the beginning of the period (\hat{l}_{init}^{stor}) .

$$\sum_{es \in \mathcal{E}S} l_{es,t}^{stor} - \sum_{es \in \mathcal{E}S} l_{es,t-1}^{stor} = \sum_{es \in \mathcal{E}S} l_{es,t}^{charge} - \sum_{es \in \mathcal{E}S} l_{es,t}^{disch} \qquad \forall t \in \mathcal{T} \qquad (45)$$

$$l_{es,t}^{stor} \leq \hat{C}_{es}^{max} \qquad \forall es \in \mathcal{E}S \quad \forall t \in \mathcal{T} \qquad (46)$$

$$(l_{es,t}^{stor} - l_{es,t-1}^{stor}) \leq \hat{P}_{es}^{max,charge} \cdot \Delta t \qquad \forall es \in \mathcal{E}S \quad \forall t \setminus \{1\} \in \mathcal{T} \qquad (47)$$

$$(l_{es,t-1}^{stor} - l_{es,t}^{stor}) \leq \hat{P}_{es}^{max,disch} \cdot \Delta t \qquad \forall es \in \mathcal{E}S \quad \forall t \setminus \{1\} \in \mathcal{T} \qquad (48)$$

$$l_{es,0}^{stor} = \hat{l}_{init}^{stor} \qquad \forall es \in \mathcal{E}S \qquad (49)$$

$$l_{es,0}^{stor} = l_{es,T}^{stor} \qquad \forall es \in \mathcal{E}S \qquad (50)$$

Since electric energy can be either sold or both from the grid at two different price, the binary variable s_t is used as a flag to denote if electricity is flowing into the grid or it's withdraw from the grid. The variable El_t^{grid} takes into account the cost of energy sold/purchased in the objective function and it's assume positive values when the electricity is sold and negative values when bought from the grid. In modeling following set of constrain a standard "big M" formulation was adopted.

$$el_t^{grid} \ge (s_t - 1) \cdot M_{4,t}$$
 $\forall t \in \mathcal{T}$ (51)

$$el_t^{grid} \le s_t \cdot M_{3,t}$$
 $\forall t \in \mathcal{T}$ (52)

$$El_t^{grid} \le el_t^{grid} \cdot \hat{c}_t^{el,sold} + (1 - s_t) \cdot M_{1,t}$$
 $\forall t \in \mathcal{T}$ (53)

$$El_t^{grid} \le el_t^{grid} \cdot \hat{c}_t^{el,purch} + s_t \cdot M_{2,t}$$
 $\forall t \in \mathcal{T}$ (54)

where:

$$M_{1,t} = M_{4,t} \cdot \hat{c}_t^{el,purch}$$
 $\forall t \in \mathcal{T} \quad (55)$

$$M_{2,t} = M_{3,t} \cdot \hat{c}_t^{el,sold}$$
 $\forall t \in \mathcal{T}$ (56)

$$M_{3,t} = \left(\sum_{m \in \mathcal{P}^+} \sum_{s \in S} \hat{el}_{m,s,t}^{max,gen}\right) \cdot 1.5$$
 $\forall t \in \mathcal{T}$ (57)

$$M_{4,t} = \left(\hat{E}l_t^{demand} + \sum_{m \in \mathcal{P}^-} \sum_{s \in \mathcal{S}} \hat{e}l_{m,s,t}^{max,cons}\right) \cdot 1.5$$
 $\forall t \in \mathcal{T}$ (58)

The parameters $\hat{el}_{m,s,t}^{max,gen}$ and $\hat{el}_{m,s,t}^{max,cons}$ represent the maximum energy that can be respectively generated or consumed by machine m in slot s at time t.