

6)  $x(t) = t^{-\frac{1}{3}}, y(t) = t, r = 1, L^2(0; 1).$

$$\rho(x(t), y(t)) = \max_{0 < t < 1} \left| \int_0^1 \left( t^{-\frac{2}{3}} - t^2 \right) dt \right| = \max_{0 < t < 1} \left| 3t^{\frac{1}{3}} - \frac{t^3}{3} \right| =$$

$$= \lim_{t \rightarrow 1} \left( 3t^{\frac{1}{3}} - \frac{t^3}{3} \right) = 3 - \frac{1}{3} = 2\frac{2}{3} > 1(r) \Rightarrow \text{не принадлежит к шару с } r=1.$$

$$\rho(x(t), y(t)) = \max_{0 < t < 1} \sqrt{\int_0^1 \left( t^{-\frac{1}{3}} - t \right)^2 dt} = \max_{0 < t < 1} \sqrt{\int_0^1 \left( t^{-\frac{2}{3}} - 2t t^{-\frac{1}{3}} + t^2 \right) dt} =$$

$$= \max_{0 < t < 1} \sqrt{3t^{\frac{1}{3}} - \frac{6}{5} t t^{\frac{2}{3}} + \frac{t^3}{3}} \Big|_0^1 = \sqrt{3 - \frac{6}{5} + \frac{1}{3}} = \sqrt{\frac{4}{15} + \frac{1}{3}} =$$

$$= \sqrt{1\frac{17}{15}} > 1(r) \Rightarrow \text{не принадлежит к шару с } r=1.$$