Signals and systems Homework #3 Part 1/2



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Spring 97-98
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Deadline: 4th Ordibehesht, 1398 [23:55]

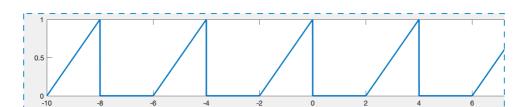
- Homeworks will not be accepted after the deadline.
- For theoretical problems, gather them in a single *.pdf file.
- For the matlab problems, provide both these materials:
 - codes [*.m files]
 - a simple **report** that includes all plots and screenshots.
- Notice that the homeworks will be checked by plagiarism detectors, avoid any similarities.
- Matlab problems and theoretical problems will be graded seperately (both will be graded out of 100), but their weights may be different and is determined by the course professor.

Question 1 (10 points)

determine the fourier series coefficients for the following periodic signals :

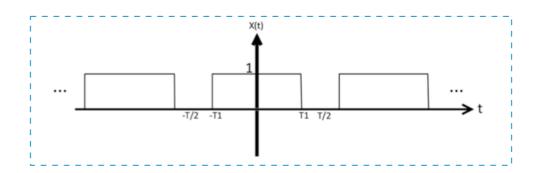
[a]
$$x(t) = 2\cos\left(\frac{2\pi t}{3} + \frac{\pi}{6}\right)$$

[b]



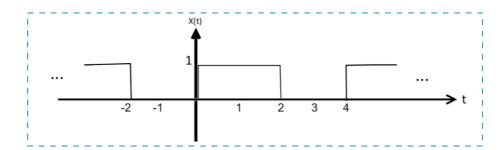
Question 2 (20 points)

[a] determine the Fourier series coefficients of the following signals

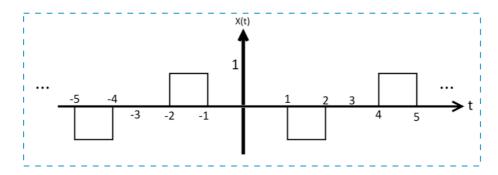


using the results of part a and fourier series charasteristics, determine the fourier series of the following signals :

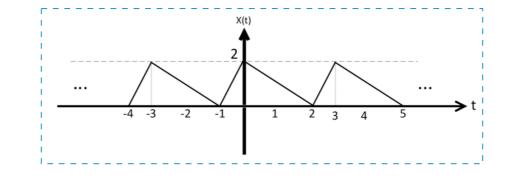
[b]



[c]



[d]

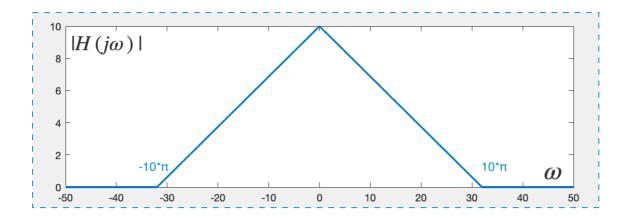


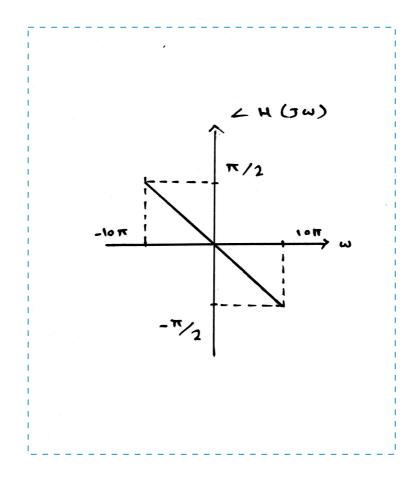
Question 3 (10 points)

Imagine x(t) is a periodic signal with fundamental period of $T_0 = \frac{1}{2}$ and Fourier series coefficients of $a_0 = 1$, $a_1 = a_{-1} = \frac{1}{2}$, $a_2 = a_{-2} = \frac{1}{4}$ and $a_k = 0$ for $\begin{vmatrix} k \\ k \end{vmatrix} > 2$.

We apply this signal to a system with following frequency response $H(j\omega)$

Determine the output.





Question 4 (10 points)

Imagine the Fourier series of signal x(t) is
$$x\left(t\right) = \sum_{k=-\infty}^{+\infty} \frac{1}{2^{\left|k\right|}} e^{j2k\pi t}$$

Determine the power of output signal if we apply $\mathbf{x}(t)$ to a system with the following frequency response

