

# The Dynamic Consequences of Technology and Discount Factor Shocks in Medium-Scale RANK vs TANK Models

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# Roadmap

1. Introduction and Related Literature
2. The Models
3. The Shocks
4. Results
5. Conclusion

# Introduction

[▶ Go to related literature](#)

- aim: contrast a representative-agent to a two-agent framework  
⇒ RANK vs TANK
- two household types in TANK: standard agents and **hand-to-mouth** agents
- analyse how dynamics after aggregate shocks are altered
- two shocks: to technology and to the **discount factor**

# Key Results

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2. underlying heterogeneity of **individual-level** responses is interesting feature of TANK
3. two parameters are key in shaping the quantitative differences between RANK and TANK

# The Models

- building on Gust et al. (2012) and Boehl (2022) with price indexation
- crucial difference RANK vs TANK: household sector

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- building on Gust et al. (2012) and Boehl (2022) with price indexation
- crucial difference RANK vs TANK: household sector
- RANK: representative, consumption-smoothing agent with access to investment, bonds, profits, etc. resulting in standard labour supply and Euler equation:

$$w_t = \chi n_t^\eta (c_t - hc_{t-1}) \quad (2.1)$$

$$1 = \beta_{t+1} \frac{R_t}{\pi_{t+1}} \frac{(c_t - hc_{t-1})}{(c_{t+1} - hc_t)} \quad (2.2)$$

plus standard budget constraint

[▶ Go to budget constraint](#)



# The TANK Model (I)

- unit-mass population, of which a share  $(1 - \lambda)$  are standard, consumption-smoothing households
- these **unconstrained** agents behave just as RANK agents  
⇒ identical equations (2.1), (2.2), budget constraint

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- unit-mass population, of which a share  $(1 - \lambda)$  are standard, consumption-smoothing households
- these **unconstrained** agents behave just as RANK agents  
⇒ identical equations (2.1), (2.2), budget constraint
- a share  $\lambda$  is **hand-to-mouth** and consume only current-period labour income with no access to consumption-smoothing tools

## The TANK Model (II)

- hand-to-mouth households are characterised by labour supply and budget constraint:

$$w_t = \chi(n_t^H)^\eta (c_t^H - hc_{t-1}^H) \quad (2.3)$$

$$c_t^H = w_t n_t^H \quad (2.4)$$

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- hand-to-mouth cannot save or dissave in the face of shocks
- consumption of hand-to-mouth tied exclusively to labour market  
 $\Rightarrow$  labour market of great importance for TANK dynamics

# The TANK Model (III)

- final step for TANK model is economy-wide aggregation:

$$c_t = (1 - \lambda)c_t^U + \lambda c_t^H \quad (2.5)$$

$$n_t = (1 - \lambda)n_t^U + \lambda n_t^H, \quad (2.6)$$

where:

$c_t, n_t$ : aggregate consumption and employment

$c_t^U, n_t^U$ : unconstrained agents' consumption and employment

$c_t^H, n_t^H$ : hand-to-mouth agents' consumption and employment

# The Discount Factor Shock

- the discount factor evolves according to:

$$\beta_t = \beta_{ss} \left( \frac{\beta_{t-1}}{\beta_{ss}} \right)^{\rho_\beta} \exp(\varepsilon_{\beta,t}) \quad (3.1)$$

where  $\varepsilon_{\beta,t} = 0.02$  in  $t = 1$ ,  $\beta_{ss} = 0.98$ ,  $\rho_\beta = 0.8$

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- what can one expect to happen?
  - contraction in today's consumption, output, wages, inflation, interest rates (both models)
  - in TANK, unconstrained agents should act analogously to RANK-agents; hand-to-mouth will most likely be hit somewhat stronger as they cannot smooth consumption

# Results

- calibration: mostly used the given values, but following Kaplan et al. (2018) and Debortoli and Galí (2018):  $\lambda = 0.3$  and  $\eta = 1$

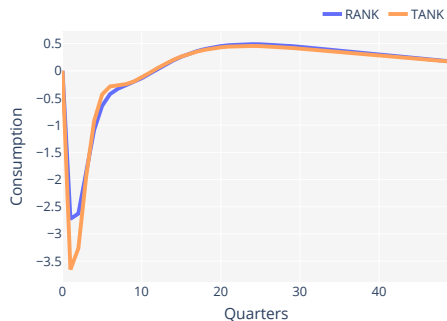


# Results

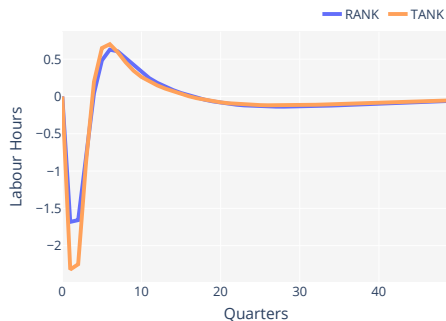
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- roadmap for the results:
  1. responses to a discount factor shock
    - ▶ Go to technology shock
  2. influence of  $\lambda$  and  $\eta$  on quantitative differences

## Figure: Aggregate Responses to a Discount Factor Shock

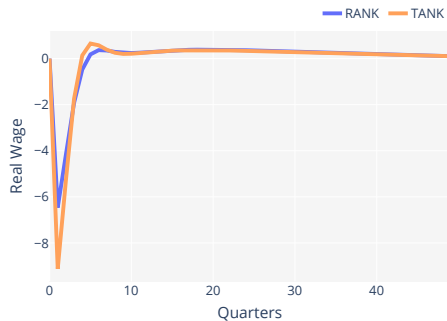
(a) Consumption



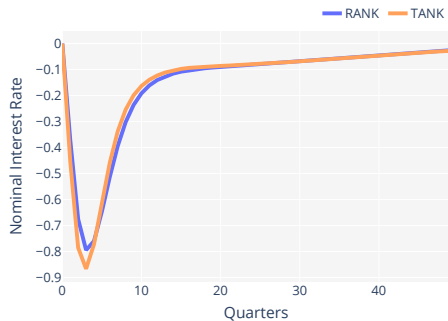
(b) Labour Hours



(c) Wage

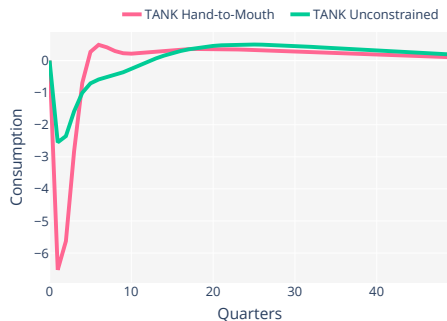


(d) Nominal Interest Rate

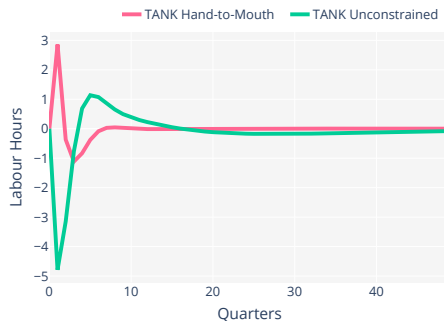


## Figure: Individual-Level Responses to a Discount Factor Shock (TANK)

(a) Consumption



(b) Labour Hours

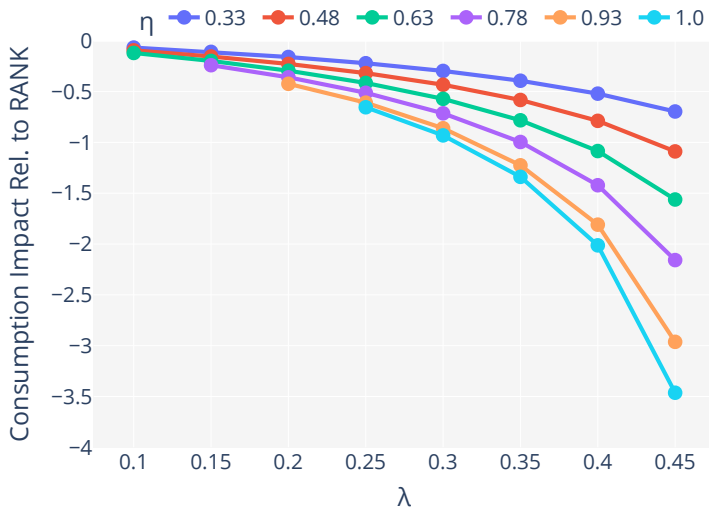


# Sensitivity Analysis (I)

- check how the quantitative **relative differences** between RANK and TANK depend on choices of  $\lambda$  and  $\eta$
- focus on aggregate consumption effects **on impact** after discount factor shock

► Go to technology shock

**Figure:** Aggregate Consumption Response on Impact to a Discount Factor Shock as a Function of  $\lambda$  and  $\eta$



## Sensitivity Analysis (II)

- higher  $\lambda \Rightarrow$  stronger impact in TANK relative to RANK for given  $\eta$
- higher  $\eta \Rightarrow$  stronger impact in TANK relative to RANK for given  $\lambda$

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- higher  $\lambda \Rightarrow$  stronger impact in TANK relative to RANK for given  $\eta$
- higher  $\eta \Rightarrow$  stronger impact in TANK relative to RANK for given  $\lambda$
- **interaction** of high  $\eta$  and  $\lambda$  leads to most pronounced difference
- intuition: together, high  $\lambda$  and high  $\eta$ , imply:
  - labour market developments matter substantially (many hand-to-mouth)
  - **and** wage changes do not translate as much into changes in hours worked (low elasticity of labour to wages)



# Conclusion

- key findings of simple RANK vs TANK comparison:
  1. responses usually coincide qualitatively
  2. for baseline calibration, quantitative differences not too large
  3. magnitude of differences depends on  $\lambda$  and  $\eta$

# Conclusion

- key findings of simple RANK vs TANK comparison:
  1. responses usually coincide qualitatively
  2. for baseline calibration, quantitative differences not too large
  3. magnitude of differences depends on  $\lambda$  and  $\eta$
- myriad of possible extensions:
  - include HANK and compare it to RANK & TANK
  - consider fiscal policy and redistribution
  - estimation of key parameters, especially  $\lambda$  and  $\eta$

**Thank you very much for your attention!**

Any questions?

# References

- Boehl, G. (2022). *Econpizza: Solving Nonlinear Heterogeneous Agents Models Using Machine Learning Techniques*.  
<https://econpizza.readthedocs.io/en/latest/index.html>
- Debortoli, D., & Galí, J. (2018). Monetary Policy with Heterogeneous Agents: Insights from TANK Models.  
<https://repositori.upf.edu/handle/10230/44714>
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- Kaplan, G., Moll, B., & Violante, G. L. (2018). Monetary Policy According to HANK. *American Economic Review*, 108(3), 697–743.

# Appendix A: Related Literature [▶ Back](#)

- one of the first papers to do TANK similar to the present model is by Galí et al. ([2007](#))
- seminal paper by Kaplan et al. ([2018](#)) on monetary policy transmission in fully-fledged HANK models: direct vs indirect effects of a real interest rate shock
- Debortoli and Galí ([2018](#)): prototypical HANK model features three key aspects of heterogeneity; the most important one is the gap in consumption between unconstrained and constrained agents; TANK can replicate this and its aggregate responses are thus close to HANK

## Appendix B: Household Budget Constraint [▶ Back](#)

- this is the budget constraint of RANK households as well as of unconstrained TANK agents:<sup>1</sup>

$$\begin{aligned} dd_t + c_t + \tau_t + \frac{\Phi}{2} \left( \frac{i_t}{i_{t-1}} - 1 \right)^2 i_t &= w_t n_t + \frac{R_{t-1}}{\pi_t} dd_{t-1} + \dots \quad (6.1) \\ \dots \left( 1 - mc_t - \frac{\psi}{2} \left( \frac{\pi_t}{\tilde{\pi}_{t-1}} - 1 \right)^2 \right) y_t &+ \dots \\ \dots \left( q_t \left( 1 - \frac{\Phi}{2} \left( \frac{i_t}{i_{t-1}} - 1 \right)^2 - 1 \right) i_t + bprof_t \right) \end{aligned}$$

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<sup>1</sup>In the latter case,  $c_t^U$  and  $n_t^U$  replace  $c_t$  and  $n_t$ , respectively.

## Appendix C: The Technology Shock [▶ Back](#)

- technology adheres to:

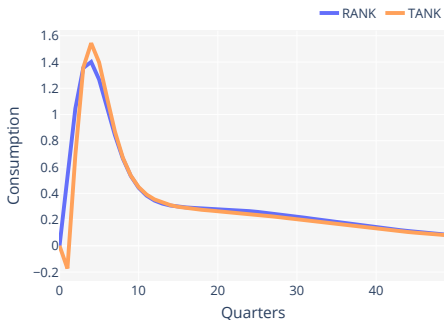
$$z_t = z_{ss} \left( \frac{z_{t-1}}{z_{ss}} \right)^{\rho_z} \exp(\varepsilon_{z,t}) \quad (6.2)$$

where  $\varepsilon_{z,t} = 0.02$  in  $t = 1$ ,  $z_{ss} = 1$ ,  $\rho_z = 0.8$

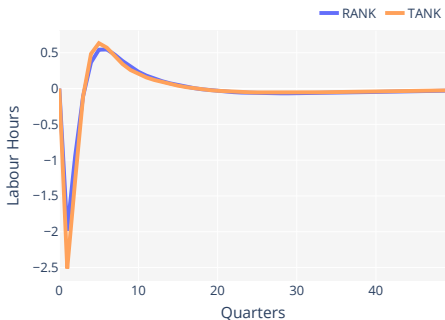
- what can one expect to happen?
  - most likely expansion in production, output, consumption as well as drop in labour hours (well-documented fact in NK literature) and inflation (as output does not rise sufficiently due to price adjustment costs), leading to decrease in nominal interest rate
  - in TANK certainly heterogeneous effects as unconstrained households receive higher firm profits and hand-to-mouth suffer from decrease in wages

## Figure: Aggregate Responses to a Technology Shock

(a) Consumption

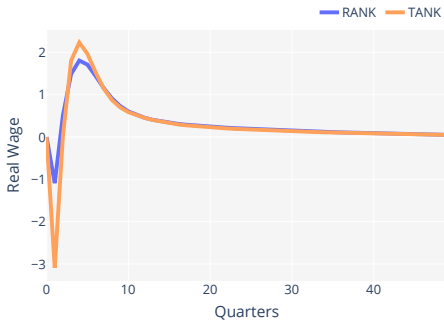


(b) Labour Hours





(c) Wage



(d) Nominal Interest Rate

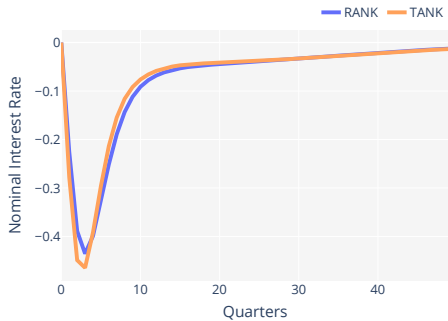
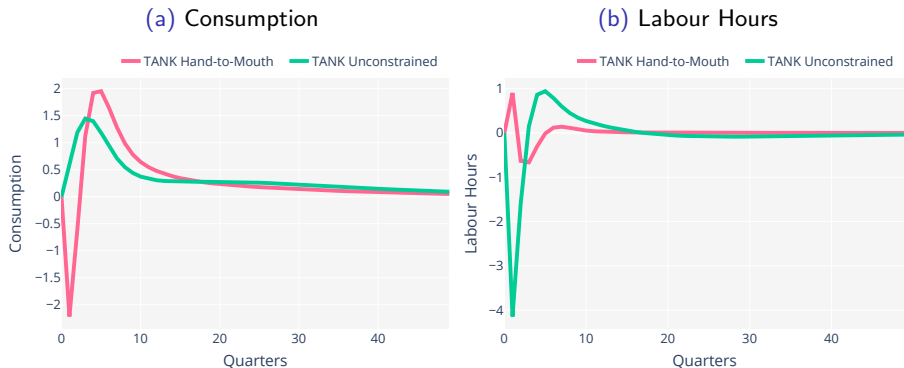


Figure: Individual-Level Responses to a Technology Shock (TANK)



**Figure:** Aggregate Consumption Response on Impact to a Technology Shock as a Function of  $\lambda$  and  $\eta$

