

PplOps (ppl.Ppl.Dist.PplOps)

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Module Dist.PplOps

Operators for distributions

```
type 'a dist
```

```
val (+~) : int dist -> int dist -> int dist  
val (-~) : int dist -> int dist -> int dist  
val (*~) : int dist -> int dist -> int dist  
val (/~) : int dist -> int dist -> int dist  
val (+.~) : float dist -> float dist -> float dist  
val (-.~) : float dist -> float dist -> float dist  
val (*.~) : float dist -> float dist -> float dist  
val (/~) : float dist -> float dist -> float dist  
val (&~) : bool dist -> bool dist -> bool dist  
val (|~) : bool dist -> bool dist -> bool dist  
val not : bool dist -> bool dist  
val (^~) : string dist -> string dist -> string dist
```

Up â ppl » Ppl » Dist

Module Ppl.Dist

Module used for defining probabilistic models

Contains a type dist which is used to represent probabilistic models.

- Condition Operators
- Monad Ffunctions
- Sampling
- Prior Distribution

exception Undefined

type prob = float
A type for which values need to sum to 1

type likelihood = float
A type for which values don't need to sum to 1

type 'a samples = ('a * prob) list
A set of weighted samples, summing to one

type _ dist =

| Return : 'a -> 'a dist

distribution with a single value

| Bind : 'a dist * ('a -> 'b dist) -> 'b dist

monadic bind

| Primitive : 'a Primitive.t -> 'a dist

primitive exact distribution

| Conditional : ('a -> float) * 'a dist -> 'a dist

variant that defines likelihood model

Type for representing distributions

Condition Operators

```
val condition' : ('a -> likelihood) -> 'a dist -> 'a dist
val condition : bool -> 'a dist -> 'a dist
val score : likelihood -> 'a dist -> 'a dist
val observe : 'a -> 'a Primitive.t -> 'b dist -> 'b dist
```

Monad Ffunctions

include Ppl.Monad.Monad with type 'a t := 'a dist

type 'a t

```
val return : 'a -> 'a t
val bind : 'a t -> ('a -> 'b t) -> 'b t
val (>>=) : 'a t -> ('a -> 'b t) -> 'b t
```

PplOps (ppl.Ppl.Dist.PplOps)

```
val let* : 'a t -> ('a -> 'b t) -> 'b t
val fmap : ('a -> 'b) -> 'a t -> 'b t
val liftM : ('a -> 'b) -> 'a t -> 'b t
val liftM2 : ('a -> 'b -> 'c) -> 'a t -> 'b t -> 'c t
val mapM : ('a -> 'b t) -> 'a list -> 'b list t
val sequence : 'a t list -> 'a list t
```

Primitives

These functions create dist values which correspond to primitive distributions so that they can be used in models. Ok

```
type 'a primitive
```

```
val binomial : int -> float -> int primitive
```

Create a binomial distribution, the output is the number of successes from n independent trials with probability of success p

```
val normal : float -> float -> float primitive
```

```
val categorical : ('a * float) list -> 'a primitive
```

```
val discrete_uniform : 'a list -> 'a primitive
```

```
val beta : float -> float -> float primitive
```

```
val gamma : float -> float -> float primitive
```

```
val continuous_uniform : float -> float -> float primitive
```

```
val bernoulli : likelihood -> bool dist
```

```
val choice : likelihood -> 'a dist -> 'a dist -> 'a dist
```

Sampling

```
val sample : 'a dist -> 'a
```

```
val sample_n : int -> 'a dist -> 'a array
```

```
val sample_with_score : 'a dist -> 'a * likelihood
```

```
val dist_of_n_samples : int -> 'a dist -> 'a list dist
```

Prior Distribution

```
val prior' : 'a dist -> 'a dist
```

```
val prior : 'a dist -> ('a * likelihood) dist
```

```
val prior_with_score : 'a dist -> ('a * likelihood) dist
```

```
val support : 'a dist -> 'a list
```

```
module PplOps : Ppl.Sigs.Ops with type 'a dist := 'a dist
  Operators for distributions
```

Up â ppl » Ppl » Inference

Module Pp1 . Inference

Implementation of inference algorithms

Inference algorithms to be called on probabilistic models defined using Dist

- Helpers
- Exact Inference
- Importance Sampling
- Rejection Sampling
- Sequential Monte Carlo
- Metropolis Hastings
- Particle Independent Metropolis Hastings
- Particle Cascade
- Common

```
exception Undefined
```

```
type 'a samples = ('a * float) list
```

Helpers

```
val unduplicate : 'a samples -> 'a samples  
val resample : 'a samples -> 'a samples Dist.dist  
val normalise : 'a samples -> 'a samples  
val flatten : ('a samples * float) list -> 'a samples
```

Exact Inference

```
val enumerate : 'a Dist.dist -> float -> 'a samples  
val exact_inference : 'a Dist.dist -> 'a Dist.dist
```

Importance Sampling

```
val importance : int -> 'a Dist.dist -> 'a samples Dist.dist  
val importance' : int -> 'a Dist.dist -> 'a Dist.dist
```

Rejection Sampling

```
type rejection_type =
```

```
| Hard  
| Soft
```

```
val pp_rejection_type : Stdlib.Format.formatter -> rejection type -> unit  
val show_rejection_type : rejection type -> string  
val create' : int -> 'a option Dist.dist -> 'a list -> 'a list  
val create : int -> 'a option Dist.dist -> 'a list
```

PplOps (ppl.Ppl.Dist.PplOps)

```
val reject_transform_hard : ? threshold:float -> 'a Dist.dist -> ('a * float) Dist.dist
val reject'' : 'a Dist.dist -> 'a option Dist.dist
val reject_transform_soft : 'a Dist.dist -> ('a * float) Dist.dist
val rejection_transform : ? n:int -> rejection type -> 'a Dist.dist -> 'a Dist.dist
val rejection_soft : 'a Dist.dist -> ('a * float) option Dist.dist
val rejection_hard : ? threshold:Core.Float.t -> 'a Dist.dist -> ('a * float) option Dist.dist
val rejection : ? n:int -> rejection type -> 'a Dist.dist -> 'a Dist.dist
```

Sequential Monte Carlo

```
val smc : int -> 'a Dist.dist -> 'a samples Dist.dist
val smc' : int -> 'a Dist.dist -> 'a Dist.dist
val smcStandard : int -> 'a Dist.dist -> 'a samples Dist.dist
val smcStandard' : int -> 'a Dist.dist -> 'a Dist.dist
val smcMultiple : int -> int -> 'a Dist.dist -> 'a samples Dist.dist
val smcMultiple' : int -> int -> 'a Dist.dist -> 'a Dist.dist
```

Metropolis Hastings

```
val mh' : int -> 'a Dist.dist -> 'a Dist.dist
val mh'' : int -> 'a Dist.dist -> 'a Dist.dist
val mh_sampler : int -> 'a Dist.dist -> 'a list Dist.dist
val mh : burn:int -> 'a Dist.dist -> unit -> 'a
val mh_transform : burn:int -> 'a Dist.dist -> 'a Dist.dist
```

Particle Independent Metropolis Hastings

```
val pimh : int -> 'a Dist.dist -> 'a samples list Dist.dist
val pimh' : int -> int -> 'a Dist.dist -> 'a Dist.dist
```

Particle Cascade

```
val resamplePC : 'a samples -> int -> 'a samples Dist.dist
val cascade : int -> 'a Dist.dist -> 'a samples Dist.dist
val cascade' : int -> 'a Dist.dist -> 'a Dist.dist
```

Common

```
type infer_strat =

| MH of int
| SMC of int
| PC of int
| PIMH of int
| Importance of int
```


PplOps (ppl.Ppl.Dist.PplOps)

- | Rejection of int * rejection type
- | RejectionTrans of int * rejection type
- | Prior
- | Enum
- | Forward

```
val pp_infer_strat : Stdlib.Format.formatter -> infer strat -> unit
val show_infer_strat : infer strat -> string
val print_infer_strat : infer strat -> string
val print_infer_strat_short : infer strat -> string
val infer : 'a Dist.dist -> infer strat -> 'a Dist.dist
val infer_sampler : 'a Dist.dist -> infer strat -> unit -> 'a
```

Up â _ppl » Ppl » Primitive » PRIM_DIST

Module type `Primitive.PRIM_DIST`

The signature for new primitives distributions

```
type t

val sample : unit -> t
val pdf : t -> float
val cdf : t -> float
val ppf : t -> float
val support : t support
```

Up â _ppl » Ppl » Primitive

Module Ppl.Primitive

Module defining a type for primitive distributions

- New Distributions
- Predefined Distributions
- Basic Operations
- Other

```
type 'a support =
```

DiscreteFinite of 'a list	A list of valid values
DiscreteInfinite	discrete dist with infinite support e.g. poisson
ContinuousFinite of ('a * 'a) list	set of endpoints
ContinuousInfinite	continuous dist with an infinite support e.g.
Merged of 'a <u>support</u> * 'a <u>support</u>	combination of any of the above

The type of supports - the values with a distribution can take

```
module type PRIM_DIST = sig ... end
```

The signature for new primitives distributions

```
type 'a t
```

Type of primitive dists wrapping a module

New Distributions

```
val create_primitive : sample:(unit -> 'a) -> pdf:('a -> float) ->  
cdf:('a -> float) -> support:'a support -> ppf:('a -> float) -> 'a t
```

Predefined Distributions

```
val binomial : int -> float -> int t  
val categorical : ('a * float) list -> 'a t  
val normal : float -> float -> float t  
val discrete_uniform : 'a list -> 'a t  
val beta : float -> float -> float t  
val gamma : float -> float -> float t  
val poisson : float -> int t  
val continuous_uniform : float -> float -> float t
```

Basic Operations

```
val pdf : 'a t -> 'a -> float  
val logpdf : 'a t -> 'a -> float  
val cdf : 'a t -> 'a -> float  
val ppf : 'a t -> 'a -> float  
val sample : 'a t -> 'a  
val support : 'a t -> 'a support
```

Other

```
val merge_supports : ('a support * 'a support) -> 'a support
```

Up â _ppl » Ppl » Helpers

Module Ppl.Helpers

Utilities for working with distributions

A set of utilities for generating statistics and printing distributions

- [Samples](#)
- [Printing](#)
- [Others](#)

Samples

```
val sample_mean : ? n:int -> float Dist.dist -> float
val sample_variance : ? n:int -> float Dist.dist -> float
val take_k_samples : int -> 'a Dist.dist -> 'a array
val unduplicate : ('a * float) list -> ('a * float) list
```

Removes duplicates and sums the probabilities associated so that each value appears once

```
val flatten : (('a * float) list * float) list -> ('a * float) list
val normalise : ('a * float) list -> ('a * float) list
val weighted_dist : ? n:int -> 'a Dist.dist -> ('a, &int) Core.Map.Poly.t
```

Printing

```
val print_exact_exn : (module Base.Stringable.S with type t = 'a) -> 'a
Dist.dist -> unit
val print_exact_bool : bool Dist.dist -> unit
val print_exact_int : int Dist.dist -> unit
val print_exact_float : float Dist.dist -> unit
```

Others

```
val time : (unit -> 'a) -> 'a * float
val memo : ('a -> 'b) -> 'a -> 'b
val memo_no_poly : (module Base___.Hashtbl_intf.Key.S with type t = 'a) ->
('a -> 'b) -> 'a -> 'b
```

[Up](#) â [_ppl](#) » [Ppl](#) » Evaluation

Module Ppl.Evaluation

A module for evaluating the correctness of models and inference procedures

Contains functionality to perform hypothesis tests and KL-divergences for both continuous and discrete distributions

- KL-Divergence
- Hypothesis Tests

```
type 'a samples = 'a Empirical.Discrete.t  
type 'a dist = 'a Dist.dist
```

KL-Divergence

```
val kl_discrete : ? n:int -> 'a Primitive.t -> 'a dist -> float  
    Find the KL divergence for two discrete distributions
```

```
val kl_continuous : ? n:int -> float Primitive.t -> float dist -> float  
    Find the KL divergence for two continuous distributions
```

```
val kl_cum_discrete : int array -> 'a Primitive.t -> 'a dist -> (int *  
float) array
```

Hypothesis Tests

```
val kolmogorov_smirnov : ? n:int -> ? alpha:float -> float dist -> float  
Primitive.t -> Owl_stats.hypothesis  
    Perform kolmogorov smirnov test, returns a hypothesis which is true if the null hypothesis is  
    rejected
```

```
val chi_sq : ? n:int -> ? alpha:float -> 'a dist -> 'a Primitive.t ->  
Owl_stats.hypothesis  
    Perform chi-squared test, returns a hypothesis which is true if the null hypothesis is rejected
```

Up â _ppl » Ppl » Plot

Module Ppl.Plot

Plotting utilities

Plot provides helper functions that wrap Owl_plplot to graph PPL distributions

- [Histograms](#)
- [Other Plots](#)

Histograms

```
val hist_dist_continuous : ? h:Owl_plplot.Plot.handle -> ? n:int ->  
  ? fname:string -> ? title:string -> ? xlabel:string -> ? ylabel:string ->  
  float Dist.dist -> Owl_plplot.Plot.handle  
val hist_dist_discrete : ? h:Owl_plplot.Plot.handle -> ? n:int ->  
  ? fname:string -> ? title:string -> ? xlabel:string -> ? ylabel:string ->  
  float Dist.dist -> Owl_plplot.Plot.handle
```

Other Plots

```
val qq_plot : ? h:Owl_plplot.Plot.handle -> ? n:int -> ? fname:string ->  
  ? title:string -> ? xlabel:string -> ? ylabel:string -> float Dist.dist ->  
  float Primitive.t -> Owl_plplot.Plot.handle  
val pp_plot : ? h:Owl_plplot.Plot.handle -> ? n:int -> ? fname:string ->  
  ? title:string -> ? xlabel:string -> ? ylabel:string -> float Dist.dist ->  
  float Primitive.t -> Owl_plplot.Plot.handle  
val ecdf_continuous : ? h:Owl_plplot.Plot.handle -> ? n:int ->  
  ? fname:string -> ? title:string -> ? xlabel:string -> ? ylabel:string ->  
  float Dist.dist -> Owl_plplot.Plot.handle  
val ecdf_discrete : ? h:Owl_plplot.Plot.handle -> ? n:int -> ? fname:string  
  -> ? title:string -> ? xlabel:string -> ? ylabel:string -> float Dist.dist  
  -> Owl_plplot.Plot.handle  
val add_pdf : ? scale:float -> dist:float Primitive.t ->  
  Owl_plplot.Plot.handle -> Owl_plplot.Plot.handle  
val show : Owl_plplot.Plot.handle -> unit
```

[Up](#) â [_ppl](#) » [Ppl](#) » Empirical

Module Ppl.Empirical

```
module type S = sig ... end
module Discrete : S
module Continuous : sig ... end
Up â _ppl » Ppl » Empirical » Discrete
```


Module Empirical.Discrete

```
type 'a t

val from_dist : ? n:int -> 'a Dist.dist -> 'a_t
    Create a empirical distribution from a distribution object, using n samples to approximate it

val empty : 'a t
    Create an empty distribution

val add_sample : 'a t -> 'a -> 'a t
    Add another sample to the distribution

val get_num : 'a t -> 'a -> int
    Get the numer of samples with the value

val get_prob : 'a t -> 'a -> float
    Get the probability of a particular value

val to_pdf : 'a t -> 'a -> float
    Create a pdf function

val print_map : (module Core.Pretty_printer.S with type t = 'a) -> 'a t
-> unit
    print the entire distribution

val to_arr : 'a t -> ('a * int) array
val to_norm_arr : 'a t -> ('a * float) array
val support : 'a t -> 'a list
    Get the set of values for the distribution
```

[Up](#) â [_ppl](#) » [Ppl](#) » [Empirical](#) » Continuous

Module Empirical.Continuous

```
type bin = float * float
type element = float
type endpoints = {
  start : float;
  finish : float;
}
type 'a t = Owl_stats.histogram

val empty : Owl_stats.histogram
val from_dist : ? n:int -> float Dist.dist -> Owl_stats.histogram
```

Up â _ppl » Ppl » Empirical » S

Module type Empirical.S

```
type 'a t

val from_dist : ? n:int -> 'a Dist.dist -> 'a_t
    Create a empirical distribution from a distribution object, using n samples to approximate it

val empty : 'a t
    Create an empty distribution

val add_sample : 'a t -> 'a -> 'a t
    Add another sample to the distribution

val get_num : 'a t -> 'a -> int
    Get the numer of samples with the value

val get_prob : 'a t -> 'a -> float
    Get the probability of a particular value

val to_pdf : 'a t -> 'a -> float
    Create a pdf function

val print_map : (module Core.Pretty_printer.S with type t = 'a) -> 'a t
-> unit
    print the entire distribution

val to_arr : 'a t -> ('a * int) array
val to_norm_arr : 'a t -> ('a * float) array
val support : 'a t -> 'a list
    Get the set of values for the distribution
```