

# Module Pp1

A shallowly embedded DSL for Probabilistic Programming

This is a library for universal probabilistic programming using distributions as monads. Includes several approximate inference algorithms. Contains utilities to plot distributions and evaluate correctness of inference.

- [Core](#)
- [Extra](#)

## Core

```
module Dist : sig ... end
  Module used for defining probabilistic models

module Primitive : sig ... end
  Module defining a type for primitive distributions

module Empirical : sig ... end
  A module for empirical distributions generated from samplers

module Inference : sig ... end
  Implementation of inference algorithms
```

## Extra

```
module Plot : sig ... end
  Plotting utilities

module Evaluation : sig ... end
  A module for evaluating the correctness of models and inference procedures

module Helpers : sig ... end
  Utilities for working with distributions
```

# Module Pp1.Dist

Module used for defining probabilistic models

Contains a type [dist](#) which is used to represent probabilistic models.

- [Condition Operators](#)
- [Monad Functions](#)
- [Sampling](#)
- [Prior Distribution](#)

```
exception Undefined
```

```
module Prob : Ppl.Sigs.Prob
  The module used to represent probability, can be switched to use log probs
```

```

type prob = Prob.t
    A type for which values need to sum to 1 (not an enforced property)

type likelihood = Prob.t
    A type for which values don't need to sum to 1 (not an enforced property)

type 'a samples = ('a * prob) list
    A set of weighted samples, summing to one

type _ dist = private

| Return : 'a -> 'a dist                distribution with a single value
| Bind : 'a dist * ('a -> 'b dist) -> 'b dist    monadic bind
| Primitive : 'a Primitive.t -> 'a dist        primitive exact distribution
| Conditional : ('a -> likelihood) * 'a dist -> 'a dist    variant that defines likelihood model
| Independent : 'a dist * 'b dist -> ('a * 'b) dist    for combining two independent distributions

```

GADT for representing distributions, private to avoid direct manipulation

## Condition Operators

```

val condition' : ('a -> float) -> 'a dist -> 'a dist
    The most general condition operator

val condition : bool -> 'a dist -> 'a dist
    Hard conditioning

val score : float -> 'a dist -> 'a dist
    Soft conditioning, add a constant score to a trace

val observe : 'a -> 'a Primitive.t -> 'b dist -> 'b dist
    Soft conditioning for observations from a known distribution

```

## Monad Functions

Monad functions

```

type 'a t

val return : 'a -> 'a t
val bind : 'a t -> ('a -> 'b t) -> 'b t
val (>>=) : 'a t -> ('a -> 'b t) -> 'b t
val let* : 'a t -> ('a -> 'b t) -> 'b t
val fmap : ('a -> 'b) -> 'a t -> 'b t
val liftM : ('a -> 'b) -> 'a t -> 'b t
val liftM2 : ('a -> 'b -> 'c) -> 'a t -> 'b t -> 'c t
val mapM : ('a -> 'b t) -> 'a list -> 'b list t
val sequence : 'a t list -> 'a list t

val and* : 'a dist -> 'b dist -> ('a * 'b) dist

```

## Primitives

These functions create dist values which correspond to primitive distributions so that they can be used in models.

```
type 'a primitive
```

```
val binomial : int -> float -> int primitive
val normal : float -> float -> float primitive
val categorical : ('a * float) list -> 'a primitive
val discrete_uniform : 'a list -> 'a primitive
val beta : float -> float -> float primitive
val gamma : float -> float -> float primitive
val continuous_uniform : float -> float -> float primitive

val bernoulli : float -> bool dist
```

## Sampling

```
val sample : 'a dist -> 'a
val sample_n : int -> 'a dist -> 'a array
val sample_with_score : 'a dist -> 'a * likelihood
```

## Prior Distribution

```
val prior' : 'a dist -> 'a dist

val prior_with_score : 'a dist -> ('a * likelihood) dist
val support : 'a dist -> 'a list

module PplOps : Ppl . Sigs.Ops with type 'a dist := 'a dist
    Common operators for combining distributions
```

Up â ppl » Ppl » Inference

## Module Ppl . Inference

Implementation of inference algorithms

Inference algorithms to be called on probabilistic models defined using Dist. The `infer` method can be used to call all the inference algorithms listed, but the underlying method is also exposed for convenience. The

- Helpers
- Exact Inference
- Importance Sampling
- Rejection Sampling
- Sequential Monte Carlo
- Metropolis Hastings
- Particle Independent Metropolis Hastings
- Particle Cascade
- Common

```
exception Undefined
```

```
type 'a samples = ('a * Dist.prob) list
```

## Helpers

```
val unduplicate : 'a samples -> 'a samples  
val resample : 'a samples -> 'a samples Dist.dist  
val normalise : 'a samples -> 'a samples  
val flatten : ('a samples * Dist.prob) list -> 'a samples
```

## Exact Inference

```
val enumerate : 'a Dist.dist -> float -> 'a samples  
val exact_inference : 'a Dist.dist -> 'a Dist.dist
```

## Importance Sampling

```
val importance : int -> 'a Dist.dist -> 'a samples Dist.dist
```

## Rejection Sampling

```
type rejection_type =
```

```
| Hard  
| Soft
```

```
val pp_rejection_type : Stdlib.Format.formatter -> rejection type -> unit  
val show_rejection_type : rejection type -> string  
val rejection : ? n:int -> rejection type -> 'a Dist.dist -> 'a Dist.dist
```

## Sequential Monte Carlo

```
val smcStandard' : int -> 'a Dist.dist -> 'a Dist.dist  
val smcMultiple' : int -> int -> 'a Dist.dist -> 'a Dist.dist
```

## Metropolis Hastings

```
val mh' : int -> 'a Dist.dist -> 'a Dist.dist
```

## Particle Independent Metropolis Hastings

```
val pimh' : int -> int -> 'a Dist.dist -> 'a Dist.dist
```

## Particle Cascade

```
val cascade' : int -> 'a Dist.dist -> 'a Dist.dist
```

## Common

```
type infer_strat =
```

```
| MH of int  
| SMC of int  
| PC of int
```

```
| PIMH of int
| Importance of int
| Rejection of int * rejection type
| Prior
| Enum
| Forward
```

```
val pp_infer_strat : Stdlib.Format.formatter -> infer strat -> unit
```

```
val infer : 'a Dist.dist -> infer strat -> 'a Dist.dist
val infer_sampler : 'a Dist.dist -> infer strat -> unit -> 'a
```

Up â \_ppl » Ppl » Empirical

## Module Ppl.Empirical

A module for empirical distributions generated from samplers

Contains a signature as well as two implementations, for continuous and discrete distributions respectively

```
module type S = sig ... end
module Discrete : S
module ContinuousArr : sig ... end
Up â _ppl » Ppl » Empirical » S
```

## Module type Empirical.S

```
type 'a t
```

```
val from_dist : ? n:int -> 'a Dist.dist -> 'a t
    Create a empirical distribution from a distribution object, using n samples to approximate it
```

```
val empty : 'a t
    Create an empty distribution
```

```
val add_sample : 'a t -> 'a -> 'a t
    Add another sample to the distribution
```

```
val get_num : 'a t -> 'a -> int
    Get the number of samples with the value
```

```
val get_prob : 'a t -> 'a -> float
    Get the probability of a particular value
```

```
val to_pdf : 'a t -> 'a -> float
    Create a pdf function
```

```
val print_map : (module Core.Pretty_printer.S with type t = 'a) -> 'a t
-> unit
    print the entire distribution
```

```
val to_arr : 'a t -> ('a * int) array
    Get array of samples
```

```
val support : 'a t -> 'a list
    Get the set of values for the distribution
```

[Up](#) â [\\_ppl](#) » [Ppl](#) » [Primitive](#) » PRIM\_DIST

## Module type `Primitive.PRIM_DIST`

The signature for new primitive distributions

```
type t

val sample : unit -> t
val pdf : t -> float
val cdf : t -> float
val ppf : t -> float
val support : t support
```

[Up](#) â [\\_ppl](#) » [Ppl](#) [Sigs](#) » Prob

## Module type `Ppl__Sigs.Prob`

This is an signature for types representing probabilities - it overloads mathematical operators which are commonly used in probability calculations. At the moment, there are two implementations - ordinary float probabilities and log probabilities. Both are backed by floats, but use of the LogProb module can lead to a reduced risk of underflow.

```
type t

val to_float : t -> float
val of_float : float -> t
val (=) : t -> t -> bool
val (*.) : t -> t -> t
val (/.) : t -> t -> t
val (+) : t -> t -> t
val min : t -> t -> t
val one : t
val zero : t
```