

# TURBOMACHINERY: COMPRESSOR PRELIMINARY DESIGN

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## 1 Problem Description

## 2 Mean Line

## 3 Models

## 4 turboLIB & Results



# Initial conditions & constraints

## Inlet conditions

- $P_{T0} = 1\text{bar}$
- $T_{T0} = 300\text{K}$

## Constraints

- $r_{max} = 0.45\text{m}$
- $\beta_{TT} = 1.45$
- $\dot{m} = 100 \frac{\text{kg}}{\text{s}}$
- $\max \eta$

Due to the **course track** and **preference**, the turbomachinery design will be on an **axial** compressor.



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Main design quantities

$V_{tmean}$ ,  $V_{amean}$ ,  $U_{mean}$  & velocity triangles

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## Problem setup: hypothesis

### Hypothesis

- **not using** an **inlet guide vane** for simplicity of design
- keeping, in the similarity/adimensional analysis of the compressor,  $V_{a_{mean}}$  **constant**<sup>1</sup>
- keeping the blade height,  $b_0$ , **constant** both in rotor and stator
- using a **mixed vortex** model for the **rotor** velocity triangles
- using a **second order** function for the **stator** velocity triangles
- neglecting inlet **entropy** generation and assuming **rotor inlet** quantities **constant**
- **shrouding** at blade tip not present
- **rotor-stator** losses neglected

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<sup>1</sup> $\dot{m}$  corrections will be made later on in the **radial equilibrium** solution.

## Problem setup: solution steps

### Main procedural steps:

- $\lambda$  and  $\psi$  computation from  $\chi$  and  $V_{t0}$
- $\phi$  and  $\eta$  computation
- $V_{a_{mean}}$  and  $L_{eu}$  computation from  $\phi$ ,  $\beta_{TT}$  and  $\eta$
- computing **mean** velocity triangles, using the above hypothesis
- computing **mean thermodynamic** quantities
- computing **blade height**

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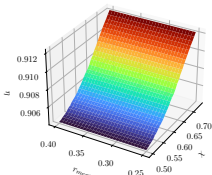




# Graph analysis: $\chi$ & $r_{mean}$

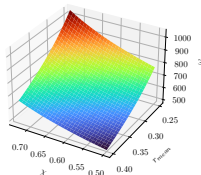
$$\chi = 0.58, r_{mean} = 0.32$$

$$\eta = 0.906$$

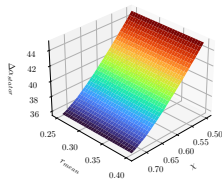


$$\Delta\beta = -36.63^\circ$$

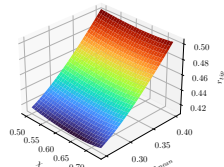
$$\omega = 658.25 \frac{rad}{s}, rpm = 6286$$



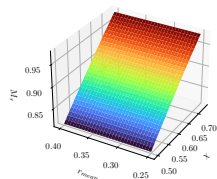
$$\Delta\alpha_{stator} = 41.07^\circ$$



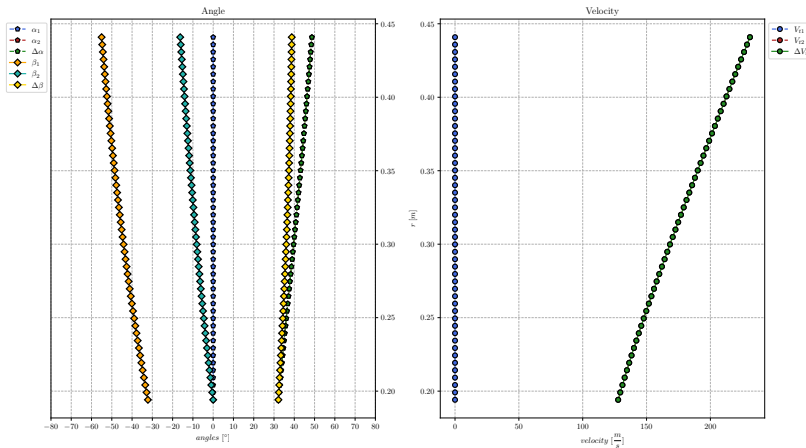
$$r_{tip} = 0.446m, b_0 = 0.252m$$



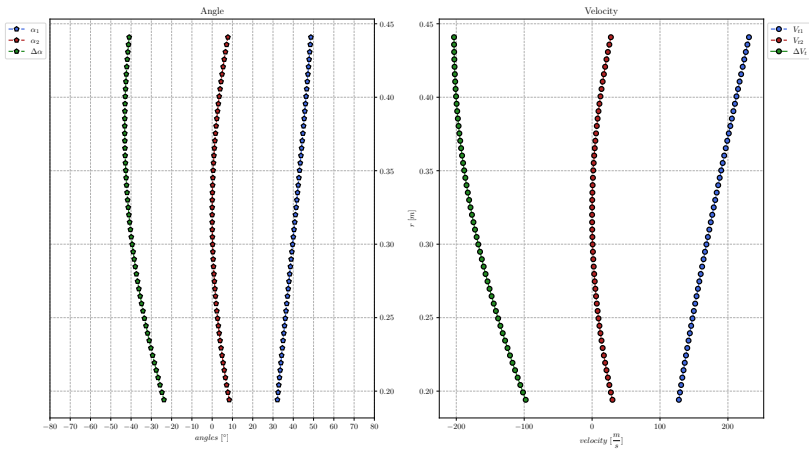
$$M_r = 0.87$$



# Graph analysis: **rotor** $\alpha$ , $\beta$ & $V_t$



# Graph analysis: stator $\alpha$ & $V_t$



$\lambda$  &  $\psi$ 

From the previous **graphs**:

- $^2\chi = 0.58$
- $r_{mean} = 0.32m$
- $\frac{V_{t0}}{U_{mean}} = 0$

Taking into account the previous modeling **hypothesis**:

$$\lambda = \left( 1 - \chi - \frac{V_{t0}}{U_{mean}} \right) \cdot 4$$

$$\psi = \frac{\lambda}{2}$$

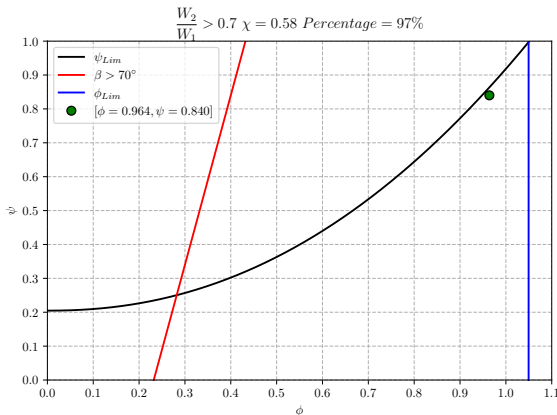
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$$^2\chi = \frac{h_1 - h_0}{h_{T1} - h_{T0}} = \frac{\frac{w_0^2}{2} - \frac{w_1^2}{2}}{U_{mean}(V_{t1} - V_{t0})} = \frac{\frac{w_{a0}^2}{2} + \frac{w_{t0}^2}{2} - \frac{w_{a1}^2}{2} - \frac{w_{t1}^2}{2}}{U_{mean}(V_{t1} - V_{t0})} = \frac{\frac{w_{t0}^2}{2} - \frac{w_{t1}^2}{2}}{U_{mean}(V_{t1} - V_{t0})}$$



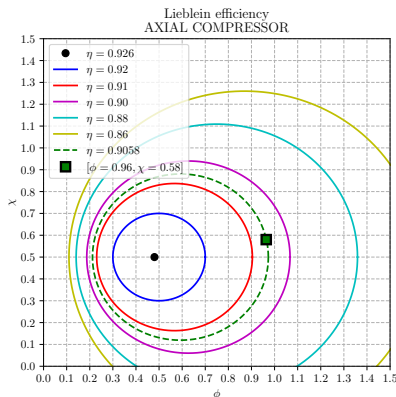
$$\phi(\psi)$$

From [Aun04, Sec. 10.4] it is imposed that  $\frac{W_2}{W_1} \geq 0.7$  with a *safety* margin of 3%.  $\phi_{lim}$  line is related to the **surge safety margin**.



$\eta$  &  $L_{eu}$ 

$\eta$  is computed from an **Lieblein** efficiency chart<sup>3</sup> given  $\phi$  and  $\chi$ . This parameter will be used for the computation of  $L_{eu}$  given the  $\beta_{TT}$  target.



$$L_{is} = \frac{\gamma R}{\gamma - 1} T_{T0} \left( \beta_{TT}^{\frac{\gamma-1}{\gamma}} - 1 \right)$$

$$L_{eu} = \frac{L_{is}}{\eta}$$

<sup>3</sup>This chart has been interpolated from the course slides charts.



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# $V_{a_{mean}}$ , $V_{t_{mean}}$ & $U_{mean}$

$$U_{mean} = \frac{L_{eu}}{\psi}$$

$$V_{a_{mean}} = \phi U_{mean}$$

$$L_{eu_{mean}} = U_{1_{mean}} V_{t1_{mean}} - U_{0_{mean}} V_{t0_{mean}} \stackrel{U_1=U_0}{=} U_{mean} \Delta V_{t_{mean}}$$

$$V_{t1_{mean}} = \Delta V_{t_{mean}} + V_{t0_{mean}}$$

- $\Delta V_{t_{mean}}$  computation allows us to get a *first sketch* of the **velocity triangles**<sup>4</sup> using  $\phi$ ,  $\psi$  and  $L_{eu}$ <sup>5</sup> definitions.  $V_a$  is assumed **constant** all through the stage.
- The first analysis results are stored in `compressor_0.58_0.32_45_35.txt`

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<sup>4</sup> **Mixed vortex** model and **second order** function based.

<sup>5</sup>  $L_{eu} = U_1 V_{t1} - U_0 V_{t0}$





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Radial equilibrium  
Blade shape

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### Losses modeling

Profile losses

Compressibility losses

Secondary flow losses

End wall losses

Shock losses

Tip leakage losses

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## Profile losses

The profile losses used are related to the **Leiblein modeling** approach<sup>6</sup>.

The model is based on the **equivalent diffusion factor**<sup>7</sup>,  $D_{eq}$ :

$$\frac{W_{max}}{W_1} = 1.12 + 0.61 \frac{\cos(\beta_1)^2}{\sigma} \cdot \frac{r_1 V_{t1} - r_2 V_{t2}}{r_1 V_{a1}}$$

$$D_{eq} = \frac{W_{max}}{W_1} \cdot \frac{W_1}{W_2}$$

$D_{eq}$  will be used for the computation of  $\bar{\omega}_{profile}$  as:

$$\bar{\omega}_{profile} = \frac{0.004 \left( 1 + 3.1 (D_{eq} - 1)^2 + 0.4 (D_{eq} - 1)^8 \right) 2 \sigma}{\cos(\beta_2) \left( \frac{W_1}{W_2} \right)^2}$$

<sup>6</sup>The following equations are interpolated data from [Aun04, Sec. 6.4].

<sup>7</sup>It describes how important is the **velocity change** along the blade. It can be seen as an *indicator* of the **blade loading**.

## Compressibility losses – I

These losses can be seen as a **correction** of the **profile** losses due to the compressibility of the gas along its *journey* in the stage.

The correction refers to a **Leiblein correction** model that uses the **positive** and **negative** blade section incidence angle<sup>8</sup>,  $i_c$  and  $i_s$ .

These new stall incidence angles will build a new **mean** incidence angle,  $i_m$ , that can be seen as the **optimum** incidence angle related to the inlet Mach conditions<sup>9</sup>.

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<sup>8</sup> $i_c$  and  $i_s$  are related to the total pressure losses,  $\bar{\omega}_c$  and  $\bar{\omega}_s$ , that are **twice** the minimum total pressure loss,  $\bar{\omega}$ , obtained at the **design incidence angle**,  $i^*$ .

<sup>9</sup>The implemented model follows [Aun04, Sec. 6.6]

# Compressibility losses – II

$\bar{\omega}_{compressibility}$  setup:

- $R_c$  and  $R_s$  computation<sup>10</sup>:

$$R_c = 9 - \left[ 1 - \left( \frac{30}{\beta_1} \right)^{0.48} \right] \frac{\theta}{8.2}$$

$$R_s = 10.3 + \left( 2.92 - \frac{\beta_1}{15.6} \right) \frac{\theta}{8.2}$$

- $i_c$  and  $i_s$  computation due to **compressibility** effects:

$$i_c = i^* - \frac{R_c}{1 + 0.5 M_1^3}$$

$$i_s = i^* + \frac{R_s}{1 + 0.5 (K_{sh} M_1)^3}$$

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<sup>10</sup>  $R_c$  and  $R_s$  are **range indices** for the computation of  $i_c$  and  $i_s$ .



## Compressibility losses – III

- $i_m$  computation<sup>11</sup>:  $i_m = i_c + (i_s - i_c) \frac{R_c}{R_c + R_s}$
- $\bar{\omega}_m$  computation:  $\bar{\omega}_m = \bar{\omega}_{profile} \left[ 1 + \frac{(i_m - i^*)^2}{R_s^2} \right]$
- $\bar{\omega}_{compressibility}$  computation<sup>12</sup>:

$$\bar{\omega}_{compressibility} = \bar{\omega}_m + \bar{\omega}_m \left[ \frac{i - i_m}{i_c - i_m} \right]^2, \text{ if } i \leq i_m$$

$$\bar{\omega}_{compressibility} = \bar{\omega}_m + \bar{\omega}_m \left[ \frac{i - i_m}{i_s - i_m} \right]^2, \text{ if } i \geq i_m$$

<sup>11</sup> $i_m$  is the incidence angle at which corresponds, having accounted the **compressibility**, the **minimum pressure loss**,  $\bar{\omega}_m$ .

<sup>12</sup>After having computed  $i_c$ ,  $i_s$ ,  $i_m$  and  $\bar{\omega}_m$ .  $\bar{\omega}_{compressibility}$  is a function of  $i$ . In the **total pressure losses study**:  $\bar{\omega}_{compressibility} = \bar{\omega}_{compressibility(i^*)}$ .

## Secondary flow losses

These losses are relative to the **secondary flow** inside the compressor and are *usually* **greater** than the other losses. These losses are related to **eddies** generated with the **blade-flow** interaction and **streamlines** displacement due to the presence of **pressure gradients**.

These losses are computed with **Howell's** model [Aun04, Ch. 6]<sup>13</sup>:

$$\bar{\beta} = \frac{\arctan(\tan(\beta_1) + \tan(\beta_2))}{2}; \quad \text{I}$$

$$C_L = 2 \cos(\bar{\beta}) \cdot \frac{\tan(\beta_1) - \tan(\beta_2)}{\sigma}; \quad \text{II}$$

$$C_D = 0.18 C_L^2; \quad \text{III}$$

$$\bar{\omega}_{secondary} = C_D \sigma \cdot \frac{\cos(\beta_1)^2}{\cos(\bar{\beta})^3}; \quad \text{loss computation}$$

<sup>13</sup>Howell computed a secondary flow loss model that is automatically embedded into  $\bar{\omega}_{profile}$ : this model is used for the **estimation** of the stator/rotor



## End wall losses

These losses are related the interaction between the flow and the **compressor case**. They are *lower* than the **secondary flow** losses. It has been used a simple and fast relation made by **Howell** [Aun04, Ch. 6]<sup>14</sup>:

$$C_D = 0.02 \frac{s}{b_0}$$
$$\bar{\omega}_{endWall} = C_D \sigma \cdot \frac{\cos(\beta_1)^2}{\cos(\bar{\beta})^3}; \quad \text{loss computation}$$

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<sup>14</sup>This loss is kept into account in the **blade numbering** study.





## Shock losses – I

The **relative** Mach number at the rotor inlet is slightly above **sonic speed**; a **shock wave** will be present at the rotor tip. From [MF20], **shock pattern** is related to **Mach number** and **airfoil shape**.

The **shock** losses modeling is related to **König losses** modeling approach. This model describes a **2 shock waves loss** using a **single normal shock** with respect to a computed Mach number,  $M_{in}$ .

**König model** [Aun04, Sec. 6.7] depends mainly on **blade deflection angle**,  $\theta$ , and **relative inlet Mach**,  $M_1$ .

# Shock losses – II

- computation of the **expansion wave** angle,  $\phi$ :  

$$\phi = \frac{s \cos(\psi)}{s \sin(\psi) R_u}, \text{ where } \psi = \psi(\beta_1, \gamma, \theta)$$
- computation of  $W_s$  and  $M_s$  using the **Prandtl-Meyer** expansion:  $\phi = \int_{W_1}^{W_s} \sqrt{M^2 - 1} \frac{dW}{W}$
- $M_{in}$  computation:  $M_{in} = \sqrt{M_1 M_s}$
- **normal shock** solution and computation of  $\Delta P_T$
- from  $\Delta P_T$ , computation of  $\bar{\omega}_{shock}$



## Tip leakage losses

Again these losses are computed from [Aun04, Sec. 6.9]. The main concept is: computing a **total** blade pressure loss and **assuming linear distribution** of losses from the hub to the tip<sup>15</sup>.

$$\tau = \pi \delta_c \left[ r_1 \rho_1 V_{a1_{mean}} + r_2 \rho_2 V_{a2_{mean}} \right] \left[ r_2 V_{t2_{mean}} - r_1 V_{t1_{mean}} \right]$$

$$\Delta P = \frac{\tau}{Z r_{tip} \delta_c c \cos(\gamma)}$$

$$U_c = 0.816 \frac{\sqrt{\frac{2\Delta P}{\rho_{mean}}}}{N_{row}^{0.2}}$$

$$\dot{m}_c = \rho_{mean} U_c Z \delta_c c \cos(\gamma)$$

$$\Delta P_T = \frac{\Delta P \dot{m}_c}{\dot{m}}$$

$\Delta P_T$  is the **overall** total pressure loss due to **tip leakage**.

<sup>15</sup> $Z$  is the number of blades.  $\delta_c$  is the tip clearance.  $N_{row}$  is the number of blade rows in the compressor.

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## Equation setup

The **radial equilibrium** equation:  $\frac{\partial h_t}{\partial r} = T \frac{\partial s}{\partial r} + V_a \frac{\partial V_a}{\partial r} + V_t \frac{\partial r V_t}{\partial r}$  is converted into, for the exit station<sup>16</sup> of the blade, a **1st order ODE**:

$$-\frac{1}{2} \frac{\partial V_{a2}^2}{\partial r} + \frac{V_{a2}^2}{2 c_P} \frac{\partial s_2}{\partial r} = -c_P \frac{\partial T_{T1}}{\partial r} - \omega \frac{\partial r V_{t2}}{\partial r} + \omega \frac{\partial r V_{t1}}{\partial r} + T_{T1} \frac{\partial s_2}{\partial r} + \frac{\omega}{c_P} r V_{t2} \frac{\partial s_2}{\partial r} - \frac{\omega}{c_P} r V_{t1} \frac{\partial s_2}{\partial r} - \frac{1}{2 c_P} V_{t2}^2 \frac{\partial s_2}{\partial r} + \frac{V_{t2}}{r} \frac{\partial r V_{t2}}{\partial r}$$

- The **ODE** will be solved for  $V_{a2}^2$
- $s_2$  is computed from  $\sum_i \bar{\omega}_i$  treated earlier
- $\omega$ ,  $V_{t1}$ ,  $V_{t2}$  and  $T_{T1}$  are known

<sup>16</sup>1 is the blade inlet station and 2 is the blade outlet section.



## Δs computation

From pressure loss coefficients it is possible compute the **outlet total pressure** as:

$$P_{T2,r} = P_{T1,r} + \sum_i \bar{\omega}_i (P_{T1,r} - P_{1,r})$$

The **entropy variation** is computed as:

$$s_2 - s_1 = c_p \log \frac{T_{T2,r}}{T_{T1,r}} - R \log \frac{P_{T2,r}}{P_{T1,r}}$$

### Frames

- $T_{T2} = T_{T1}$  in **stators** and  $T_{T2,r} = T_{T1,r}$  in **rotors**
- $\bar{\omega}_*$  have to be computed using **relative** quantities for **rotors** and **absolute** quantities for **stators**
- $T_{T,r} = T + \frac{W^2}{2c_p} = T_T + \frac{W^2 - V^2}{2c_p}$
- $P_{T,r} = P_T \left( \frac{T_{T,r}}{T_T} \right)^{\frac{\gamma}{\gamma-1}}$



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## Blade shape setup

The **Leiblein model** from [Aun04, Ch. 6] has been used for the blade shape computation.

NACA – 65 profile has been chosen for the blade generation<sup>17</sup>.

The **main constraints** are:  $\frac{t_b}{c} \approx 0.1$  and  $\sigma$  is related just to  $s$ <sup>18</sup>.

Due to the many possible blade configurations, an **optimization** procedure has been used for the computation of  $i^*$ ,  $\delta$  and  $\theta$ .

Each section airfoil shape is **computed** from  $\theta$  and NACA – 65  $C_{L0}$  surface coordinates.

<sup>17</sup>Due to the low tip sonic Mach number it has been chosen to use this profile as well for the blade tip instead of a supersonic adapted profile shape.

<sup>18</sup> $\frac{t_b}{c} \approx 0.1$  allows setting  $K_{sh} \approx 0.1$ . The blade chord,  $c$ , is set up as constant during the **blade numbering** study: using  $AR = \frac{b_0}{c}$ .



# $i^*$ computation

The **incidence angle**,  $i^*$ , is computed using:

$$K_{t,i} = \left( 10 \frac{t_b}{c} \right)^q ; \text{ where } q = \frac{0.28}{0.1 + \left( \frac{t_b}{c} \right)^{0.3}}$$

$$(i_0^*)_{10} = \frac{\beta_0^p}{5 + 46 \cdot e^{-2.3\sigma}} - 0.1 \sigma^3 e^{\frac{\beta_0 - 70}{4}} ; \text{ where } p = 0.914 + \frac{\sigma^3}{160}$$

$$n = 0.025\sigma - 0.06 - \frac{\left( \frac{\beta_0}{90} \right)^{1+1.2\sigma}}{1.5 + 0.43\sigma}$$

$$i^* = K_{sh} K_{t,i} (i_0^*)_{10} + n \theta$$



# $\delta$ computation

The **deviation angle**,  $\delta$ , is computed using:

$$K_{t,\delta} = 6.25 \frac{t_b}{c} + 37.5 \left( \frac{t_b}{c} \right)^2$$

$$(\delta_0^*)_{10} = 0.01\sigma\beta_0 + (0.74\sigma^{1.9} + 3\sigma) \left( \frac{\beta_0}{90} \right)^{1.67+1.09\sigma}$$

$$b = 0.9625 - 0.17 \frac{\beta_0}{100} - 0.85 \left( \frac{\beta_0}{100} \right)^3$$

$$m = \frac{m_{1.0}}{\sigma^b} ; \text{ where } m_{1.0} = 0.17 - 0.0333 \frac{\beta_0}{100} + 0.333 \left( \frac{\beta_0}{100} \right)^2$$

$$\delta = K_{sh} K_{t,\delta} (\delta_0^*)_{10} + m \theta$$



## $\theta$ computation

Starting from the **known** flow deflection angle<sup>19</sup>,  $\varepsilon$ , it is necessary to compute:

$$\theta = \varepsilon - i^* + \delta$$

Since  $i^*$  and  $\delta$  are functions of  $\theta$ , the computation of  $\theta$  is made by an **iterative process**:

$$\theta = \varepsilon - i_{(\theta)}^* + \delta_{(\theta)}$$

Once found  $\theta$ , the **total pressure loss** coefficients,  $\bar{\omega}_*$ , are computed.

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<sup>19</sup> $\varepsilon = \beta_{inlet} - \beta_{outlet}$ .  $\beta_1$  and  $\beta_2$  change with respect to the **axial speed**.

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turboLIB

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NISRE

.stl & .scad generation

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# turboLIB

The preliminary compressor design model program **turboLIB** can be downloaded from GitHub.

## Main objects and modules

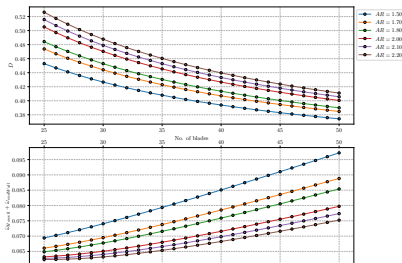
- `turboClass.turboBlade.blade`: blade object
- `turboCoeff`: engineering coefficients module
  - `losses`: losses modeling
  - `similarity`: adimensional analysis
  - `lieblein`: blade modeling
- `geometry.bladeGeometry.geometryData`: airfoil object

# Blade number

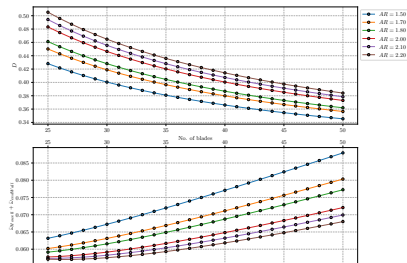
In order to define a proper number of blades for the rotor and the stator, **Howell's** relations have been used for the estimation of the **losses**. These relations, [Aun04, Ch. 6], are:

- $\bar{\omega}_{profile+secondary}$ , this is a relation that takes into account **profile** and **3D** losses
- $\bar{\omega}_{endWall}$ , this is previous expalined **end wall** loss

Rotor



Stator



# NISRE setup

The NISRE is solved through a **double nested** loop:

- **continuity loop.** Inside the **continuity loop** the `scipy.integrate.odeint` function is used for the solution of the  $V_{a2}^2$  **ODE**.
- **entropy loop.** Inside the **entropy loop** the `scipy.optimize.minimize` function is used for the computation of the blade **shape**.





## .stl & .scad generation

At the end of the NISRE, all the main blade quantities are available for the **generation** of the **3D geometry**. This geometry can be converted into a .stl file that can be used in OpenFOAM for the flow properties study. In addition a .scad file is made for understanding position and checking possible contacts between rotor and stator blades.

[Bas06] suggested that a good distance between rotor and stator blades is half of the rotor chord<sup>20</sup>.

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<sup>20</sup>In the radial equilibrium study losses between rotor and stator blades are **neglected**.

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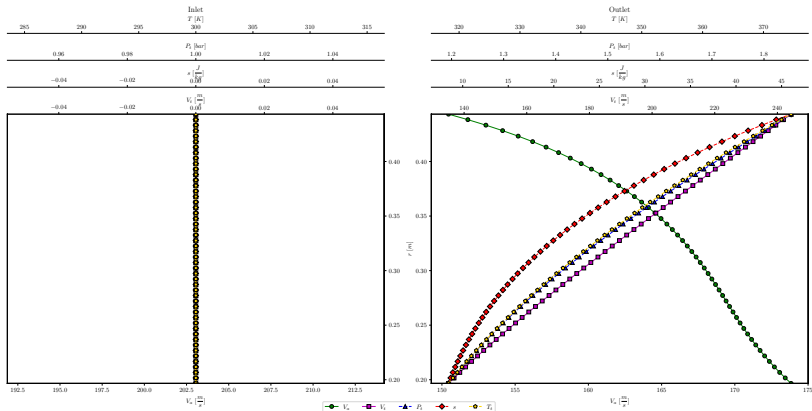
NISRE and main quantities

Efficiency

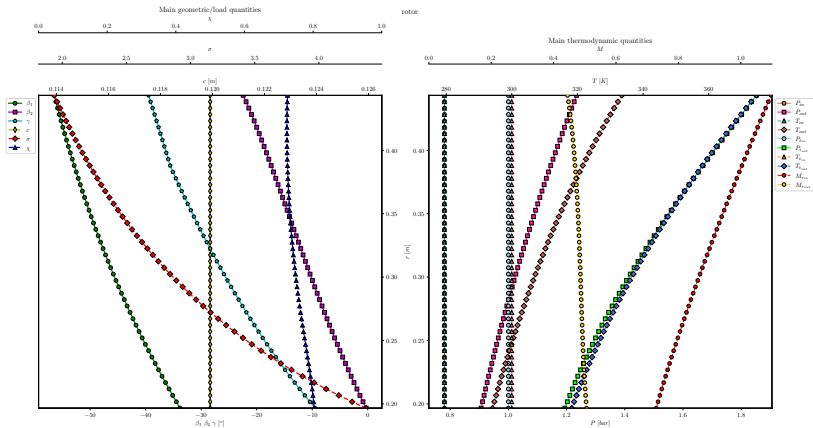


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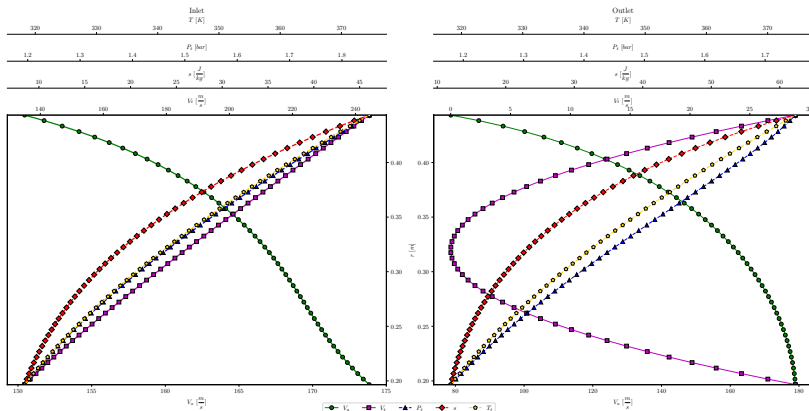
# Rotor equilibrium results: NISRE



# Rotor equilibrium results: main quantities

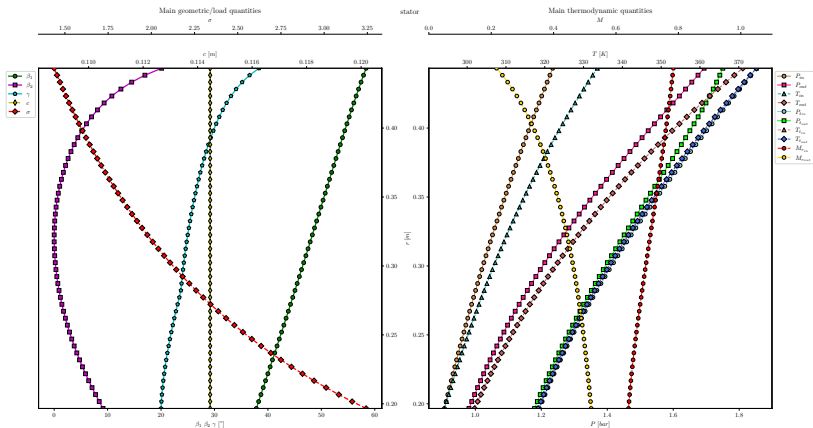


# Stator equilibrium results: NISRE



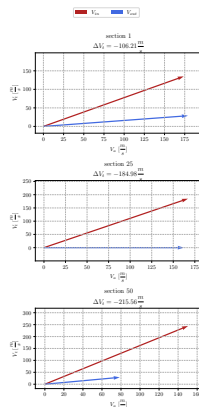
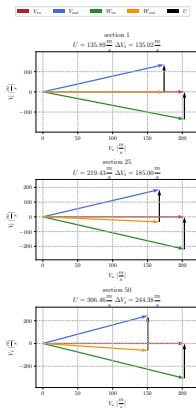
POLITECNICO  
MILANO 1863

# Stator equilibrium results: main quantities



# Velocity triangles

- Inlet: **axial** velocity
- Outlet: **mixed vortex** model



# Rotor & stator blades

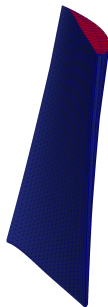


Figure 1: Rotor blade.

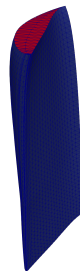
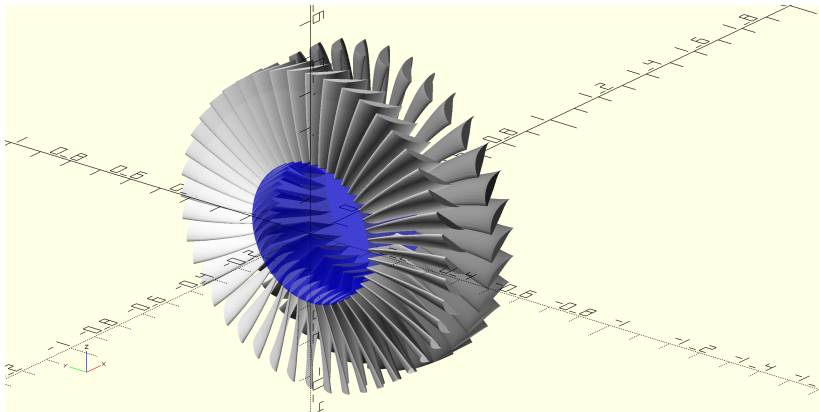


Figure 2: Stator blade.





# Stage plot



# Efficiency

The **rotor** efficiency is computed with:

$$\eta_{is_{rotor}} = \frac{W_1^2 - W_{2is}^2}{W_1^2 - W_2^2}$$

The **stator** efficiency is computed with:

$$\eta_{is_{stator}} = \frac{\Delta h_{is}}{\Delta h_{real}}$$

The modeling results are stored into  
`compressor_0.58_0.32_45_35.txt`.



- [Aun04] Ronald H. Aungier. “Axial-Flow Compressors: a Strategy for Aerodynamic Design and Analysis”. In: *Appl. Mech. Rev.* 57.4 (2004).
- [Bas06] Erian A. Baskharone. *Principles of turbomachinery in air-breathing engines*. Cambridge University Press, 2006.
- [MF20] Marco Manfredi and Fabrizio Fontaneto. “Transonic Axial Compressors Loss Correlations: Part I—Analysis and Update of Loss Models”. In: *Turbo Expo: Power for Land, Sea, and Air*. Vol. 84065. American Society of Mechanical Engineers. 2020, V02AT32A029.



*Thank you!*

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