

An effective approach to defect detection

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Abstract—Quality control is a main issue in any industry. The need of assuring a human-like evaluation during products quality control has resulted in an active research aiming to develop an automatic defect detection scheme. In this paper an effective solution to defect detection on steel surfaces from images is presented. Firstly, a preprocessing step aiming to spot plausible defective areas is discussed. Lastly, the classification of these proposed regions is made. Hence, a proper pixel-wide segmentation scheme is described.

Index Terms—Computer Vision, Image Processing, Defect Detection.

I. INTRODUCTION

A fundamental aim in any industry is to achieve highly efficient and effective quality control processes. Therefore, the research area focusing on automatic defect detection systems have become even more fecund in the last decades.

There is a large variety of previous work on defect detection on steel surfaces, even though many ideas [1–3] are as interesting as they are poorly tested and very dependent on assumptions about the uniformity of the background surface. When different motifs of steel surfaces are analyzed, this approaches easily fail. Moreover, simple thresholding techniques poorly perform on more complex defect shapes and different light exposures. There are solution using deep learning architectures [4, 5], although with ridicolously small datasets, which provide an attempt to a robust defect segmentation. Other more refined approaches rely on wavelets to detect abrupt changes in the surfaces, and this kind of previous work [6–9] has been widely used in the textile industry. The core of this paper is based on wavelet analysis and on deep learning, due to two main reasons.

Firstly, multi-resolution analysis (MRA) based on wavelets have been proven effective in facing localization both in spatial and in frequency domains [10–12]. This because of their mathematical properties, compared to Fourier’s transform.

Secondly, deep learning [13, 14] has outperformed in the last years any human-designed classifier, indeed computer vision and image processing are increasing in popularity and they are being used ever more in many fields, from autonomous driving vehicles to retail and retail security. Hence, there has been an appreciable improvement in the effectiveness of defect detection based on visual systems and a lot of work has been done since the rise of deep learning applications [15]. Three main computer vision tasks have been outlined: classification, object localization and object detection.

The classification task faces the supervised learning problem of identifying to which of a set of categories a given object belongs to. In computer vision this means assigning one of the available labels to an image. This is the simplest of the three tasks and recognizing the category of the principal object in a picture is the standard application of Convolutional Neural Network (CNN), from handwritten characters [16, 17] and house numbers [18] to traffic signs [17].

The main reason why CNNs have become so popular since LeCun originally introduced them [15, 16, 19, 20] is that they represent a black box from raw pixels to categories labels, therefore they overcome the intrinsic difficulties of designing tailored features extractors. Moreover, they are also more likely to be shift and scale invariant [20], and they have been proved to have enviable classification accuracies.

A classification task in defect detection field is accounted when objects, e.g. steel surfaces, need to be binary classified as defective or flawless. When visual systems are considered and pictures are taken to classify a particular object, this would be negligently in practical applications. Indeed, monitoring locally the product concerned would be overly expensive, whereas a single global visual system is patently appetible. Moreover, a local analysis may miss some global features of a particular defect; this is the case of burst defects.

Object localization sights to find a given number of items in a given context, predicting both their position and their class. Object detection removes the constraint on the number of items, allowing either zero or any finite number of objects. In computer vision, in particular in 2D images, the position is described by a bounding box.

CNNs have been used along with sliding window and multiscale approaches for object detection [21–23], and there is a lot of work aiming to improve performances and bounding boxes accuracies, both by designing different neural network architectures [21] or by tailoring existing one [19]. Regarding to scale-dependence in the object detection task, a solution is given by either brute-force learning (and CNN oversizing) or image pyramids [21], whereas the bounding boxes accuracies can be optimized by combining different scale sliding windows results, taking into account activation confidences in a particular area of the image and applying thresholding techniques.

In this paper a further refined system is presented, since the purpose of the defect detection algorithm is not only to globally mark an image as picturing a flawless or defective

steel surface, but both to highlight flawed regions inside the image and to label it as belonging to a particular defect class.

Pixel-wide classification is known in literature as image segmentation task, and there are three main families of techniques: hysteresis thresholding, edge-based and region-based [24]. Thresholding exploits a previously known function from the pixels space and classifies pixels through comparison with some discrete values (thresholds) [25], but it is typically used within other techniques rather than alone. Region-based approaches use graph algorithms [26, 27] or watersheds analogies [28]. Edge-based techniques, instead, use an edge detection filter [29–31], along with denoising and thresholding considerations, to solve the boundary detection problem. Remark that although similar, boundary detection aims to describe changes in pixel ownership from one object or surface to another, whereas an edge is an abrupt change which can be a sub-domain of a border. There are also more advanced techniques [32] boundary-related which rely on energy minimization and are embedded on region-based approaches. Indeed, all these techniques can be mixed both together and with learning algorithms, either unsupervised [24] or supervised [33].

The approach here described merges the more effective and efficient ideas of previously described work, balancing the drawbacks of different techniques. Since segmentation is needed, an edge-based contour detector is presented here, to reach high speed segmentation. Wavelet are used along with image preprocessing and alpha-shape [34] to identify proposals, i.e. regions of interest for the classifier, which may contain a defective area. To overcome the bias introduced from hand-crafting the edge-detection filter, the hyperparameters of the algorithm are tuned with Bayesian Optimization [35–37]. A multi-column CNN (MC-CNN) [17] is then used to combine the segmentation information with a well-known classifier architecture, exploiting both local information and global information. The proposed architecture is shown to have optimal performances on the *Severstal: Steel Defect Detection* Kaggle competition dataset.

II. STEEL SURFACES DEFECT DETECTION

A. Problem statement

Given a set of steel surfaces images with the description of their defective areas, learn to detect defective pixels in new pictures.

The surfaces may have more disjunct defective areas, and there are four defective classes, described in II-B.

For each of this classes, a thorough characterization of the pixels in the defective areas is given.

Defective pixels are described using a Run Length Encoding (RLE) approach. The rationale is that an efficient way to store pixel-wide information is needed, and it is reasonable to believe that many defective pixels will be adjacent.

To do so, the binary matrix describing interesting pixels is firstly vectorized column-wise, i.e. each column vector is appended to the previous.

Secondly, pixels are enumerated in this vectorized map.

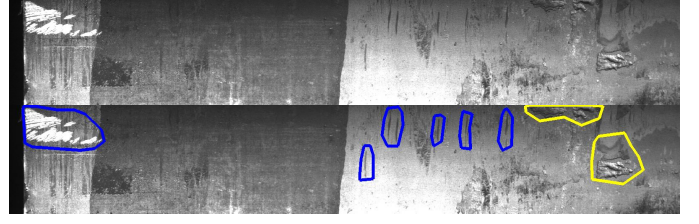


Fig. 1. Detection process input and output.

Finally, the rle algorithm is used on the indices of the considered pixels.

Example:

Suppose the ones in the below matrix need to be encoded:

$$\begin{array}{c} \begin{array}{|c|c|c|c|c|} \hline 1 & 0 & 1 & 1 & \\ \hline 1 & 1 & 1 & 0 & \\ \hline 0 & 1 & 1 & 0 & \\ \hline \end{array} \end{array}$$

The interested cells, expressed as (x, y) coordinates, are:

$$\begin{array}{l} (1, 1) (1, 2) (2, 2) (2, 3) \\ (3, 1) (3, 2) (3, 3) (4, 1) \end{array}$$

The vectorized matrix is:

$$[1 \ 1 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 0]$$

Which can be encoded as:

$$"1 \ 2 \ 4 \ 6"$$

An optimized implementation in MATLAB of both the rle encoding and decoding scheme described is proposed in [38].

A visual description of the end to end process is given in figure 1, where defective areas have been highlighted with different colors, depending on the defect class.

A mathematical description of the task is:

Given a *training set* $(\underline{\mathbf{X}}_{train}, \underline{\mathbf{y}}_{train})$ and a *test set* $(\underline{\mathbf{X}}_{test}, \underline{\mathbf{y}}_{test})$, the goal is to build a *trainer* system \mathcal{T} and a *predictor* function \mathcal{P} such that:

$$\underline{\Theta} = \mathcal{T}(\underline{\mathbf{X}}_{train}, \underline{\mathbf{y}}_{train}); \quad |\mathcal{P}(\underline{\mathbf{X}}_{test}; \underline{\Theta}) - \underline{\mathbf{y}}_{test}| \rightarrow 0$$

Both the trainer and the predictor are implemented through deep learning techniques and they are described in III.

B. Defect analysis

1) *Defect class #1:* ***** TODO: propose explanation *****

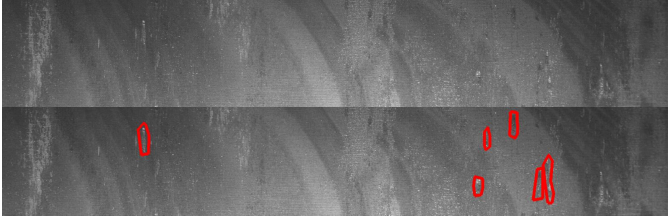


Fig. 2. Steel surface with defect class #1.

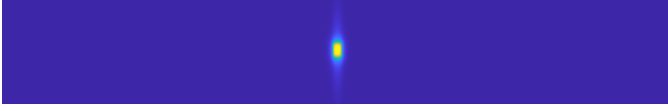


Fig. 3. Shape distribution for defect class #1.

***** TODO: gaussian bivariate statistics *****

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2) Defect class #2: ***** TODO: propose explanation *****

***** TODO: gaussian bivariate statistics *****

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3) Defect class #3: ***** TODO: propose explanation *****

***** TODO: gaussian bivariate statistics *****

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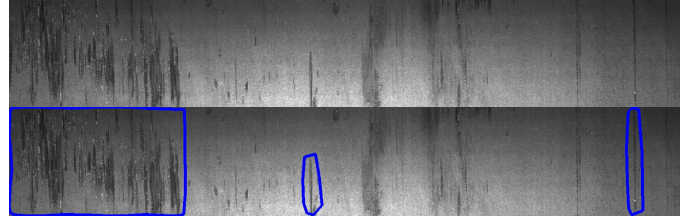


Fig. 6. Steel surface with defect class #3.

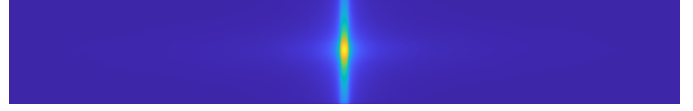


Fig. 7. Shape distribution for defect class #3.

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4) Defect class #4: ***** TODO: propose explanation *****

***** TODO: gaussian bivariate statistics *****

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C. Dataset considerations

*** TODO: include dataset statistics, data augmentation, ... ***

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To keep proper spatial information(data augmentation)

III. ARCHITECTURE OVERVIEW

The defect detection system architecture proposed in this paper is shown in figure 10.

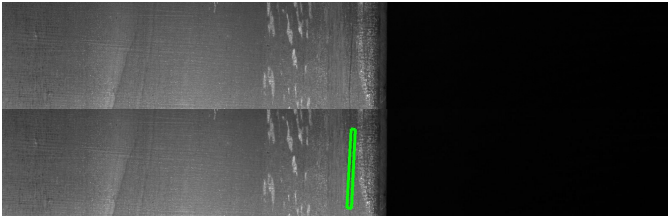


Fig. 4. Steel surface with defect class #2.

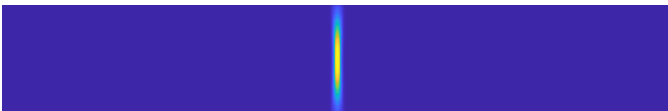


Fig. 5. Shape distribution for defect class #2.

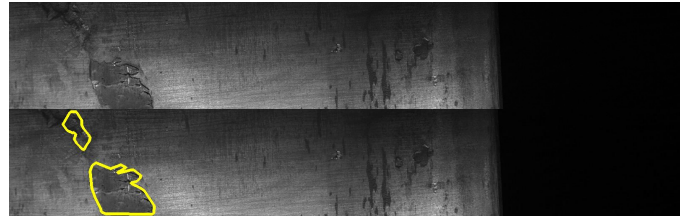


Fig. 8. Steel surface with defect class #4.

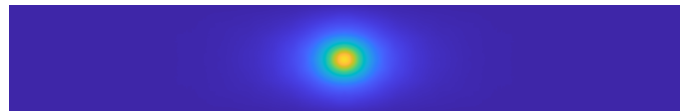


Fig. 9. Shape distribution for defect class #4.

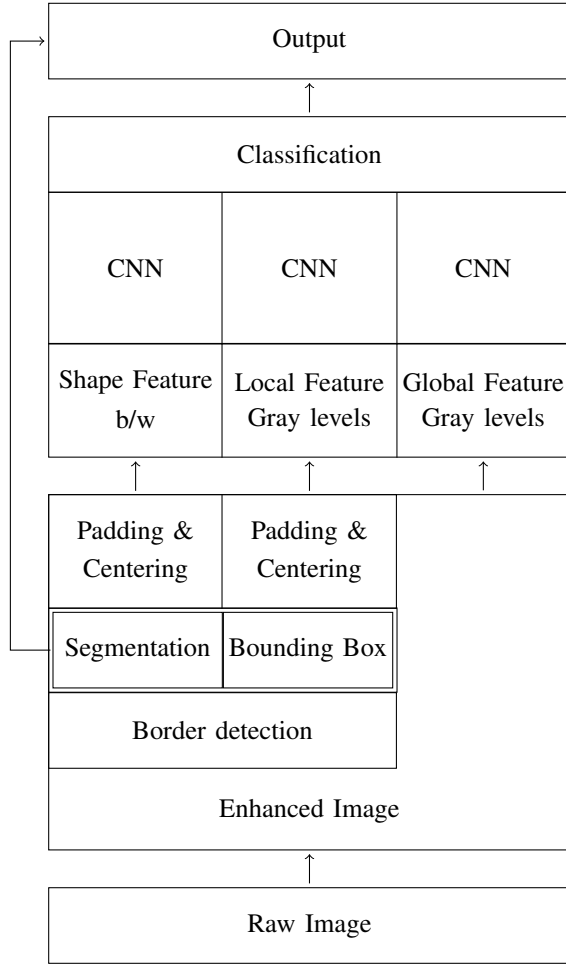


Fig. 10. Proposed defect detection system architecture

Steel surfaces pictures of 1600×256 pixels are taken at the input of the process. Since they may be taken one with a different light exposure condition than the others, some preprocessing is made to enhance the quality of the image, e.g. hystogram equalization or linear scaling. Moreover, the images considered have three equal colours levels, therefore they are converted into gray levels, to save space. This first step is further described in IV.

The aim of this paper is both to detect pixels representing steel imperfections and to classify those regions. Therefore, image segmentation is either obtained as an output of the system or it is needed in some step during the process. To achieve this, a brute-force multi-scale sliding window on the picture could be used, but to improve performances without reducing accuracy a particular implementation of a Region based CNN (R-CNN) [21, 22] is proposed in VI. This R-CNN uses a MC-CNN to combine and consider separately interesting regions, which are called proposals and which are described in V, to reduce the number of evaluations. Moreover, both local and global information are combined to improve classification accuracy. This approach avoids the complexity of combining different scale information and handling windows

with different classes of defects. A further description with relevant comparisons and results is provided in VI.

The column of the MC-CNN concerned with global information is fed with the full enhanced image. Conceptually, this CNN learns to evaluate the probability of presence of the different types of defects in the whole surface picture. The other two columns consider local information instead. This local information is obtained from a further processing step, described in V. Firstly, a contour detection algorithm (V-A) is used to spot proposals. Secondly, image segmentation (V-B) is done, to feed the MC-CNN only with some interesting regions. This segmentation results in a black and white (b/w) map describing the shape of the plausible defects. One column of the MC-CNN is fed with this map, therefore it learns to classify regions only observing their borders. The other column is fed with the portion of original image enveloped in the bounding box (V-C) of the map, therefore it is trained to consider luminance levels inside, outside and on the border of the considered proposal.

Since defects may have different dimensions, the local information are centered in a 1600×256 pixels black image.

The two MC-CNN columns concerning local information ends with a soft-max layer, because they focus on a region which is proposed to represent a single class defect. Instead, the one dealing with global information has a different output layer. Their results are then combined in order to properly classify the local regions, and the approach is described in VI.

Finally, if the classification outcome labels the region as defective, segmentation coordinates are kept. When all the proposals of the considered image have been processed, defective pixels are encoded with RLE algorithm. The output given is the RLE-encoding of all defective pixels grouped by class. If the surface is flawless, all this encodings are empty.

IV. IMAGE PREPROCESSING

In this section image preprocessing is introduced, and the raw image is enhanced to improve learning quality. In VIII the contribution of preprocessing is evaluated.

Firstly, since given images have three equal colours levels, they can be considered gray-levels. Therefore it is possible to shrink the space occupied on disk by discarding hue and saturation information and using only luminance.

Rec.ITU-R BT.601-7 calculates luminance ($E[y]$) as:

$$E[y] = 0.299 * R + 0.587 * G + 0.114 * B$$

where R, G, B are the three image channels. Observe that since $R = G = B$, also $E[y] = R = G = B$, which justifies the assumption that discarding hue and saturation does not affect effectiveness of the system, whereas improving space and computational efficiency. Luminance is denoted by $E[y]$ since brightness is named y in literature, therefore the luminance, i.e. the physical intensity expected, is labeled in this way.

Secondly, since pictures may be taken under different light exposure conditions, and since learning has heuristically be

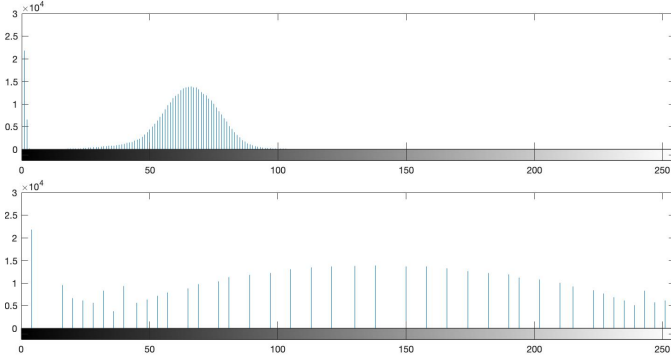


Fig. 11. Histogram of luminance distribution on sample image before and after equalization.

proven to be more effective if input assumptions are always the same, the luminance histogram of the image is normalized.

Linear scaling ensure that all images gray levels spread over all the range of possible values. $\mathcal{I}(x, y)$ refers to the luminance level of pixel (x, y) of image \mathcal{I} . Therefore, denoting with G_{max} the greater luminance level (typically $2^k - 1$ for some k), the luminance scaled image is obtained as:

$$\mathcal{I}_{new}(x, y) = G_{max} \frac{\mathcal{I}(x, y) - \mathcal{I}_{min}}{\mathcal{I}_{max} - \mathcal{I}_{min}}$$

$$\mathcal{I}_{max} = \max_{x, y} \mathcal{I}(x, y) ; \quad \mathcal{I}_{min} = \min_{x, y} \mathcal{I}(x, y)$$

However, histogram equalization is preferred over linear scaling.

Indeed, although both linear scaling and histogram equalization are effective in spreading over all the spectrum the luminance levels of an image, the former only ensure that all the intensities are used whereas the latter is also concerned about the shape of the resulting histogram, which ideally should be flat.

In fact, histogram equalization aims to transform a scalar image \mathcal{I} such that all grey levels appear equally often in the transformed image \mathcal{I}_{new} , i.e.:

$$H_{\mathcal{I}_{new}}(u) = \text{const} = \frac{N_{cols} N_{rows}}{G_{max} + 1} \quad 0 \leq u \leq G_{max}$$

Where N_{cols} and N_{rows} are, respectively, the number of columns and rows of the image. $H_{\mathcal{I}}(u)$ is the absolute frequency of luminance level u .

However, this is not practically feasible, since identical value in \mathcal{I} must be mapped on the same value of \mathcal{I}_{new} . Therefore, the transform is just an approximate solution.

Intensities u in \mathcal{I} are mapped onto new intensities $v = g(u)$ by the gradation function g :

$$g(u) = c_{\mathcal{I}}(u) \cdot G_{max}$$

Where $c_{\mathcal{I}}$ is the relative cumulative frequency function.

In figure 11 the effects of equalization a sample image histogram of luminance distribution are shown.

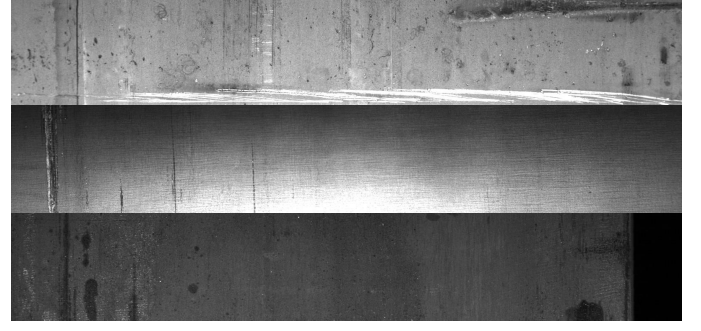


Fig. 12. Sample images before preprocessing.

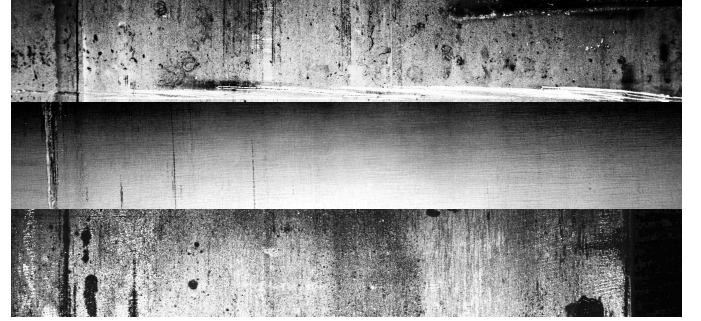


Fig. 13. Sample images after preprocessing.

Pictures 12 and 13 show the preprocessing output on some samples images. It is patently visible that the different light exposures of the three images are compensated through the histogram equalization.

V. DETECTOR

.... The first part of the architecture is a *detector* for region proposals.... Explain how to pick region of interests (ROI)....

A. Contour detection

B. Image Segmentation

Introduction to alpha shapes and cite article describing proper segmentation usign alpha shapes.... describe parameters and present limitations of such an approach in this practical application.... Therefore, bayesian optimization is proposed for alpha value.... Present table comparing different alpha values.... Explain evaluation scheme for alpha value optimization....

C. Bounding box

VI. CLASSIFIER

The ROIs are then fed into the second part of the proposed architecture, the *classifier*, and properly classified as flawless or flawed; in the latter, they are assigned a defect class.

The *classifier* is structured as a MC-CNN, which in general has a structure similar to the one in figure 14.

Firstly, the input image I is eventually preprocessed to extract n column input P .

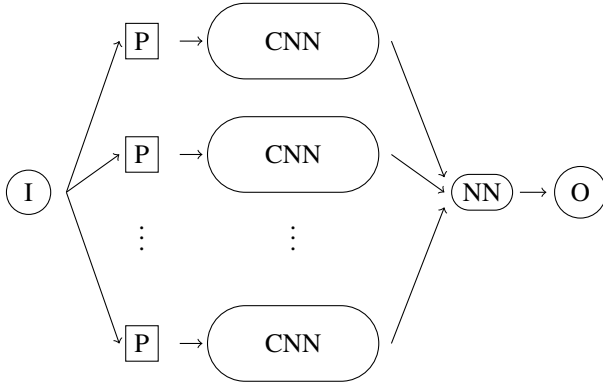


Fig. 14. General structure of a MC-CNN

Secondly, these P are fed into different CNNs in parallel, therefore independently.

Finally, the output of the MC-CNN columns is combined through a final classifier, e.g. a neural network (NN), to produce the appropriate output.

The choice of using a MC-CNN is due to several reasons, beyond the proved effectiveness described in [17].

Primarily, the training of a MC-CNN is highly parallelizable, indeed the different columns can learn separately one from another, once their corresponsive input is prepared.

Moreover, it is possible to merge both local and global information in a far easier way then using a traditional, single-column, CNN. Indeed, instead of focusing only on a rectangular area, which brings only the local information about the plausible defect, with a MC-CNN it is immediate to add another column concerning with the whole image.

This is the main point in favour of MC-CNN, since the class of a defect may be inferred using global patterns, such as the number of similar area. Imagine, for example, an error burst on the surface. Although traditional single-column CNNs may consider directly the input to the global column, this would face problems regarding the presence of multiple defects classes on the same surface. Therefore, a MC-CNN approach with some columns concerning local information and other focusing on global patterns is heuristically better.

However, in IX another approach to combine such information through a CNN is described. Although possible, is patently more convoluted then the MC-CNN approach. It would still be interesting to compare them in order to characterize the effectiveness.

Observe that the output of global column must be calculated only once per each image, since it is constant throughout the single surface, hence both the training and the predicting process can be lighten.

Finally, as an incidental outcome, it is possible to further study the amount of contribution of the different columns in accurately determining the defective class, if any, of the considered area. This considerations are reported in VIII.

The proposed MC-CNN has three columns, namely a *shape*, a *local* and a *global* column.



Fig. 15. Shape column input.

Fig. 16. Shape column CNN layers

A final consideration about the architecture training has to be done in order to comprehend the upper bound reported in VIII. Indeed, the *classifier* has been implemented before the *detector*. In fact, although the former relies on the latter for the ROIs and their relative features (described in VI-A, VI-B and VI-C), it has been preempting supposed to have an ideal *detector*, i.e. one which proposes the optimal ROIs.

This effort-outcome oriented approach has been done for two main reasons.

Firstly, this approach highlight the upper bound reachable with the whole architecture.

Secondly, dividing the *detector* outcome from the *classifier* input during the training allows to export the trained MC-CNN and to use it within the challengers architectures, explained in VII. This specifies the effectiveness of the *detector* proposed.

A. Shape column

The *shape column* is concerned to learn from the shape of the proposed region. This is fed into the CNN as a binary matrix, in which ones represent points in the border of the area.

An example of this binary images is given in figure 15. The shape is centered in a 1600×256 black image. Indeed, the size of the input is set to the largest area that could be found, i.e. a defect spanning over the entire surface. The shape is centered to ensure that the classifier is translation independent.

In order to provide also negative examples, i.e. flawless areas proposed by the *detector*, while training the *classifier* with ideal input, it is needed to generate those.

*** TODO DESCRIBE FAKE ELEMENTS GENERATION ***

The layers of this CNN are shown in 16. *** ... explanation, dimensioning, type of layers Stats on defects shapes.... ***

The output layer is a $n + 1$ vector, where n is the number of defect classes. Each entry of this vector describe the confidence of the network in considering the input shape as flawless or related to one of the n defect classes.

B. Local column

The *local column* is thought to consider luminance levels around the border of the defect, to learn from the local context wheter a region proposal is defective or not, and eventually its class.

Therefore, the column is fed with the grey scale portion of the image in which the considered region is. As an example, in figure 17 is illustrated a plausible input to the *local column*.



Fig. 17. Local column input.

Fig. 18. Local column CNN layers

This grey scale portion is generated from the shape of the region and the original image.

Firstly, the bounding box of the shape is calculated. Secondly, the original image outside the bounding box is discarded. Finally, the cropped image is centered in a black 1600×256 picture. The reasons behind the centering and the dimensioning of the input are the same described in VI-A.

The layers of this CNN are shown in 18. *** ... explanation ... Stats on defects shapes... ***

The output layer is analogous to the one in VI-A.

C. Global column

The *global column* is concerned in detecting global patterns like flaws burst. Hence, it is fed with the whole image. An example of input is shown in figure 19.

*** structure, explanation, output ***

*** MAYBE OUTPUT AS MULTIPLE COMBINATIONS CLASSES? ***

*** DESCRIBE STRUCTURE, RATIONALE BEHIND DIMENSIONING, USE DEFECT STATS ***

D. Final classifier

... the three columns are then combined....

... nn used to combine ... because manually tuning would be ineffective

The results of this architecture are shown in VIII.

VII. CHALLENGERS

.... explain the need for challengers

A. Sliding window

... explain briefly the approach

... image pyramids

B. Landmarks

... explain briefly the approach



Fig. 19. Global column input.

Fig. 20. Global column CNN layers

Fig. 21. Shape column confusion matrix on ideal input.

Fig. 22. Local column confusion matrix on ideal input.

C. Thresholding and location aggregation

... In both cases segmentation is needed Explain how from confidence value on different region of interests one can build the localization of defects area

VIII. RESULTS

Review the article, make some considerations on results

*** Confronto con esplicitamente indicati il contributo di ogni step al miglioramento del risultato ***

The whole system implementation can be found in the GitHub repository [38].

IX. FURTHER WORK

... provide suggestions to further work...

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Fig. 23. Global column confusion matrix on ideal input.

Fig. 24. Final classifier confusion matrix on ideal input.

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