

Introduction to Deep Learning (CS474)

Lecture 13

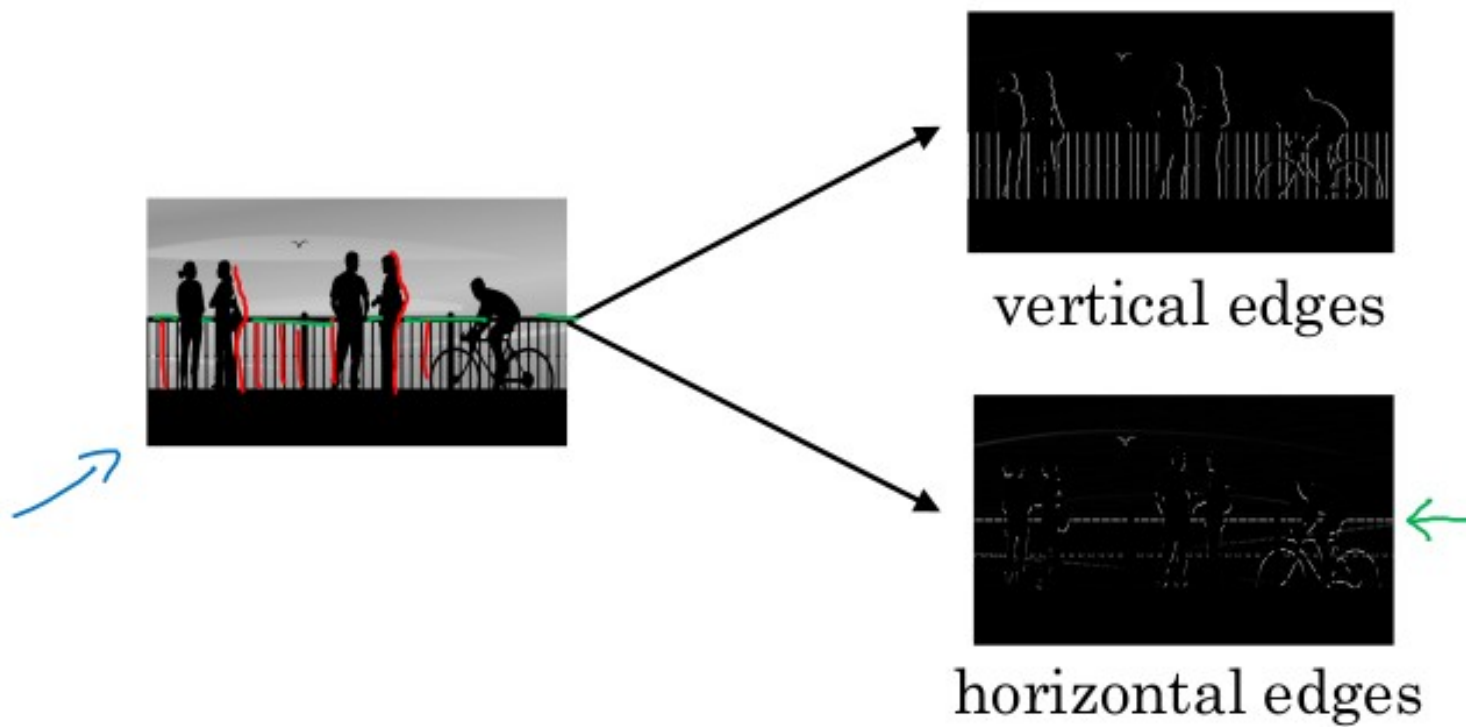
Outline

- **Module 2**
 - Understanding Convolutions

Introduction

- Let's get to the bottom of what convolutions are and how we can use them in our neural networks.
- If we want to recognize patterns corresponding to objects, like an airplane in the sky, we will likely need to look at how nearby pixels are arranged, and we will be less interested in how pixels that are far from each other appear in combination.
- Convolution is defined for a 2D image as the scalar product of a weight matrix, the kernel, with every neighborhood in the input.

Example



Slide credit: Prof. Andrew Ng

Example: Vertical Edge Detection

$$3 \times 1 + 1 \times 1 + 2 \times 1 + 0 \times 0 + 5 \times 0 + 7 \times 0 + 1 \times -1 + 8 \times -1 + 2 \times -1 = -5$$

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

6x6

"convolution"
↓
*

1	0	-1
1	0	-1
1	0	-1

3x3
filter

=

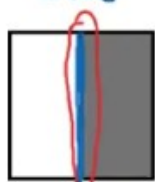
-5			

4x4

Example: Vertical Edge Detection

10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	<u>10</u>	<u>10</u>	<u>0</u>	0	0
10	<u>10</u>	<u>10</u>	<u>0</u>	0	0
10	<u>10</u>	<u>10</u>	<u>0</u>	0	0

6x6



*

1	0	-1
1	0	-1
1	0	-1

3x3

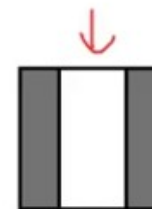
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0	30	30	0
0	30	30	0
0	30	30	0
0	<u>30</u>	<u>30</u>	0

4x4



Slide credit: Prof. Andrew Ng

Example: Vertical and Horizontal Edge Detection

1	0	-1
1	0	-1
1	0	-1

Vertical

1	1	1
0	0	0
-1	-1	-1

Horizontal

10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10

*

1	1	1
0	0	0
-1	-1	-1

=

0	0	0	0
30	10	-10	-30
30	10	-10	-30
0	0	0	0



Example:

1	0	-1
1	0	-1
1	0	-1



3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

→

1	0	-1
2	0	-2
1	0	-1

Sobel filter



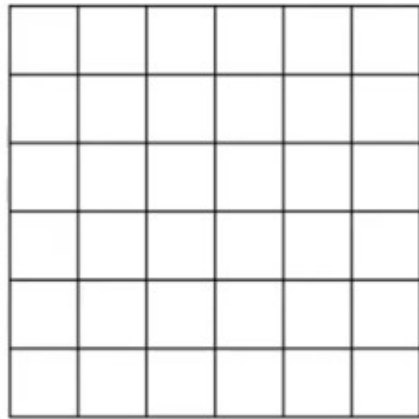
w_1	w_2	w_3
w_4	w_5	w_6
w_7	w_8	w_9



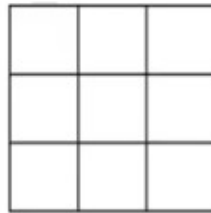
3	0	-3
10	0	-10
3	0	-3

Scharr filter

Problem with Earlier Set-Up



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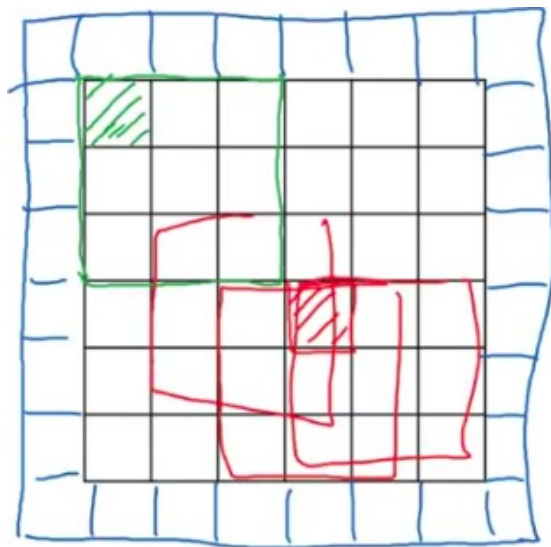
3×3
 $f \times f$

$\frac{6 \times 6}{n \times n}$

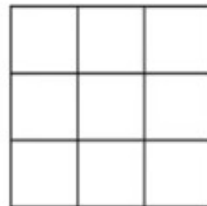
$n - f + 1 \times n - f + 1$
 $6 - 3 + 1 = 4$

$\rightarrow \underline{\underline{4 \times 4}}$

Padding



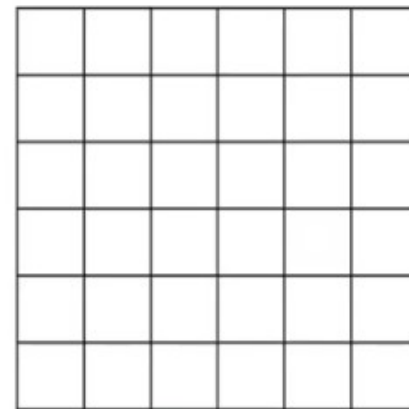
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$$3 \times 3$$

$$f \times f$$

=



$$6 \times 6$$

$$\frac{6 \times 6}{n \times n} \rightarrow 8 \times 8$$

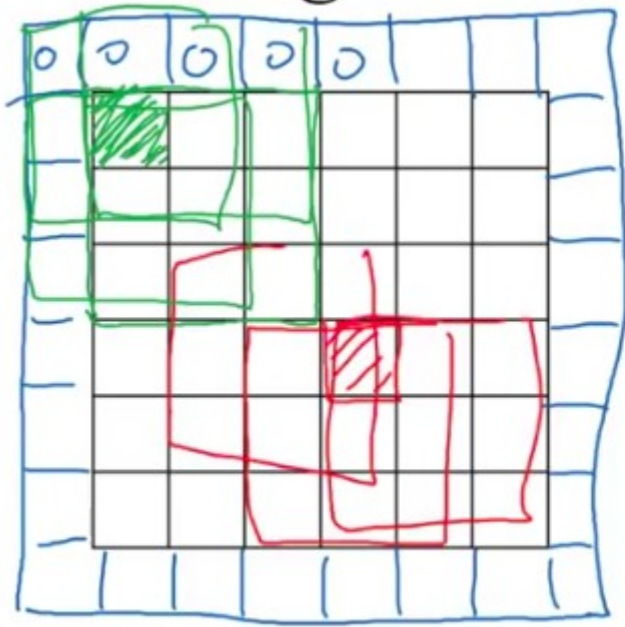
$$n - f + 1 \times n - f + 1$$

$$6 - 3 + 1 = 4$$

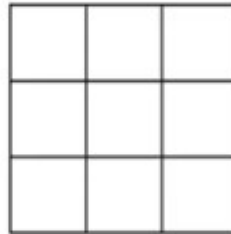
$$\rightarrow \cancel{4 \times 4}$$

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Padding

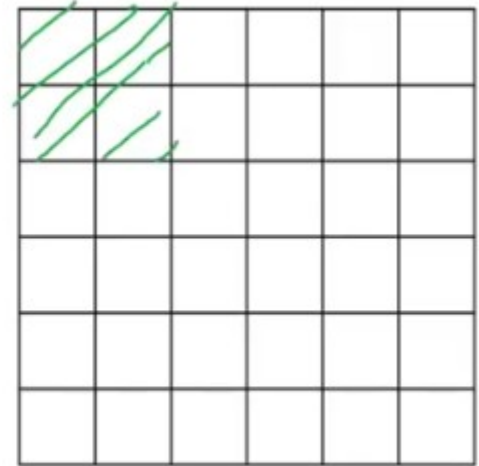


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3×3
 $f \times f$

=



Slide credit: Prof. Andrew Ng

Padding

→ no padding

“Valid”: $n \times n$ \times $f \times f$ $\rightarrow \frac{n-f+1}{4} \times \frac{n-f+1}{4}$
 6×6 \times 3×3 $\rightarrow 4 \times 4$

“Same”: Pad so that output size is the same as the input size. $[n+2p-f+1=n]$

References

- All the contents present in the slides are taken from various online resources. Due credit is given in the respective slides. These slides are used for *academic* purposes only.