

Notation

MIP formulation

- Variables

- Constraints

- Objective

Notation

- ▶ a set $T = \{0, \dots, m - 1\}$ of m machine types
- ▶ a set $P = \{0, \dots, n - 1\}$ of n time periods

Production variables

- ▶ $x_p^t \in \{0, 1\}$ for $t \in T$, $p \in P$ with $x_p^t = 1 \Leftrightarrow$ an item of machine type t is produced at time period p

State variables

- ▶ $y_p^t \in \{0, 1\}$ for $t \in T$, $p \in P$ with $y_p^t = 1 \Leftrightarrow$ the machine is ready to produce an item of machine type t at time period p .

Stock variables

- ▶ $s_p^t \in \mathbb{R}_{\geq 0}$ for $t \in T$, $p \in P \cup \{-1\}$ with $s_p^t = \ell$ representing that ℓ items of machine type t are kept in stock at time period p

Transition variables

- ▶ $u_p^{ij} \in \{0, 1\}$ for $i \in T, j \in T, p \in P$ with $u_p^{ij} = 1 \Leftrightarrow$ the production changes from machine type i to machine type j in time period p

Initial stock constraints

- ▶ ensure an empty stock for each machine type before production begins

$$s_{-1}^t = 0 \text{ for } t \in T \quad (1)$$

Demand constraints

- ▶ ensure that the demand for each machine type is met by production and stock
- ▶ let $d_p^t \in \{0, 1\}$ be the given demand of machine type t at time period p

$$s_{p-1}^t + x_p^t = d_p^t + s_p^t \text{ for } t \in T, p \in P \quad (2)$$

State constraints

- ▶ ensures that the machine is ready to produce machine type t at time period p when producing machine type t at p

$$x_p^t \leq y_p^t \text{ for } t \in T, p \in P \quad (3)$$

Configuration constraints

- ▶ ensure that the machine is in exactly one state at any time

$$\sum_{t \in T} y_p^t = 1 \text{ for } p \in P \quad (4)$$

Transition constraints

- ▶ ensure that the values of the transition variables are set correctly

$$u_p^{ij} \geq y_{p-1}^i + y_p^j - 1 \text{ for } i \in T, j \in T, p \in P \setminus \{0\} \quad (5)$$

Entire formulation

- ▶ let $h \in \mathbb{R}$ be the stocking cost representing the cost for stocking an item (of any machine type) for one time period
- ▶ let $c_{ij} \in \mathbb{R}$ for $i \in T, j \in T$ be the transition cost representing the cost for changing the machine configuration from machine type i to machine type j

$$\min \sum_{t \in T} \sum_{p \in P} h s_p^t + \sum_{i \in T} \sum_{j \in T} \sum_{p \in P \setminus \{0\}} c_{ij} u_p^{ij}$$

s.t. (1) – (5).