# Package 'dfrr'

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<b>Description</b> Implementing Function-on-Scalar Regression model in which the response function is dichotomized and observed sparsely. This package provides smooth estimations of functional regression coefficients and principal components for the dfrr model.
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dfrr-package

dfrr: Dichotomized Functional Response Regression

### **Description**

Implementing Function-on-Scalar Regression model in which the response function is dichotomized and observed sparsely. This package provides smooth estimations of functional regression coefficients and principal components for the dfrr model.

#### **Details**

Implementing Function-on-Scalar Regression model in which the response function is dichotomized and observed sparsely. This package provides smooth estimations of functional regression coefficients and principal components for the dfrr model. The main function in the dfrr-package is dfrr().

### Author(s)

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### References

Fatemeh Asgari, Alamatsaz Mohammad Hossein, Hayati Saeed (2021). Dichotomized Functional Response Regression Model. <a href="http://arxive.org/adress\_to\_paper">http://arxive.org/adress\_to\_paper</a>

### See Also

Useful links:

- https://github.com/asgari-fatemeh/dfrr
- Report bugs at https://github.com/asgari-fatemeh/dfrr/issues

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```
X=X,time=time)
dfrr_fit<-dfrr(Y~X,yind=time)</pre>
coefs<-coef(dfrr_fit)</pre>
  plot(coefs)
fitteds<-fitted(dfrr_fit)</pre>
  plot(fitteds)
resids<-residuals(dfrr_fit)</pre>
plot(resids)
fpcs<-fpca(dfrr_fit)</pre>
plot(fpcs,plot.contour=TRUE,plot.3dsurface = TRUE)
newdata < -data.frame(X=c(1,0))
  preds<-predict(dfrr_fit,newdata=newdata)</pre>
  plot(preds)
newdata<-data.frame(X=c(1,0))</pre>
newydata < -data.frame(.obs=rep(1,5),.index=c(0.0,0.1,0.2,0.3,0.7),.value=c(1,1,1,0,0))
preds<-predict(dfrr_fit,newdata=newdata,newydata = newydata)</pre>
plot(preds)
```

basis

Get the basis functions from a dfrr-object

### **Description**

Returns the basis functions employed in fitting a dfrr-object.

### Usage

```
basis(dfrr_fit)
```

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```
evaluated_coefs<-coefs%*%t(fda::eval.basis(time,basis))
#Plotting the regression coefficients
par(mfrow=c(1,2))
plot(time,evaluated_coefs[1,],1,main="Intercept")
plot(time,evaluated_coefs[2,],1,main="X")</pre>
```

coef.dfrr

Get estimated coefficients from a dfrr fit

### **Description**

Returns estimations of the smooth functional regression coefficients  $\beta(t)$ . The result is a matrix of either Fourier coefficients or evaluations. See Details.

### Usage

```
## S3 method for class dfrr
coef(
  object,
  standardized = NULL,
  unstandardized = !standardized,
  return.fourier.coefs = NULL,
  return.evaluations = !return.fourier.coefs,
  time_to_evaluate = NULL,
  ...
)
```

### **Arguments**

object a dfrr-object standardized, unstandardized

a boolean indicating whether stanadrdized/unstandardized regression coefficients are reported. Only standardized regression coefficients are identifiable, thus the arugment is defaults to standardized=TRUE.

return.fourier.coefs, return.evaluations

a boolean indicating whether the Fourier coefficients of regression coefficients are returned (return.fourier.coefs=TRUE), or evaluations of the regression coefficients (return.evaluations=TRUE). Defaults to return.fourier.coefs=TRUE.

dot argument, just for consistency with the generic function

### Details

This function will return either the Fourier coefficients or the evaluation of estimated coefficients. Fourier coefficients which are reported are based on the a set of basis which can be determined by basis(dfrr\_fit). Thus the evaluation of regression coefficients on the set of time points specified by vector time, equals to fitted(dfrr\_fit)%\*%t(eval.basis(time,basis(dfrr\_fit))).

Consider that the unstandardized estimations are not identifiable. So, it is recommended to extract and report the standardized estimations.

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### See Also

```
plot.coef.dfrr
```

### **Examples**

dfrr

Dichotomized Functional Response Regression

### **Description**

Implementing Function-on-Scalar Regression model, in which the response function is dichotomized and observed sparsely.

### Usage

```
dfrr(
  formula,
  yind = NULL,
  data = NULL,
  ydata = NULL,
  method = c("REML", "ML"),
  rangeval = NULL,
  basis = NULL,
  times_to_evaluate = NULL,
  ...
)
```

### **Arguments**

formula an object of class "formula" (or one that can be coerced to that class with

as. formula: a symbolic description of the model to be fitted.

yind a vector with length equal to the number of columns of the matrix of functional

responses giving the vector of evaluation points  $(t_1,...,t_G)$ . If not supplied,

yind is set to 1:ncol(<response>).

data an (optional) data. frame containing the covariate data. the variable terms will

be searched from the columns of data, covariates also can be read from the

workspace if it is not available in data.

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ydata an (optional) data. frame consists of three columns .obs, .index and .value,

supplying the functional responses that are not observed on a regular grid. ydata

must be provided if the sampling design is irregular.

method detrmines the estimation method of functional parameters. Defaults to "REML"

estimation.

rangeval an (optional) vector of length two, indicating the lower and upper limit of the

domain of latent functional response. If not specified, it will set by minimum

and maximum of yind or .index column of ydata.

basis an (optional) object of class basisfd. Defaults to cubic bspline basis.

times\_to\_evaluate

a numeric vector indicating the set of time points for evaluating the functional

regression coefficients and principal components.

... other arguments that can be passed to the inner function AMCEM.

#### **Details**

The output is a dfrr-object, which then can be injected into other methods/functions to postprocess the fitted model, including: coef.dfrr,fitted.dfrr, basis, residuals.dfrr, predict.dfrr, fpca, summary.dfrr, model.matrix.dfrr,plot.coef.dfrr,plot.fitted.dfrr,plot.residuals.dfrr,plot.predict.dfrr,plot.fpca.dfrr

```
set.seed(2000)
N < -50; M < -24
X<-rnorm(N,mean=0)</pre>
time<-seq(0,1,length.out=M)</pre>
Y<-simulate_simple_dfrr(beta0=function(t){cos(pi*t+pi)},
                           beta1=function(t){2*t},
                           X=X,time=time)
dfrr_fit<-dfrr(Y~X,yind=time)</pre>
plot(dfrr_fit)
##### Fitting dfrr model to the Madras Longitudinal Schizophrenia data
data(madras)
ids<-unique(madras$id)</pre>
N<-length(ids)
ydata<-data.frame(.obs=madras$id,.index=madras$month,.value=madras$y)</pre>
xdata<-data.frame(Age=rep(NA,N),Gender=rep(NA,N))</pre>
for(i in 1:N){
  dt<-madras[madras$id==ids[i],]</pre>
  xdata[i,]<-c(dt$age[1],dt$gender[1])</pre>
rownames(xdata)<-ids</pre>
madras_dfrr<-dfrr(Y~Age+Gender+Age*Gender, data=xdata, ydata=ydata, J=11)</pre>
coefs<-coef(madras_dfrr)</pre>
plot(coefs)
```

fitted.dfrr 7

```
fpcs<-fpca(madras_dfrr)
plot(fpcs)
plot(fpcs,plot.eigen.functions=FALSE,plot.contour=TRUE,plot.3dsurface = TRUE)

par(mfrow=c(2,2))
fitteds<-fitted(madras_dfrr) #Plot first four fitted functions
    plot(fitteds,id=c(1,2,3,4))

resids<-residuals(madras_dfrr)
plot(resids)

newdata<-data.frame(Age=c(1,1,0,0),Gender=c(1,0,1,0))
    preds<-predict(madras_dfrr,newdata=newdata)
    plot(preds)

newdata<-data.frame(Age=c(1,1,0,0),Gender=c(1,0,1,0))
newydata<-data.frame(.obs=rep(1,5),.index=c(0,1,3,4,5),.value=c(1,1,1,0,0))
preds<-predict(madras_dfrr,newdata=newdata,newydata = newydata)
plot(preds)</pre>
```

fitted.dfrr

Obtain fitted curves for a dfrr model

### **Description**

Fitted curves refer to the estimations of latent functional response curves. The results can be either the Fourier coefficients or evaluation of the fitted functions. See Details.

### Usage

```
## S3 method for class dfrr
fitted(
  object,
  return.fourier.coefs = NULL,
  return.evaluations = !return.fourier.coefs,
  time_to_evaluate = NULL,
  standardized = NULL,
  unstandardized = !standardized,
  ...
)
```

### **Arguments**

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```
time_to_evaluate
```

a numeric vector indicating the set of time points for evaluating the fitted latent functions, for the case of return.evaluations=TRUE.

standardized, unstandardized

a boolean indicating whether stanadrdized/unstandardized fitted latent curves is reported. Only standardized fitted curves are identifiable, thus the arugment is defaults to standardized=TRUE.

... dot argument, just for consistency with the generic function

### **Details**

This function will return either the Fourier coefficients or the evaluation of fitted curves to the binary sequences. Fourier coefficients which are reported are based on the a set of basis which can be determined by basis(dfrr\_fit). Thus the evaluation of fitted latent curves on the set of time points specified by vector time, equals to fitted(dfrr\_fit)%\*%t(eval.basis(time,basis(dfrr\_fit))).

Consider that the unstandardized estimations are not identifiable. So, it is recommended to extract and report the standardized estimations.

#### See Also

```
plot.fitted.dfrr
```

### **Examples**

fpca

Functional principal component analysis of a dfrr fit

### Description

fpca() returns estimations of the smooth principal components/eigen-functions and the corresponding eigen-values of the residual function in the dfrr model. The result is a named list containing the vector of eigen-values and the matrix of Fourier coefficients. See Details.

```
fpca(dfrr_fit, standardized = NULL, unstandardized = !standardized)
```

fpca 9

### **Arguments**

standardized, unstandardized

a boolean indicating whether stanadrdized/unstandardized pricipal components/eigen-functions are reported. Only standardized pricipal components/eigen-functions are identifiable, thus the arugment is defaults to standardized=TRUE.

#### **Details**

Fourier coefficients which are reported are based on the a set of basis which can be determined by basis(dfrr\_fit). Thus the evaluation of pricipal component/eigen-function on the set of time points specified by vector time, equals to fpca(dfrr\_fit)%\*%t(eval.basis(time,basis(dfrr\_fit))).

Consider that the unstandardized estimations are not identifiable. So, it is recommended to extract and report the standardized estimations.

### Value

fpca(dfrr\_fit) returns a list containtng the following components:

values a vector containing the eigen-values of the standardized/unstandardized covari-

ance operator of the residual function term in dfrr model, sorted in decreasing

order.

vectors a matrix whose columns contain the Fourier coefficients of the principal components/eigen-

functions of the standaridized/unstandardized covariance operator of the residual function term in dfrr model, sorted based on the corresponding eigen-

values.

### See Also

```
plot.fpca.dfrr
```

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madras

Madras Longitudinal Schizophrenia Study.

### **Description**

Monthly records of presence/abscence of psychiatric symptom 'thought disorder' of 86 patients over the first year after initial hospitalisation for disease.

### Usage

madras

#### **Format**

A data frame with 1032 observations and 5 variables

id identification number of a patient

y response 'thought disorder': 0 = absent, 1 = present

month month since hospitalisation

age age indicator: 0 = less than 20 years, 1 = 20 or over

**gender** sex indicator: 0 = male, 1 = female

#### **Source**

Diggle PJ, Heagerty P, Liang KY, Zeger SL (2002). The analysis of Longitudinal Data, second ed., pp. 234-43. Oxford University Press, Oxford.

<a href="http://faculty.washington.edu/heagerty/Books/AnalysisLongitudinal/datasets.html">http://faculty.washington.edu/heagerty/Books/AnalysisLongitudinal/datasets.html</a>

### References

Jokinen J. Fast estimation algorithm for likelihood-based analysis of repeated categorical responses. *Computational Statistics and Data Analysis* 2006; 51:1509-1522.

model.matrix.dfrr

Obtain model matrix for a dfrr fit

### **Description**

Obtain model matrix for a dfrr fit

### Usage

```
## S3 method for class dfrr
model.matrix(object, ...)
```

### **Arguments**

```
object a dfrr-object
```

... dot argument, just for consistency with the generic function

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plot.coef.dfrr

Plot dfrr coefficients

### Description

Plot a coef.dfrr object. The output is the plot of regression coefficients.

### Usage

```
## S3 method for class coef.dfrr
plot(x, select = NULL, ask.hit.return = TRUE, ...)
```

### **Arguments**

```
x a coef.dfrr-object.

select a vector of length one or more of indices of regression coefficients to plot.

ask.hit.return a boolean indicating whether to wait for interaction of the user between any two plots.

... graphical parameters passed to plot.
```

### **Examples**

plot.dfrr

Plot a dfrr fit

### **Description**

Plot the regression coefficients, principal components, kernel function and residuals of a dfrr-object.

```
## S3 method for class dfrr plot(x, ...)
```

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### **Arguments**

... graphical parameters passed to plot.coef.dfrr

### **Details**

The contour plot of the kernel function is produced if the package ggplot2 is installed. Plotting the 3d surface of the kernel function is also depends on the package plotly. To produce the qq-plot, the package car must be installed.

### **Examples**

plot.fitted.dfrr

Plot dfrr fitted latent functions

### Description

Plot a fitted.dfrr object.

```
## S3 method for class fitted.dfrr
plot(
    X,
    id = NULL,
    main = NULL,
    col = "blue",
    lwd = 2,
    lty = "solid",
    cex.circle = 1,
    col.circle = "black",
    ylim = NULL,
    ...
)
```

plot.fpca.dfrr 13

### **Arguments**

```
x the output of the function fitted.dfrr

id a vector of length one or more containing subject ids to plot. Must be matched with rownames(<response>) or the .obs column of ydata. Defaults to all subject ids.

main a vector of length one or length(id) containing the title of plots.

col, lwd, lty, ... graphical parameters passed to plot

cex.circle, col.circle size and color of circles and filled circles.

ylim a vector of length two indicating the range of y-axis of the plot.
```

### **Details**

The output is the plot of latent curves over the observed binary sequence. The binary sequence is illustrated with circles and filled circles for the values of zero and one, respectively.

### **Examples**

plot.fpca.dfrr

Plot dfrr functional principal components

### **Description**

Plot a fpca.dfrr object.

14 plot.fpca.dfrr

```
plot.3dsurface.pars = list(xlab = NULL, ylab = NULL, zlab = NULL, title = NULL,
    colors = NULL),
    ask.hit.return = TRUE,
    ...
)
```

### **Arguments**

```
a fpca.dfrr-object to be plotted. It is the output of the function fpca()
plot.eigen.functions
                  a boolean indicating whether to print the principal components/eigen-functions.
                  Defaults to TRUE.
select
                  a vector of length one or more of indices of eigenfunctions to be plotted.
                  a boolean indicating whether to print the contour plot of the kernel function. It
plot.contour
                  requires ggplot2-package to be installed. Defaults to FALSE.
plot.3dsurface a boolean indicating whether to print the 3d surface plot of the kernel function.
                  It requires the package plotly to be installed. Defaults to FALSE.
plot.contour.pars
                  a named list of graphical parameters passed to the function ggplot.
plot.3dsurface.pars
                  a named list of graphical parameters passed to the function plot_ly.
ask.hit.return a boolean indicating whether to wait for interaction of the user between any two
                  plots.
                  graphical parameters passed to plot function in drawing 2D eigenfunctions.
. . .
```

### **Details**

This function plots the functional principal components, contour plot and 3d surface of the kernel function.

If ggplot2-package is installed, the contour plot of the kernel function is produced by setting the argument plot.contour=TRUE. Some graphical parameters of the contour plot can be modified by setting the (optional) argument plot.contour.pars.

If the package plotly is installed, the 3d surface of the kernel function is produced by setting the argument plot.3dsurface=TRUE. Some graphical parameters of the 3d surface can be modified by setting the (optional) argument plot.3dsurface.pars.

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plot.predict.dfrr Plot dfrr predictions

### **Description**

Plot a predict.dfrr object.

### Usage

```
## $3 method for class predict.dfrr
plot(
    X,
    id = NULL,
    conf.band.type = "BEc",
    conf.level = NULL,
    main = id,
    col = "blue",
    lwd = 2,
    lty = "solid",
    cex.circle = 1,
    col.circle = "black",
    ylim = NULL,
    ...
)
```

### **Arguments**

```
a predict.dfrr-object
Х
id
                  a vector of length one or more containing subject ids to plot. Must be matched
                  with rownames (newdata). Defaults to all subject ids.
conf.band.type a type of confidence band specified in package fregion. Can be either NULL
                  for omitting the confidence band from the plot, "BEc" for modified Scheffe
                  style band constructing from a hyper-ellipsoid region, "Bs" for Parametric boot-
                  strap simultaneous confidence band, or any other conf.band.type acceptable
                  to package fregion. Defaults to NULL. See References.
                  Confidence bands are drawn if the conf.level argument is set to a valid value
                  in the interval (0,1).
conf.level
                  confidence levels for the bands to achieve. Defaults to NULL.
main
                  a vector of length one or length(id) containing the title of plots.
col, lwd, lty, ...
                  graphical parameters passed to plot
cex.circle, col.circle
                  size and color of circles and filled circles.
                  a vector of length two indicating the range of y-axis of the plot.
ylim
```

#### **Details**

The output is the plot of predictions of latent functions given the new covariates. For the case in which newydata is also given, the predictions are plotted over the observed binary sequence. The binary sequence is illustrated with circles and filled circles for the values of zero and one, respectively. Confidence bands can also be added to the plot if the package fregion is installed.

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#### References

Choi, H., & Reimherr, M. A geometric approach to confidence regions and bands for functional parameters . *Journal of the Royal Statistical Society, Series B Statistical methodology* 2018; 80:239-260.

### **Examples**

plot.residuals.dfrr QQ-plot for dfrr residuals

### **Description**

The output gives the qq-plot of estimated measurment error.

### Usage

```
## S3 method for class residuals.dfrr plot(x, ...) ## S3 method for class dfrr qq(x, ...)
```

### **Arguments**

```
x a residuals.dfrr-object.... graphical parameters passed to car::qqPlot
```

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### **Examples**

predict.dfrr

Prediction for dichotomized function-on-scalar regression

### **Description**

Takes a dfrr-object created by dfrr() and returns predictions given a new set of values for a model covariates and an optional ydata-like data. frame of observations for the dichotomized response.

### Usage

```
## S3 method for class dfrr
predict(
  object,
  newdata,
  newydata = NULL,
  standardized = NULL,
  unstandardized = !standardized,
  return.fourier.coefs = NULL,
  return.evaluations = !return.fourier.coefs,
  time_to_evaluate = NULL,
  ...
)
```

### **Arguments**

object a fitted dfrr-object obtained from invoking the function dfrr.

newdata a data. frame containing the values of all of the model covariates at which the

latent functional response is going to be predicted.

newydata (optional) a ydata-like data. frame containing the values of dichotomized re-

sponse sparsly observed in the domain of function.

standardized, unstandardized

a boolean indicating whether stanadrdized/unstandardized predictions are re-

ported. Defaults to standardized=TRUE.

qq

#### **Details**

This function will return either the Fourier coefficients or the evaluation of predictions. Fourier coefficients which are reported are based on the a set of basis which can be determined by basis(dfrr\_fit). Thus the evaluation of predictions on the set of time points specified by vector time, equals to fitted(dfrr\_fit,return.fourier.coefs=T)%\*%t(eval.basis(time,basis(dfrr\_fit))).

### See Also

```
plot.predict.dfrr
```

### **Examples**

qq

qq-plot Generic function

### **Description**

This is a generic function for qq() method.

```
qq(x, ...)
```

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### **Arguments**

x an object

... extra parameters passed to S3 methods

residuals.dfrr

Obtain residuals for a dfrr model

### Description

Returns the residuals of a fitted dfrr model. A dfrr model is of the form:

$$Y_i(t) = I(W_i(t) > 0),$$

in which I(.) is the indicator function and  $W_i(t) = Z_i(t) + \epsilon_i(t) \times \sigma^2$ , where  $Z_i(t)$  is the functional part of the model and  $epsilon_i(t) \times \sigma^2$  is the measurement error. The functional part of the model, consisting a location and a residual function of the form:

$$Z_i(t) = \sum_{j=1}^{q} \beta_j(t) * x_{ji} + \varepsilon_i(t),$$

and  $\epsilon_i(t)$  are iid standard normal for each i and t. The residuals reported in the output of this functions is the estimation of the measurement error of the model i.e.  $\epsilon_i(t) \times \sigma^2$ , which is estimated by:

$$E(W_i(t) - Z_i(t) \mid Y_i(t)).$$

#### Usage

```
## S3 method for class dfrr
residuals(object, standardized = NULL, unstandardized = !standardized, ...)
```

### **Arguments**

object a fitted dfrr-object obtained from invoking the function dfrr. standardized, unstandardized

a boolean indicating whether stanadrdized/unstandardized residuals are reported. Defaults to standardized=TRUE.

dot argument, just for consistency with the generic function

### See Also

```
plot.residuals.dfrr,qq.dfrr
```

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```
X=X,time=time)
dfrr_fit<-dfrr(Y~X,yind=time)
resid<-residuals(dfrr_fit)
plot(resid)
#qq(dfrr_fit)</pre>
```

simulate\_simple\_dfrr Simulating a Simple dfrr Model

### **Description**

Simulation from a simple dfrr model:

$$Y_i(t) = I(\beta_0(t) + \beta_1(t) * x_i + \varepsilon_i(t) + \epsilon_i(t) \times \sigma^2 > 0),$$

where I(.) is the indicator function,  $\varepsilon_i$  is a Gaussian random function, and  $\epsilon_i(t)$  are iid standard normal for each i and t independent of  $\varepsilon_i$ . For demonstration purpose only.

### Usage

```
simulate_simple_dfrr(
  beta0 = function(t) {       cos(pi * t + pi) },
  beta1 = function(t) {       2 * t },
      X = rnorm(50),
      time = seq(0, 1, length.out = 24),
      sigma2 = 0.2
)
```

### **Arguments**

beta0, beta1 (optional) functional intercept and slope parameters

X an (optional) vector consists of scalar covariate

time an (optional) vector of time points for which, each sample curve is observed at.

sigma2 variance of the measurement error in the dfrr model

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summary.dfrr

Summary for a dfrr fit

### Description

Summarise a fitted dfrr-object. Not implemented.

### Usage

```
## S3 method for class dfrr
summary(object, ..)
```

### Arguments

object a dfrr-object

... dot argument, just for consistency with the generic function

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