
CRRLpy Documentation

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Contents:

CRRLPY

Tools for processing Carbon **R**adio **R**ecombination **L**ine spectra.

The models are not shipped with the modules and scripts.

The documentation can be found in: <http://astrofle.github.io/CRRLpy/>

CRRLPY.CRRLS MODULE

`crrlpy.crrls.alphanum_key(s)`

Turn a string into a list of string and number chunks.

Parameters *s* – String

Returns List with strings and integers.

Return type `list`

Example

```
>>> alphanum_key("z23a")
["z", 23, "a"]
```

`crrlpy.crrls.average(data, axis, n)`

Averages data along the given axis by combining n adjacent values.

Parameters

- **data** (*numpy array*) – Data to average along a given axis.
- **axis** (*int*) – Axis along which to average.
- **n** (*int*) – Factor by which to average.

Returns Data decimated by a factor n along the given axis.

Return type `numpy array`

`crrlpy.crrls.best_match_idx(value, array)`

Searchs for the index of the closest entry to value inside an array.

Parameters

- **value** (*float*) – Value to find inside the array.
- **array** (*list or numpy.array*) – List to search for the given value.

Returns Best match index for the value inside array.

Return type `float`

Example

```
>>> a = [1, 2, 3, 4]
>>> best_match_idx(3, a)
2
```

`crrlpy.crrls.best_match_idx_tol(value, array, tol)`

Searchs for the best match to a value inside an array given a tolerance.

Parameters

- **value** (*float*) – Value to find inside the array.
- **tol** (*float*) – Tolerance for match.
- **array** (*numpy.array*) – List to search for the given value.

Returns Best match for val inside array.

Return type *float*

`crrlpy.crrls.best_match_value(value, array)`
Searchs for the closest occurrence of value in array.

Parameters

- **value** (*float*) – Value to find inside the array.
- **array** (*list or numpy.array*) – List to search for the given value.

Returns Best match for the value inside array.

Return type *float*.

Example

```
>>> a = [1,2,3,4]
>>> best_match_value(3.5, a)
3
```

`crrlpy.crrls.blank_lines(freq, tau, reffreqs, v0, dv)`
Blanks the lines in a spectra.

Parameters

- **freq** (*array, MHz*) – Frequency axis of the spectra.
- **tau** (*array*) – Optical depth axis of the spectra.
- **reffreqs** (*list*) – List with the reference frequency of the lines. Should be the rest frequency.
- **v0** (*float*) – Velocity shift to apply to the lines defined by *reffreq*. (km/s)
- **dv** (*float*) – Velocity range to blank around the lines. (km/s)

`crrlpy.crrls.blank_lines2(freq, tau, reffreqs, dv)`
Blanks the lines in a spectra.

Parameters

- **freq** (*array*) – Frequency axis of the spectra. (MHz)
- **tau** (*array*) – Optical depth axis of the spectra.
- **reffreqs** (*list*) – List with the reference frequency of the lines. Should be the rest frequency.
- **dv** (*float*) – Velocity range to blank around the lines. (km/s)

`crrlpy.crrls.df2dv(f0, df)`
Convert a frequency delta to a velocity delta given a central frequency.

Parameters

- **f0** (*float*) – Rest frequency. (Hz)
- **df** (*float*) – Frequency delta. (Hz)

Returns The equivalent velocity delta for the given frequency delta.

Return type float in Hz

`crrlpy.crpls.dv2df(f0, dv)`

Convert a velocity delta to a frequency delta given a central frequency.

Parameters

- **f0** (*float*) – Rest frequency. (Hz)
- **dv** (*float*) – Velocity delta. (m/s)

Returns The equivalent frequency delta for the given velocity delta.

Return type float in m s^{-1}

`crrlpy.crpls.dv_minus_doppler(dV, ddV, dD, ddD)`

Returns the Lorentzian contribution to the line width assuming that the line has a Voigt profile.

Parameters

- **dV** (*float*) – Total line width
- **ddV** (*float*) – Uncertainty in the total line width.
- **dD** (*float*) – Doppler contribution to the line width.
- **ddD** – Uncertainty in the Doppler contribution to the line width.

Returns The Lorentz contribution to the total line width.

Return type float

`crrlpy.crpls.dv_minus_doppler2(dV, ddV, dD, ddD)`

Returns the Lorentzian contribution to the line width assuming that the line has a Voigt profile.

Parameters

- **dV** (*float*) – Total line width
- **ddV** (*float*) – Uncertainty in the total line width.
- **dD** (*float*) – Doppler contribution to the line width.
- **ddD** – Uncertainty in the Doppler contribution to the line width.

Returns The Lorentz contribution to the total line width.

Return type float

`crrlpy.crpls.f2n(f, line, n_max=1500)`

Converts a given frequency to a principal quantum number n for a given line.

Parameters

- **f** (*array*) – Frequency to convert. (MHz)
- **line** (*string*) – The equivalent n will be referenced to this line.
- **n_max** (*int*) – Maximum n number to include in the search. (optional, Default 1)

Returns Corresponding n for a given frequency and line. If the frequency is not an exact match, then it will return an empty array.

Return type array

`crrlpy.crpls.find_lines_sb(freq, line, z=0, verbose=False)`

Finds if there are any lines of a given type in the frequency range. The line frequencies are corrected for redshift.

Parameters

- **freq** (*array*) – Frequency axis in which to search for lines.
- **line** (*string*) – Line type to search for.
- **z** (*float*) – Redshift to apply to the rest frequencies.
- **verbose** (*bool*) – Verbose output?

Returns Lists with the principal quantum number and the reference frequency of the line. The frequencies are redshift corrected in MHz.

Return type array.

Example

```
>>> freq = [10, 11]
>>> ns, rf = crrls.find_lines_sb(freq, 'CIalpha')
>>> ns
array([[ 843.,  844.,  845.,  846.,  847.,  848.,  849.,  850.,  851.,
        852.,  853.,  854.,  855.,  856.,  857.,  858.,  859.,  860.,
        861.,  862.,  863.,  864.,  865.,  866.,  867.,  868.,  869.]])
```

`crrlpy.crpls.fit_continuum(x, y, degree, p0)`

Divide tb by given a model and starting parameters p0. Returns: tb/model - 1

`crrlpy.crpls.fit_model(x, y, model, p0, wy=None, mask=None)`

Fits a model to the data defined by x and y. It uses p0 as starting values.

Parameters

- **x** (*array*) – Abscissa values of the data to be fit.
- **y** (*array*) – Ordinate values of the data to be fit.
- **model** (*callable*) – Model to be fit.
- **p0** (*dict*) – Dictionary with the starting values for the fit.
- **wy** (*array*) – Weights of the ordinate values. (Optional)
- **mask** (*array*) – Mask to apply to the x and y values. (Optional)

Returns An object containing the results of the fit.

Return type `lmfit.model.ModelResult`

`crrlpy.crpls.freq2vel(f0, f)`

Convert a frequency axis to a velocity axis given a central frequency. Uses the radio definition of velocity.

Parameters

- **f0** (*float*) – Rest frequency for the conversion. (Hz)
- **f** (*numpy array*) – Frequencies to be converted to velocity. (Hz)

Returns f converted to velocity given a rest frequency f_0 .

Return type numpy array

`crrlpy.crpls.fwhm2sigma(fwhm)`

Converts a FWHM to the standard deviation, σ of a Gaussian distribution.

Parameters **fwhm** (*array*) – FWHM of the Gaussian.

Returns Equivalent standard deviation of a Gaussian with a Full Width at Half Maximum *fwhm*.

Return type array

Example

```
>>> 1/fwhm2sigma(1)
2.3548200450309493
```

`crrlpy.crrls.gauss_area(amplitude, sigma)`

Returns the area under a Gaussian of a given amplitude and sigma.

Parameters

- **amplitude** – Amplitude of the Gaussian, A .
- **sigma** (*array*) – Standard deviation fo the Gaussian, σ .

Returns The area under a Gaussian of a given amplitude and standard deviation.

Return type *array*

`crrlpy.crrls.gauss_area_err(amplitude, amplitude_err, sigma, sigma_err)`

Returns the error on the area of a Gaussian of a given *amplitude* and *sigma* with their corresponding errors. It assumes no correlation between *amplitude* and *sigma*.

Parameters

- **amplitude** (*array*) – Amplitude of the Gaussian.
- **amplitude_err** (*array*) – Error on the amplitude.
- **sigma** – Standard deviation of the Gaussian.
- **sigma_err** – Error on sigma.

Returns The error on the area.

Return type *array*

`crrlpy.crrls.gaussian(x, sigma, center, amplitude)`

Gaussian function in one dimension.

Parameters

- **x** (*array*) – x values for which to evaluate the Gaussian.
- **sigma** (*float*) – Standard deviation of the Gaussian.
- **center** (*float*) – Center of the Gaussian.
- **amplitude** (*float*) – Amplitude of the Gaussian.

Returns Gaussian function of the given amplitude and standard deviation evaluateated at x.

Return type *array*

`crrlpy.crrls.get_axis(header, axis)`

Constructs a cube axis.

Parameters

- **header** (*pyfits header*) – Fits cube header.
- **axis** (*int*) – Axis to reconstruct.

Returns cube axis

Return type numpy array

`crrlpy.crrls.get_line_mask(freq, reffreq, v0, dv)`

Return a mask with ranges where a line is expected in the given frequency range for a line with a given reference frequency at expected velocity v0 and line width dv0.

Parameters

- **freq** (*numpy array or list*) – Frequency axis where the line is located.
- **reffreq** (*float*) – Reference frequency for the line.
- **v0** (*float, km/s*) – Velocity of the line.
- **dv** (*float, km/s*) – Velocity range to mask.

Returns Mask centered at the line center and width *dv0* referenced to the input *freq*.

```
crrlpy.crpls.get_line_mask2(freq, reffreq, dv)
```

Return a mask with ranges where a line is expected in the given frequency range for a line with a given reference frequency and line width *dv*.

Parameters

- **freq** (*numpy array or list*) – Frequency axis where the line is located.
- **reffreq** (*float*) – Reference frequency for the line.
- **dv** (*float, km/s*) – Velocity range to mask.

Returns Mask centered at the line center and width *dv0* referenced to the input *freq*.

```
crrlpy.crpls.get_min_sep(array)
```

Get the minimum element separation in an array.

Parameters **array** (*array*) – Array where the minimum separation is wanted.

Returns The minimum separation between the elements in *array*.

Return type *float*

```
crrlpy.crpls.get_rchi2(x_obs, x_mod, y_obs, y_mod, dy_obs, dof)
```

Computes the reduced χ squared, $\chi^2_\nu = \chi^2/dof$.

Parameters

- **x_obs** (*array*) – Abscissa values of the observations.
- **x_mod** (*array*) – Abscissa values of the model.
- **y_obs** (*array*) – Ordinate values of the observations.
- **y_mod** (*array*) – Ordinate values of the model.
- **dy_obs** (*array*) – Error on the ordinate values of the observations.
- **dof** (*float*) – Degrees of freedom.

```
crrlpy.crpls.get_rms(data, axis=None)
```

Computes the rms of the given data.

Parameters

- **data** (*numpy array or list*) – Array with values where to compute the rms.
- **axis** (*int*) – Axis over which to compute the rms. Default: None

Returns The rms of data.

$$\text{rms} = \sqrt{\langle \text{data} \rangle^2 + V[\text{data}]}$$

where *V* is the variance of the data.

```
crrlpy.crpls.is_number(str)
```

Checks whether a string is a number or not.

Parameters *str* (*string*) – String.

Returns True if *str* can be converted to a float.

Return type bool

Example

```
>>> is_number('10')
True
```

`crrlpy.crpls.linear(x, a, b)`
Linear model.

Parameters

- **x** (*array*) – x values where to evaluate the line.
- **a** (*float*) – Slope of the line.
- **b** (*float*) – y value for x equals 0.

Returns A line defined by $ax + b$.

Return type array

`crrlpy.crpls.load_model(prop, specie, temp, dens, other=None)`
Loads a model for the CRRL emission.

`crrlpy.crpls.load_ref(specie, trans)`
Loads the reference spectrum for the specified atomic specie and transition. Available species and transitions: CI alpha CI beta CI delta CI gamma CI13 alpha HeI alpha HeI beta HI alpha HI beta SI alpha SI beta

`crrlpy.crpls.load_ref2(transition)`
Loads the reference spectrum for the specified atomic specie and transition. Available transitions: CIalpha CIbeta CIDelta CIGamma CI13alpha HeIalpha HeIbeta HIalpha HIBeta SIalpha SIBeta

`crrlpy.crpls.lookup_freq(n, specie, trans)`
Returns the frequency of a given transition.

`crrlpy.crpls.lorentz_width(n, ne, Te, Tr, W, dn=1)`
Gives the Lorentzian line width due to a combination of radiation and collisional broadening. The width is the FWHM in Hz. It uses the models of Salgado et al. (2015).

Parameters

- **n** (*array*) – Principal quantum number for which to evaluate the Lorentz widths.
- **ne** (*float*) – Electron density to use in the collisional broadening term.
- **Te** (*float*) – Electron temperature to use in the collisional broadening term.
- **Tr** (*float*) – Radiation field temperature.
- **W** (*float*) – Cloud covering factor used in the radiation broadening term.
- **dn** (*int*) – Separation between the levels of the transition. e.g., $dn=1$ for CIalpha.

Returns The Lorentz width of a line due to radiation and collisional broadening.

Return type array

`crrlpy.crpls.mask_outliers(data, m=2)`
Masks values larger than m times the data median. This is similar to sigma clipping.

Parameters **data** (*array*) – Data to mask.

Returns An array of the same shape as data with True where the data should be flagged.

Return type array

Example

```
>>> data = [1,2,3,4,5,6]
>>> mask_outliers(data, m=1)
array([ True, False, False, False, False,  True], dtype=bool)
```

`crrlpy.crrls.n2f(n, line, n_min=1, n_max=1500, unitless=True)`

Converts a given principal quantum number *n* to the frequency of a given line.

`crrlpy.crrls.natural_sort(list)`

Sort the given list in the way that humans expect. Sorting is done in place.

Parameters *list* (*list*) – List to sort.

Example

```
>>> my_list = ['spec_3', 'spec_4', 'spec_1']
>>> natural_sort(my_list)
>>> my_list
['spec_1', 'spec_3', 'spec_4']
```

`crrlpy.crrls.plot_fit(fig, x, y, fit, params, vparams, sparams, rms, x0, refs, refs_cb=None, refs_cd=None, refs_cg=None)`

`crrlpy.crrls.plot_fit_single(fig, x, y, fit, params, rms, x0, refs, refs_cb=None, refs_cd=None, refs_cg=None)`

`crrlpy.crrls.plot_model(x, y, xm, ym, out)`

`crrlpy.crrls.plot_spec_vel(out, x, y, fit, A, Aerr, x0, x0err, sx, sxerr)`

`crrlpy.crrls.pressure_broad(n, Te, ne)`

Pressure induced broadening in Hz. Shaver (1975)

`crrlpy.crrls.pressure_broad_coefs(Te)`

Defines the values of the constants *a* and γ that go into the collisional broadening formula of Salgado et al. (2015).

Parameters *Te* (*float*) – Electron temperature.

Returns The values of *a* and γ .

Return type list

`crrlpy.crrls.pressure_broad_salgado(n, Te, ne, dn=1)`

Pressure induced broadening in Hz. This gives the FWHM of a Lorentzian line. Salgado et al. (2015)

Parameters

- *n* (*float or array*) – Principal quantum number for which to compute the line broadening.
- *Te* (*float*) – Electron temperature to use when computing the collisional line width.
- *ne* (*float*) – Electron density to use when computing the collisional line width.
- *dn* (*int*) – Difference between the upper and lower level for which the line width is computed. (default 1)

Returns The collisional broadening FWHM in Hz using Salgado et al. (2015) formulas.

Return type float or array

`crrlpy.crrls.radiation_broad(n, W, Tr)`

Radiation induced broadening in Hz. Shaver (1975)

`crllpy.crlls.radiation_broad_salgado(n, W, Tr)`

Radiation induced broadening in Hz. This gives the FWHM of a Lorentzian line. Salgado et al. (2015)

`crllpy.crlls.radiation_broad_salgado_general(n, W, Tr, nu0, alpha)`

Radiation induced broadening in Hz. This gives the FWHM of a Lorentzian line. The expression is valid for power law like radiation fields. Salgado et al. (2015)

`crllpy.crlls.sigma2fwhm(sigma)`

Converts the σ parameter of a Gaussian distribution to its FWHM.

Parameters `sigma` (*float*) – σ value of the Gaussian distribution.

Returns The FWHM of a Gaussian with a standard deviation σ .

Return type *float*

`crllpy.crlls.sigma2fwhm_err(dsigma)`

Converts the error on the sigma parameter of a Gaussian distribution to the error on the FWHM.

Parameters `dsigma` – Error on sigma of the Gaussian distribution.

Returns The error on the FWHM of a Gaussian with a standard deviation σ .

Return type *float*

`crllpy.crlls.stack_interpol(spectra, vmin, vmax, dv, show=True, rmsvec=False)`

`crllpy.crlls.stack_irregular(lines, window='', **kargs)`

Stacks spectra by adding them together and then convolving with a window to reduce the noise. Available window functions: Gaussian, Savitzky-Golay and Wiener.

`crllpy.crlls.temp2tau(x, y, model, p0, wy=None, mask=None)`

Converts a temperature to optical depth. It will fit the continuum using model and then subtract it and divide by it.

Parameters

- `x` (*array*) – x values.
- `y` (*array*) – y values to be converted into optical depths.
- `model` (*callable*) – Model to fit to the continuum.
- `p0` – Starting values for the model to be fit to the continuum.
- `wy` (*array*) – Weights for the y values. (Optional)
- `mask` (*array*) – Mask to apply to the x and y values.

Returns `y/model - 1`.

Return type *array*

`crllpy.crlls.tryint(str)`

Returns an integer if `str` can be represented as one.

Parameters `str` (*string*) – String to check.

Returns True if str can be cast to an int.

Return type *int*

`crllpy.crlls.vel2freq(f0, vel)`

Convert a velocity axis to a frequency axis given a central frequency. Uses the radio definition, $\nu = f_0(1 - v/c)$.

Parameters

- `f0` (*float*) – Rest frequency in Hz.

- **vel** (*float or array*) – Velocity to convert in m/s.

Returns The frequency which is equivalent to vel.

Return type float or array

`crrlpy.crrls.voigt(x, sigma, gamma, center, amplitude)`

The Voigt line shape in terms of its physical parameters.

Parameters

- **x** – independent variable
- **sigma** – HWHM of the Gaussian
- **gamma** – HWHM of the Lorentzian
- **center** – the line center
- **amplitude** – the line area

`crrlpy.crrls.voigt_(x, y)`

`crrlpy.crrls.voigt_area(amp, fwhm, gamma, sigma)`

Returns the area under a Voigt profile. This approximation has an error of less than 0.5%

`crrlpy.crrls.voigt_area_err(area, amp, damp, fwhm, dfwhm, gamma, sigma)`

Returns the error of the area under a Voigt profile. Assumes that the parameter c has an error of 0.5%.

`crrlpy.crrls.voigt_fwhm(dD, dL)`

Computes the FWHM of a Voigt profile. http://en.wikipedia.org/wiki/Voigt_profile#The_width_of_the_Voigt_profile

$$FWHM_V = 0.5346dL + \sqrt{0.2166dL^2 + dD^2}$$

Parameters

- **dD** (*array*) – FWHM of the Gaussian core.
- **dL** (*array*) – FWHM of the Lorentz wings.

Returns The FWHM of a Voigt profile.

Return type array

`crrlpy.crrls.voigt_fwhm_err(dD, dL, ddD, ddL)`

Computes the error in the FWHM of a Voigt profile. http://en.wikipedia.org/wiki/Voigt_profile#The_width_of_the_Voigt_profile

Parameters

- **dD** (*array*) – FWHM of the Gaussian core.
- **dL** (*array*) – FWHM of the Lorentz wings.
- **ddD** (*array*) – Error on the FWHM of the Gaussian.
- **ddL** (*array*) – Error on the FWHM of the Lorentzian.

Returns The FWHM of a Voigt profile.

Return type array

`crrlpy.crrls.voigt_peak(A, alphaD, alphaL)`

Gives the peak of a Voigt profile given its Area and the Half Width at Half Maximum of the Gaussian and Lorentz profiles.

Parameters

- **A** (*array*) – Area of the Voigt profile.

- **alphaD** (*array*) – HWHM of the Gaussian core.
- **alphaL** (*array*) – HWHM of the Lorentz wings.

Returns The peak of the Voigt profile.

Return type *array*

`crrlpy.crrls.voigt_peak2area` (*peak, alphaD, alphaL*)

Converts the peak of a Voigt profile into the area under the profile given the Half Width at Half Maximum of the profile components.

Parameters

- **peak** (*array*) – Peak of the Voigt profile.
- **alphaD** (*array*) – HWHM of the Gaussian core.
- **alphaL** (*array*) – HWHM of the Lorentz wings.

Returns The area under the Voigt profile.

Return type *array*

`crrlpy.crrls.voigt_peak_err` (*peak, A, dA, alphaD, dalphaD*)

Gives the error on the peak of the Voigt profile. It assumes no correlation between the parameters and that they are normally distributed.

Parameters

- **peak** (*array*) – Peak of the Voigt profile.
- **A** – Area under the Voigt profile.
- **dA** (*array*) – Error on the area *A*.
- **alphaD** (*array*) – HWHM of the Gaussian core.

CRRLPY.MODELS.RRLMOD MODULE

`crrlpy.models.rrlmod.I_Bnu(specie, Z, n, Inu_func, *args)`

Calculates the product $B_{n+\Delta n,n} I_\nu$ to compute the line broadening due to a radiation field I_ν .

Parameters

- **specie** (*string*) – Atomic specie to calculate for.
- **n** (*int or list*) – Principal quantum number at which to evaluate $\frac{2}{\pi} \sum_{\Delta n} B_{n+\Delta n,n} I_{n+\Delta n,n}(\nu)$.
- **Inu_func** (*function*) – Function to call and evaluate $I_{n+\Delta n,n}(\nu)$. It's first argument must be the frequency.
- **args** – Arguments to *Inu_func*. The frequency must be left out. The frequency will be passed internally in units of MHz. Use the same unit when required. *Inu_func* must take the frequency as first parameter.

Returns (Hz)

Return type `array`

Example

```
>>> I_Bnu('CI', 1., 500, I_broken_plaw, 800, 26*u.MHz.to('Hz'), -1., -2.6)
array([ 6.65540582])
```

`crrlpy.models.rrlmod.I_CII(Te, R, NCII)`

Frequency integrated line intensity. Optically thin limit without radiative transfer.

Returns The frequency integrated line intensity in units of Jy Hz or g s-3

`crrlpy.models.rrlmod.I_CII_rt(wav, dnu, T158)`

Frequency integrated line intensity. Optically thin limit with radiative transfer.

Returns The frequency integrated line intensity in units of Jy Hz or g s-3

`crrlpy.models.rrlmod.I_broken_plaw(nu, Tr, nu0, alpha1, alpha2)`

Returns the blackbody function evaluated at nu. As temperature a broken power law is used. The power law shape has parameters: Tr, nu0, alpha1 and alpha2.

Parameters

- **nu** ((Hz) or `astropy.units.Quantity`) – Frequency. (Hz) or `astropy.units.Quantity`
- **Tr** – Temperature at nu0. (K) or `astropy.units.Quantity`
- **nu0** – Frequency at which the spectral index changes. (Hz) or `astropy.units.Quantity`
- **alpha1** – spectral index for $\nu < \nu_0$
- **alpha2** – spectral index for $\nu \geq \nu_0$

Returns Specific intensity in $\text{erg cm}^{-2} \text{Hz}^{-1} \text{s}^{-1} \text{sr}^{-1}$. See `astropy.analytic_functions.blackbody.blackbody_nu`

Return type `astropy.units.Quantity`

`crrlpy.models.rrlmod.I_cont(nu, Te, tau, I0, unitless=False)`

Computes the specific intensity due to a blackbody at temperature T_e and optical depth τ . It considers that there is background radiation with I_0 .

Parameters

- **nu** ((Hz) or `astropy.units.Quantity`) – Frequency.
- **Te** – Temperature of the source function. (K) or `astropy.units.Quantity`
- **tau** – Optical depth of the medium.
- **I0** – Specific intensity of the background radiation. Must have units of $\text{erg / (cm}^2 \text{ Hz s sr)}$ or see *unitless*.
- **unitless** – If True the return

Returns The specific intensity of a ray of light after traveling in an LTE medium with source function $B_\nu(T_e)$ after crossing an optical depth τ_ν . The units are $\text{erg / (cm}^2 \text{ Hz s sr)}$. See `astropy.analytic_functions.blackbody.blackbody_nu`

`crrlpy.models.rrlmod.I_external(nu, Tbkg, Tff, tau_ff, Tr, nu0=<Quantity 100000000.0 MHz>, alpha=-2.6)`

This method is equivalent to the IDL routine

Parameters **nu** – Frequency. (Hz) or `astropy.units.Quantity`

`crrlpy.models.rrlmod.I_total(nu, Te, tau, I0, eta)`

`crrlpy.models.rrlmod.Mdn(dn)`

Gives the $M(\Delta n)$ factor for a given Δn . ref. Menzel (1968)

Parameters **dn** – Δn .

Returns $M(\Delta n)$

Return type `float`

Example

```
>>> Mdn(1)
0.1908
>>> Mdn(5)
0.001812
```

`crrlpy.models.rrlmod.R_CII(ne, nh, gamma_e, gamma_h)`

Ratio between the fine structure level population of CII, and the level population in LTE. It ignores the effect of collisions with molecular hydrogen.

`crrlpy.models.rrlmod.T_CII(Te, tau, R)`

`crrlpy.models.rrlmod.alpha_CII(Te, R)`

Computes the value of $\alpha_{1/2}$. Sorochenko & Tsivilev (2000).

`crrlpy.models.rrlmod.beta_CII(Te, R)`

Computes the value of β_{158} . Sorochenko & Tsivilev (2000).

`crrlpy.models.rrlmod.broken_plaw(nu, nu0, T0, alpha1, alpha2)`
 Defines a broken power law.

$$T(\nu) = T_0 \left(\frac{\nu}{\nu_0} \right)^{\alpha_1} \quad \text{if } \nu < \nu_0$$

$$T(\nu) = T_0 \left(\frac{\nu}{\nu_0} \right)^{\alpha_2} \quad \text{if } \nu \geq \nu_0$$

Parameters

- **nu** – Frequency.
- **nu0** – Frequency at which the power law breaks.
- **T0** – Value of the power law at nu0.
- **alpha1** – Index of the power law for nu<nu0.
- **alpha2** – Index of the power law for nu>=nu0.

Returns Broken power law evaluated at nu.

`crrlpy.models.rrlmod.chi(n, Te, Z)`
 Computes the χ_n value as defined by Salgado et al. (2015).

`crrlpy.models.rrlmod.eta(freq, Te, ne, nion, Z, Tr, trans, n_max=1500)`
 Returns the correction factor for the Planck function.

`crrlpy.models.rrlmod.gamma_e_CII(Te)`
 Computes the de-excitation rate of the CII atom due to collisions with electrons.

Parameters **Te** (*float*) – Electron temperature.

Returns The collisional de-excitation rate in units of cm⁻³ s⁻¹.

Return type *float*

`crrlpy.models.rrlmod.gamma_h_CII(Te)`
 Computes the de-excitation rate of the CII atom due to collisions with hydrogen atoms.

Parameters **Te** (*float*) – Electron temperature.

Returns The collisional de-excitation rate in units of cm⁻³ s⁻¹.

Return type *float*

`crrlpy.models.rrlmod.italu(temp, dens, line, n_min=5, n_max=1000, other='', verbose=False, value='italu')`

Gives the integrated optical depth for a given temperature and density. The emission measure is unity. The output units are Hz.

Parameters

- **temp** (*string*) – Electron temperature. Must be a string of the form ‘8d1’.
- **dens** (*float*) – Electron density.
- **line** (*string*) – Line to load models for.
- **n_min** (*int*) – Minimum n value to include in the output. Default 1
- **n_max** (*int*) – Maximum n value to include in the output. Default 1500, Maximum allowed value 9900
- **other** (*string*) – String to search for different radiation fields and others.
- **verbose** (*bool*) – Verbose output?

- **value** (*string*) – ['itau' | 'bbnMdn' | 'None'] Value to output. itau will output the integrated optical depth. bbnMdn will output the $\beta_{n,n'} b_n$ times the oscillator strenght $M(\Delta n)$. None will output the $\beta_{n,n'} b_n$ values.

Returns The principal quantum number and its asociated value.

```
crrlpy.models.rrlmod.itau_h(temp, dens, trans, n_max=1000, other='', verbose=False,
                             value='itau')
```

Gives the integrated optical depth for a given temperature and density. The emission measure is unity. The output units are Hz.

```
crrlpy.models.rrlmod.itau_norad(n, te, b, dn, mdn)
```

Returns the optical depth with only the approximate solution to the radiative transfer problem.

```
crrlpy.models.rrlmod.j_line_lte(n, ne, nion, Te, Z, trans)
```

```
crrlpy.models.rrlmod.kappa_cont(freq, Te, ne, nion, Z)
```

Computes the absorption coefficient for the free-free process.

```
crrlpy.models.rrlmod.kappa_cont_base(nu, Te, ne, nion, Z)
```

```
crrlpy.models.rrlmod.kappa_line(Te, ne, nion, Z, Tr, trans, n_max=1500)
```

Computes the line absorption coefficient for CRRLs between levels n_i and n_f , $n_i > n_f$. This can only go up to n_{\max} 1500 because of the tables used for the Einstein Anm coefficients.

Parameters

- **Te** (*float*) – Electron temperature of the gas. (K)
- **ne** (*float*) – Electron density. (cm^{-3})
- **nion** (*float*) – Ion density. (cm^{-3})
- **Z** (*int*) – Electric charge of the atoms being considered.
- **Tr** (*float*) – Temperature of the radiation field felt by the gas. This specifies the temperature of the field at 100 MHz. (K)
- **trans** (*string*) – Transition for which to compute the absorption coefficient.
- **n_max** (*int*<1500) – Maximum principal quantum number to include in the output.

Returns

Return type array

```
crrlpy.models.rrlmod.kappa_line_lte(nu, Te, ne, nion, Z, Tr, line, n_min=1, n_max=1500)
```

Returns the line absorption coefficient under LTE conditions.

Parameters

- **nu** (*array*) – Frequency. (Hz)
- **Te** (*float*) – Electron temperature of the gas. (K)
- **ne** (*float*) – Electron density. (cm^{-3})
- **nion** (*float*) – Ion density. (cm^{-3})
- **Z** (*int*) – Electric charge of the atoms being considered.
- **Tr** (*float*) – Temperature of the radiation field felt by the gas. This specifies the temperature of the field at 100 MHz. (K)
- **trans** (*string*) – Transition for which to compute the absorption coefficient.
- **n_max** (*int*<1500) – Maximum principal quantum number to include in the output.

Returns**Return type** array`crrlpy.models.rrlmod.level_pop_lte` (*n*, *ne*, *nion*, *Te*, *Z*)Returns the level population of level *n*. The return has units of cm^{-3} .`crrlpy.models.rrlmod.load_betabn` (*temp*, *dens*, *other*='', *trans*='CIalpha', *verbose*=False)

Loads a model for the CRRL emission.

`crrlpy.models.rrlmod.load_betabn_h` (*temp*, *dens*, *other*='', *trans*='alpha', *verbose*=False)

Loads a model for the HRRL emission.

`crrlpy.models.rrlmod.load_bn` (*temp*, *dens*, *other*='')Loads the b_n values from the CRRL models.`crrlpy.models.rrlmod.load_bn2` (*Te*, *ne*, *Tr*='', *n_min*=5, *n_max*=1000, *verbose*=False)Loads the b_n values from the CRRL models.**Parameters**

- **Te** (*string*) – Electron temperature of the model.
- **ne** (*string*) – Electron density of the model.
- **Tr** (*string*) – Radiation field of the model.
- **verbose** (*bool*) – Verbose output?

Returns The b_n value for the given model conditions.**Return type** array`crrlpy.models.rrlmod.load_bn_all` (*n_min*=5, *n_max*=1000, *verbose*=False)`crrlpy.models.rrlmod.load_bn_dict` (*dict*, *n_min*=5, *n_max*=1000, *verbose*=False)Loads the b_n values defined by dict.**Parameters**

- **dict** (*dict*) – Dictionary containing a list with values for *Te*, *ne* and *Tr*.
- **line** (*string*) – Which models should be loaded.
- **n_min** (*int*) – Minimum *n* number to include in the output.
- **n_max** (*int*) – Maximum *n* number to include in the output.
- **verbose** (*bool*) – Verbose output?

Returns List with the b_n values for the conditions defined by dict.**Return type** numpy.array**Example**

First define the range of parameters

```
>>> Te = np.array(['1d1', '2d1', '3d1', '4d1', '5d1',
                  '6d1', '7d1', '8d1', '9d1', '1d2',
                  '1.2d2', '1.5d2', '2d2', '3d2',
                  '4d2', '5d2', '6d2', '7d2', '8d2',
                  '1d3', '2d3'])
>>> ne = np.arange(0.01, 0.105, 0.01)
>>> Tr = np.array([800, 1200, 1600, 2000])
```

Put them in a dictionary

```
>>> models = {'Te':[t_ for t_ in Te for n_ in ne for tr_ in Tr],
              'ne':[round(n_,3) for t_ in Te for n_ in ne for tr_ in Tr],
              'Tr':['case_diffuse_{0}'.format(rrlmod.val2str(tr_))
                    for t_ in Te for n_ in ne for tr_ in Tr]}
```

Load the models

```
>>> bn = rrlmod.load_bn_dict(models, n_min=n_min, n_max=n_max, verbose=False)
```

Plot the first model

```
>>> import pylab as plt
>>> plt.plot(bn[0,0], bn[0,-1])
>>> plt.show()
```

```
crrlpy.models.rrlmod.load_itaui_all(line='CIalpha', n_min=5, n_max=1000, verbose=False,
                                   value='itaui')
```

Loads all the available models for Carbon.

Parameters

- **line** (*string*) – Which models should be loaded.
- **n_min** (*int*) – Minimum n number to include in the output.
- **n_max** (*int*) – Maximum n number to include in the output.
- **verbose** (*bool*) – Verbose output?
- **value** (*string*) – ['itaui','bbnMdn',None] Which value should be in the output.

```
crrlpy.models.rrlmod.load_itaui_all_hydrogen(trans='alpha', n_max=1000, ver-
                                            bose=False, value='itaui')
```

Loads all the available models for Hydrogen.

```
crrlpy.models.rrlmod.load_itaui_all_match(trans_out='alpha', trans_tin='beta',
                                           n_max=1000, verbose=False, value='itaui')
```

Loads all trans_out models that can be found in trans_tin. This is useful when analyzing line ratios.

```
crrlpy.models.rrlmod.load_itaui_all_norad(trans='alpha', n_max=1000)
```

Loads all the available models.

```
crrlpy.models.rrlmod.load_itaui_dict(dict, line, n_min=5, n_max=1000, verbose=False,
                                   value='itaui')
```

Loads the models defined by dict.

Parameters

- **dict** (*dict*) – Dictionary containing a list with values for Te, ne and Tr.
- **line** (*string*) – Which models should be loaded.
- **n_min** (*int*) – Minimum n number to include in the output.
- **n_max** (*int*) – Maximum n number to include in the output.
- **verbose** (*bool*) – Verbose output?
- **value** (*string*) – ['itaui','bbnMdn',None] Which value should be in the output.

Example

First define the range of parameters

```
>>> Te = np.array(['1d1', '2d1', '3d1', '4d1', '5d1',
                  '6d1', '7d1', '8d1', '9d1', '1d2',
                  '1.2d2', '1.5d2', '2d2', '3d2',
                  '4d2', '5d2', '6d2', '7d2', '8d2',
                  '1d3', '2d3'])
>>> ne = np.arange(0.01, 0.105, 0.01)
>>> Tr = np.array([800, 1200, 1600, 2000])
```

Put them in a dictionary

```
>>> models = {'Te': [t_ for t_ in Te for n_ in ne for tr_ in Tr],
              'ne': [round(n_, 3) for t_ in Te for n_ in ne for tr_ in Tr],
              'Tr': ['case_diffuse_{0}'.format(rrlmod.val2str(tr_))
                     for t_ in Te for n_ in ne for tr_ in Tr]}
```

Load the models

```
>>> itau_mod = rrlmod.load_itau_dict(models, 'CIalpha', n_min=n_min, n_max=n_max,
                                     verbose=False, value='itau')
```

Plot the first model

```
>>> import pylab as plt
>>> plt.plot(itau_mod[0,0], itau_mod[0,1])
>>> plt.show()
```

```
rrlpy.models.rrlmod.load_itau_nelim(temp, dens, trad, trans, n_max=1000, verbose=False,
                                     value='itau')
```

Loads models given a temperature, radiation field and an upper limit for the electron density.

```
rrlpy.models.rrlmod.load_models(models, trans, n_max=1000, verbose=False, value='itau')
```

Loads the models in backwards compatible mode. It will sort the models by Te, ne and Tr.

```
rrlpy.models.rrlmod.make_betabn(line, temp, dens, n_min=5, n_max=1000, other='')
```

```
rrlpy.models.rrlmod.make_betabn2(line, temp, dens, n_min=5, n_max=1000, other='')
```

```
rrlpy.models.rrlmod.plaw(x, x0, y0, alpha)
```

Returns a power law.

$$y(x) = y_0 \left(\frac{x}{x_0} \right)^\alpha$$

Parameters

- **x** (*float or array like*) – x values for which to compute the power law.
- **x0** (*float*) – x value for which the power law has amplitude y0.
- **y0** (*float*) – Amplitude of the power law at x0.
- **alpha** (*float*) – Index of the power law.

Returns A power law of index *alpha* evaluated at *x*, with amplitude *y0* at *x0*.

Return type float or array

```
rrlpy.models.rrlmod.str2val(str)
```

Converts a string representing a number to a float. The string must follow the IDL convention for floats.

Parameters **str** (*string*) – String to convert.

Returns The equivalent number.

Return type `float`

Example

```
>>> str2val('2d2')
200
```

`crrlpy.models.rrlmod.tau_CII` (*Te*, *R*, *nc*, *L*, *dnu*)

Computes the optical depth of the far infrared line of CII. Crawford et al. (1985).

Parameters

- **Te** (*float*) – Electron temperature.
- **R** (*float*) – Ratio of collisional excitation to spontaneous emission.
- **nc** (*float*) – Ionized carbon number density.
- **L** (*float*) – Path lenght.
- **dnu** (*float*) – Line width FWHM in Hz.

Returns

Return type `float`

`crrlpy.models.rrlmod.val2str` (*val*)

Converts a float to the string format required for loading the CRRL models.

Parameters **val** (*float*) – Value to convert to a string.

Returns The value of *val* represented as a string in IDL double format.

Return type `string`

Example

```
>>> val2str(200)
'2d2'
```

`crrlpy.models.rrlmod.valid_ne` (*line*)

Checks all the available models and lists the available ne values.

CRRLPY.CRRLS.FREC_CALC MODULE

`crrlpy.frec_calc.line_freq(Z, R_X, n, dn)`

Uses the Rydberg formula to get the frequency of a transition to quantum number n for a given atom.

Parameters

- **Z** (*int*) – Charge of the atom.
- **R_X** (*float*) –
- **n** (*int*) – Principal quantum number of the transition. $n + \Delta n \rightarrow n$.
- **dn** (*int*) – Difference between the principal quantum number of the initial state and the final state. $\Delta n = n_f - n_i$.

Returns The frequency of the transition in MHz.

Return type `float`

`crrlpy.frec_calc.main()`

Main body of the program. Useful for calling as a script.

`crrlpy.frec_calc.make_line_list(line, n_min=1, n_max=1500, unitless=True)`

Creates a list of frequencies for the corresponding line. The frequencies are in MHz.

Parameters

- **line** (*string*) – Line to compute the frequencies for.
- **n_min** (*int*) – Minimum n number to include in the list.
- **n_max** (*int*) – Maximum n number to include in the list.
- **unitless** (*bool*) – If True the list will have no units. If not the list will be of `astropy.units.Quantity` objects.

Returns 3 lists with the line name, principal quantum number and frequency of the transitions.

Return type `list`

`crrlpy.frec_calc.set_dn(name)`

Sets the value of Delta n depending on the transition name.

Parameters **name** (*string*) – Name of the transition.

Returns Δn for the given transition.

Return type `int`

Example

```
>>> set_dn('CIalpha')
1
>>> set_dn('CIdelta')
4
```

`crrlpy.frec_calc.set_specie(specie)`

Sets atomic constants based on the atomic specie.

Parameters `specie` (*string*) – Atomic specie.

Returns Array with the atomic mass in a.m.u., ionization potential, abundance relative to HI, $V_X - V_H$ and the electric charge.

Example

```
>>> set_specie('CI')
[12.0, 11.4, 0.0003, 149.5, 1.0]
```

`crrlpy.frec_calc.set_trans(dn)`

Sets a name depending on the difference between atomic levels.

Parameters `dn` (*int*) – Separation between n_i and n_f , $\Delta n = n_i - n_f$.

Returns alpha, beta, gamma, delta or epsilon depending on Δn .

Return type *string*

Example

```
>>> set_trans(5)
'epsilon'
```

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