# **CRRLpy Documentation**

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**Pedro Salas** 

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# CHAPTER

# **ONE**

# **CRRLPY**

Tools for processing Carbon Radio Recombination Line spectra.

The models are not shipped with the modules and scripts.

The documentation can be found in: http://astrofle.github.io/CRRLpy/

# CRRLPY.CRRLS MODULE

```
crrlpy.crrls.alphanum_key(s)
```

Turn a string into a list of string and number chunks.

**Parameters** s – String

**Returns** List with strings and integers.

Return type list

# Example

```
>>> alphanum_key("z23a")
["z", 23, "a"]
```

```
crrlpy.crrls.average(data, axis, n)
```

Averages data along the given axis by combining n adjacent values.

### **Parameters**

- data (numpy array) Data to average along a given axis.
- axis (int) Axis along which to average.
- **n** (*int*) Factor by which to average.

**Returns** Data decimated by a factor n along the given axis.

**Return type** numpy array

```
crrlpy.crrls.best_match_indx(value, array, tol)
```

Searchs for the best match to a value inside an array given a tolerance.

#### **Parameters**

- **value** (*float*) Value to find inside the array.
- tol (*float*) Tolerance for match.
- array (numpy.array) List to search for the given value.

**Returns** Best match for val inside array.

Return type float

```
crrlpy.crrls.best_match_indx2 (value, array)
```

Searchs for the index of the closest entry to value inside an array.

#### **Parameters**

- **value** (*float*) Value to find inside the array.
- array (*list or numpy.array*) List to search for the given value.

**Returns** Best match index for the value inside array.

Return type float

# Example

```
>>> a = [1,2,3,4]
>>> best_match_indx2(3, a)
2
```

# crrlpy.crrls.best\_match\_value(value, array)

Searchs for the closest ocurrence of value in array.

#### **Parameters**

- **value** (*float*) Value to find inside the array.
- array (list or numpy.array) List to search for the given value.

**Returns** Best match for the value inside array.

Return type float.

# **Example**

```
>>> a = [1,2,3,4]
>>> best_match_value(3.5, a)
3
```

# crrlpy.crrls.blank\_lines (freq, tau, reffreqs, v0, dv)

Blanks the lines in a spectra.

### **Parameters**

- **freq** (*array*, *MHz*) Frequency axis of the spectra.
- tau (array) Optical depth axis of the spectra.
- **reffreqs** (*list*) List with the reference frequency of the lines. Should be the rest frequency.
- v0 (float) Velocity shift to apply to the lines defined by reffreq. (km/s)
- dv (*float*) Velocity range to blank around the lines. (km/s)

```
crrlpy.crrls.blank_lines2 (freq, tau, reffreqs, dv)
```

Blanks the lines in a spectra.

#### **Parameters**

- **freq** (*array*) Frequency axis of the spectra. (MHz)
- tau (array) Optical depth axis of the spectra.
- **reffreqs** (*list*) List with the reference frequency of the lines. Should be the rest frequency.
- dv (*float*) Velocity range to blank around the lines. (km/s)

```
\mathtt{crrlpy.crrls.df2dv}\,(\mathit{f0},\mathit{df})
```

Convert a frequency delta to a velocity delta given a central frequency.

### **Parameters**

- **f0** (*float*) Rest frequency. (Hz)
- **df** (*float*) Frequency delta. (Hz)

**Returns** The equivalent velocity delta for the given frequency delta.

Return type float in Hz

```
crrlpy.crrls.dv2df (f0, dv)
```

Convert a velocity delta to a frequency delta given a central frequency.

#### **Parameters**

- **f0** (*float*) Rest frequency. (Hz)
- **dv** (*float*) Velocity delta. (m/s)

**Returns** The equivalent frequency delta for the given velocity delta.

**Return type** float in m  $s^{-1}$ 

```
crrlpy.crrls.dv_minus_doppler(dV, ddV, dD, ddD)
```

Returns the Lorentzian contribution to the line width assuming that the line has a Voigt profile.

#### **Parameters**

- **dV** (*float*) Total line width
- **ddV** (*float*) Uncertainty in the total line width.
- **dD** (*float*) Doppler contribution to the line width.
- ddD Uncertainty in the Doppler contribution to the line width.

**Returns** The Lorentz contribution to the total line width.

Return type float

```
\texttt{crrlpy.crrls.dv\_minus\_doppler2} \ (\textit{dV}, \textit{ddV}, \textit{dD}, \textit{ddD})
```

Returns the Lorentzian contribution to the line width assuming that the line has a Voigt profile.

### **Parameters**

- dV (float) Total line width
- **ddV** (*float*) Uncertainty in the total line width.
- **dD** (*float*) Doppler contribution to the line width.
- ddD Uncertainty in the Doppler contribution to the line width.

**Returns** The Lorentz contribution to the total line width.

Return type float

```
crrlpy.crrls.f2n (f, line, n_max=1500)
```

Converts a given frequency to a principal quantum number n for a given line.

#### **Parameters**

- **f** (*array*) Frequency to convert. (MHz)
- line (string) The equivalent n will be referenced to this line.
- n\_max (int) Maximum n number to include in the search. (optional, Default 1)

**Returns** Corresponding n for a given frequency and line. If the frequency is not an exact match, then it will return an empty array.

Return type array

```
crrlpy.crrls.find lines sb(freq, line, z=0, verbose=False)
```

Finds if there are any lines of a given type in the frequency range. The line frequencies are corrected for redshift.

#### **Parameters**

- **freq** (*array*) Frequency axis in which to search for lines.
- line (*string*) Line type to search for.
- **z** (*float*) Redshift to apply to the rest frequencies.
- **verbose** (*bool*) Verbose output?

**Returns** Lists with the principipal quantum number and the reference frequency of the line. The frequencies are redshift corrected in MHz.

# Return type array.

# Example

```
crrlpy.crrls.fit_continuum(x, y, degree, p0)
```

Divide tb by given a model and starting parameters p0. Returns: tb/model - 1

```
crrlpy.crrls.fit_model (x, y, model, p0, wy=None, mask=None)
```

Fits a model to the data defined by x and y. It uses p0 as starting values.

#### **Parameters**

- **x** (array) Abscissa values of the data to be fit.
- y (array) Ordinate values of the data to be fit.
- model (callable) Model to be fit.
- p0 (dict) Dictionary with the starting values for the fit.
- wy (array) Weights of the ordinate values. (Optional)
- mask(array) Mask to apply to the x and y values. (Optional)

**Returns** An object containing the results of the fit.

Return type lmfit.model.ModelResult

```
crrlpy.crrls.freq2vel(f0, f)
```

Convert a frequency axis to a velocity axis given a central frequency. Uses the radio definition of velocity.

#### **Parameters**

- **f0** (*float*) Rest frequency for the conversion. (Hz)
- **f** (numpy array) Frequencies to be converted to velocity. (Hz)

**Returns** f converted to velocity given a rest frequency  $f_0$ .

Return type numpy array

```
crrlpy.crrls.fwhm2sigma(fwhm)
```

Converts a FWHM to the standard deviation,  $\sigma$  of a Gaussian distribution.

Parameters fwhm (array) – FWHM of the Gaussian.

**Returns** Equivalent standard deviation of a Gausian with a Full Width at Half Maximum fwhm.

# Return type array

#### Example

```
>>> 1/fwhm2sigma(1)
2.3548200450309493
```

# crrlpy.crrls.gauss\_area(amplitude, sigma)

Returns the area under a Gaussian of a given amplitude and sigma.

#### **Parameters**

- amplitude Amplitude of the Gaussian, A.
- **sigma** (array) Standard deviation fo the Gaussian,  $\sigma$ .

**Returns** The area under a Gaussian of a given amplitude and standard deviation.

# Return type array

```
crrlpy.crrls.gauss_area_err (amplitude, amplitude_err, sigma, sigma_err)
```

Returns the error on the area of a Gaussian of a given *amplitude* and *sigma* with their corresponding errors. It assumes no correlation between *amplitude* and *sigma*.

#### **Parameters**

- amplitude (array) Amplitude of the Gaussian.
- amplitude\_err (array) Error on the amplitude.
- sigma Standard deviation of the Gaussian.
- sigma\_err Error on sigma.

**Returns** The error on the area.

# Return type array

```
crrlpy.crrls.gaussian(x, sigma, center, amplitude)
```

Gaussian function in one dimension.

#### **Parameters**

- $\mathbf{x}$  (array) x values for which to evaluate the Gaussian.
- sigma (float) Standard deviation of the Gaussian.
- center (float) Center of the Gaussian.
- amplitude (*float*) Amplitude of the Gaussian.

**Returns** Gaussian function of the given amplitude and standard deviation evalueated at x.

# Return type array

```
crrlpy.crrls.get_axis (header, axis)
```

Constructs a cube axis.

#### **Parameters**

- header (pyfits header) Fits cube header.
- axis (int) Axis to reconstruct.

Returns cube axis

Return type numpy array

```
crrlpy.crrls.get_line_mask(freq, reffreq, v0, dv)
```

Return a mask with ranges where a line is expected in the given frequency range for a line with a given reference frequency at expected velocity v0 and line width dv0.

# **Parameters**

- **freq** (*numpy array or list*) Frequency axis where the line is located.
- **reffreq** (*float*) Reference frequency for the line.
- **v0** (*float*, *km/s*) Velocity of the line.
- **dv** (*float*, *km/s*) Velocity range to mask.

**Returns** Mask centered at the line center and width dv0 referenced to the input freq.

```
crrlpy.crrls.get_line_mask2 (freq, reffreq, dv)
```

Return a mask with ranges where a line is expected in the given frequency range for a line with a given reference frequency and line width dv.

#### **Parameters**

- **freq** (*numpy array or list*) Frequency axis where the line is located.
- **reffreq** (*float*) Reference frequency for the line.
- dv (*float*, *km/s*) Velocity range to mask.

**Returns** Mask centered at the line center and width dv0 referenced to the input freq.

```
crrlpy.crrls.get_min_sep(array)
```

Get the minimum element separation in an array.

**Parameters** array (array) – Array where the minimum separation is wanted.

**Returns** The minimum separation between the elements in *array*.

Return type float

```
crrlpy.crrls.get_rchi2 (x\_obs, x\_mod, y\_obs, y\_mod, dy\_obs, dof)
Computes the reduced \chi squared, \chi^2_{\nu} = \chi^2/dof.
```

### **Parameters**

- **x\_obs** (*array*) Abscissa values of the observations.
- **x\_mod** (*array*) Abscissa values of the model.
- **y\_obs** (*array*) Ordinate values of the observations.
- **y\_mod** (*array*) Ordinate values of the model.
- dy obs (array) Error on the ordinate values of the observations.
- **dof** (*float*) Degrees of freedom.

```
crrlpy.crrls.get_rms (data, axis=None)
```

Computes the rms of the given data.

#### **Parameters**

- data (numpy array or list) Array with values where to compute the rms.
- axis (int) Axis over which to compute the rms. Default: None

**Returns** The rms of data.

rms = 
$$\sqrt{\langle \text{data} \rangle^2 + V[\text{data}]}$$

where V is the variance of the data.

```
crrlpy.crrls.is_number(str)
```

Checks wether a string is a number or not.

Parameters str (string) - String.

**Returns** True if *str* can be converted to a float.

Return type bool

# Example

```
>>> is_number('10')
True
```

crrlpy.crrls.linear (x, a, b)

Linear model.

#### **Parameters**

- $\mathbf{x}$  (array) x values where to evalueate the line.
- **a** (*float*) Slope of the line.
- **b** (*float*) y value for x equals 0.

**Returns** A line defined by ax + b.

Return type array

crrlpy.crrls.load\_model(prop, specie, temp, dens, other=None)

Loads a model for the CRRL emission.

```
crrlpy.crrls.load_ref (specie, trans)
```

Loads the reference spectrum for the specified atomic specie and transition. Available species and transitions: CI alpha CI beta CI delta CI gamma CI13 alpha HeI alpha HeI beta HI alpha HI beta SI alpha SI beta

```
crrlpy.crrls.load_ref2 (transition)
```

Loads the reference spectrum for the specified atomic specie and transition. Available transitions: CIalpha CIbeta CIdelta CIgamma CI13alpha HeIalpha HeIbeta HIalpha HIbeta SIalpha SIbeta

```
crrlpy.crrls.lookup_freq(n, specie, trans)
```

Returns the frequency of a given transition.

```
crrlpy.crrls.lorentz_width(n, ne, Te, Tr, W, dn=1)
```

Gives the Lorentzian line width due to a combination of radiation and collisional broadening. The width is the FWHM in Hz. It uses the models of Salgado et al. (2015).

#### **Parameters**

- n (array) Principal quantum number for which to evaluate the Lorentz widths.
- **ne** (*float*) Electron density to use in the collisional broadening term.
- **Te** (*float*) Electron temperature to use in the collisional broadening term.
- **Tr** (*float*) Radiation field temperature.
- **W** (*float*) Cloud covering factor used in the radiation broadening term.
- dn (int) Separation between the levels of the transition. e.g., dn=1 for CIalpha.

**Returns** The Lorentz width of a line due to radiation and collisional broadening.

#### Return type array

```
crrlpy.crrls.mask_outliers(data, m=2)
```

Masks values larger than m times the data median. This is similar to sigma clipping.

**Parameters data** (array) – Data to mask.

**Returns** An array of the same shape as data with True where the data should be flagged.

Return type array

# Example

```
>>> data = [1,2,3,4,5,6]
>>> mask_outliers(data, m=1)
array([ True, False, False, False, True], dtype=bool)
```

```
crrlpy.crrls.n2f(n, line, n_min=1, n_max=1500, unitless=True)
```

Converts a given principal quantum number n to the frequency of a given line.

```
crrlpy.crrls.natural_sort (list)
```

Sort the given list in the way that humans expect. Sorting is done in place.

Parameters list (list) – List to sort.

#### **Example**

```
>>> my_list = ['spec_3', 'spec_4', 'spec_1']
>>> natural_sort(my_list)
>>> my_list
['spec_1', 'spec_3', 'spec_4']
```

```
crrlpy.crrls.plot_fit_single (fig, x, y, fit, params, rms, x0, refs, refs_cb=None, refs_cd=None, refs_cg=None)
```

```
crrlpy.crrls.plot_model(x, y, xm, ym, out)
```

```
crrlpy.crrls.plot_spec_vel(out, x, y, fit, A, Aerr, x0, x0err, sx, sxerr)
```

```
crrlpy.crrls.pressure_broad(n, Te, ne)
```

Pressure induced broadening in Hz. Shaver (1975)

```
crrlpy.crrls.pressure_broad_coefs(Te)
```

Defines the values of the constants a and  $\gamma$  that go into the collisional broadening formula of Salgado et al. (2015).

**Parameters Te** (*float*) – Electron temperature.

**Returns** The values of a and  $\gamma$ .

Return type list

```
crrlpy.crrls.pressure_broad_salgado(n, Te, ne, dn=1)
```

Pressure induced broadening in Hz. This gives the FWHM of a Lorentzian line. Salgado et al. (2015)

#### **Parameters**

- n (float or array) Principal quantum number for which to compute the line broadening.
- **Te** (*float*) Electron temperature to use when computing the collisional line width.
- **ne** (*float*) Electron density to use when computing the collisional line width.

• dn (int) – Difference between the upper and lower level for which the line width is computed. (default 1)

**Returns** The collisional broadening FWHM in Hz using Salgado et al. (2015) formulas.

Return type float or array

crrlpy.crrls.radiation\_broad(n, W, Tr)

Radiation induced broadening in Hz.

crrlpy.crrls.radiation\_broad\_salgado(n, W, Tr)

Radiation induced broadening in Hz. This gives the FWHM of a Lorentzian line. Salgado et al. (2015)

crrlpy.crrls.radiation\_broad\_salgado\_general(n, W, Tr, nu0, alpha)

Radiation induced broadening in Hz. This gives the FWHM of a Lorentzian line. The expression is valid for power law like radiation fields. Salgado et al. (2015)

crrlpy.crrls.sigma2fwhm(sigma)

Converts the  $\sigma$  parameter of a Gaussian distribution to its FWHM.

**Parameters** sigma (float) –  $\sigma$  value of the Gaussian distribution.

**Returns** The FWHM of a Gaussian with a standard deviation  $\sigma$ .

Return type float

crrlpy.crrls.sigma2fwhm\_err(dsigma)

Converts the error on the sigma parameter of a Gaussian distribution to the error on the FWHM.

Parameters dsigma – Error on sigma of the Gaussian distribution.

**Returns** The error on the FWHM of a Gaussian with a standard deviation  $\sigma$ .

Return type float

crrlpy.crrls.stack\_interpol(spectra, vmin, vmax, dv, show=True, rmsvec=False)

crrlpy.crrls.stack\_irregular(lines, window='', \*\*kargs)

Stacks spectra by adding them together and then convolving with a window to reduce the noise. Available window functions: Gaussian, Savitzky-Golay and Wiener.

crrlpy.crrls.temp2tau(x, y, model, p0, wy=None, mask=None)

Converts a temperature to optical depth. It will fit the continuum using model and then subtract it and divide by it

#### **Parameters**

- $\mathbf{x}$  (array) x values.
- y (array) y values to be converted into optical depths.
- model (callable) Model to fit to the continuum.
- p0 Starting values for the model to be fit to the continuum.
- wy (array) Weights for the y values. (Optional)
- mask(array) Mask to apply to the x and y values.

**Returns** y/model - 1.

Return type array

crrlpy.crrls.tryint(str)

Returns True if str is an integer.

Parameters str (string) - String to check.

**Returns** True is str can be cast to an int.

Return type bool

crrlpy.crrls.vel2freq(f0, vel)

Convert a velocity axis to a frequency axis given a central frequency. Uses the radio definition,  $\nu = f_0(1 - v/c)$ .

#### **Parameters**

- **f0** (*float*) Rest frequency in Hz.
- **vel** (*float or array*) Velocity to convert in m/s.

**Returns** The frequency which is equivalent to vel.

**Return type** float or array

crrlpy.crrls.voigt (x, sigma, gamma, center, amplitude)

The Voigt line shape in terms of its physical parameters.

#### **Parameters**

- **x** independent variable
- sigma HWHM of the Gaussian
- gamma HWHM of the Lorentzian
- center the line center
- amplitude the line area

crrlpy.crrls.voigt\_(x, y)

crrlpy.crrls.voigt\_area(amp, fwhm, gamma, sigma)

Returns the area under a Voigt profile. This approximation has an error of less than 0.5%

crrlpy.crrls.voigt\_area\_err(area, amp, damp, fwhm, dfwhm, gamma, sigma)

Returns the error of the area under a Voigt profile. Assumes that the parameter c has an error of 0.5%.

crrlpy.crrls.voigt\_fwhm(dD, dL)

Computes the FWHM of a Voigt profile. http://en.wikipedia.org/wiki/Voigt\_profile#The\_width\_of\_the\_Voigt\_profile

$$FWHM_V = 0.5346dL + \sqrt{0.2166dL^2 + dD^2}$$

#### **Parameters**

- dD (array) FWHM of the Gaussian core.
- **dL** (*array*) FWHM of the Lorentz wings.

**Returns** The FWHM of a Voigt profile.

Return type array

 $\texttt{crrlpy.crrls.voigt\_fwhm\_err}\,(\textit{dD},\textit{dL},\textit{ddD},\textit{ddL})$ 

 $Computes \ the \ error \ in \ the \ FWHM \ of \ a \ Voigt \ profile. \ http://en.wikipedia.org/wiki/Voigt \ profile\#The \ width \ of \ the \ Voigt \ profile$ 

#### **Parameters**

- dD (array) FWHM of the Gaussian core.
- **dL** (array) FWHM of the Lorentz wings.
- ddD (array) Error on the FWHM of the Gaussian.
- **ddL** (*array*) Error on the FWHM of the Lorentzian.

**Returns** The FWHM of a Voigt profile.

# Return type array

# crrlpy.crrls.voigt\_peak(A, alphaD, alphaL)

Gives the peak of a Voigt profile given its Area and the Half Width at Half Maximum of the Gaussian and Lorentz profiles.

# **Parameters**

- **A** (*array*) Area of the Voigt profile.
- alphaD (array) HWHM of the Gaussian core.
- alphaL (array) HWHM of the Lorentz wings.

**Returns** The peak of the Voigt profile.

# Return type array

# crrlpy.crrls.voigt\_peak2area(peak, alphaD, alphaL)

Converts the peak of a Voigt profile into the area under the profile given the Half Width at Half Maximum of the profile components.

#### **Parameters**

- **peak** (*array*) Peak of the Voigt profile.
- alphaD (array) HWHM of the Gaussian core.
- alphaL (array) HWHM of the Lorentz wings.

**Returns** The area under the Voigt profile.

# Return type array

# crrlpy.crrls.voigt\_peak\_err (peak, A, dA, alphaD, dalphaD)

Gives the error on the peak of the Voigt profile. It assumes no correlation between the parameters and that they are normally distributed.

# **Parameters**

- peak (array) Peak of the Voigt profile.
- **A** Area under the Voigt profile.
- dA(array) Error on the area A.
- alphaD (array) HWHM of the Gaussian core.

# CRRLPY.MODELS.RRLMOD MODULE

crrlpy.models.rrlmod.**I\_Bnu** (specie, Z, n, Inu\_funct, \*args)

Calculates the product  $B_{n+\Delta n,n}I_{\nu}$  to compute the line broadening due to a radiation field  $I_{\nu}$ .

### **Parameters**

- **specie** (*string*) Atomic specie to calculate for.
- $\mathbf{n}$  (int or list) Principal quantum number at which to evaluate  $\frac{2}{\pi} \sum_{\Delta n} B_{n+\Delta n,n} I_{n+\Delta n,n}(\nu)$ .
- Inu\_funct (function) Function to call and evaluate  $I_{n+\Delta n,n}(\nu)$ . It's first argument must be the frequency.
- **args** Arguments to *Inu\_funct*. The frequency must be left out. The frequency will be passed internally in units of MHz. Use the same unit when required. *Inu\_funct* must take the frequency as first parameter.

Returns (Hz)

Return type array

# Example

```
>>> I_Bnu('CI', 1., 500, I_broken_plaw, 800, 26*u.MHz.to('Hz'), -1., -2.6)
array([ 6.65540582])
```

crrlpy.models.rrlmod.I\_broken\_plaw(nu, Tr, nu0, alpha1, alpha2)

Returns the blackbody function evaluated at nu. As temperature a broken power law is used. The power law shape has parameters: Tr, nu0, alpha1 and alpha2.

# **Parameters**

- nu ((Hz) or astropy.units.Quantity) Frequency. (Hz) or astropy.units.Quantity
- **Tr** Temperature at nu0. (K) or astropy.units.Quantity
- nu0 Frequency at which the spectral index changes. (Hz) or astropy.units.Quantity
- alpha1 spectral index for  $\nu < \nu_0$
- alpha2 spectral index for  $\nu \ge \nu_0$

**Returns** Specific intensity in  $\operatorname{erg} \operatorname{cm}^{-2} \operatorname{Hz}^{-1} \operatorname{s}^{-1} \operatorname{sr}^{-1}$ . See astropy.analytic\_functions.blackbody\_blackbody\_nu

Return type astropy.units.Quantity

crrlpy.models.rrlmod.**I\_cont** (*nu*, *Te*, *tau*, *IO*, *unitless=False*)

Computes the specific intensity due to a blackbody at temperature  $T_e$  and optical depth  $\tau$ . It considers that there is background radiation with  $I_0$ .

#### **Parameters**

- nu ((Hz) or astropy.units.Quantity) Frequency.
- Te Temperature of the source function. (K) or astropy.units.Quantity
- tau Optical depth of the medium.
- **IO** Specific intensity of the background radiation. Must have units of erg / (cm2 Hz s sr) or see *unitless*.
- unitless If True the return

**Returns** The specific intensity of a ray of light after traveling in an LTE medium with source function  $B_{\nu}(T_e)$  after crossing an optical depth  $\tau_{\nu}$ . The units are erg / (cm2 Hz s sr). See astropy.analytic\_functions.blackbody\_blackbody\_nu

crrlpy.models.rrlmod.**I\_external** (nu, Tbkg, Tff, tau\_ff, Tr, nu0=<Quantity 100000000.0 MHz>, alpha=-2.6)

This method is equivalent to the IDL routine

Parameters nu – Frequency. (Hz) or astropy.units.Quantity

```
crrlpy.models.rrlmod.I_total(nu, Te, tau, IO, eta)
```

crrlpy.models.rrlmod.Mdn (dn)

Gives the  $M(\Delta n)$  factor for a given  $\Delta n$ . ref. Menzel (1968)

Parameters  $dn - \Delta n$ .

**Returns**  $M(\Delta n)$ 

Return type float

#### **Example**

```
>>> Mdn(1)
0.1908
>>> Mdn(5)
0.001812
```

crrlpy.models.rrlmod.broken\_plaw (nu, nu0, T0, alpha1, alpha2)

Defines a broken power law.

 $T(\nu) = T_0 \left(\frac{\nu}{\nu_0}\right)^{\alpha_1} \text{ if } \nu < \nu_0$ 

$$T(\nu) = T_0 \left(\frac{\nu}{\nu_0}\right)^{\alpha_2} \text{ if } \nu \ge \nu_0$$

#### **Parameters**

- **nu** Frequency.
- **nu0** Frequency at which the power law breaks.
- **TO** Value of the power law at nu0.
- **alpha1** Index of the power law for nu<nu0.
- alpha2 Index of the power law for nu>=nu0.

Returns Broken power law evalueated at nu.

crrlpy.models.rrlmod.eta(freq, Te, ne, nion, Z, Tr, trans, n\_max=1500)

Returns the correction factor for the Planck function.

```
crrlpy.models.rrlmod.itau(temp, dens, line, n_min=5, n_max=1000, other='', verbose=False, value='itau')
```

Gives the integrated optical depth for a given temperature and density. The emission measure is unity. The output units are Hz.

#### **Parameters**

- temp (string) Electron temperature. Must be a string of the form '8d1'.
- dens (*float*) Electron density.
- line (*string*) Line to load models for.
- n\_min (int) Minimum n value to include in the output. Default 1
- n\_max (int) Maximum n value to include in the output. Default 1500, Maximum allowed value 9900
- other (*string*) String to search for different radiation fields and others.
- **verbose** (*bool*) Verbose output?
- value (*string*) ['itau'l'bbnMdn'l'None'] Value to output. itau will output the integrated optical depth. bbnMdn will output the  $\beta_{n,n'}b_n$  times the oscillator strenght  $M(\Delta n)$ .

**Returns** The principal quantum number and its associated value.

Gives the integrated optical depth for a given temperature and density. The emission measure is unity. The output units are Hz.

```
crrlpy.models.rrlmod.itau_norad(n, te, b, dn, mdn)
```

Returns the optical depth with only the approximate solution to the radiative transfer problem.

```
crrlpy.models.rrlmod.j_line_lte(n, ne, nion, Te, Z, trans)
```

```
crrlpy.models.rrlmod.kappa_cont (freq, Te, ne, nion, Z)
```

Computes the absorption coefficient for the free-free process.

```
crrlpy.models.rrlmod.kappa_cont_base(nu, Te, ne, nion, Z)
```

```
crrlpy.models.rrlmod.kappa_line(Te, ne, nion, Z, Tr, trans, n_max=1500)
```

Computes the line absorption coefficient for CRRLs between levels  $n_i$  and  $n_f$ ,  $n_i > n_f$ . This can only go up to  $n_{\text{max}}$  1500 because of the tables used for the Einstein Anm coefficients.

#### **Parameters**

- **Te** (*float*) Electron temperature of the gas. (K)
- **ne** (*float*) Electron density.  $(cm^{-3})$
- nion (float) Ion density. (cm<sup>-3</sup>)
- **z** (*int*) Electric charge of the atoms being considered.
- **Tr** (*float*) Temperature of the radiation field felt by the gas. This specifies the temperature of the field at 100 MHz. (K)
- **trans** (*string*) Transition for which to compute the absorption coefficient.
- n\_max (int<1500) Maximum principal quantum number to include in the output.

# Returns

### Return type array

crrlpy.models.rrlmod.kappa\_line\_lte (nu, Te, ne, nion, Z, Tr, line, n\_min=1, n\_max=1500) Returns the line absorption coefficient under LTE conditions.

#### **Parameters**

- nu (array) Frequency. (Hz)
- **Te** (*float*) Electron temperature of the gas. (K)
- **ne** (*float*) Electron density.  $(cm^{-3})$
- nion (float) Ion density. (cm<sup>-3</sup>)
- **Z** (*int*) Electric charge of the atoms being considered.
- **Tr** (*float*) Temperature of the radiation field felt by the gas. This specifies the temperature of the field at 100 MHz. (K)
- trans (*string*) Transition for which to compute the absorption coefficient.
- n\_max (int<1500) Maximum principal quantum number to include in the output.

#### Returns

#### **Return type** array

- crrlpy.models.rrlmod.level\_pop\_lte (n, ne, nion, Te, Z)Returns the level population of level n. The return has units of cm<sup>-3</sup>.
- crrlpy.models.rrlmod.load\_betabn (temp, dens, other='', trans='Clalpha', verbose=False)
  Loads a model for the CRRL emission.
- crrlpy.models.rrlmod.load\_betabn\_h (temp, dens, other='', trans='alpha', verbose=False)
  Loads a model for the HRRL emission.
- crrlpy.models.rrlmod.load\_bn (temp, dens, other='')
  Loads the bn values from the CRRL models.
- crrlpy.models.rrlmod.load\_bn2 (temp, dens, other='')
  Loads the bn values from the CRRL models.
- crrlpy.models.rrlmod.load\_itau\_all(trans='Clalpha', n\_min=5, n\_max=1000, verbose=False, value='itau')

  Loads all the available models for Carbon.
- crrlpy.models.rrlmod.load\_itau\_all\_hydrogen(trans='alpha', n\_max=1000, ver-bose=False, value='itau')

  Loads all the available models for Hydrogen.

Loads all trans\_out models that can be found in trans\_tin. This is useful when analyzing line ratios.

- crrlpy.models.rrlmod.load\_itau\_all\_norad(trans='alpha', n\_max=1000) Loads all the available models.
- crrlpy.models.rrlmod.load\_itau\_dict(dict, trans, n\_min=5, n\_max=1000, verbose=False, value='itau')

  Loads the models defined by dict.
- crrlpy.models.rrlmod.load\_itau\_nelim(temp, dens, trad, trans, n\_max=1000, verbose=False, value='itau')

  Loads models given a temperature, radiation field and an upper limit for the electron density.
- crrlpy.models.rrlmod.load\_models (models, trans, n\_max=1000, verbose=False, value='itau') Loads the models in backwards compatible mode. It will sort the models by Te, ne and Tr.

```
crrlpy.models.rrlmod.make_betabn (line, temp, dens, n_min=5, n_max=1000, other='')
crrlpy.models.rrlmod.make_betabn2 (line, temp, dens, n_min=5, n_max=1000, other='')
crrlpy.models.rrlmod.plaw(x, x0, y0, alpha)
    Returns a power law.
```

 $y(x) = y_0 \left(\frac{x}{x_0}\right)^{\alpha}$ 

# y(x) =

#### **Parameters**

- **x** (*float or array like*) x values for which to compute the power law.
- $\mathbf{x0}$  (*float*) x value for which the power law has amplitude y0.
- **y0** (*float*) Amplitude of the power law at *x0*.
- alpha (*float*) Index of the power law.

**Returns** A power law of index *alpha* evaluated at x, with amplitude y0 at x0.

Return type float or array

```
crrlpy.models.rrlmod.str2val(str)
```

Converts a string representing a number to a float. The string must follow the IDL convention for floats.

**Parameters** str (*string*) – String to convert.

**Returns** The equivalent number.

Return type float

# Example

```
>>> str2val('2d2')
200
```

```
crrlpy.models.rrlmod.val2str(val)
```

Converts a float to the string format required for loading the CRRL models.

**Parameters val** (*float*) – Value to convert to a string.

**Returns** The value of val represented as a string in IDL double format.

Return type string

# Example

```
>>> val2str(200)
'2d2'
```

```
crrlpy.models.rrlmod.valid_ne (trans)
```

Checks all the available models and lists the available ne values.

crrlpy.models.rrlmod.xi (n, Te, Z)

# CRRLPY.CRRLS.FREC CALC MODULE

```
crrlpy.frec_calc.line_freq(Z, R_X, n, dn)
```

Uses the Rydberg formula to get the frequency of a transition to quantum number n for a given atom.

# **Parameters**

- **Z** (*int*) Charge of the atom.
- R X (float) -
- **n** (*int*) Principal quantum number of the transition.  $n + \Delta n \rightarrow n$ .
- dn (int) Difference between the principal quantum number of the initial state and the final state.  $\Delta n = n_f n_i$ .

**Returns** The frequency of the transition in MHz.

#### Return type float

```
crrlpy.frec_calc.main()
```

Main body of the program. Useful for calling as a script.

crrlpy.frec\_calc.make\_line\_list(line, n\_min=1, n\_max=1500, unitless=True)

Creates a list of frequencies for the corresponding line. The frequencies are in MHz.

#### Parameters

- line (*string*) Line to compute the frequencies for.
- n\_min (int) Minimum n number to include in the list.
- n max (int) Maximum n number to include in the list.
- unitless (*bool*) If True the list will have no units. If not the list will be of astropy.units.Quantity objects.

**Returns** 3 lists with the line name, principal quantum number and frequency of the transitions.

# Return type list

```
crrlpy.frec_calc.set_dn(name)
```

Sets the value of Delta n depending on the transition name.

**Parameters** name (*string*) – Name of the transition.

**Returns**  $\Delta n$  for the given transition.

Return type int

Example

```
>>> set_dn('CIalpha')
1
>>> set_dn('CIdelta')
4
```

```
crrlpy.frec_calc.set_specie(specie)
```

Sets atomic constants based on the atomic specie.

Parameters specie (string) – Atomic specie.

**Returns** Array with the atomic mass in a.m.u., ionization potential, abundance relative to HI,  $V_X - V_H$  and the electric charge.

# **Example**

```
>>> set_specie('CI')
[12.0, 11.4, 0.0003, 149.5, 1.0]
```

```
crrlpy.frec_calc.set_trans(dn)
```

Sets a name depending on the difference between atomic levels.

**Parameters** dn (int) – Separation between  $n_i$  and  $n_f$ ,  $\Delta n = n_i - n_f$ .

**Returns** alpha, beta, gamma, delta or epsilon depending on  $\Delta n$ .

Return type string

# **Example**

```
>>> set_trans(5)
'epsilon'
```

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