

**CSE 207**  
**CT 2-SET B**  
**Date: 10/01/2022**  
**Time: 20 minutes**

**Name:** \_\_\_\_\_

**ID:**\_\_\_\_\_

1. Both in Dijkstra and in Prim we have a set of nodes  $S$  (that initially contains only  $s$ ), and we add one additional node in each iteration. Prove or disprove that in both algorithms the nodes are added to  $S$  in the same order.
2. Give an efficient algorithm to find the length (number of edges) of a minimum length negative-weight cycle in a graph.
3. Decide whether you think the following statement is true or false. If it is true, give a short explanation. If it is false, give a counterexample.  
Let  $G$  be an arbitrary flow network, with a source  $s$ , a sink  $t$ , and a positive integer capacity  $c_e$  on every edge  $e$ . If  $f$  is a maximum  $s$ - $t$  flow in  $G$ , then  $f$  saturates every edge out of  $s$  with flow (i.e., for all edges  $e$  out of  $s$ , we have  $f(e)=c_e$ ).