

UNIT-4

SCHEMA REFINEMENT and NORMAL FORMS

Syllabus: Problems caused by redundancy, Decompositions, problem related to decomposition, reasoning about FDS, FIRST, SECOND, THIRD Normal forms, BCNKF, Lossless join Decomposition, Dependency preserving Decomposition, Schema refinement in Data base Design, Multi valued Dependencies, FORTH Normal Form.

Schema Refinement: The purpose of Schema refinement is used for a refinement approach based on decompositions. Redundant storage of information (i.e. duplication of data) is main cause of problem. This redundancy is eliminated by decompose the relation.

Q. Problems caused by redundancy: Redundancy is a method of storing the same information repeatedly. It means, storing the same data more than one place with in a database is can lead several problems. Such as

1) **Redundant Storage:** It removes the multi-valued attribute. It means, some tuples or information is stored repeatedly.

2) **Update Anomalies:** Suppose, if we update one row (or record) then DBMS will update more than one similar row, causes update anomaly.

For example, if we update the department name those who getting the salary 40000 then that will update more than one row of employee table is causes update anomaly.

3) **Insertion Anomalies:** In insertion anomaly, when allows insertion for already existed record again, causes insertion anomaly.

4) **Deletion Anomalies:** In deletion anomaly, when more than one record is deleted instead of specified or one, causes deletion anomaly.

Consider the following example,

Eno	ename	salary	rating	hourly_wages	hours_worked
111	suresh	25000	8	10	40
222	eswar	30000	8	10	30
333	sankar	32000	5	7	30
444	padma	31000	5	7	32
555	aswani	35000	8	10	40

In this example,

1) **Redundancy storage:** The rating value 8 corresponds to the hourly_wages 10 and there is repeated three times.

2) **Update anomalies:** If the hourly_wages in the first tuple is updated, it does not make changes in the corresponding second and last tuples. Because, the key element of tuples is emp_id.

i.e. update employee set hourly_wages = 12 where emp_id = 140; But the question is update hourly_wages from 10 to 12.

3) **Insertion anomalies:** If we have to inset a new tuple for an employee, we should know both the values rating value as well as hourly_wages value.

4) **Deletion anomalies:** Delete all the tuples through a given rating value, causes deletion anomaly.

Q. Decompositions: A relation schema (table) R can be decomposed into a collection of smaller relation schemas (tables) (i.e. R_1, R_2, \dots, R_m) to eliminate anomalies caused by the redundancy in the original relation R is called Decomposition of relation. This is shown in Relational Algebra as

$$R_i \subseteq R \text{ for } 1 \leq i \leq m \text{ and } R_1 \cup R_2 \cup R_3 \dots R_m = R.$$

(or)

A decomposition of a relation schema R consists of replacing the relation schema by two or more relation schemas that each contains a subset of the attributes of R and together include all attributes in R.

(or)

In simple words, "The process of breaking larger relations into smaller relations is known as decomposition".

Consider the above example that can be decomposed the following hourly_emps relation into two relations.

Hourly_emp (eno, ename, salary, rating, hourly_wages, hours_worked)

This is decomposed into

Hourly_empsd(eno, ename, salary, rating, hours_worked) and

Wages(rating, hourly_wages)

Eno	ename	salary	rating	hours_worked
111	suresh	25000	8	40
222	eswar	30000	8	30
333	sankar	32000	5	30
444	padma	31000	5	32
555	aswani	35000	8	40

rating	hourly_wages
8	10
5	7

Q. Problems Related to Decomposition:

The use of Decomposition is to split the relation into smaller parts to eliminate the anomalies. The question is

1. What are problems that can be caused by using decomposition?
2. When do we have to decompose a relation?

The answer for the **first** question is, two properties of decomposition are considered.

- 1) **Lossless-join Property:** This property helps to identify any instance of the original relation from the corresponding instance of the smaller relation attained after decomposition.
- 2) **Dependency Preservation:** This property helps to enforce constraint on smaller relation in order to enforce the constraints on the original relation.

The answer for the **second** question is, number of normal forms exists. Every relation schema is in one of these normal forms and these normal forms can help to decide whether to decompose the relation schema further or not.

The **Disadvantage** of decomposition is that it enforces us to join the decomposed relations in order to solve the queries of the original relation.

Q. What is Relation?: A relation is a named two-dimensional table of data. Each relation consists of a set of named columns and an arbitrary number of unnamed rows.

For example, a relation named Employee contains following attributes, emp-id, ename, dept name and salary.

Emp-id	ename	dept name	salary
100	Simpson	Marketing	48000
140	smith	Accounting	52000
110	Lucero	Info-systems	43000
190	Davis	Finance	55000
150	martin	marketing	42000

marketing 42000

What are the Properties of relations?:

The properties of relations are defined on two dimensional tables. They are:

- ❑ Each relation (or table) in a database has a unique name.
- ❑ An entry at the intersection of each row and column is atomic or single. These can be no multiplied attributes in a relation.
- ❑ Each row is unique, no two rows in a relation are identical.
- ❑ Each attribute or column within a table has a unique name.
- ❑ The sequence of columns (left to right) is insignificant the column of a relation can be interchanged without changing the meaning use of the relation.
- ❑ The sequence of rows (top to bottom) is insignificant. As with column, the rows of relation may be interchanged or stored in any sequence.

Q. Removing multi valued attributes from tables: the "second property of relations" in the above is applied to this table. In this property, there is no multi valued attributes in a relation. This rule is applied to the table or relation to eliminate the one or more multi valued attribute. Consider the following the example, the employee table contain 6 records. In this the course title has multi valued values/attributes. The employee 100 taken two courses vc++ and ms-office. The record 150 did not taken any course. So it is null.

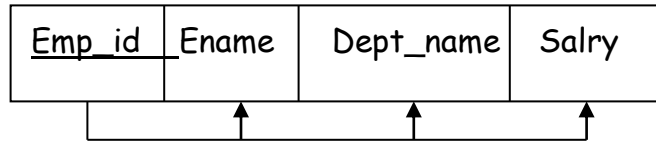
Emp-id	name	dept-name	salary	course_title
100	Krishna	cse	20000	vc++, msoffice
140	Rajasekhar	cse	18000	C++, DBMS,DS

Now, this multi valued attributes are eliminated and shown in the following employee2 table.

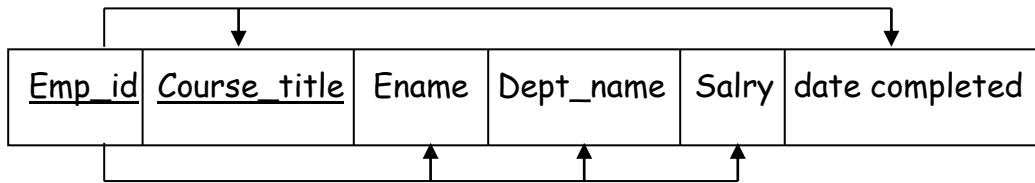
Emp-id	name	dept-name	salary	course_title
100	Krishna	cs	20000	vc++
100	Krishna	cs	20000	MSoffice
140	Rajasekhar	cs	18000	C++
140	Rajasekhar	cs	18000	DBMS
140	Rajasekhar	cs	18000	DS

Functional dependencies : A functional dependency is a constraint between two attributes (or) two sets of attributes.

For example, the table EMPLOYEE has 4 columns that are Functionally dependencies on EMP_ID.



Partial functional dependency : It is a functional dependency in which one or more non-key attributes are functionally dependent on part of the primary key. Consider the following graphical representation, in that some of the attributes are partially depend on primary key.



In this example, Ename, Dept_name, and salary are fully functionally depend on Primary key of Emp_id. But Course_title and date_completed are partial functional dependency. In this case, the partial functional dependency creates redundancy in that relation.

Q. What is Normal Form? What are steps in Normal Form?

NORMALIZATION: Normalization is the process of decomposing relations to produce smaller, well-structured relation.

To produce smaller and well structured relations, the user needs to follow six normal forms.

Steps in Normalization:

A normal form is state of relation that result from applying simple rules from regarding functional dependencies (relationships between attributes to that relation. The normal form are

1. First normal form
2. Second normal form
3. Third normal form
4. Boyce/codd normal form
5. Fourth normal form
6. Fifth normal form

- 1) **First Normal Form**: Any multi-valued attributes (also called repeating groups) have been removed,
- 2) **Second Normal Form**: Any partial functional dependencies have been removed.
- 3) **Third Normal Form**: Any transitive dependencies have been removed.
- 4) **Boyce/Codd Normal Form**: Any remaining anomalies that result from functional dependencies have been removed.
- 5) **Fourth Normal Form**: Any multi-valued dependencies have been removed.
- 6) **Fifth Normal Form**: Any remaining anomalies have been removed.

Advantages of Normalized Relations Over the Un-normalized Relations: The advantages of normalized relations over un-normalized relations are,

- 1) Normalized relation (table) does not contain repeating groups whereas, un-normalized relation (table) contains one or more repeating groups.
- 2) Normalized relation consists of a primary key. There is no primary key presents in un-normalized relation.
- 3) Normalization removes the repeating group which occurs many times in a table.
- 4) With the help of normalization process, we can transform un-normalized table to First Normal Form (1NF) by removing repeating groups from un-normalized tables.
- 5) Normalized relations (tables) gives the more simplified result whereas un-normalized relation gives more complicated results.
- 6) Normalized relations improve storage efficiency, data integrity and scalability. But un-normalized relations cannot improvise the storage efficiency and data integrity.
- 7) Normalization results in database consistency, flexible data accesses.

Q. FIRST NORMAL FORM (1NF): A relation is in first normal form (1NF) contains no multi-Valued attributes. Consider the example employee, that contain multi valued attributes that are removing and converting into single valued attributes

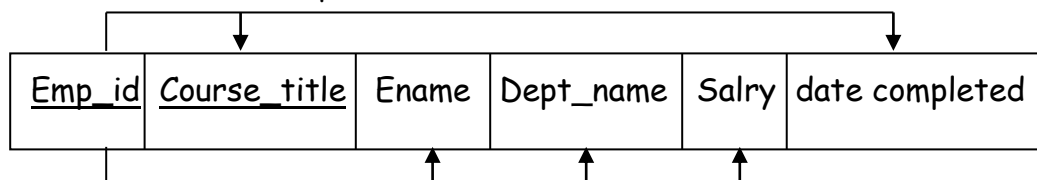
Multi valued attributes in course title

Emp-id	name	dept-name	salary	course_title
100	Krishna	cse	20000	vc++, msoffice
140	Raja	it	18000	C++, DBMS, DS

Removing the multi valued attributes and converting single valued using First NF

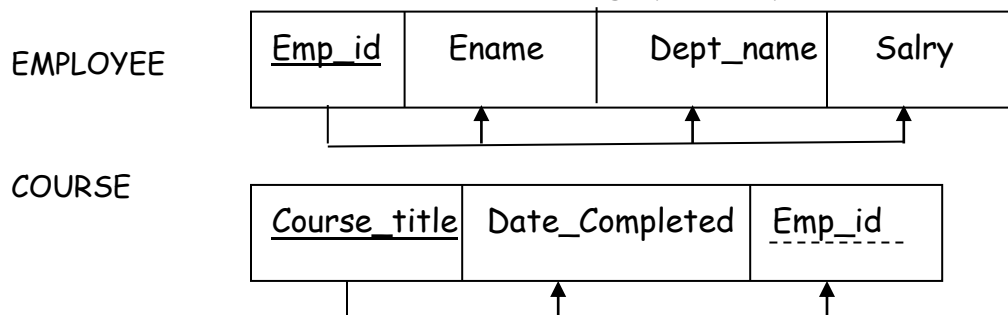
Emp-id	name	dept-name	salary	course_title
100	Krishna	cse	20000	vc++
100	Krishna	cse	20000	msoffice
140	Raja	it	18000	C++
140	Raja	it	18000	DBMS
140	Raja	it	18000	DS

SECOND NORMAL FORM(2NF): A relation in Second Normal Form (2NF) if it is in the 1NF and if all non-key attributes are fully functionally dependent on the primary key. In a functional dependency $X \rightarrow Y$, the attribute on left hand side (i.e. x) is the primary key of the relation and right side attributes on right hand side i.e. Y is the non-key attributes. In some situation some non key attributes are partial functional dependency on primary key. Consider the following example for partial functional specification and also that convert into 2 NF to decompose that into two relations.



In this example, Ename, Dept_name, and salary are fully functionally depend on Primary key of Emp_id. But Course_title and date_completed are partial functional dependency. In this case, the partial functional dependency creates redundancy in that relation.

- To avoid this, convert this into Second Normal Form. The 2NF will decompose the relation into two relations, shown in graphical representation.

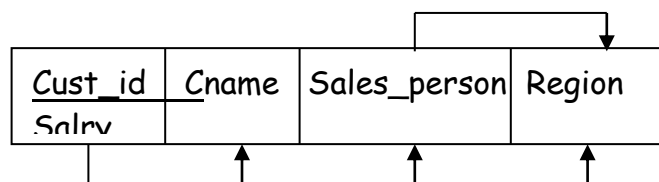


In the above graphical representation

- the EMPLOYEE relation satisfies rule of 1 NF in Second Normal form and
- the COURSE relation satisfies rule of 2 NF by decomposing into two relation.

THIRD NORMAL FORM(3NF): A relation that is in Second Normal form and has no transitive dependencies present.

Transitive dependency : A transitive is a functional dependency between two non key attributes. For example, consider the relation Sales with attributes cust_id, name, sales person and region that shown in graphical representation.



<u>CUST ID</u>	<u>NAME</u>	<u>SALESPERSON</u>	<u>REGION</u>
1001	Anand	Smith	South
1002	Sunil	kiran	West
1003	Govind	babu rao	East
1004	Manohar	Smith	South
1005	Madhu	Somu	North

In this example, to insert, delete and update any row that facing Anomaly.

- Insertion Anomaly:** A new salesperson is assigned to North Region without assign a customer to that salesperson. This causes insertion Anomaly.
- Deletion Anomaly:** If a customer number say 1003 is deleted from the table, we lose the information of salesperson who is assigned to that customer. This causes, Deletion Anomaly.
- Modification Anomaly:** If salesperson Smith is reassigned to the East region, several rows must be changed to reflect that fact. This causes, update anomaly.

To avoid this Anomaly problem, the transitive dependency can be removed by decomposition of SALES into two relations in **3NF**.

Consider the following example, that removes Anomaly by decomposing into two relations.

CUST_ID	NAME	SALESPERSON	SALESPERSON	REGION
1001	Anand	Smith	Smith	South
1002	Sunil	kiran	kiran	West
1003	Govind	babu rao	babu rao	East
1004	Manohar	Smith	Smith	South
1005	Madhu	Somu	Somu	North

SALES PERSON

Sales_person	Region
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CUSTOMER

<u>Cust_id</u>	Cname	Salry
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Q. BOYCE/CODD NORMAL FORM(BCNF): A relation is in BCNF if it is in 3NF and every determinant is a candidate key.

FD in F^+ of the form $X \rightarrow A$ where $X \subseteq S$ and $A \in S$, X is a super key of R .

Boyce-Codd normal form removes the remaining anomalies in 3NF that are resulting from functional dependency, we can get the result of relation in BCNF.

For example, STUDENT-ADVISOR IN 3NF

STUDENT-ADVISOR

Student-id	major-subject	faculty-advisor
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STUDENT-ADVISOR relation with simple data.

<u>STYDENT-ID</u>	<u>MAJOR-SUBJECT</u>	FACULTY-ADVISOR
1	MATHS	B
2	MATHS	B
3	MATHS	B
4	STATISTICS	A
5	STATISTICS	A

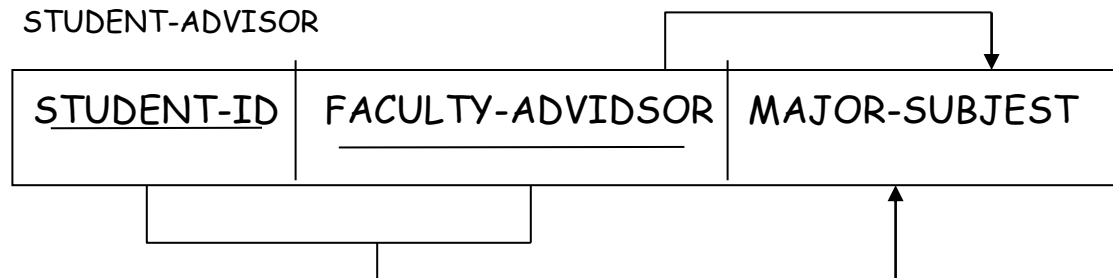
In the above relation the primary key is student-id and major-subject. Here the part of the primary key major-subject is dependent upon a non key attribute faculty-advisor. So, here the determinant is the faculty-advisor. But it is not a candidate key.

Here in this example there are no partial dependencies and transitive dependencies. There is only functional dependency between part of the primary key and non key attribute. Because of this dependency there is an anomaly in this relation.

Suppose that in maths subject the advisor 'B' is replaced by X. This change must be made in two or more rows in this relation. This is an update anomaly.

To convert a relation to BCNF the first step in the original relation is modified that the determinant(non key attributes) becomes a component of the primary key of new relation. The attribute that is dependent on determinant becomes a non key attributes .

STUDENT-ADVISOR



The second step in the conversion process is decompose the relation to eliminate the partial functional dependency. This results in two relations. these relations are in 3NF and BCNF . since there is only one candidate key. That is determinant.

Two relations are in BCNF.

ADVISOR

<u>Faculty- advisor</u>	major-subject
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STUDENT

<u>Student-id</u>	faculty-advisor
-------------------	-----------------

In these two relations the student relation has a composite key , which contains attributes student-id and faculty-advisor. Here faculty-advisor a foreign key which is referenced to the primary key of the advisor relation.

Two relations are in BCNF with simple data.

<u>Faculty Advisor</u>	Major_subject_
B	MATHS
A	PHYSICS

Student_id	Faculty_Advisor
1	B
2	B
3	A
4	A
5	A

Q.Fourth Normal Form (4 NF) : A relation is in BCNF that contain no multi-valued dependency. In this case, 1 NF will repeated in this step. For example, R be a relation schema, X and Y be attributes of R, and F be a set of dependencies that includes both FDs and MVDs. (i.e. Functional Dependency and Multi-valued Dependencies). Then R is said to be in Fourth Normal Form (4NF) if for every MVD $X \twoheadrightarrow Y$ that holds over R, one of the following statements is true.

1) $Y \subseteq X$ or $XY = R$, or 2) X is a super key.

Example: Consider a relation schema ABCD and suppose that are FD $A \rightarrow BCD$ and the MVD $B \twoheadrightarrow C$ are given as shown in Table

It shows three tuples from relation ABCD that satisfies the given MVD $B \twoheadrightarrow C$. From the definition of a MVD, given tuples t_1 and t_2 , it follows that tuples t_3 must also be included in the above relation. Now, consider tuples t_2 and t_3 . From the given FD $A \rightarrow BCD$ and the fact that these tuples have the same A-value, we can compute

B	C	A	D	tuples
b	c ₁	a ₁	d ₁	- tuple t ₁
b	c ₂	a ₂	d ₂	- tuple t ₂
b	c ₁	a ₂	d ₂	- tuple t ₃

the $C_1 = C_2$. Therefore, we see that the FD $B \rightarrow C$ must hold over ABCD whenever the FD $A \rightarrow BCD$ and the MVD $B \twoheadrightarrow C$ holds. If $B \rightarrow C$ holds, the relation is not in BCNF but the relation is in 4 NF.

The fourth normal form is useful because it overcomes the problems of the various approaches in which it represents the multi-valued attributes in a single relation.

Q. Fifth Normal Form (5 NF) : Any remaining anomalies from 4 NF relation have been removed.

A relation schema R is said to be in Fifth Normal Form (5NF) if, for every join dependency

$\star (R_1, \dots, R_n)$ that holds over R, one of the following statements is true.

* $R_i = R$ for some i , or

* The JD is implied by the set of those FDs over R in which the left side is a key for R. It deals with a property loss less joins.

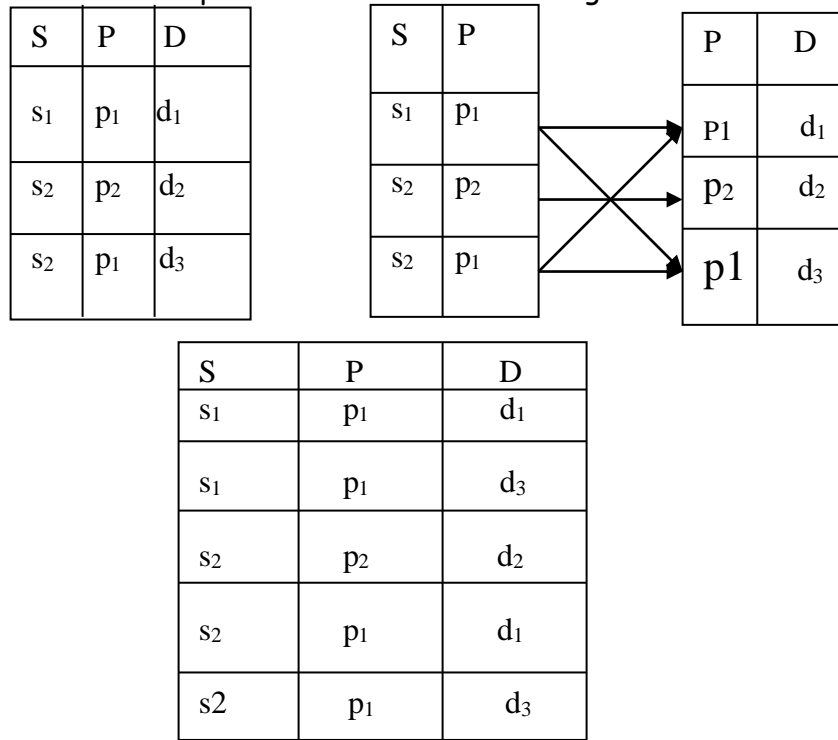
Q. LOSSELESS-JOIN DECOMPOSITION:

Let R be a relation schema and let F be a set FDs (Functional Dependencies) over R. A decomposition of R into two schemas with attribute X and Y is said to be lossless-join decomposition with respect to F, if for every instance r of R that satisfies the dependencies in F_r .

$$\pi_X(r) \bowtie \pi_Y(r) = r$$

In simple words, we can recover the original relation from the decomposed relations.

In general, if we take projection of a relation and recombine them using natural join, we obtain some additional tuples that were not in the original relation.



The decomposition of relation schema r i.e. SPD into SP i.e. PROJECTING $\pi_{sp}(r)$ and PD i.e., projecting $\pi_{pd}(r)$ is therefore lossless decomposition as it gains back all original tuples of relation ' r ' as well as with some additional tuples that were not in original relation ' r '.

Q. Dependency-Preserving Decomposition:

Dependency-preserving decomposition property allows us to check integrity constraints efficiently. In simple words, a dependency-preserving decomposition allows us to enforce all FDs by examining a single relation on each insertion or modification of a tuple.

Let R be a relation schema that is decomposed in two schemas with attributes X and Y and let F be a set of FDs over R . The projection of F on X is the set of FDs in the closure F^+ that involves only attributes in X . We denote the projection of F on attributes X as F_x . Note that a dependency $U \rightarrow V$ in F^+ is in F_x only if all the attributes in U and V are in X . The decomposition of relation schema R with FDs F into schemas with attributes X and Y is dependency-preserving if $(F_x \cup F_y)^+ = F^+$.

That is, if we take the dependencies in F_x and F_y and compute the closure of their union, then we get back all dependencies in the closure of F . To enforce F_x , we need to examine only relation X (that inserts on that relation) to enforce F_y , we need to examine only relation Y .

Example: Suppose that a relation R with attributes ABC is decomposed into relations with attributes AB and BC . The set F of FDs over r includes $A \rightarrow B$, $B \rightarrow C$ and $C \rightarrow A$. Here, $A \rightarrow B$ is in F_{AB} and $B \rightarrow C$ is in F_{BC} and both are dependency-preserving. Where as $C \rightarrow A$ is not implied by the dependencies of F_{AB} and F_{BC} . Therefore $C \rightarrow A$ is not dependency-preserving.

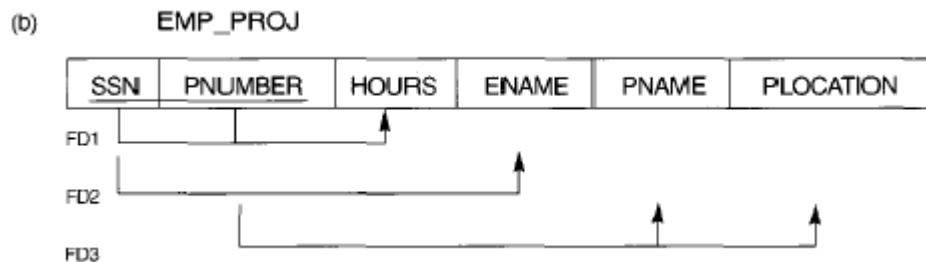
Consequently, F_{AB} also contains $B \rightarrow A$ as well as $A \rightarrow B$ and F_{BC} contains $C \rightarrow B$ as well as $B \rightarrow C$. Therefore $F_{AB} \cup F_{BC}$ contain $A \rightarrow B$, $B \rightarrow C$, $B \rightarrow A$ and $C \rightarrow B$.

Now, the closure of the dependencies in F_{AB} and F_{BC} includes $C \rightarrow A$ (because, from $C \rightarrow B$, $B \rightarrow A$ and transitivity rule, we compute as $C \rightarrow A$).

Functional Dependency (FD) is a constraint that determines the relation of one attribute to another attribute in a Database Management System (DBMS). Functional Dependency helps to maintain the quality of data in the database.

A functional dependency is denoted by an arrow " \rightarrow ". The functional dependency of X on Y is represented by $X \rightarrow Y$. Let's understand Functional Dependency in DBMS with example

$$x \rightarrow y$$

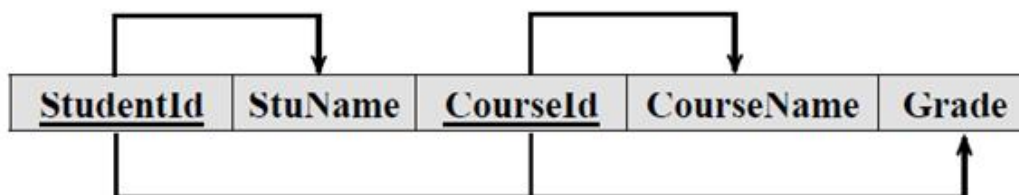


FD1: {SSN, PNUMBER} \rightarrow HOURS

FD2: SSN \rightarrow ENAME

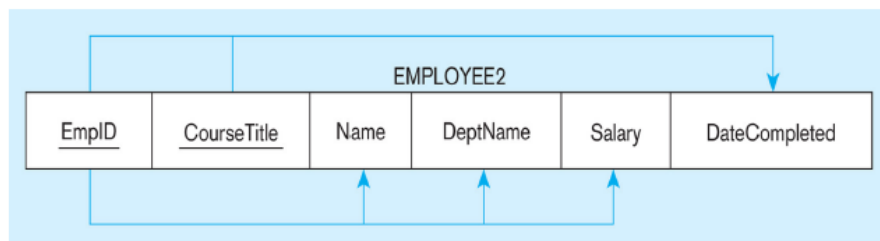
FD3: PNUMBER \rightarrow {PNAME, PLOCATION}

Functional Dependencies in Student



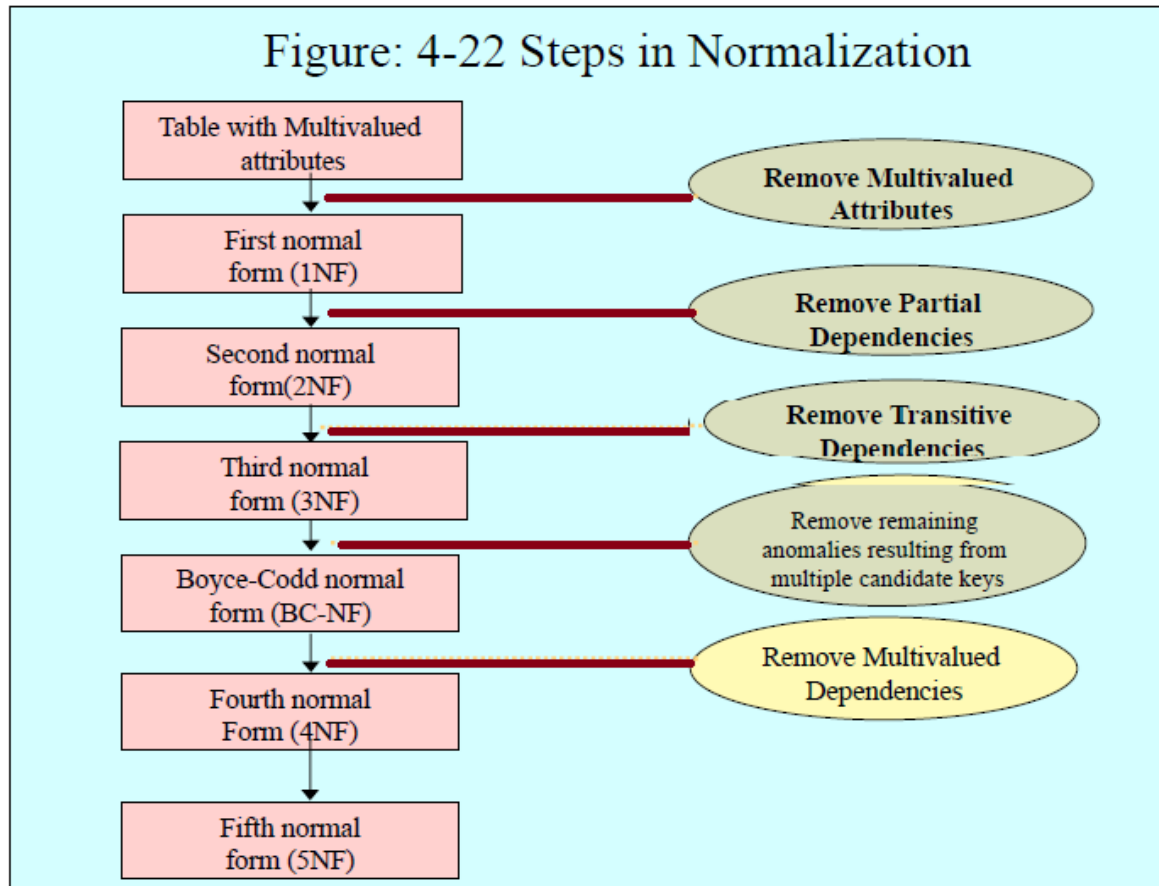
Can represent FDs with arrows as above, or

- StudentId \rightarrow StuName,
- CourseId \rightarrow CourseName
- StudentId, CourseId \rightarrow Grade (and StuName, CourseName)



EmpID → _____

EmpID, CourseTitle → _____



10.3.4 First Normal Form

First normal form (1NF) is now considered to be part of the formal definition of a relation in the basic (flat) relational model;¹² historically, it was defined to disallow multivalued attributes, composite attributes, and their combinations. It states that the domain of an attribute must include only *atomic* (simple, indivisible) *values* and that the value of any attribute in a tuple must be a *single value* from the domain of that attribute. Hence, 1NF disallows having a set of values, a tuple of values, or a combination of both as an attribute value for a *single tuple*. In other words, 1NF disallows “relations within relations” or “relations as attribute values within tuples.” The only attribute values permitted by 1NF are single **atomic** (or **indivisible**) **values**.

Consider the DEPARTMENT relation schema shown in Figure 10.1, whose primary key is DNUMBER, and suppose that we extend it by including the DLOCATIONS attribute as shown in Figure 10.8a. We assume that each department can have a *number of* locations. The DEPARTMENT schema and an example relation state are shown in Figure 10.8. As we can see,

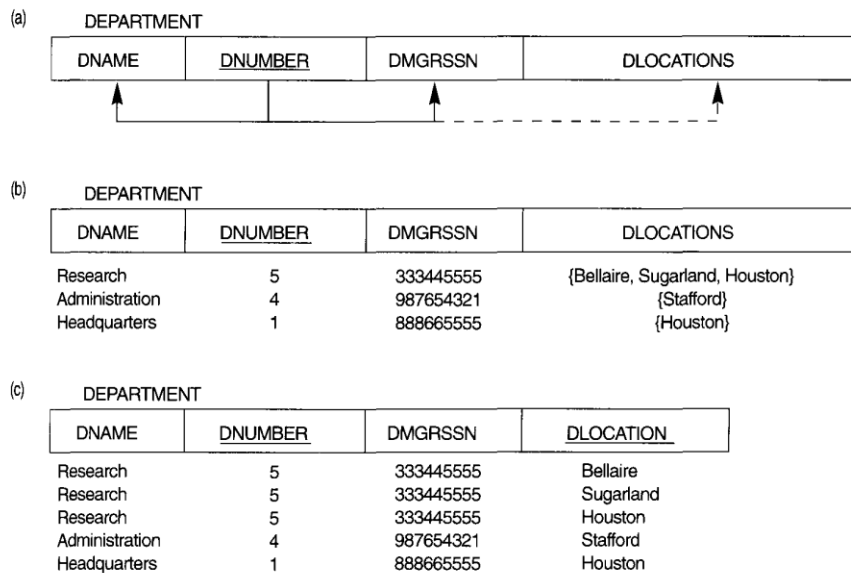


FIGURE 10.8 Normalization into 1NF. (a) A relation schema that is not in 1NF. (b) Example state of relation DEPARTMENT. (c) 1NF version of same relation with redundancy.

12. This condition is removed in the *nested relational model* and in *object-relational systems* (ORDBMSs), both of which allow *unnormalized relations* (see Chapter 22).

(a) **EMP_PROJ**

SSN	ENAME	PROJS	
		PNUMBER	HOURS

(b) **EMP_PROJ**

SSN	ENAME	PNUMBER	HOURS
123456789	Smith, John B.	1	32.5
		2	7.5
666884444	Narayan, Ramesh K.	3	40.0
453453453	English, Joyce A.	1	20.0
		2	20.0
333445555	Wong, Franklin T.	2	10.0
		3	10.0
		10	10.0
		20	10.0
999887777	Zelaya, Alicia J.	30	30.0
987987987	Jabbar, Ahmad V.	10	10.0
		30	5.0
987654321	Wallace, Jennifer S.	30	20.0
888665555	Borg, James E.	20	15.0
		20	null

(c) **EMP_PROJ1**

<u>SSN</u>	ENAME
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EMP_PROJ2

<u>SSN</u>	<u>PNUMBER</u>	HOURS
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FIGURE 10.9 Normalizing nested relations into 1NF. (a) Schema of the EMP_PROJ relation with a “nested relation” attribute PROJS. (b) Example extension of the EMP_PROJ relation showing nested relations within each tuple. (c) Decomposition of EMP_PROJ into relations EMP_PROJ1 and EMP_PROJ2 by propagating the primary key.

tuple represents the employee’s projects and the hours per week that employee works on each project. The schema of this EMP_PROJ relation can be represented as follows:

EMP_PROJ(SSN, ENAME, {PROJS(PNUMBER, HOURS)})

The set braces { } identify the attribute PROJS as multivalued, and we list the component attributes that form PROJS between parentheses (). Interestingly, recent trends for supporting complex objects (see Chapter 20) and XML data (see Chapter 26) using the relational model attempt to allow and formalize nested relations within relational database systems, which were disallowed early on by 1NF.

If a relation schema is not in 2NF, it can be “second normalized” or “2NF normalized” into a number of 2NF relations in which nonprime attributes are associated only with the part of the primary key on which they are fully functionally dependent. The functional dependencies FD1, FD2, and FD3 in Figure 10.3b hence lead to the decomposition of EMP_PROJ into the three relation schemas EP1, EP2, and EP3 shown in Figure 10.10a, each of which is in 2NF.

10.3.6 Third Normal Form

Third normal form (3NF) is based on the concept of *transitive dependency*. A functional dependency $X \rightarrow Y$ in a relation schema R is a **transitive dependency** if there is a set of

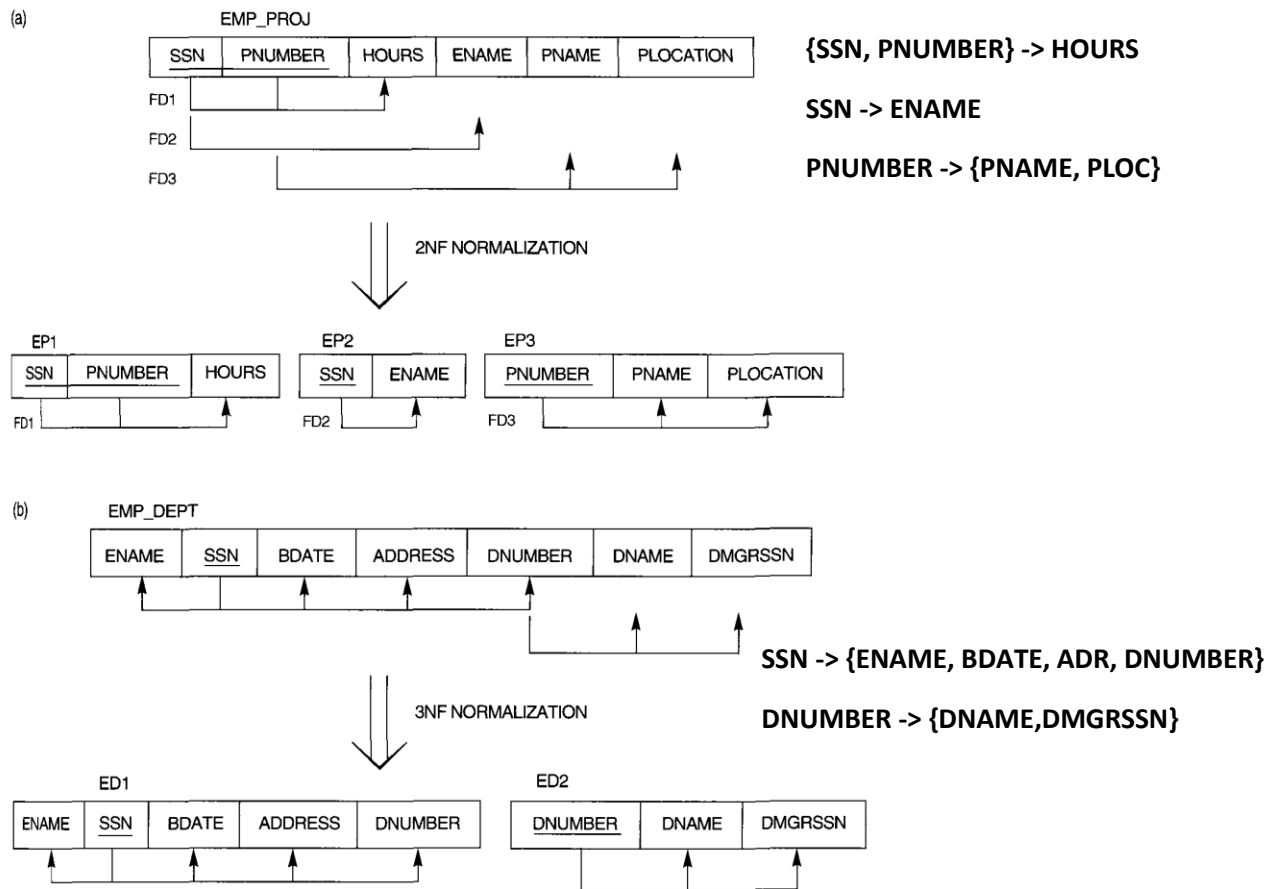


FIGURE 10.10 Normalizing into 2NF and 3NF. (a) Normalizing EMP_PROJ into 2NF relations. (b) Normalizing EMP_DEPT into 3NF relations.

Rules for 4th Normal Form

For a table to satisfy the Fourth Normal Form, it should satisfy the following two conditions:

1. It should be in the **Boyce-Codd Normal Form**.
2. And, the table should not have any **Multi-valued Dependency**.

Let's try to understand what multi-valued dependency is in the next section

What is Multi-valued Dependency?

A table is said to have multi-valued dependency, if the following conditions are true,

1. For a dependency $A \twoheadrightarrow B$, if for a single value of A, multiple value of B exists, then the table may have multi-valued dependency.
2. Also, a table should have at-least 3 columns for it to have a multi-valued dependency.
3. And, for a relation $R(A,B,C)$, if there is a multi-valued dependency between, A and B, then B and C should be independent of each other.

If all these conditions are true for any relation(table), it is said to have multi-valued dependency.

Time for an Example

Below we have a college enrolment table with columns **s_id**, **course** and **hobby**.

S_id	Course	Hobby
1	Science	Cricket
1	Maths	Hockey
2	C#	Cricket
2	Php	Hockey

As you can see in the table above, student with **s_id 1** has opted for two courses, **Science** and **Maths**, and has two hobbies, **Cricket** and **Hockey**.

you must be thinking what problem this can lead to, right?

Well the two records for student with **s_id 1**, will give rise to two more records, as shown below, because for one student, two hobbies exists, hence along with both the courses, these hobbies should be specified.

s_id	course	hobby
1	Science	Cricket
1	Maths	Hockey
1	Science	Hockey
1	Maths	Cricket

And, in the table above, there is no relationship between the columns **course** and **hobby**. They are independent of each other.

So there is multi-value dependency, which leads to un-necessary repetition of data and other anomalies as well.

How to satisfy 4th Normal Form?

To make the above relation satisfy the 4th normal form, we can decompose the table into 2 tables.

Course_Opted Table

S_id	Course
1	Science
1	Maths
2	C#
2	Php

Hobbies Table,

S_id	Hobby
1	Cricket
1	Hockey
2	Cricket
2	Hockey

Now this relation satisfies the fourth normal form.

A table can also have functional dependency along with multi-valued dependency. In that case, the functionally dependent columns are moved in a separate table and the multi-valued dependent columns are moved to separate tables.

Functional Dependency:

Prime Attribute → Non Prime Attributes

Partial dependency :

Part of Prime Attributes → Non Prime Attributes

Transitive Dependency:

Non Prime Attributes → Non Prime Attributes

BCNF Not allow this one

Non Prime Attributes → Prime Attributes

Rules for BCNF :

For a table to satisfy the Boyce-Codd Normal Form, it should satisfy the following two conditions:

1. It should be in the Third Normal Form.
2. And, for any dependency $A \rightarrow B$, A should be a super key.

The second point sounds a bit tricky, right? In simple words, it means, that for a dependency $A \rightarrow B$, A cannot be a non-prime attribute, if B is a prime attribute.

Example : Below we have a college enrolment table with columns student_id, subject and professor.

<u>student id</u>	<u>subject</u>	professor
101	Java	Ashok
101	C++	siva
102	Java	srinu
103	C#	ravi
104	Java	Ashok

(Student id,subject) → professor

Professor → subject

In the table above:

1. One student can enrol for multiple subjects. For example, student with student_id 101, has opted for subjects - Java & C++
2. For each subject, a professor is assigned to the student.
3. And, there can be multiple professors teaching one subject like we have for Java.

Well, in the table above student_id, subject together form the primary key, because using student_id and subject, we can find all the columns of the table. One more important point to note here is, one professor teaches only one subject, but one subject may have two different professors. Hence, there is a dependency between subject and professor here, where subject depends on the professor name.

This table satisfies the **1st Normal form** because all the values are atomic, column names are unique and all the values stored in a particular column are of same domain.

This table also satisfies the **2nd Normal Form** as there is **no Partial Dependency**.

And, there is **no Transitive Dependency**, hence the table also satisfies the **3rd Normal Form**.

But this table is not in Boyce-Codd Normal Form.

How to satisfy BCNF?

To make this relation(table) satisfy BCNF, we will decompose this table into two tables, **student table** and **professor table**.

Below we have the structure for both the tables.

Student Table

student_id	p_id
101	1
101	2
And so on..	

Professor Table

p_id	professor	subject
1	Ashok	Java
2	siva	C++

Rules for 4th Normal Form :

For a table to satisfy the Fourth Normal Form, it should satisfy the following two conditions:

1. It should be in the Boyce-Codd Normal Form.
2. And, the table should not have any Multi-valued Dependency

What is Multi-valued Dependency?

A table is said to have multi-valued dependency, if the following conditions are true,

1. For a dependency $A \twoheadrightarrow B$, if for a single value of A, multiple value of B exists, then the table may have multi-valued dependency.
2. Also, a table should have at-least 3 columns for it to have a multi-valued dependency.
3. And, for a relation $R(A,B,C)$, if there is a multi-valued dependency between, A and B, then B and C should be independent of each other.

If all these conditions are true for any relation(table), it is said to have multi-valued dependency.

Time for an Example

Below we have a college enrolment table with columns **s_id**, **course** and **hobby**.

s_id	course	hobby
1	Science	Cricket
1	Maths	Hockey
2	C#	Cricket
2	Php	Hockey

As you can see in the table above, student with **s_id 1** has opted for two courses, **Science** and **Maths**, and has two hobbies, **Cricket** and **Hockey**.

You must be thinking what problem this can lead to, right?

Well the two records for student with **s_id 1**, will give rise to two more records, as shown below, because for one student, two hobbies exists, hence along with both the courses, these hobbies should be specified.

s_id	course	hobby
1	Science	Cricket
1	Maths	Hockey
1	Science	Hockey
1	Maths	Cricket

And, in the table above, there is no relationship between the columns **course** and **hobby**. They are independent of each other.

So there is multi-value dependency, which leads to un-necessary repetition of data and other anomalies as well.

How to satisfy 4th Normal Form?

To make the above relation satisfy the 4th normal form, we can decompose the table into 2 tables.

CourseOpted Table

s_id	course
1	Science
1	Maths
2	C#
2	Php

And, Hobbies Table,

s_id	hobby
1	Cricket
1	Hockey
2	Cricket
2	Hockey

Now this relation satisfies the fourth normal form.

A table can also have functional dependency along with multi-valued dependency. In that case, the functionally dependent columns are moved in a separate table and the multi-valued dependent columns are moved to separate tables.