## 1 Explanation Generation

```
Algorithm 1: CSP-Explain(\mathcal{T}, f [, \mathcal{I}_0])
    input
                               : \mathcal{T} set of constraints
    input
                               : f a consistent objective function
    optional input: \mathcal{I}_0 a partial interpretation
                               : Explanation sequence
 1 begin
          \mathcal{I}_{end} \leftarrow \texttt{propagate}(\mathcal{I}_0, \ \mathcal{T})
                                                                                                                                            // Goal state
 \mathbf{2}
          \mathcal{I} \leftarrow \mathcal{I}_0
                                                                                                      // Initial partial interpretation
 3
          Seq \leftarrow \emptyset
                                                                                                                         // explanation sequence
 4
          while \mathcal{I} \neq \mathcal{I}_{end} do
 5
               for i \in \mathcal{I}_{end} \setminus \mathcal{I} do
 6
                     X_i \leftarrow \texttt{OMUS}(\{\neg i\} \land \mathcal{I} \land \mathcal{S})
 7
                     E_i \leftarrow \mathcal{I} \cap X_i
                                                                                                                                            // Facts used
 8
                     S_i \leftarrow \mathcal{T} \cap X_i
                                                                                                                                   // Constraint used
                     \mathcal{N}_i \leftarrow \mathtt{propagate}(E_i \wedge \mathcal{S}_i)
                                                                                                                           // Newly derived facts
10
11
                (E_{best}, S_{best}, N_{best}) \leftarrow (E_i, S_i, N_i) with lowest f(E_i, S_i, N_i)
12
                append (E_{best}, S_{best}, N_{best}) to Seq
13
               \mathcal{I} \leftarrow \mathcal{I} \cup \{N_{best}\}
          end
16 end
```

## Algorithm 2: CSP-Explain-Incremental $(\mathcal{T}, f [, \mathcal{I}_0])$

```
1 \mathcal{I}_{end} \leftarrow \texttt{propagate}(\mathcal{I}_0, \ \mathcal{T})
  \mathbf{2} \ \mathcal{I} \leftarrow \mathcal{I}_0
  \mathbf{3} , \mathcal{W} \leftarrow \emptyset
                                                                                                          // Collection of MSSes generated during {\tt OMUS}
  4 Seq \leftarrow \emptyset
  5 while \mathcal{I} \neq \mathcal{I}_{end} do
             for i \in \mathcal{I}_{end} \setminus \mathcal{I} do
                    X_i,~\mathcal{MSS} \leftarrow \mathtt{OMUS-DELAYED}(\{ \lnot i \} \land \mathcal{I} \land \mathcal{S} , \mathcal{M})
                     E_i \leftarrow \mathcal{I} \cap X_i
  8
                     S_i \leftarrow \mathcal{T} \cap X_i
                    \mathcal{N}_i \leftarrow \mathtt{propagate}(E_i \wedge \mathcal{S}_i)
10
                    \mathcal{M} \leftarrow \mathcal{M} \cup \mathcal{MSS}
11
              end
12
              (E_{best}, S_{best}, N_{best}) \leftarrow (E_i, S_i, N_i) with lowest f(E_i, S_i, N_i)
13
              append (E_{best}, S_{best}, N_{best}) to Seq
14
             \mathcal{I} \leftarrow \mathcal{I} \cup \{N_{best}\}
15
16 end
```

## **Algorithm 3:** OMUS-Delayed( $\mathcal{F}, \mathcal{M}, f_{cost}$ )

```
// F = unsatisfiable CNF formula; M = Collection of MSSes; f_{cost} = cost function
 1~\mathcal{K} \leftarrow \emptyset
     // grow mss from input mss
 2 foreach \mathcal{MSS} \in \mathcal{M} do
          \mathcal{MSS}' \leftarrow \mathtt{Grow}(\mathcal{F} \cap \mathcal{MSS})
          \mathcal{K} \leftarrow \mathcal{K} \cup \{\mathcal{F} \setminus \mathcal{MSS}'\}
 5 end
 \mathbf{6} \mod \leftarrow \mod_{\operatorname{greedy}}
    while true do
          while true do
 8
                switch nonOptLevel do
 9
                     case mode\_incr
10
                          hs \leftarrow \texttt{FindIncrementalHittingSet}(\mathcal{K}, \mathcal{C}, hs)
11
                     \mathbf{case}\ mode\_greedy
12
                          hs \leftarrow \texttt{FindGreedyHittingSet}(\mathcal{K})
13
                end
14
                (\text{sat?}, \kappa) \leftarrow \texttt{SatSolver}(hs)
15
                if not sat? then
16
                     \mathbf{switch}\ nonOptLevel\ \mathbf{do}
17
                           case mode\_incr
18
                                mode \leftarrow mode\_greedy
19
                           case mode_greedy
20
                                mode \leftarrow mode\_opt
21
                                break
22
                     end
23
\mathbf{24}
                else
                     MSS \leftarrow \texttt{Grow}(hs)
25
                     \mathcal{M} \leftarrow \mathcal{M} \cup \{MSS\}
26
                     \mathcal{K} \leftarrow \mathcal{K} \cup \{\mathcal{F} \setminus MSS\}
27
                     mode \leftarrow mode\_incr
28
29
          end
          hs \leftarrow \texttt{OptimalHittingSet}(\mathcal{K}, f_{cost})
30
          (\text{sat?}, \kappa) \leftarrow \texttt{SatSolver}(hs)
31
          if not sat? then
32
               return hs, \mathcal{M}
33
          end
34
          MSS \leftarrow \texttt{Grow}(hs)
35
          \mathcal{M} \leftarrow \mathcal{M} \cup \{MSS\}
36
          \mathcal{K} \leftarrow \mathcal{K} \cup \{\mathcal{F} \setminus MSS\}
37
          mode \leftarrow mode\_incr
39 end
```

## Algorithm 4: OMUS-Delayed( $\mathcal{F}, \mathcal{M}, f_{cost}$ )

```
// F = unsatisfiable CNF formula; M = Collection of MSSes; f_{cost} = cost function
 1 \mathcal{K} \leftarrow \emptyset
     // grow mss from input mss
 2 foreach \mathcal{MSS} \in \mathcal{M} do
          \mathcal{MSS}' \leftarrow \mathtt{Grow}(\mathcal{F} \cap \mathcal{MSS})
          \mathcal{K} \leftarrow \mathcal{K} \cup \{\mathcal{F} \setminus \mathcal{MSS}'\}
 5 end
 \mathbf{6} \mod \leftarrow \mod_{\operatorname{greedy}}
 7 while true do
          \mathbf{switch}\ nonOptLevel\ \mathbf{do}
 9
                case mode\_incr
                      \mathcal{MCS} \leftarrow \{\mathcal{F} \setminus MSS\}
10
                     hs \leftarrow \texttt{FindIncrementalHittingSet}(\mathcal{K}, \mathcal{MCS}, hs)
11
                case mode\_greedy
12
                     hs \leftarrow \texttt{FindGreedyHittingSet}(\mathcal{K})
13
                \mathbf{case}\ mode\_opt
14
                     hs \leftarrow \texttt{OptimalHittingSet}(\mathcal{K}, \mathcal{W})
15
          end
16
          (\text{sat?}, \kappa) \leftarrow \texttt{SatSolver}(hs)
17
          if not sat? then
18
                switch nonOptLevel do
19
                      \mathbf{case}\ mode\_incr
20
                          mode \leftarrow mode\_greedy
21
                      case mode\_greedy
\mathbf{22}
                           mode \leftarrow mode\_opt
\mathbf{23}
\mathbf{24}
                           break
                      \mathbf{case}\ mode\_opt
25
                           return hs, \mathcal{M}
26
27
               end
          else
28
                MSS \leftarrow \texttt{Grow}(hs)
\mathbf{29}
                \mathcal{M} \leftarrow \mathcal{M} \cup \{MSS\}
30
                \mathcal{K} \leftarrow \mathcal{K} \cup \{\mathcal{F} \setminus MSS\}
31
                mode \leftarrow mode\_incr
32
33 end
```