```
D INPUT
      Explanation Generation
                                                      a Carf.
             XPY:ciok 28994:
  Algorithm 1: EXPLAINCSP(C, U, f)
    // Hyp:
 1 E \leftarrow \langle \rangle
 2 I_{end} \leftarrow \text{OptimalPropagate}(\mathcal{C}, U)
                                                                                        // assignment on variables of U
 3 bart: What's a better way to get the initial interpr.?
 I_{end} = \{i \in I_{end} | f(-i) = inf\} // contains the indicator literals and the initial assignment
 5 while I \neq I_{end} do
        X \leftarrow \text{BESTSTEP}(\mathcal{C}, f, I_{end}, I)
        I_{best} \leftarrow I \cap X
        N_{best} \leftarrow \{C \cup I_{best}, U\} OPTIMALPROPAGATE(C \cup I_{best}, U)
        add \{I_{best} \implies N_{best}\} to E
        I \leftarrow I \cup N_{best}
11 end
12 return E
 Algorithm 2: BESTSTEP-C-OUS(C, f, I_{end}, I)
 1 A \leftarrow I \cup (\overline{I_{end}} \setminus \overline{I})
                                                                                            // Optimal US is subset of A
                                                                              Pis the constraint
 2 set p such that exactly one of \overline{I_{end}} in the hitting set
 3 return C-OUS(C, f, p, A)
 Algorithm 3: C-OUS(C, f, p, A)
    // Hyp: C \cup A is unsatisfiable
 2 while true do
        A' \leftarrow \text{CONDOPTHITTINGSET}(f, p, A, \mathcal{H})
        if \neg SAT(\mathcal{C} \cup A') then
                                       - HOW WE AKT DAT C mody ! provdis )
           return A'
        end
 6
        A'' \leftarrow GROW(A', A)
        \mathcal{H} \leftarrow \mathcal{H} \cup \{A \setminus A''\}
                                   // We can reuse the H across diff call to alg 1 was H \cup \{F \setminus F''\}
 9 end
 Algorithm 4: OptimalPropagate(C, U)
                                                                                         = Set Pikeoly
 1 sat?, \mu \leftarrow SAT(\mathcal{C})
                                     DOES NOT PARSE: M
 \mathbf{2} \ \mu \leftarrow \mu \ \cap \ \mathcal{U}
 3 Should I add the blocking variables b_i to the newly added clause?
 4 while true do
        \mathcal{C} \leftarrow \mathcal{C} \wedge ( \quad \bigvee \quad \neg x_i)
                    1 \le i \le |\mu|
        or \mathcal{C} \leftarrow \mathcal{C} \wedge (\bigvee_{1 \leq i \leq |\mu|} \neg x_i)
 6
        or \mathcal{C} \leftarrow \mathcal{C} \wedge (\neg x_1 ... \vee \neg x_n)
        or \mathcal{C} \leftarrow \mathcal{C} \wedge (\neg b_i)
 9
        sat?, \mu' \leftarrow SAT(\mathcal{C})
10
        if \neg sat? then
11
         return \mu
12
        end
13
        \mu \leftarrow \mu \cap \mu' \cap \mathcal{U}
14
15 end
```

## 2 OUS Algorithm

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Algorithm 5: BESTSTEP-OUS(C, f, I, I_{end})
```

```
\begin{array}{l} \mathbf{1} \ X_{best} \leftarrow \{\mathcal{C} \land I \land \overline{I_{end}}\} \\ \mathbf{2} \ \mathbf{for} \ l \in \{I_{end} \setminus I\} \ \mathbf{do} \\ \mathbf{3} \ \mid \ X \leftarrow \mathrm{OUS}(\mathcal{C} \land I \land \neg l, \ f) \\ \mathbf{4} \ \mid \ \mathbf{if} \ f(X) < f(X_{best}) \ \mathbf{then} \\ \mathbf{5} \ \mid \ X_{best} \leftarrow X \\ \mathbf{6} \ \mid \ \mathbf{end} \\ \mathbf{7} \ \mathbf{end} \\ \mathbf{8} \ \mathbf{return} \ X_{best} \end{array}
```

## Algorithm 6: OUS-INC( $\mathcal{F}, f$ )

```
_{1}\ \mathbf{SSOfF}\leftarrow\emptyset
  2 for S \in \mathbf{SSs} do
               S_{\mathcal{F}} \leftarrow S \cap \mathcal{F}
               if \neg \exists S' \in \mathbf{SSOfF} : S_{\mathcal{F}} \subseteq S' then
  4
                       S_{\mathcal{F}} \leftarrow \text{Grow}(S_{\mathcal{F}}, \mathcal{F})
  5
                       \mathcal{H} \leftarrow \mathcal{H} \cup \{\mathcal{F} \setminus S_{\mathcal{F}}\}\
  6
                       \mathbf{SSOfF} \leftarrow \mathbf{SSOfF} \cup \{S_{\mathcal{F}}\}
              end
  9 end
10 while true do
              \mathcal{F}' \leftarrow \text{OptHittingSet}(\mathcal{H}, f)
               if \neg SAT(\mathcal{F}') then
12
                      \mathbf{return}\; \mathcal{F}'
13
               end
14
               \mathcal{F}'' \leftarrow \operatorname{Grow}(\mathcal{F}', \mathcal{F})
15
              \mathcal{H} \leftarrow \mathcal{H} \cup \{\mathcal{F} \setminus \mathcal{F}''\}
16
              SSs \leftarrow SSs \cup \{(\mathcal{F}'', M)\}
17
18 end
```

## Algorithm 7: Postponing hitting set optimization for OUS (to be inserted before of )

```
_1 while true do
 \mathbf{2}
            while |\mathcal{H}| > 0 do
                   \mathcal{F}' \leftarrow \mathcal{F}' + min_f element of last MCS in \mathcal{H};
 3
                   if \neg SAT(\mathcal{F}') then
  4
                    break
  5
                   end
  6
                   \mathcal{H} \leftarrow \mathcal{H} \cup \{\mathcal{F} \setminus \text{Grow}(\mathcal{F}', \mathcal{F})\};
            \mathcal{F}' \leftarrow \text{GREEDYHITTINGSET}(\mathcal{H}, f);
 9
            if \neg SAT(\mathcal{F}') then
10
                   break
11
            end
12
            \mathcal{H} \leftarrow \mathcal{H} \cup \{\mathcal{F} \setminus \text{Grow}(\mathcal{F}', \mathcal{F})\};
13
14 end
```