Exercise set 8

Bjørn Christian Weinbach

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Clear R environment

```
rm(list = ls())
```

Exercise 8.4

Note: MLE for $\hat{\lambda} = n/\sum_{i=1}^{n} X_i$, where X denote time between failure

Refer to the air-conditioning data set **aircondit** provided in the boot library. The 12 observations are the times in hours between failures of air-conditioning equipment

3 5 7 18 43 85 91 98 100 130 230 487

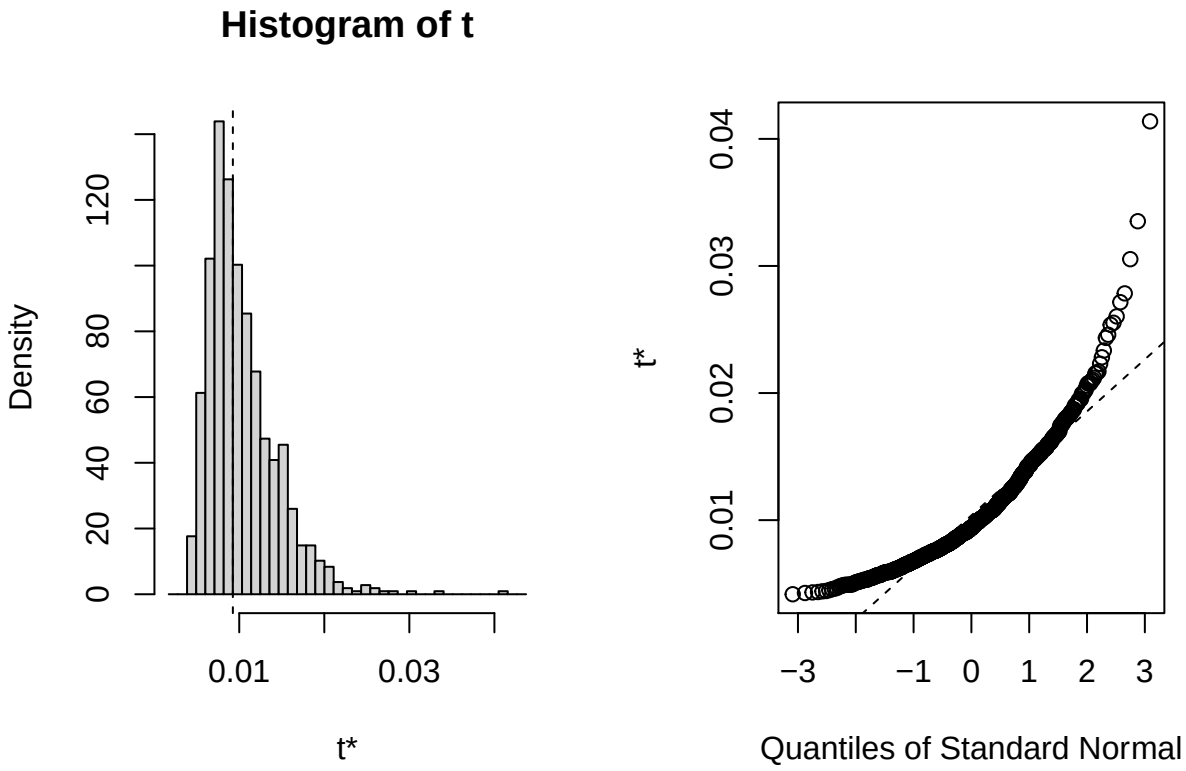
Assume that the times between failures follow an exponential model with rate λ. Obtain the MLE of the hazard rate λ and use bootstrap to estimate the bias and standard error of the estimate.

in R:

```
library(boot)

# MLE for hazard rate of exponential distributed data
mle <- function(data, i) {
  return(length(data[i])/sum(data[i]))
}

# bootstrapping with 1000 replications
results <- boot(data=aircondit$hours, statistic = mle, R=1000)

# view results
results
```

```
##
## ORDINARY NONPARAMETRIC BOOTSTRAP
##
##
## Call:
## boot(data = aircondit$hours, statistic = mle, R = 1000)
##
##
## Bootstrap Statistics :
##       original      bias    std. error
## t1* 0.00925212 0.001118388 0.004093092
```

```
plot(results)
```




```
# get 95% confidence interval
boot.ci(results, type=c("bca", "norm", "perc"))
```

```
## BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
## Based on 1000 bootstrap replicates
##
## CALL :
## boot.ci(boot.out = results, type = c("bca", "norm", "perc"))
##
## Intervals :
## Level      Normal             Percentile            BCa
## 95%   ( 0.0001,  0.0162 )   ( 0.0052,  0.0202 )   ( 0.0046,  0.0180 )
## Calculations and Intervals on Original Scale
## Some BCa intervals may be unstable
```

Exercise 8.5

Bibliography