

# Report on econ Data Set

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## Abstract

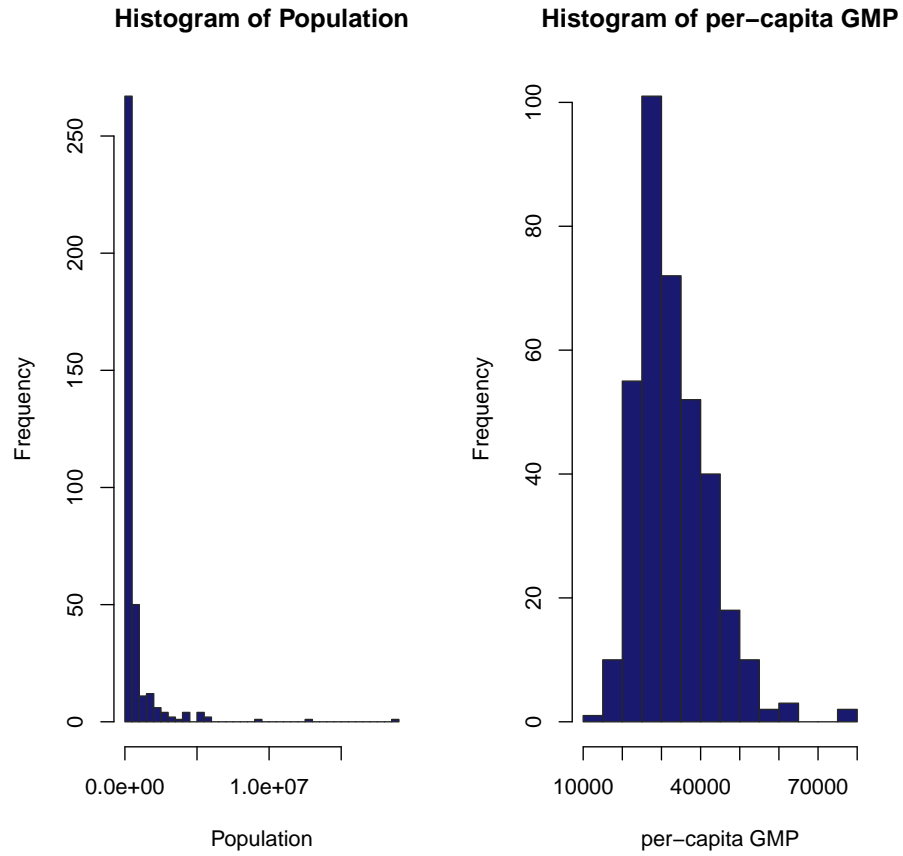
The data file econ.csv contains information about the economies of the 366 “metropolitan statistical areas” ( cities) of the US in 2006. In particular, it lists, for each city, the population, the total value of all goods and services produced for sale in the city that year per person (“per capita gross metropolitan product”, pcgmp), and the share of economic output coming from four selected industries.

Loading the data file econ.csv which contains information about the economies of the 366 “metropolitan statistical areas” ( $\approx$  cities) of the US in 2006.

```
## [1] 366 7
```

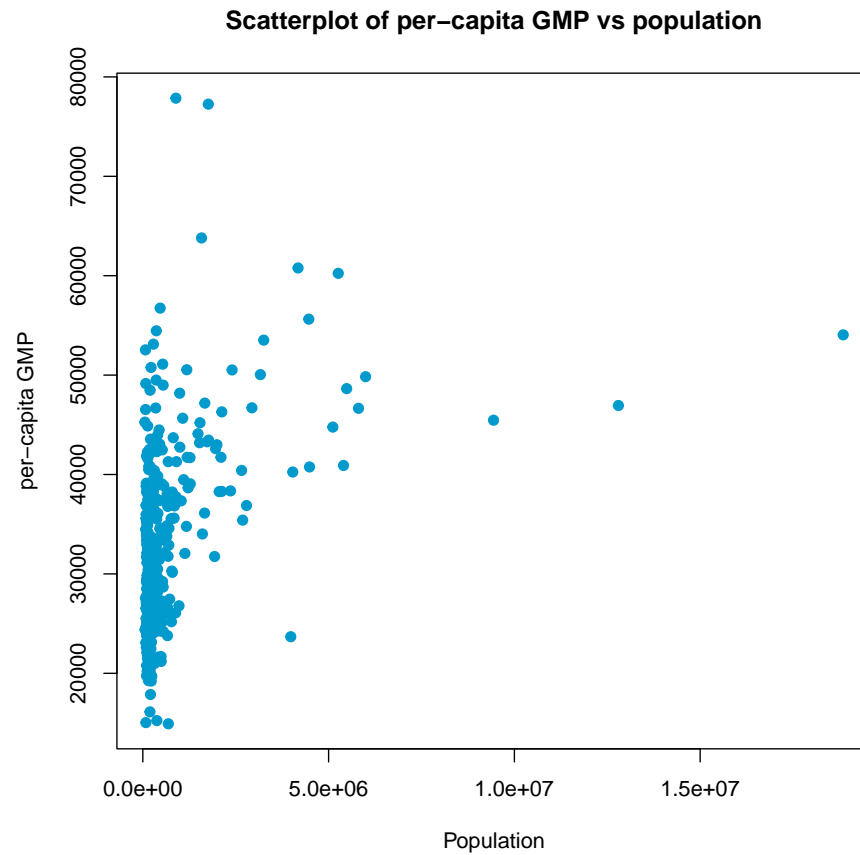
It contains the name of the cities (metropolitan statistical areas) in a column corresponding to each observation. Thats why, it should have seven columns.

```
##      pcgmp      pop      finance      prof.tech
## Min.   :14920  Min.   : 54980  Min.   :0.03845  Min.   :0.01474
## 1st Qu.:26533  1st Qu.: 135625  1st Qu.:0.10403  1st Qu.:0.02932
## Median :31615  Median : 231500  Median :0.14140  Median :0.04213
## Mean   :32923  Mean   : 680898  Mean   :0.15082  Mean   :0.04905
## 3rd Qu.:38213  3rd Qu.: 530875  3rd Qu.:0.18122  3rd Qu.:0.05932
## Max.   :77860  Max.   :18850000  Max.   :0.38480  Max.   :0.19080
##                                     NA's   :12      NA's   :112
##      ict      management
## Min.   :0.00349  Min.   :0.00042
## 1st Qu.:0.01215  1st Qu.:0.00294
## Median :0.02218  Median :0.00651
## Mean   :0.03910  Mean   :0.00908
## 3rd Qu.:0.04072  3rd Qu.:0.01191
## Max.   :0.58600  Max.   :0.05431
## NA's   :76      NA's   :157
```



The distribution of population is highly positively skewed i.e. a large number of cities have a little amount of population, and very few cities have huge population.

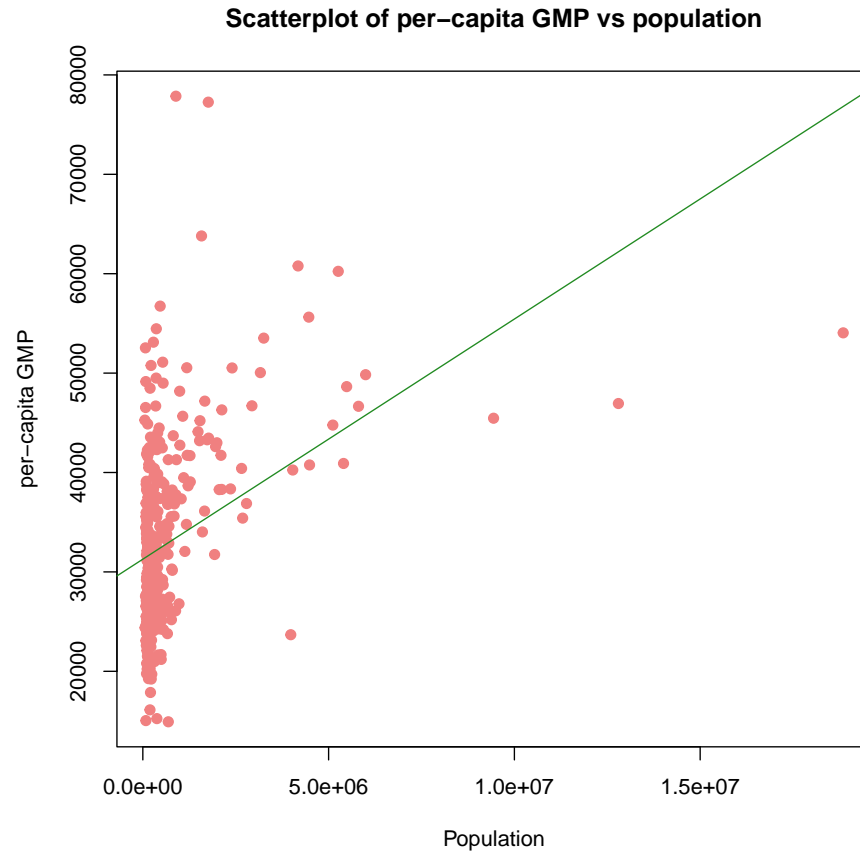
The distribution of per-capita GMP is slightly positively skewed.



```
## [1] 0.002416201
## [1] 31277.57
```

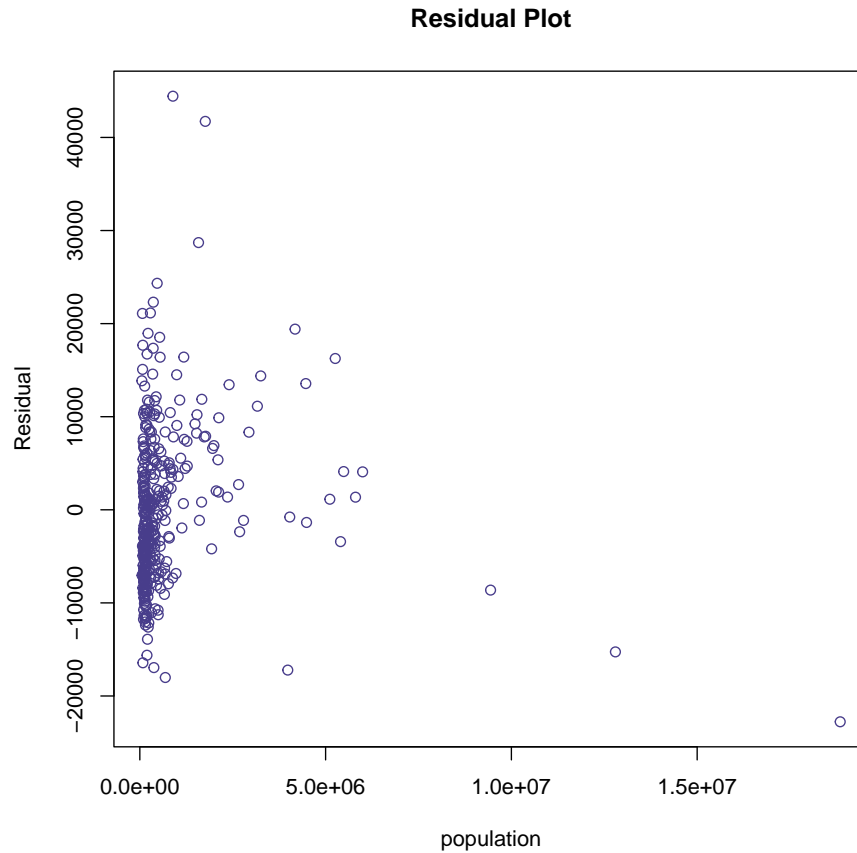
```
##      pop
## 0.002416201
## (Intercept)
## 31277.57
```

It agrees with the answer in the previous part. Yes, it should agree.



The line doesn't fit the data well.

Checking that if the assumptions of the simple linear regression model appear to hold or not.



From the above residual plot we can see that the variance of the residuals is decreasing with  $x$ . So, the homoscedasticity assumption of the error variables gets violated here.

```
## [1] 2361000
```

The population of Pittsburgh is 2361000.

```
## [1] 38350
```

The per-capita GMP of Pittsburgh is 38350.

```
## (Intercept)
## 36982.22
```

The per-capita GMP predicted by the model is 36982.22

```
## (Intercept)
##      1367.775
```

The residual for Pittsburgh is 1367.775

```
## [1] 70697145
```

The mean squared error of the regression is 70697145

Consider the ratio of Residual square for Pittsburgh to the Mean Residual Square or MSE:

```
## (Intercept)
##      0.02646231
```

Clearly, the residual square for Pittsburgh is only 2.6% (approx.) of the MSE. Now, as the residual for Pittsburgh is greater than 1, so we can say that the residual for Pittsburgh is quite small compared to the mean squared error.

Interpretation of the estimated slope:

If we select two sets of cases from the un-manipulated distribution where the population differs by 1, we expect per-capita GMP to differ by 0.002416201 (=estimated slope) unit.

```
## (Intercept)
##      37223.84
```

The predicted per-capita GMP for a city with  $10^5$  more people than Pittsburgh is 37223.84

If  $10^5$  people were added to the population, by a policy intervention, then the predicted Pittsburgh per-capita GMP would become more closer to the observed per-capita GMP i.e. the residual would decrease.