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## CSED332 ASSIGNMENT 3

Due Monday, October 4

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### Objectives

- Write formal specifications and black-box test cases for abstract interfaces
- Understand the Liskov substitution principle (a.k.a., behavioral subtyping)
- Learn Java programming language (Generics)

### Background: Graphs and Trees

- A *directed graph* is a pair  $G = (V, E)$ , where  $V$  is a set of *vertices* (also called nodes) and  $E \subseteq V \times V$  is a set of edges that connects two vertices. For example, Fig. 1 shows the graph:

$$V = \{1, 2, 3, 4, 5, 6\}, \quad E = \{(1, 1), (1, 2), (3, 6), (4, 1), (4, 2), (6, 3)\}$$

- A (rooted) *tree* is a directed graph  $G = (V, E)$  such that one vertex is designated as the root and there exists exactly one path from the root to any vertex. For example, Fig. 2 show the tree:

$$V = \{1, 2, 3, 4, 5, 6\}, \quad E = \{(1, 2), (1, 4), (2, 3), (2, 6), (4, 5)\}, \quad \text{where 1 is the root}$$

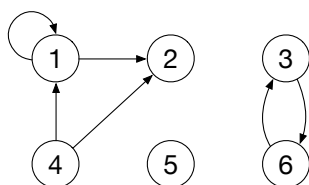


Figure 1: A graph

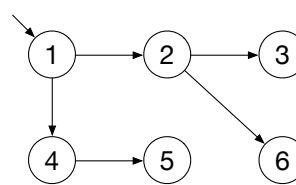


Figure 2: A tree

### Problem 1: Abstract Interface Specifications for Graphs and Trees

- In this assignment, we consider generic abstract interfaces for graphs and trees, where vertices are represented as any elements of a given (immutable and comparable) type  $N$ :
  - `Graph<N>`: an interface for direct graphs
  - `Tree<N>`: an interface for rooted trees, extending `Graph<N>`
  - `MutableGraph<N>`: an interface with mutable operations, extending `Graph<N>`
  - `MutableTree<N>`: an interface with mutable operations, extending `Tree<N>`

Note that `Graph<N>` and `Tree<N>` do *not* contain methods for mutable operations, such as adding or removing vertices and edges. These interfaces are described in detail in the source code.

- The interfaces declare *abstract data types* for graphs and trees, which specify mathematical *abstract values* and their associated operations.
  - Abstract values of graphs are pairs  $G = (V, E)$ , where each vertex in  $V$  has type  $N$ .
  - Abstract values of trees are triples  $T = (V, E, v_{root})$ , where  $v_{root}$  is the root.

The implementation may use concrete values with extra information invisible to the client. This is a form of *information hiding*, one of the fundamental concepts of object-oriented programming.

- The goal is to write formal abstract specifications of these interfaces *with respect to abstract values*; namely, a class invariant of each interface, and a precondition and a postcondition of each method.
- Fill out the attached Markdown file `homework3.md`, indicating the interfaces and methods for which you need to write formal abstract specifications, including some notations and examples.<sup>1</sup>

## Problem 2: Behavioral Subtypes of Graphs and Trees

- The Liskov substitution principle states that if type  $S$  is a subtype of  $T$ , then code written for objects of type  $T$  also operates correctly for objects of type  $S$ .
  - In other words, objects of type  $T$  can be substituted with objects of type  $S$  without altering any of the properties of  $T$ , such as class invariants, preconditions, postconditions, etc.
  - As shown in the class, subclassing does *not* guarantee subtyping, and trying to meet the Liskov substitution principle for subclassing is a good software design practice.
- The goal is to identify whether the abstract interfaces satisfy the Liskov substitution principle; that is, to answer the following questions:
  - is  $\text{Tree}\langle N \rangle$  a subtype of  $\text{Graph}\langle N \rangle$ ?
  - is  $\text{MutableGraph}\langle N \rangle$  a subtype of  $\text{Graph}\langle N \rangle$ ?
  - is  $\text{MutableTree}\langle N \rangle$  a subtype of  $\text{Tree}\langle N \rangle$ ?
  - is  $\text{MutableTree}\langle N \rangle$  a subtype of  $\text{MutableGraph}\langle N \rangle$ ?
- For each question, explain your reasoning *using the abstract specifications that you have defined in Problem 1*. For types  $S, T \in \{\text{Tree}\langle N \rangle, \text{MutableGraph}\langle N \rangle, \text{MutableTree}\langle N \rangle, \text{MutableTree}\langle N \rangle\}$ :
  - If  $S$  is a subtype of  $T$ , explain why  $S$  has a stronger specification than  $T$  in terms of their specifications (preconditions, postconditions, and class invariants).
  - If  $S$  is *not* a subtype of  $T$ , (i) explain which part of the specifications violate the Liskov substitution principle, and (ii) show code written for  $T$  that behaves differently for  $S$ .
- Similarly, fill out the attached file `homework3.md`. Note that you can easily write math expressions using GitLab Markdown: <https://docs.gitlab.com/ee/user/markdown.html#math>.

## Problem 3: Black-box Test Cases for Graphs and Trees

- The goal of this problem is to write a high-quality test suite for the interfaces  $\text{MutableGraph}\langle N \rangle$  and  $\text{MutableTree}\langle N \rangle$  with respect to their specifications.
  - Because only abstract specifications are available, you will write *black-box test cases* for the interfaces, based on equivalence partitioning.
  - E.g., for the method `addVertex( $v$ )` of  $\text{MutableGraph}\langle N \rangle$ , there are two equivalence classes based on the description:  $v$  is already in the graph, or  $v$  is previously not in the graph.
- For each method, write a test method for each equivalence class in the abstract test classes in the `src/test` directory (e.g., two test methods for `addVertex`, which are already given in the code).
  - Two abstract classes are given:  $\text{AbstractMutableGraphTest}\langle N, G \rangle$  for vertex type  $N$  and graph type  $G$ , and  $\text{AbstractMutableTreeTest}\langle N, T \rangle$  for vertex type  $N$  and tree type  $T$ .
  - Each abstract test class contains one object (either a graph of type  $G$  or a tree of type  $T$ ), and eight vertices of type  $N$ , along with some example test methods using them.

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<sup>1</sup>You do *not* have to write specifications for other interfaces/methods not in `homework3.md`.

## Problem 4: Implementing Graphs

- In this problem, we will implement a direct graph using an *adjacency list representation*<sup>2</sup>
  - You must use the following representation provided in the class `AdjacencyListGraph<N>`, a (sorted) map from vertices to the (sorted) set of their adjacent vertices.

```
private final @NotNull SortedMap<V, SortedSet<V>> adjMap;
```

- For example, the graph in Fig. 1 is represented as the sorted map<sup>3</sup>

$$\{1 \mapsto \{1, 2\}, 2 \mapsto \emptyset, 3 \mapsto \{6\}, 4 \mapsto \{1, 2\}, 5 \mapsto \emptyset, 6 \mapsto \{3\}\}$$

- Implement the class `AdjacencyListGraph<N>`, which is a subclass of `MutableGraph<N>`, using this representation of directed graphs.
  - What are an abstract function and a class invariant for `AdjacencyListGraph<N>`? Document the abstraction function and class invariant (as comments in the source code).
  - Implement the method `checkInv` that checks your class invariant. The method `toString` provides a string representation for abstract values.
- Whenever you write a method, check whether your implementation passes your black-box test cases that you have written for Problem 3, following test-driven development practice.
  - The test class `StringAdjacencyMutableGraphTest` extends your `AbstractMutableGraphTest`. It contains `setUp()` to initialize abstract graphs and vertices for black-box test cases.
  - You may write more *white-box test cases* to `StringAdjacencyMutableGraphTest` to achieve more code coverage, if needed.

## Problem 5: Implementing Trees

- In this problem, we will write two different implementations of a tree using different representations.
  - `DelegateTree<N>` uses an instance of `MutableGraph<N>` to implement its functionality.<sup>4</sup>
  - `ParentPointerTree<N>` uses *pointers to parent vertices*<sup>5</sup> to represent a rooted tree.
- Implement `DelegateTree<N>` and `ParentPointerTree<N>`. Both are subclasses of `MutableTree<N>` with the same *specification* but with different representations.
  - What are an abstract function and a class invariant of these classes? Document the abstraction function and class invariant for each class (as comments in the source code).
  - Implement the method `checkInv` that checks your class invariant for each class. Similarly, the method `toString` provides a string representation for abstract values.
  - You may find that the provided method `findReachableVertices` is useful for implementing some methods declared in `MutableGraph<N>`.
- Again, following test-driven development practice, run your black-box test cases that you have written for Problem 3 whenever you write a method.
  - There are two test classes that extend your `AbstractMutableTreeTest`, along with appropriate `setUp()`: `IntegerDelegateMutableTreeTest` and `DoubleParentPointerMutableTreeTest`.
  - Similarly, you may write more *white-box test cases* to these test classes to achieve more code coverage for `DelegateTree<N>` and `ParentPointerTree<N>`, respectively, if needed.

<sup>2</sup>[https://en.wikipedia.org/wiki/Adjacency\\_list](https://en.wikipedia.org/wiki/Adjacency_list)

<sup>3</sup><https://docs.oracle.com/en/java/javase/16/docs/api/java.base/java/util/SortedMap.html>

<sup>4</sup>[https://en.wikipedia.org/wiki/Delegation\\_\(object-oriented\\_programming\)](https://en.wikipedia.org/wiki/Delegation_(object-oriented_programming))

<sup>5</sup>[https://en.wikipedia.org/wiki/Parent\\_pointer\\_tree](https://en.wikipedia.org/wiki/Parent_pointer_tree)

## General Instruction

- Your code need to be compiled using only Maven in a command line for grading. You **MUST** ensure that your tests pass on your code using `mvn test`.
- The `src/main` directory contains the skeleton code. You should implement all the methods marked with *TODO*. Before writing code, read the description in the source code carefully.
- The `src/test` directory contains test classes. Use JaCoCo to find out how much coverage your tests have. Upload the JaCoCo report in CSV format from `target/site/jacoco/jacoco.csv`.
- Do not modify the existing interfaces, the class names, and the signatures of the public methods and `checkInv()`. You can add more private methods if you want.
  - In this assignment, we use *fixed* representations for `AdjacencyListGraph<N>`, `DelegateTree<N>`, and `ParentPointerTree<N>`. *You cannot add even private member variables to these classes.*
- Your submitted tests need to achieve at least 90% **branch coverage**. Your black-box test cases should already give high coverage, but you may add more white-box test cases if needed.
  - Your black-box test cases will be graded according to whether they clearly describe different scenarios from the specifications using equivalence partitioning.
  - *Do not add arbitrary code to your test method to just increase coverage.* In particular, this will severely affect your scores for black-box test cases.
  - The abstract test classes should only depend on abstract interfaces, namely, `MutableGraph<N>` and `MutableTree<N>`; importing concrete implementations is not allowed.

## Turning in

1. Create a private project with name `homework3` in <https://csed332.postech.ac.kr>, and clone the project on your machine.
2. Commit your changes in your `homework3` project, including `homework3.md` and a JaCoCo coverage report, and push them to the remote repository.
3. The JaCoCo coverage report, generated by `mvn jacoco:report`, and `homework3.md`, containing the answers of Problems 1 and 2, will be uploaded to the directory `homework3/`.
4. Tag your project with “submitted” and submit your homework. We will use the tagged version of your project for grading.

## Reference

- Java Language Specification: <https://docs.oracle.com/javase/specs/>
- Java Generics: <https://docs.oracle.com/javase/tutorial/java/generics/>
- Beginning Java 9 Fundamentals 2nd by Kishori Sharan, Apress, 2017 (available online at the POSTECH digital library <http://library.postech.ac.kr>)
- Maven Getting Started Tutorial: <https://maven.apache.org/guides/getting-started/>