



4 Repetition

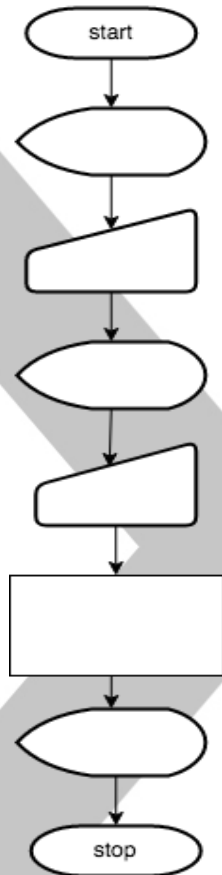


Topics

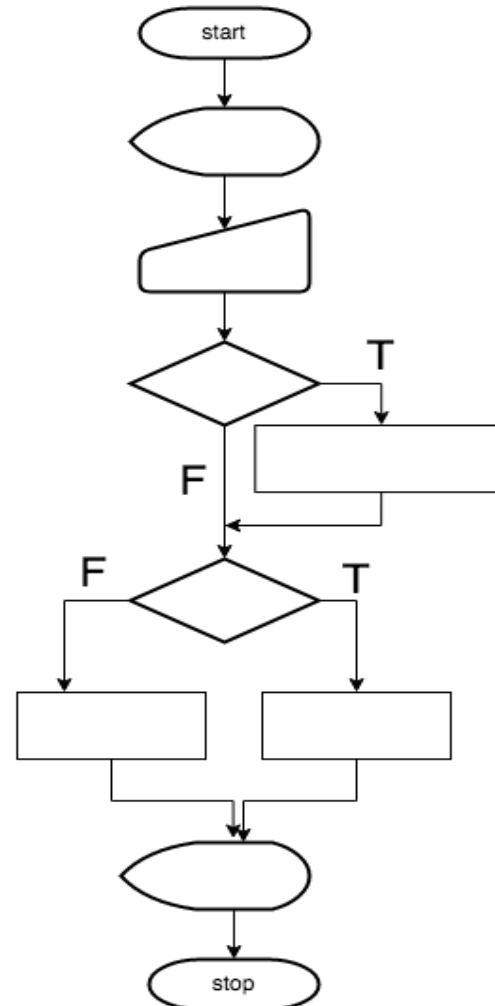
- while
- for
 - for k in range(...)
 - for ch in string
 - for elem in a list
- break

Flowchart

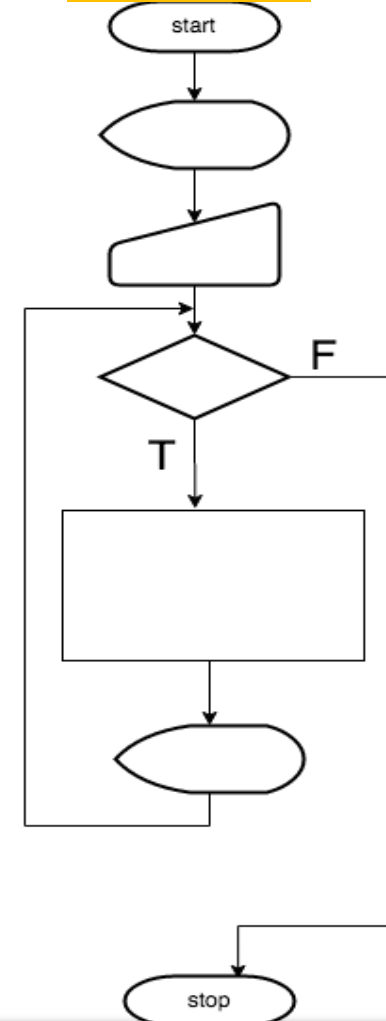
Sequential



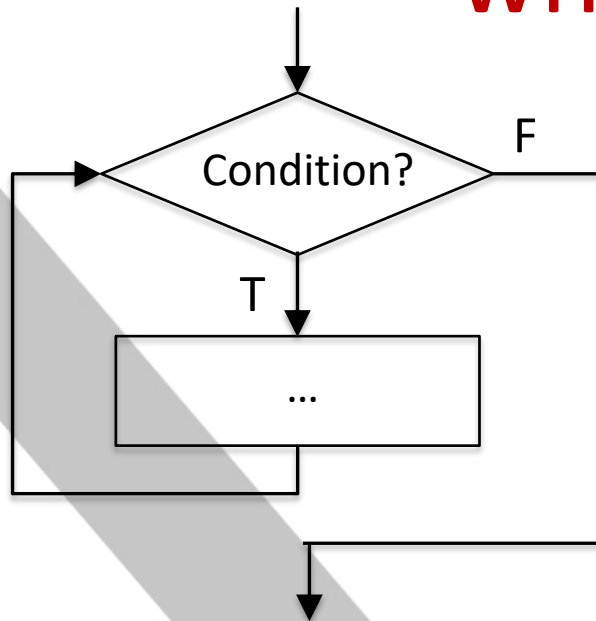
Selection



Repetition



while loop



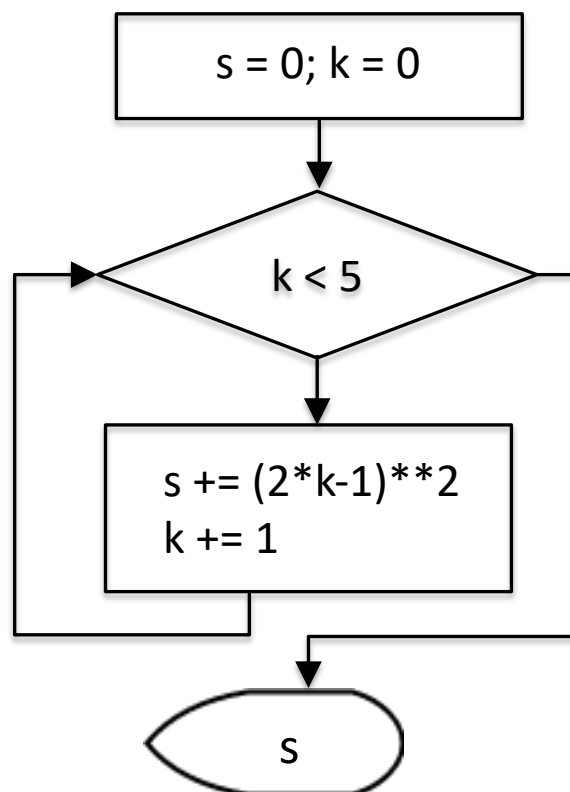
Must end with a colon.

```
while condition :  
→ instruction set
```

All instructions need to be indented equally from the left.

Example

$$\sum_{k=0}^4 (2k - 1)^2$$



Example

$$\sum_{k=0}^4 (2k - 1)^2$$

(2)

(1)

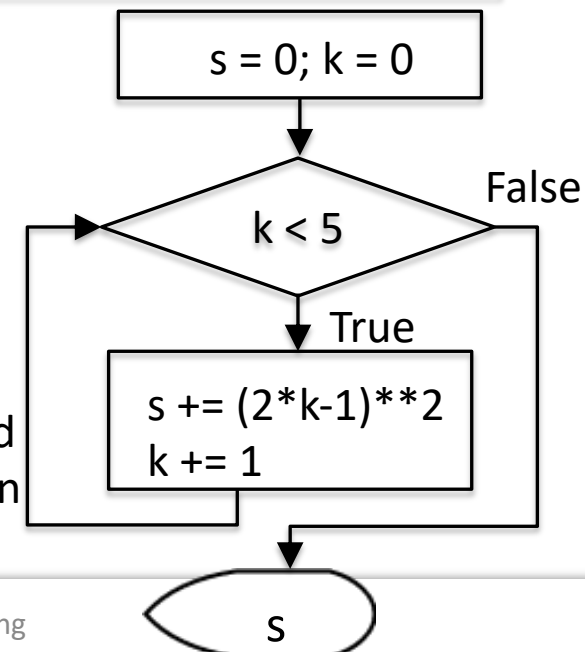
```
s = 0
s += (2*0 - 1)**2
s += (2*1 - 1)**2
s += (2*2 - 1)**2
s += (2*3 - 1)**2
s += (2*4 - 1)**2
print(s)
```

```
s = 0; k = 0
s += (2*k - 1)**2; k += 1
s += (2*k - 1)**2; k += 1
s += (2*k - 1)**2; k += 1
s += (2*k - 1)**2; k += 1
s += (2*k - 1)**2; k += 1
print(s)
```

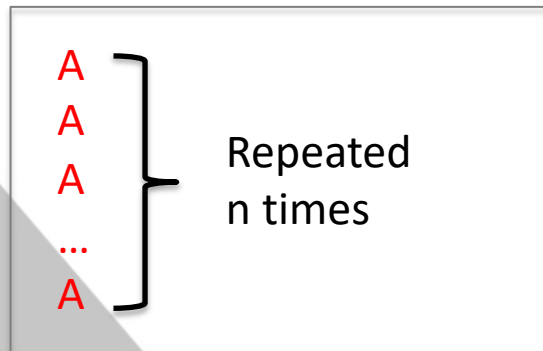
(3)

```
s = 0; k = 0
while k < 5 :
    s += (2*k - 1) **2
    k += 1
print(s)
```

Iterate 5 times, k starts from 0, incremented by 1 for each iteration, and terminated when k is 5, as the condition is false.



Loop pattern



```
k = 0  
while k < n :  
    A  
    k += 1
```

OR

```
k = 1  
while k <= n :  
    A  
    k += 1
```

Example: find the smallest among five numbers

```
min_v = float(input())
v = float(input())
if v < min_v:
    min_v = v
v = float(input())
if v < min_v:
    min_v = v
v = float(input())
if v < min_v:
    min_v = v
v = float(input())
if v < min_v:
    min_v = v
print("min = ", min_v)
```



```
min_v = float(input())
k = 0
while k < 4 :
    v = float(input())
    if v < min_v:
        min_v = v
    k += 1
print(" min = ", min_v)
```


Example: find a smallest among n numbers

Specify the number of n

(1)

4

10.0
11.2
15.5
12.4

(2)

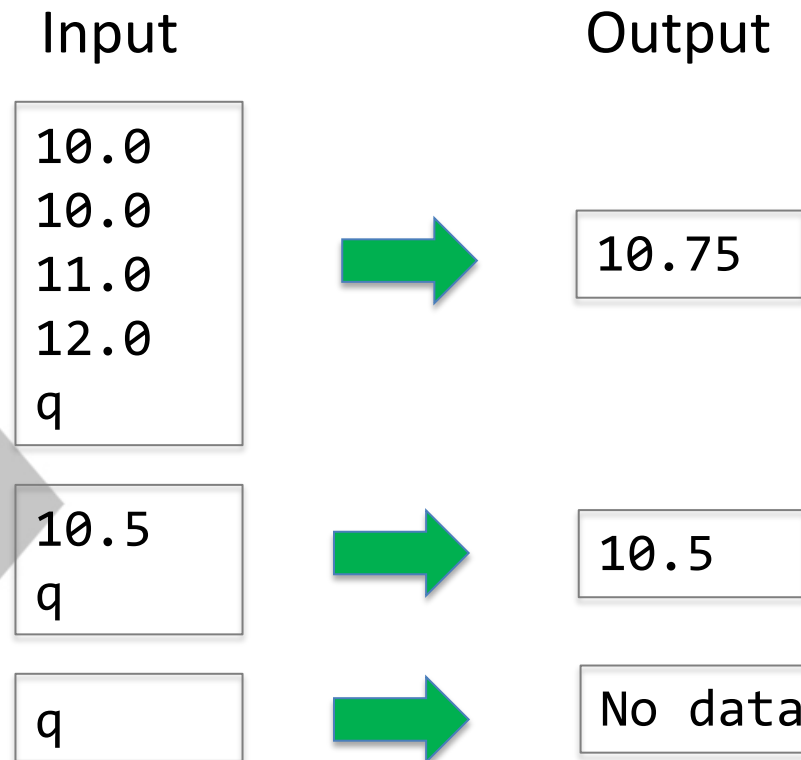
10.0
11.2
15.5
12.4

q

Specify the end of listed numbers
with "q"

Either (1) or (2) can be the input of the program.

Practice: find the average among n numbers



Example: find a square root using bisection method

- Find a square root of a
- Let $L = 0$, $U = a$
- The answer will be within $[L, U]$
- x = the middle point of L and U
- Repeat the following steps if $x^2 \neq a$
 - If $x^2 > a$:
 - Update the range to $[L, x]$
 - If $x^2 < a$:
 - Update the range to $[x, U]$
 - x = the middle point of L and U

$$x = \frac{L + U}{2}$$

a = 25		
L	U	X
0	25	12.5
0	12.5	6.25
0	6.25	3.125
3.125	6.25	4.6875
4.6875	6.25	5.46875
4.6875	5.46875	5.078125
4.6875	5.078125	4.882813
4.882813	5.078125	4.980469
4.980469	5.078125	5.029297
4.980469	5.029297	5.004883

Example: find a square root using bisection method

- Find a square root of a
- Let $L = 0$, $U = a$
- The answer will be within $[L, U]$
- x = the middle point of L and U
- Repeat the following steps if $x^2 \neq a$
 - If $x^2 > a$:
 - Update the range to $[L, x]$
 - If $x^2 < a$:
 - Update the range to $[x, U]$
 - x = the middle point of L and U

```
→ a = float(input())
→ L = 0; U = a
→ x = (L + U)/2
while x**2 != a:
    if x**2 > a:
        U = x
    else:
        L = x
    x = (L + U)/2
print(x)
```

Example: find a square root using bisection method

Got a problem!!

```

a = float(input())
L = 0; U = a
x = (L + U)/2
while x**2 != a:
    if x**2 > a:
        U = x
    else:
        L = x
    x = (L + U)/2

print(x)

```

```

a = float(input())
L = 0; U = a
x = (L + U)/2
while not close enough:
    if x**2 > a:
        U = x
    else:
        L = x
    x = (L + U)/2

print(x)

```

a and b are not close enough when $|a - b| > \varepsilon * \max(a, b)$

If a and b are positive, and $\varepsilon = 10^{-9}$

$\text{abs}(a - b) > 1e-9 * \max(a, b)$



Practice: find $\log_{10} a$ using bisection method

Write a program to get a as input and find the $\log_{10} a$ using bisection method, where $1 \leq a \leq 600$

To be more challenge, try a , which is much larger than 600

for loop

```
for k in range(start, stop, step) :  
    ...
```

```
for c in a_string :  
    ...
```

```
for e in a_list :  
    ...
```

Form #1:

for k in range(start, stop, step)

```
for k in range(4, 100, 2) :  
    ...
```

k = 4, 6, 8, ..., 98

```
for k in range(100, 0, -1) :  
    ...
```

k = 100, 99, 98, ..., 1

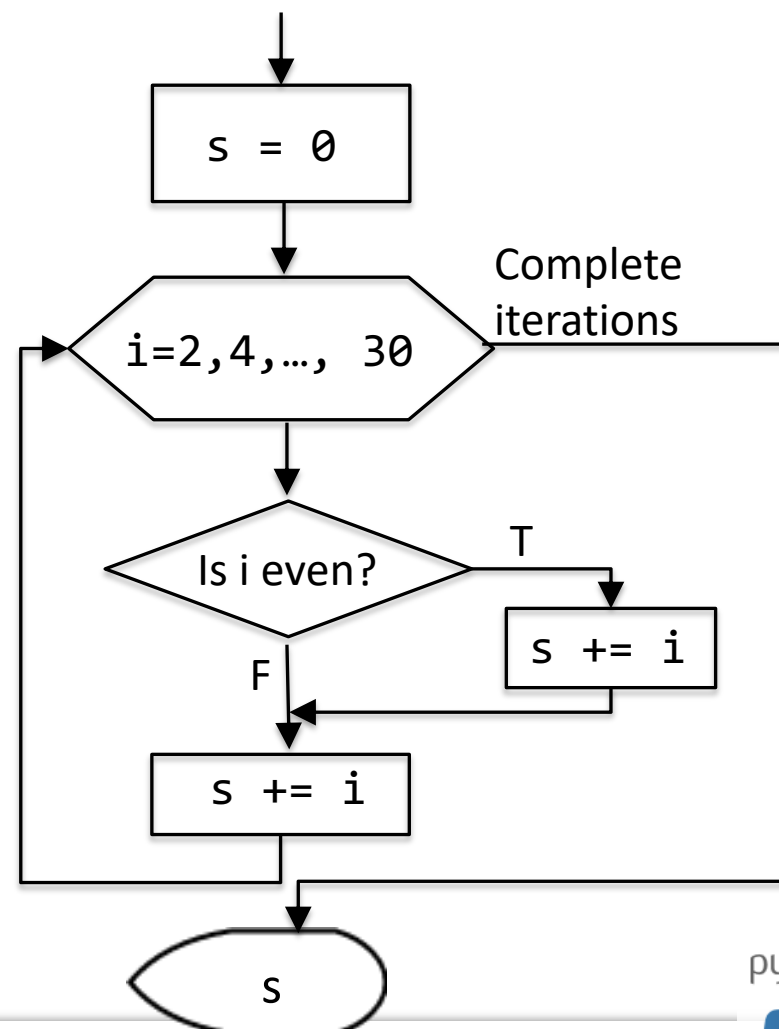
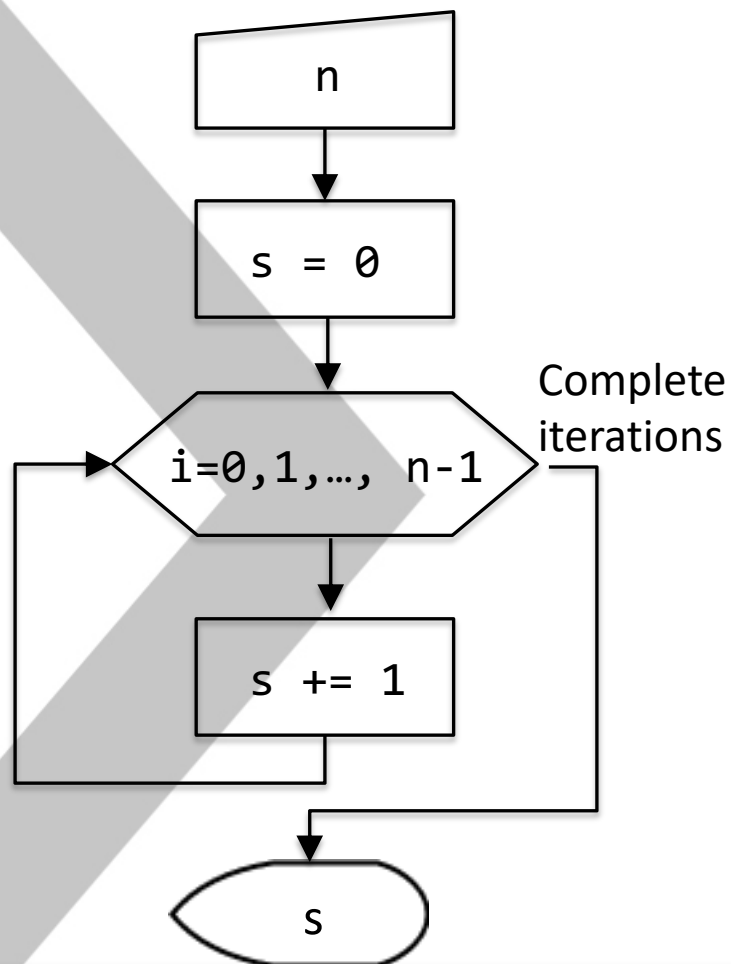
```
for k in range(5, 100) :  
    ...
```

k = 5, 6, 7, ..., 99

```
for k in range(100) :  
    ...
```

k = 0, 1, 2, ..., 99

Form #1: for k in range(start, stop, step)



Differences between while and for

```
s = 0
k = 0
while k < 5:
    s += (2*k - 1)**2
    k += 1

print(s)
```

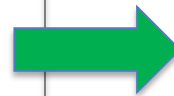


```
s = 0
for k in range(0,5,1):
    s += (2*k - 1)**2

print(s)
```

```
min_v = float(input())
k = 0
while k < 4:
    v = float(input())
    if v < min_v:
        min_v = v
    k += 1

print("min_v", min_v)
```



```
min_v = float(input())
for k in range(4):
    v = float(input())
    if v < min_v:
        min_v = v

print("min_v", min_v)
```

Example: find μ and σ

```
N = int(input())
x = [0.0]*N
for i in range(N):
    x[i] = float(input())

s = 0
for i in range(N):
    s += x[i]
mean = s/N

s2 = 0
for i in range(N):
    s2 += (x[i]-mean)**2
sd = (s2/N)**0.5

print(mean, sd)
```

Input

5
10
11
13
10
12

$$\mu = \frac{\sum_{i=1}^N x_i}{N}$$

$$\sigma = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu)^2}{N}}$$

Example: Dot Product $u \cdot v$

```
x = input().split()
u = [0.0]*len(x)
for i in range(len(x)):
    u[i] = float(x[i])

x = input().split()
v = [0.0]*len(x)
for i in range(len(x)):
    v[i] = float(x[i])

dot = 0
for i in range(len(x)):
    dot += u[i]*v[i]

print(dot)
```

1	2	0	2	1
2	2	1	2	2



12.0



Practice: check if the answer is correct

```
sol = input()    # e.g., ABBBAAABCCBABABDCCDA  
ans = input()    # e.g., ABBBAABBCCBABABDCDDDB
```

```
# count the number of matched characters between sol  
# and ans
```



Form #2:

for each_character in a_string



Example: count number of digits in a string

```
s = input()
digit_counts = 0
for ch in s:
    if "0" <= ch <= "9":
        digit_counts += 1
print(digit_counts)
```

Which one is easier?

```
s = input()
digit_counts = 0
for i in range(len(s)):
    if "0" <= s[i] <= "9":
        digit_counts += 1
print(digit_counts)
```



Example: remove all ([{ }]) from an input string

```
s = input()
result = ""
for ch in s:
    if ch not in "([{}])":
        result += ch
print(result)
```

Check character by character, if it is not any of the ([{ }]), concatenate that character to the result variable for the output.

Practice: [] and ()

Input

[x + (y - z)]



Output

(x + [y - z])

Programming



Programming

Construct a new string, replace () with [] and vice versa.



Form #3: for each_element in a_list



Example: find an average

```
x = input().split()  
s = 0  
for e in x:  
    s += float(e)  
avg = s/len(x)  
print("Average = ", avg)
```

Input

10 20 30 20 10

input().split()

["10", "20", "30", "20", "10"]

Output

Average = 18.0

Get each character one by one,
change to float, add to sum, and
find average.

Tips: Form#3 is applicable with both string and list

Get one by one character from *left to right*.

```
for e in x:  
    ...
```

Get one by one character from *right to left*.

```
for e in x[::-1]:  
    ...
```

Get one by one character from *left to right* but not include the last character.

```
for e in x[:-1]:  
    ...
```

Get only characters *with odd index* from *left to right*.

```
for e in x[1::2]:  
    ...
```

Practice: count the number of "the" and "The"

The word "the" is one of the most common words in English.

" () , . '



Replace punctuation
with space.

The word the is one of the most common words in English



Split()

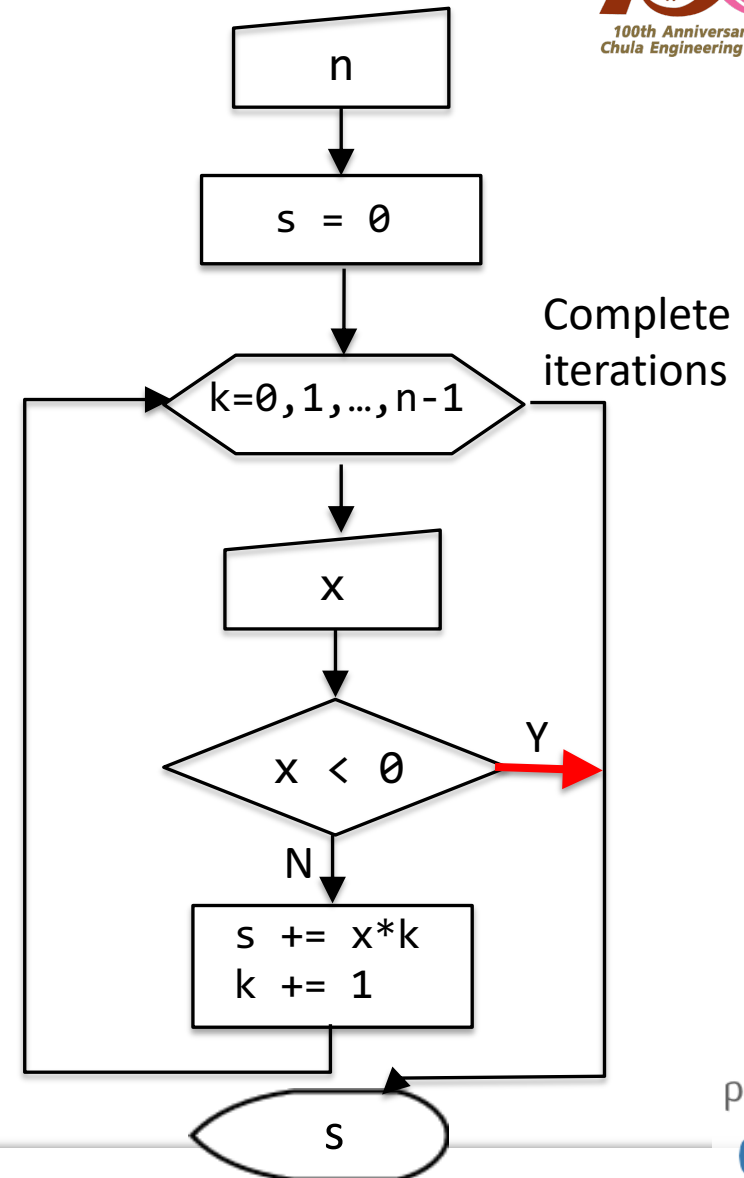
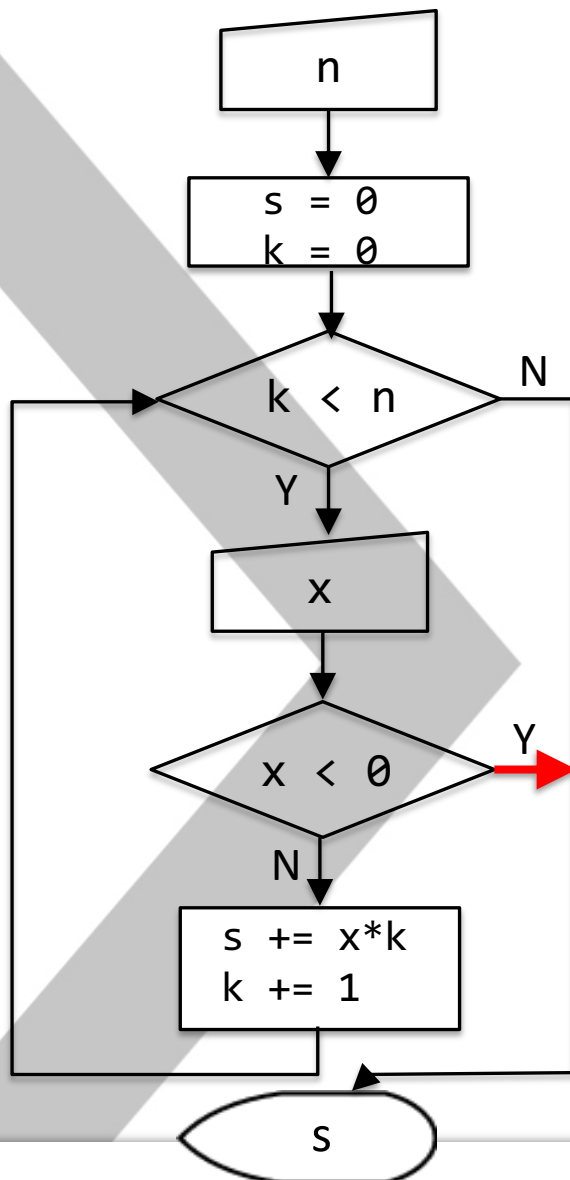
["The", "word", "the", "is", "one", "of", "the", "most",
"common", "words", "in", "English"]



Count the number of "the"
and "The".

3

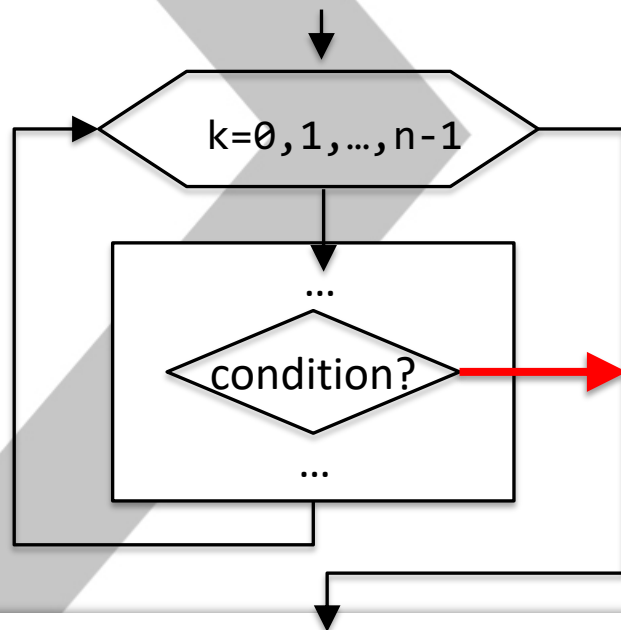
break: instruction to get out of a loop



break: instruction to get out of a *for* loop

```
for k in range(n):  
    ...  
    if condition:  
        break  
    ...
```

```
n = int(input())  
for k in range(2, n+1):  
    if n%k == 0:  
        break  
if k == n:  
    print("Prime")  
else:  
    print("Composite")
```

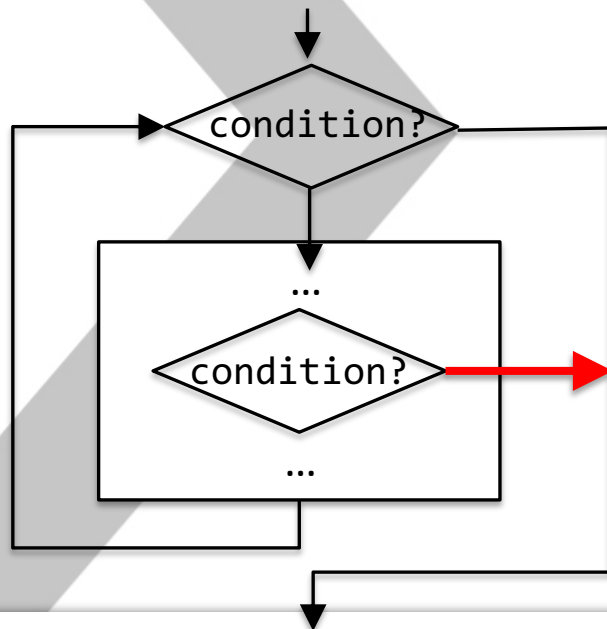


Get n from keyboard. Find all k that are n divisible,
 $k = 2, 3, \dots, n$

When get out of the loop,
if k is equal to n , n is a prime number,
otherwise, n is a composite number.

break: instruction to get out of a *while* loop

```
while condition:  
    ...  
    if condition:  
        break  
    ...
```



```
t = input() 10.0  
s = 0; n = 0 10.0  
while t != "q": 11.0  
    s += float(t) 12.0  
    n += 1 q  
t = input()  
print("Average =", s/n)
```

```
s = 0; n = 0 10.0  
while True: 10.0  
    t = input() 11.0  
    if t == "q": 12.0  
        break q  
    s += float(t)  
    n += 1  
print("Average =", s/n)
```


Practice: guess number game

Output

Guess my number (0 to 99)
You have seven tries
50
Higher
75
Lower
57
Higher
68
Lower
62
Lower
60
Lower
69
You win

Output

Guess my number (0 to 99)
You have seven tries
1
Higher
2
Higher
3
Higher
4
Higher
5
Higher
6
Higher
7
Higher
You lose, the number is 9

Practice: guess number game

```
import random
```

```
print("Guess my number (0 to 99)")
```

```
print("You have seven tries")
```

```
n = random.randint(0,99)
```

Randomly select a number between 0 to 99, inclusive

```
for k in range(7):
```

```
    m = int(input())
```

Have only 7 tries