

1, 3

HS

1
$$\vdash$$
 Ki f \rightarrow ¬¬Ki fA1×2 \vdash Ki ¬Ki f \rightarrow ¬Ki fA3✓ ×3 \vdash ¬¬Ki f \rightarrow ¬Ki ¬Ki fCP \checkmark × 2

$$6 \vdash \neg Ki \neg Ki f \rightarrow \neg \neg Ki f$$

$$7 \vdash \neg \neg Ki f \rightarrow Ki f$$

$$8 \vdash \neg Ki \neg Ki f \rightarrow Ki f \qquad \qquad HS \checkmark \checkmark \qquad 6, 7$$

$$9 \vdash Kif \leftrightarrow \neg Ki \neg Kif$$
 EI \checkmark \checkmark 4, 8

System S5 ∨ Agents (m)

4 \vdash Ki f $\rightarrow \neg$ Ki \neg Ki f

Goal
Ki f <-> !Ki !Ki f

Syntax Overview \checkmark