

$$1 \vdash p \rightarrow p$$

Α1

$$2 \vdash [p] p \leftrightarrow (p \rightarrow p)$$

A11



$$3 \quad \vdash \ ([p] \ p \leftrightarrow (p \rightarrow p)) \rightarrow ((p \rightarrow p) \leftrightarrow [p] \ p)$$

Α1

$$4 \vdash (p \rightarrow p) \leftrightarrow [p] p$$

R1



2, 3

$$5 \vdash (p \rightarrow p) \rightarrow [p] p$$

EE



4

R1



1, 5

R2



6

$$8 \quad \vdash \quad K1 \ [p] \ p \rightarrow (p \rightarrow K1 \ [p] \ p)$$



7, 8

9
$$\vdash$$
 p \rightarrow K1 [p] p

R1



10
$$\vdash$$
 [p] K1 p \leftrightarrow (p \rightarrow K1 [p] p)

A14



11
$$\vdash$$
 ([p] K1 p \leftrightarrow (p \rightarrow K1 [p] p)) \rightarrow ((p \rightarrow K1 [p] p) \leftrightarrow [p

Α1



12 \vdash (p \rightarrow K1 [p] p) \leftrightarrow [p] K1 p

R1



10, 11

13
$$\vdash$$
 (p \rightarrow K1 [p] p) \rightarrow [p] K1 p

ΕE



12

14
$$\vdash$$
 [p] K1 p

R1



9, 13

System

PA

Agents

(m)

