

$$1 \vdash p \to p$$
 A1

$$2 \vdash [p] p \leftrightarrow (p \rightarrow p)$$
 A11

$$3 \vdash (p \rightarrow p) \rightarrow [p] p$$
 EE'  $\checkmark$  2

$$4 \vdash [p] p$$
 R1  $\checkmark$  1, 3

$$5 \vdash K1[p]p$$
 R2  $\checkmark$  4

6 
$$\vdash$$
 K1 [p] p  $\to$  (p  $\to$  K1 [p] p) A1

$$7 \vdash p \to K1 [p] p$$
 R1  $\checkmark$   $\checkmark$  5, 6

$$8 \vdash [p] \mathsf{K1} \; \mathsf{p} \leftrightarrow (\mathsf{p} \to \mathsf{K1} \; [\mathsf{p}] \; \mathsf{p}) \qquad \qquad \mathsf{A14} \qquad \checkmark \checkmark$$

$$9 \vdash ([p] \mathsf{K1} \ \mathsf{p} \leftrightarrow (\mathsf{p} \to \mathsf{K1} \ [\mathsf{p}] \ \mathsf{p})) \to ((\mathsf{p} \to \mathsf{K1} \ [\mathsf{p}] \ \mathsf{p}) \leftrightarrow [\mathsf{p}] \\ \qquad \qquad \checkmark \checkmark$$

10 
$$\vdash$$
 (p  $\rightarrow$  K1 [p] p)  $\leftrightarrow$  [p] K1 p R1  $\checkmark$   $\checkmark$  8, 9

11 
$$\vdash$$
  $(p \rightarrow K1 [p] p) \rightarrow [p] K1 p$  EE  $\checkmark$  10

12 
$$\vdash$$
 [p] K1 p R1  $\checkmark$   $\checkmark$  7, 11

System PA V Agents (m)

Goal [p]K1p

Syntax Overview