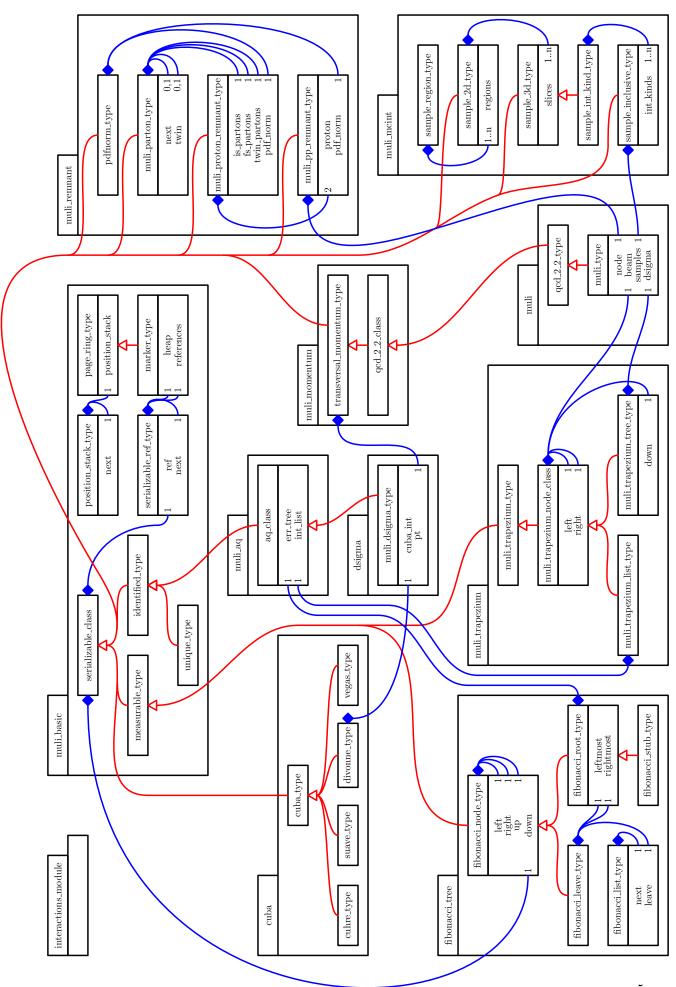
## Inhaltsverzeichnis

Inhaltsverzeichnis

# Teil I Allgemeines



## 1 Nomenklatur

## 1.1 n-te Wechselwirkung

Durch den Algorithmus werden iterativ harte, partonische, treelevel, QCD 2  $\rightarrow$  2 Wechselwirkungen mit absteigenden Wechselwirkungsskalen  $p_{\perp}^{(n)}$  generiert. Variablen, die nach jeder harten Wechselwirkung einen neuen Wert erhalten, führen die Ordnungszahl n der aktuellen Wechselwirkung hochgestellt in runden Klammern, um Verwechslungen mit Potenzen zu vermeiden.

Diese Ordnungszahl wird mit k bezeichnet, wenn sie sich nicht auf die aktuelle Wechselwirkung bezieht, sondern Summations- oder Produktindex über alle bisherigen Wechselwirkungen ist. Die Ordnungszahl der letzten Wechselwirkung wird mit N notiert. Bevor eine harte Wechselwirkung stattfindet, ist die Ordnungszahl gleich Null und kann weggelassen werden.

## 1.2 Impulse

Die Viererimpulse der Remnants sind  $P_1^{(n)}$  bzw.  $P_2^{(n)}$  für das erste bzw. das zweite Proton. Die Viererimpulse der Partonen sind  $\hat{p}_1^{(n)}$  bzw.  $\hat{p}_2^{(n)}$  für das erste bzw. das zweite Proton. Die Viererimpulse der Teilchen im Endzustand der partonischen Wechselwirkung sind für MulI nicht von Bedeutung.

Die Kinematik eines partonischen Ereignisses wird vollständig durch das kartesische Quadrupel  $p_{\text{cart}}^{(n)} = \left[x_1^{(n)}, x_2^{(n)}, p_\perp^{(n)}; s^{(n)}\right]$  bzw. das hyperbolische Quadrupel  $p_{\text{hyp}}^{(n)} = \left[h_1^{(n)}, h_2^{(n)}, h_3^{(n)}; s^{(n)}\right]$  definiert. Die entsprechende Koordinatentransformation ist in (??) angegeben. Es wird nicht zwischen der Bjorken-Scaling-Variable x und dem Impulsanteil mit  $xP = \hat{p}$  unterschieden. Wir nehmen an, dass die kinetische Energie der Protonen viel größer als die Ruhemasse der Protonen ist. In diesem Grenzwert stimmen beide Variablen überein.

#### 1.3 Flavor

Quarks und Gluonen der n-ten harten Wechselwirkung haben Flavorindizes  $a^{(n)}, b^{(n)}, c^{(n)}, d^{(n)}$ , wobei a das Flavor des Partons aus dem Remnant 1 und b das Flavor des Partons aus dem Remnant 2 ist. Wenn nicht anders angegeben, wird das LHAPDF-Schema verwendet, mit  $[\overline{t}, \overline{b}, \overline{c}, \overline{s}, \overline{u}, \overline{d}, g, d, u, s, c, b, t] = [-6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6].$ 

#### 1.4 Strukturfunktionen

Strukturfunktionen  $f(x,\mu)$  sind in diesem Dokument synonym zu Flavor-Strukturfunktionen, die Impuls-Strukturfunktionen ergeben sich dann aus  $xf(x,\mu)$ . Im Gegensatz dazu liefert evolvePDF aus LHAPDF die Impulsstrukturfunktion. MulI hat diesbezüglich die gleiche Konvention wie die Builtin-PDFs aus WHIZARD, welche ebenfalls Flavor-PDFs liefern.



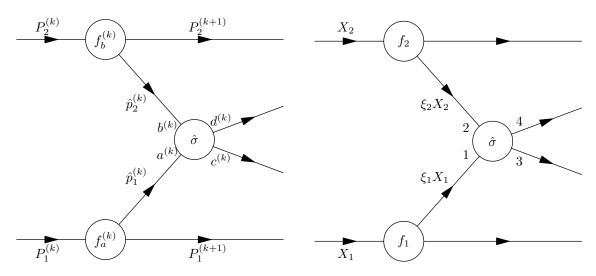


Abbildung 1.1: Links: Impulsvariablen  $P_x$  der Remnants, Impulsvariablen  $\hat{p}_x$  der Partonen und Flavorindizes  $a^{(k)}, b^{(k)}, c^{(k)}, d^{(k)}$  der Partonen in der k-ten Iteration des Multiple Interactions Algorithmus. Rechts: Die Prozeduren zur Generierung der Ereignisse kennen üblicherweise nicht die Ordnungszahl k nur einen Teil der Impulsinformation, nämlich die hadronischen Impulsanteile X mit  $P^{(k)} = XP$  und die partonischen Impulsanteile  $\xi$  mit  $\hat{p}^{(k)} = \xi P^{(k)} = xP$ . Anstatt der Flavorindizes  $a^{(k)}, b^{(k)}, c^{(k)}, d^{(k)}$  ist die festgelegte Position in dem Flavorquadrupel eingetragen.

Da beide Remnants eine verscheidene Historie haben können, sind im Allgemeinen auch beide Remnant-Strukturfunktionen verschieden. Die Zugehörigkeit wird durch den Flavorindex a für das erste und b für das zweite Proton notiert. Wir verzichten auf die Indizierung der Flavorindizes, also  $a^{(n)} \to a$ , da die Strukturfunktionen bereits Ordnungsindizes (n) haben. Wir erhalten  $f_a^{(n)}(x_1^{(n)}, \mu_F^{(n)})$  für das erste Proton und  $f_b^{(n)}(x_2^{(n)}, \mu_F^{(n)})$  für das zweite Proton.

Derzeit sind im Modul muli\_remnant Proton-Strukturfunktionen fest implementiert, es können also ohne Eingriff in den Code z.B. keine Proton-Antiproton Streuungen generiert werden. Allerdings sollte die Verallgemeinerung auf Hadronen mit maximal zwei verschiedenen Valenzquarks kaum Probleme bereiten, da die Infrastruktur des Moduls nicht geändert werden muss.

## 1.5 Wirkungsquerschnitte

Wie die Strukturfunktionen ändern sich auch die Wirkungsquerschnitte  $\sigma$  mit jeder Iteration. Allerdings können wir die Abhängigkeit komplett in die Änderung der invarianten Masse  $s^{(n)}$  der n-ten Iteration absorbieren. Wir notieren also keinen Ordnungsindex (n), sondern fügen die invariante Masse als Parameter durch ein Semikolon getrennt in die Liste der Argumente ein. Wir erhalten für den hadronischen Wirkungsquerschnitt  $\sigma$ 

$$\sigma_{ab\to cd}^{(n)}\left(x_1^{(n)}, x_2^{(n)}, p_\perp^{(n)}\right) = \sigma_{ab\to cd}\left(x_1^{(n)}, x_2^{(n)}, p_\perp^{(n)}; s^{(n)}\right). \tag{1.1}$$

Der hadronische Wirkungsquerschnitt  $\sigma$  bezieht sich auf das Streuereignis, wie in Abbildung ?? dargestellt. Der partonische Wirkungsquerschnitt hingegen ist  $\widehat{\sigma}$ .



## 1.6 Übersicht

$$s = s^{(1)} = P_1 \cdot P_2 \tag{1.2}$$

$$s^{(n)} = P_1^{(n)} \cdot P_2^{(n)} \tag{1.3}$$

$$\hat{p}_1^{(n)} = P_1^{(n)} x_1^{(n)} \tag{1.4}$$

$$s = s^{(1)} = P_1 \cdot P_2$$

$$s^{(n)} = P_1^{(n)} \cdot P_2^{(n)}$$

$$\hat{p}_1^{(n)} = P_1^{(n)} x_1^{(n)}$$

$$P_1^{(n+1)} = P_1^{(n)} (1 - x_1^{(n)})$$

$$(1.2)$$

$$(1.3)$$

$$(1.4)$$

$$X^{(n)} = \prod_{k=1}^{n} \left( 1 - x^{(k)} \right)$$

$$P_1^{(n+1)} = X_1^{(n)} P^{(1)}$$
(1.6)

$$P_1^{(n+1)} = X_1^{(n)} P^{(1)} (1.7)$$

$$p_{\perp} = \frac{\hat{t}\hat{u}}{\hat{s}} \tag{1.8}$$

## 2 Der Algorithmus

Der Algorithmus ist in meiner Dissertation in Kapitel 5 bereits dokumentiert, deswegen werde ich hier nicht alle Aspekte wiederholen. In der Dissertation wird allerdings nicht sorgfältig zwischen fertigen und geplanten Eigenschaften getrennt, deswegen gebe ich hier einen groben Überblick über den aktuellen Stand.

MulI wird derzeit ausschließlich von dem shower\_interface aus dem interleaved Branch aus dem schmidtboschmann Verzeichnis des WHIZARD-Repositories aufgerufen. Es ist noch kein MulI-Code in den WHIZARD-Core übertragen worden, stattdessen sind alle relevanten Daten in einem erweiterten Datentyp muli\_type gekapselt. muli\_type stellt ebenfalls eine vollständige Schnittstelle bereit, um MPI zu generieren und Remnant-PDFs abzurufen. Die derzeit verwendeten Methoden dieser Schnittstelle sind in Tabelle ?? aufgeführt.

## 2.1 Stratified Sampling

Die Wahrscheinlichkeit dafür, dass die Wechselwirkung aus dem Stratum  $\{\alpha, \beta\}$  mit der größten Skala  $p_{\perp} \leq p_{\parallel}^{(n-1)}$  bei der Skala  $p_{\parallel}^{(n-1)}$  stattfindet, ist durch

$$\mathcal{P}_{\text{next},a,b}^{(n)}\left(p_{\perp}^{(n)};p_{\perp}^{(n-1)},s^{(n)}\right) := \exp\left[W_{a}^{(n)}W_{b}^{(n)}\left[\mathcal{S}_{\alpha\beta}\left(p_{\perp}^{(n)};s^{(n)}\right) - \mathcal{S}_{\alpha\beta}\left(p_{\perp}^{(n-1)};s^{(n)}\right)\right]\right] \tag{2.1}$$

gegeben.  $s^{(n)}$  ist die invariante Masse des Remnant-Remnant-Systems,  $W_{\alpha}^{(n)}$  und  $W_{\beta}^{(n)}$  sind die Wichtungsfaktoren des Stratums  $\alpha$  bzw.  $\beta$  und  $\mathcal{S}_{\alpha\beta}$  ist das Stammstratum mit

$$S_{\alpha\beta}\left(p_{\perp}^{(n)};s^{(n)}\right) := \int_{p_{\perp}^{\max}}^{p_{\perp}^{(n)}} \mathrm{d}\,p_{\perp}\overline{S}_{\alpha\beta}\left(p_{\perp};s^{(n)}\right). \tag{2.2}$$

Generischer Name	Spezifischer Name
muli_type%initialize	muli_initialize
$muli\_type\%restart$	muli_restart
$\operatorname{muli\_type}\% \operatorname{finalize}$	muli_finalize
muli_type%apply_initial_interaction	muli_apply_initial_interaction
$muli\_type\%generate\_gev2\_pt2$	muli_generate_gev2_pt2
${ m muli\_type\%generate\_partons}$	muli_generate_partons
$qcd_2_2_{type\%get\_color\_correlations}$	qcd_2_2_get_color_correlations
$\operatorname{muli\_type}\%\operatorname{replace\_parton}$	muli_replace_parton
muli_type%get_parton_pdf	muli_get_parton_pdf
$\operatorname{muli\_type\%get\_momentum\_pdf}$	$muli\_get\_momentum\_pdf$

Tabelle 2.1: Die Methoden der Mull Schnittstelle für den Interleaved-Algorithmus.

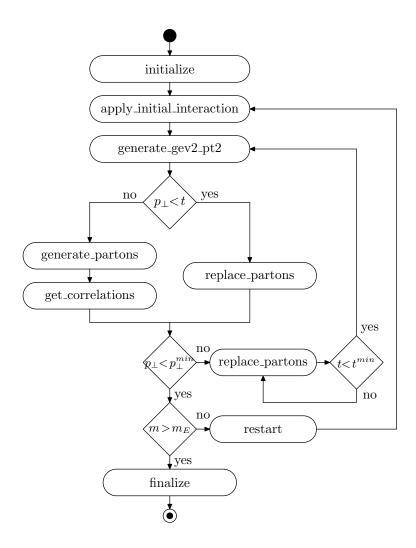


Abbildung 2.1: Flussdiagramm des Interleaved-Algorithmus. Eingetragen sind ausschließlich die Aufrufe der MulI-Schnittstelle, mit Ausnahme von get\_parton\_pdf und get\_momentum\_pdf, da diese nur für Interna des Partonshowers relevant sind und das Diagramm unnötig kompliziert machen würden. Die Generierung der Showerskalen und -Teilchen ist hier nicht dargestellt. Parallel zu generate\_gev2\_pt2 wird von dem ISR-Modul eine Showerskala t generiert und unmittelbar vor replace\_parton wird von dem ISR-Modul ein neues Showerteilchen generiert, dass durch replace\_parton in die Beschreibung des Remnants aufgenommen wird.  $m_E$  ist die Zahl der zu generierenden Events.

Stratum	Name	Partonen	Stratum	Name	Partonen
$S_1$ $S_2$ $S_3$ $S_4$	Gluon See Valenz-Down Valenz-Up (a)	$ \begin{cases} q^S : \forall q \} \\ d^V \\ u^V \end{cases} $	$S_1 \ S_2 \ S_3 \ S_4 \ S_5$	Gluon See Valenz-Down Valenz-Up Quasivalenz (b)	$ \begin{cases} q^S : \forall q \} \\ d^V \\ u^V \end{cases} $ $ \{q^Q : \forall q \} $

Tabelle 2.2: (a): Strati zur Berechnung der nächsten Skala. (b) Strati für die Wichtungsfaktoren in (??)

Das Stammstratum ist demnach eine negative Stammfunktion des integrierten Stratums  $\overline{S}_{\alpha\beta}$  mit  $p_{\parallel}^{\max}=s/4$  und

$$\overline{S}_{\alpha\beta} \left( p_{\perp}; s^{(n)} \right) := \int_{x_{\min}}^{1} d x_1 \int_{x_{\min}}^{1} d x_2 \, S_{\alpha\beta} \left( x_1, x_2, p_{\perp}; s^{(n)} \right). \tag{2.3}$$

Schließlich sind die Branchingstrati  $S_{\alpha\beta}$  mit

$$S_{\alpha\beta} := \frac{1}{\sigma_{\text{nd}}} \sum_{k \in S_a} \sum_{l \in S_k} \sum_{m,n} \frac{\partial^3 \sigma_{kl \to mn} (x_1, x_2, p_\perp; s)}{\partial x_1 \ \partial x_2 \ \partial p_\perp}$$
(2.4)

als bedingte Wahrscheinlichkeit dafür definiert, dass eine hadronische Wechselwirkung aus dem Stratum  $\{\alpha, \beta\}$  stattfindet, gegeben dass eine nicht-diffraktive hadronische Wechselwirkung stattfindet.  $\sigma_{nd}$  ist der totale, nicht-diffraktive Wirkungsquerschnitt und einer der freien Parameter des MPI-Modells. Die einfachen Strati  $S_a$  sind in Tabelle ?? dargestellt.

In Tabelle (??) sind zwei Varianten angegeben. In der ersten fehlen offensichtlich die Quasivalezquarks. Diese werden zwar vollkommen korrekt in den Remnant-Strukturfunktionen berücksichtigt, werden aber für die eigentliche Generierung der MPI aus technischen Gründen komplett ignoriert. In der Dissertation ist in Kapitel 5.2 ein Vorschlag gemacht, wie Quasivalenzquarks mitgenommen werden können. Diese Umsetzung bedeutet aber einen erheblichen Eingriff in den Quellcode.



In muli\_interactions%valid\_processes ist für jedes Feynmandiagramm in der fünften Komponente valid\_processes(5,:) die Nummer des Stratums eingetragen, zu dem das Diagramm gehört.

Die einfachen Strati  $S_{\alpha}$  heißen im Quellcode pdf\_int\_kind. Sie sind in muli\_interactions%pdf\_int\_kind\_gluon und folgende definiert. Entsprechend sind die doppelten Strati  $\{\alpha,\beta\}$  in muli\_interactions%double\_pdf\_kinds hinterlegt.



Wir bestimmen die nächste Skala des Stratums  $\{\alpha, \beta\}$  über

$$\widehat{p}_{\perp,a,b}^{(n)} = \mathcal{S}_{\alpha\beta}^{-1} \left( \cdot ; s^{(n)} \right) \left( \zeta_{\alpha\beta}^{(n)} \right) \tag{2.5}$$

mit

$$\zeta_{\alpha\beta}^{(n)} := \frac{\ln(z_{\alpha\beta}^{(n)})}{W_a^{(n)} W_b^{(n)}} + \mathcal{S}_{\alpha\beta} \left( p_{\perp}^{(n-1)}; s^{(n)} \right) = \mathcal{S}_{\alpha\beta} \left( p_{\perp}^{(n)}; s^{(n)} \right) \tag{2.6}$$

und

$$z_{\alpha\beta}^{(n)} \in (0,1], \quad \text{zufällig und gleichverteilt.}$$
 (2.7)

Durch einsetzen von  $s^{(n)}$  in  $\mathcal{S}_{\alpha\beta}$  erhalten wir eine einstellige, umkehrbare Funktion  $\mathcal{S}_{\alpha\beta}$  (  $\cdot$ ;  $s^{(n)}$ ). Somit ist  $\mathcal{S}_{\alpha\beta}^{-1}$  ( $\cdot$ ;  $s^{(n)}$ ) ( $\zeta_{\alpha\beta}^{(n)}$ ) eben diese Umkehrfunktion, ausgewertet bei  $\zeta_{\alpha\beta}^{(n)}$ .

Der größte Wert von  $\widehat{p}_{\perp,a,b}^{(n)}$  unter allen Strati ist die neue Skala  $\widehat{p}_{\perp}^{(n)}$ , das Stratum mit der größten Skala ist das neue Stratum  $\{\alpha^{(n)}, \beta^{(n)}\}$ 

Die Stammstrati in (??) hängen offensichtlich von der aktuellen hadronischen invarianten Masse  $s^{(n)}$  ab. Derzeit werden die  $\mathcal{S}_{\alpha\beta}$  aber als eindimensionale Funktionen in muli\_type%dsigma ohne s-Abhängigkeit gespeichert. Geht man zu einer zweidimensionalen Dastellung über, dann kommt man zu den Performance- und Speicherproblemen, die in der Dissertation in Kapitel 5.2 beschrieben sind. Dynamische Werte von  $s^{(n)}$  sind also nicht durch einen trivialen Patch implementierbar. Das Problem wird teilweise dadurch entschärft, dass die Skala später auf die invariante Masse normiert wird. Quotienten  $p_{\perp}/s$  werden also korrekt behandelt, nur durch Faktoren von s ohne  $p_{\perp}$  werden die Matrixelemente inkonsistent.

## 2.2 Importance Sampling

Das Stratum  $\{\alpha, \beta\}$  sowie die Skala  $p_{\perp}$  liegen fest. Wie auch in der Dissertation unterdrücken wir hier die Indizes <sup>(n)</sup>, da hier nur Werte aus der aktuellen Iteration vorkommen. Wir generieren die hyperbolischen Impulsanteile  $h_1, h_2$ , indem wir die Gleichung

$$zs\overline{S}_{ab}\left(p_{\perp}(h_3, s^{(n)}), s^{(n)}\right) \stackrel{?}{<} H_{ab}\left(h_1, h_2, h_3, s^{(n)}\right)$$
 (2.8)

 $_{
m mit}$ 

$$h_1, h_2, z \in (0, 1],$$
 zufällig und gleichverteilt (2.9)

solange mit neu generierten  $h_1, h_2, z$  auswerten, bis sie erfüllt ist. H ist eine regularisierte Form der divergenten Branchingstrati S, mit

ergenten Branchingstrati 
$$S$$
, mit
$$H_{ab}\left(h_1, h_2, h_3, s^{(n)}\right) = S_{ab}\left(x_1(h_1, h_2), x_2(h_1, h_2), p_{\perp}(h_1, h_2, s^{(n)}), s^{(n)}\right) \left(\frac{\partial h_1}{\partial x_1} \frac{\partial h_2}{\partial x_2} - \frac{\partial h_1}{\partial x_2} \frac{\partial h_2}{\partial x_1}\right) \tag{2.10}$$

und

$$h_1 := \frac{x_1 x_2 - h_3}{(1 - h_3)^{1/4}} \tag{2.11}$$

$$h_2 := \frac{1 + (x_2^2 - x_1^2)^{1/3}}{2} \tag{2.12}$$

$$h_3 := \frac{4p_{\perp}}{\widehat{s}^{(n)}} \tag{2.13}$$

$$x_1 = \sqrt{\sqrt{(h_1^4(1 - h_3) + h_3)^2 + (4(h_2 - 1/2)^3)^2 - 4(h_2 - 1/2)^3}}$$
 (2.14)

$$x_2 = \sqrt{\sqrt{(h_1^4(1 - h_3) + h_3)^2 + (4(h_2 - 1/2)^3)^2 + 4(h_2 - 1/2)^3}}$$
 (2.15)

$$p_{\perp} = \frac{h_3 \hat{s}^{(n)}}{4}.\tag{2.16}$$

 $\overline{S}_{ab}$  ist der Mittelwert von  $H_{ab}$ , gemittelt über  $h_1$  und  $h_2$ . Mit dem willkürlichen reellen Faktor s wird  $s\overline{S}_{ab}$  damit zu einer, von  $p_{\perp}$  abhängigen, Majorante von  $H_{ab}$ .

Um H noch weiter zu glätten, wird in muli\_type%samples eine Einteilung des  $\{h_1, h_2, h_3\}$ -Einheitsquaders und Unterquader abgelegt. Dabei wird der Quader zuerst so in  $h_3$ -Richtung in endlich viele Scheiben geschnitten, dass das Integral über H in jeder Scheibe etwa gleich ist. Anschließend wird jede Scheibe simultan in  $h_1$  und  $h_2$  so in Unterquader zerlegt, dass das Integral über jedes dieser Unterquader



etwa gleich groß ist und die Varianz in jedem Unterquader klein wird. Jeder Unterquader hat einen Index  $q_i$  und einen Flächeninhalt in der  $h_1 - h_2$ -Ebene von  $a_i$ .

Weiterhin werden alle Feynmandiagramme, die in dem Stratus  $\{\alpha, \beta\}$  enthalten sind, mit einem Wichtungsfaktor  $d_j$  versehen. Die tatsächliche Vorgehensweise zur Generierung der Impulse und der Flavor ist dann wie folgt:

- 1. Es wird ein Diagramm mit der Wahrscheinlichkeit  $W_j / \sum_k W_k$  gewählt.
- 2. Es wird zufällig und gleichverteilt ein Quader  $q_i$  mit der Fläche  $a_i$  aus derjenigen Scheibe gewählt, die  $h_3$  enthält.
- 3. Es werden zufällig und gleichverteilt reelle Zahlen  $h_1, h_2$  und z aus dem Einheitsintervall gewählt
- 4. Es wird

$$zsW_j\overline{S}_{ab}\left(p_{\perp}(h_3, s^{(n)}), s^{(n)}\right) \stackrel{?}{<} a_iH_{ab}\left(h_1, h_2, h_3, s^{(n)}\right)$$
 (2.17)

ausgewertet und bei 1 begonnen, bis die Ungleichung erfüllt ist.

5. Aus  $h_1$  und  $h_2$  ergeben sich die Impulsanteile  $x_1$  und  $x_2$ , aus dem Diagramm j ergeben sich die Flavor a, b, c und d.

#### 2.3 Remnants

Abweichend von der Dissertation (Gl. 4.49) werden hier fünf verschiedene Wichtungsfaktoren für die vier Strati {Gluon, See, Valenz-down, Valenz-up, Quasivalenz} zugelassen:

$$W_{G}^{(n)} \int_{\xi_{\min}^{(n)}}^{1} d\xi^{(n)} f_{g}(\xi^{(n)}, Q^{2}) + W_{S}^{(n)} \sum_{q} \int_{\xi_{\min}^{(n)}}^{1} d\xi^{(n)} f_{q^{S}}(\xi^{(n)}, Q^{2}) + \sum_{q} W_{q^{V}}^{(n)} \frac{N_{q^{V}}^{(n)}}{N_{q^{V}}^{(0)}} \int_{\xi_{\min}^{(n)}}^{1} d\xi^{(n)} f_{q}^{v}(\xi^{(n)}, Q^{2}) + W_{Q}^{(n)} \sum_{q} \int_{\xi_{\min}^{(n)}}^{1} d\xi^{(n)} f_{q}^{Q}(\xi^{(n)}, Q^{2})$$

$$(2.18)$$

Da wir nur eine Gleichung für vier Wichtungsfaktoren haben, müssen wir weitere Beziehungen festlegen. Durch den Parameter muli\_remnant%remnant\_weight\_model wird entschieden, welche Wichtungsfaktoren auf Eins gesetzt werden. Die jeweils anderen werden gleich gesetzt. Für das Quadrupel  $[W_G, W_S, W_{d^V}, W_{u^V}, W_Q]$  erhalten wir:

In (??) eingesetzt kann w eindeutig bestimmt werden.

Für remnant\_weight\_model=0 ist (??) nicht lösbar, es ist also streng genommen kein gültiges Wichtungsmodell. Stattdessen wird dadurch die Gewichtung deaktiviert.



$\_remnant\_weight\_model$	$[W_G, W_S, W_d, W_u, W_Q]$
0	[1, 1, 1, 1, 1]
1	[w,w,w,w,w]
2	[w, w, 1, 1, 1]
3	[1, 1, w, w, w]
4	$[1, \ w, 1, \ 1, \ w]$

Tabelle 2.3: remnant weight models

## 2.4 Programmfluss

Die einzeilnen Methoden sind ausführlich in muli beschrieben. Wir geben hier nur eine kurze Übersicht an:

#### • initialize

Der Monte-Carlo-Generator von Mull und die Datenstruktur der Proton-Remnants werden initialisiert.

• apply initial interaction

Eine von WHIZARD generierte harte Wechselwirkung wird an Mull übergeben. Die Remnants werden entsprechend angepasst.

• generate gev2 pt2

Mittels (??) wird eine Skala  $\widehat{p}_{\perp,a,b}^{(n)}$  und ein Stratum  $\{\alpha^{(n)},\beta^{(n)}\}$  generiert.

• generate partons

Mittels (??) werden die Impulsanteile  $x_1$  und  $x_2$  und die Flavor a, b, c und d generiert. Außerdem wird eine interne Darstellung der Farbflüsse generiert.

• get\_correlations

Die interne Darstellung der Farbflüsse wird in der vom shower\_interface gewünschten Form von Farbkorrelationen ausgegeben.

• replace parton

Der ISR-Algorithmus hat ein Branching eines aktiven Showerteilchens generiert. Dieses Showerteilchen ist fortan kein aktives Teilchen mehr, sondern ein inneres Teilchen der perturbativen Wechselwirkung. Entsprechend muss es durch replace\_parton in der Beschreibung des Remnants durch das neue aktive Teilchen ersetzt werden. Siehe Abbildung ??

• restart

Es werden einige interne Variablen zurückgesetzt, wie z.B. das "finishedFlag. Außerdem werden die Remnants zurückgesetzt.

• finalize

Der Monte-Carlo-Generator von MulI, die vorgenerierten Wirkungsquerschnitte und die Remnants werden deallociert.

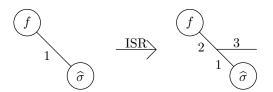


Abbildung 2.2: Ersetzung des aktiven ISR-Partons durch den ISR-Algorithmus. Links: Durch die härteste WW wurde ein Parton aus dem Hadron entfert. Dieses Parton ist ein "aktives" Parton, da ISR-Branchings für dieses Teilchen generiert werden. Alle Teilchen, die jemals generiert werden, bekommen eine eindeutige Nummer, hier die Nummer 1. Die Eigenschaften des Remants und des Teichens #1 müssen in der Summe die Eigenschaften des Protons ergeben. Rechts: Durch den ISR-Algorithmus wurde ein Branching der Teilches #1 erzeugt. Das Mutterparton hat die Nummer 2 bekommen, das andere Tochterparton hat die Nummer 3 bekommen. Jetzt müssen die Eigenschaften des Remnants und des Teilchens #2 in der Summe die Eigenschaften des Protons ergeben. In diesem Sinne müssen wir das Teilchen #1 wieder "zurücklegen" und das Teilchen #2 "herausnehmen".

# Teil II Module

## 3 Modul muli

Dieses Modul dient als Interface für den Interleaved Algorithmus. Es stellt dem Algorithmus Methoden zur Initialisierung und zum Garbage-Collecting, Methoden zur Generierung von  $p_{\perp}^{(n+1)}$ , und zur Generierung einer vollständigen Wechselwirkung, Methoden zum Austauschen von aktiven Partonen, sowie Methoden zu den Remnant-Strukturfunktionen zur Verfügung.

Alle Parameter des MulI-Algorithmus sowie der komplette aktuelle Zusatand der Remnants, einschließlich der aktiven Shower-Partonen, sind als Komponenten des erweiterten Types muli\_type definiert. Der Interleaved-Algorithmus muss also lediglich eine Instanz der Klasse muli\_type definieren und deren public Type-Bound-Procedures aufrufen.

Auf lange Sicht ist es geplant, die Strukturfunktionen in den WHIZARD-Core aufzunehmen. Dann sollte der Core die Funktionalität dieses Moduls weitgehend übernehmen. Zum einen wird dieses Modul dann obsolet, zum anderen müssen die Interfaces des Cores erweitert werden. Der Hauptgrund, warum das noch nicht geschehen ist, ist aber, dass der Core noch nicht Objekt-Orientiert ist. Es kann also keine Instanz von muli\_type an sf\_initialize übergeben werden. Es muss also entweder die Konfiguration dieses Moduls in Form von Modulkomponenten bereitgestellt werden, oder der Core muss lernen, eine Instanzen einer abstrakten PDF-Klasse entgegenzunehmen. Im letzteren Fall muss muli\_type nur diese abstrakte Klasse erweitern.



## 3.1 Abhängigkeiten

```
use muli_dsigma
use muli_mcint
use muli_remnant
```

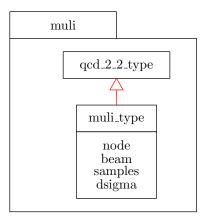


Abbildung 3.1: Klassendiagramm des Moduls muli

#### 3.2 Parameter

Für Diagnose, Testzwecke und Konsistenzprüfungen können die Remnants deaktiviert werden. Wenn auf .false. gesetzt, läuft der Algorithmus trotz Mehrfachwechselwirkungen immer mit den original Proton-PDFs

```
logical,parameter::muli_default_modify_pdfs=.true.muli_default_modify_pdfs
```

Da Mull noch nicht in den Core eingebunden ist, hat Mull keinen Zugriff auf die PDF Eigenschaften, so wie sie in den Sindarin-Files eingestellt werden können. Deswegen müssen die Proton-PDFs noch per Hand als Parameter festgelegt werden.

```
integer,parameter::muli_default_lhapdf_member=Omuli_default_lhapdf_member
character(*),parameter::muli_default_lhapdf_file=&
"cteq6ll.LHpdf"muli_default_lhapdf_file
```

## 3.3 Derived Types

```
3.3.1 \text{ qcd} 22_{\text{type}}
```

Dieser Datentyp abstrahiert die interne Darstellung einer QCD-2  $\rightarrow$  2 Wechselwirkungen und stellt Methoden mit traditionellen Namen zur Verfügung. Da verschiedene Module auf die Eigenschaften der Wechselwirkung zugreifen müssen, aber nur in dem Modul muli alle notwendigen Daten zur Verfügung stehen, ist in dem Modul muli\_momentum eine abstrakte qcd\_2\_2\_class definiert, die allen Modulen zur verfügung steht. qcd\_2\_2\_type erweitert diese Klasse und implementiert die vorgeschriebenen Methoden.

```
type, extends (qcd_2_2_class)::qcd_2_2_type
```

#### Komponenten

```
private
```

Alle gültigen Kombinationen der vier Partonflavor sind in der Modulkomponente muli\_interactions%valid\_processes durchnummeriert. process\_id gibt diese Nummer wieder und legt damit alle Flavor fest.

```
integer::process_id=-1
```

Alle Kombinationen aus Gluon, Seequark, Valenz-Up-Quark und Valenz-Down-Quark der beiden Partonen im Eingangszustand sind in der Modulkomponente muli\_interactions%double\_pdf\_kinds des Moduls muli\_interactions durchnummeriert. integrand\_id gibt diese Nummer wieder und legt damit fest, ob z.B. ein Up-Quark im Eingangszustand ein Seequark oder ein Valenzquark ist. Diese Nummer ist gleichzeitig die Ordnungsnummer des Integrationsstratums  $\{\alpha, \beta\}$  für die Generierung der Wechselwirkungsskala in muli\_type%generate\_next\_scale.

```
integer::integrand_id=-1
```

Jedes Parton, dass an einer Wechselwirkung teilnimmt, bekommt eine eindeutige Nummer. Das schließt die Partonen des ISR-Algorithmus mit ein. Diese Nummern sind wichtig, wenn der ISR-Algorithmus ein Teilchen aus der Liste der Teilchen im Eingangszustand (aka aktive Partonen) entfernt, das Mull vorher in diese Liste aufgenommen hat. Über die Parton IDs können diese zugeordnet und in muli\_type%replace\_parton konsistent eliminiert werden. parton\_ids enthält die Nummern der beiden Teilchen im direkten Eingangszustand der MPI Wechselwirkung, also ohne Showerbranchings.

```
integer,dimension(2)::parton_ids=[0,0]
```

Farbflüsse werden intern als Permutation dargestellt, die die Enden von Farblinien auf deren Angfänge abbildet. Eine 2 an dritter Stelle in flow bedeutet, dass eine Farbflusslinie in der zweiten Position beginnt und in der dritten Position endet. Die Positionen 1,2,3,4 entsprechen den Flavorindizes a,b,c,d in ??. In muli type%generate flow werden diese Farbflüsse generiert.

```
integer,dimension(4)::flow=[0,0,0,0]
```

momentum\_fractions enthält die dynamischen Impulsvariablen  $[\xi_1, \xi_2, p_{\perp}]$ , die die Kinematik einer Wechselwirkungen beschreiben, in kartesischen Koordinaten. hyperbolic\_fractions enthält dieselben Impulsvariablen in hyperbolischen Koordinaten  $[h_1, h_2, h_3]$ . Die Koordinatentransformation ist in (??) angegeben.

```
real(kind=double),dimension(3)::momentum_fractions=[-1D0,-1D0,-1D0]
real(kind=double),dimension(3)::hyperbolic_fractions=[-1D0,-1D0,-1D0]
```

#### Methoden

```
!Überschriebene serializable_class Methoden
procedure, public::write_to_marker=>qcd_2_2_write_to_marker
procedure, public::read_from_marker=>qcd_2_2_read_from_marker
procedure, public::print_to_unit=>qcd_2_2_print_to_unit
procedure,public,nopass::get_type=>qcd_2_2_get_type
!Überschriebene qcd_2_2_class Methoden
procedure,public::get_process_id=>qcd_2_2_get_process_id
procedure, public::get_integrand_id=>qcd_2_2_get_integrand_id
procedure, public::get_diagram_kind=>qcd_2_2_get_diagram_kind
procedure,public::get_lha_flavors=>qcd_2_2_get_lha_flavors
procedure, public::get_pdg_flavors=>qcd_2_2_get_pdg_flavors
procedure, public::get_parton_id=>qcd_2_2_get_parton_id
procedure, public::get_parton_kinds=>qcd_2_2_get_parton_kinds
procedure,public::get_pdf_int_kinds=>qcd_2_2_get_pdf_int_kinds
procedure, public::get_momentum_boost=>qcd_2_2_get_momentum_boost
procedure, public::get_remnant_momentum_fractions=>qcd_2_2_get_remnant_momentum_fractions
procedure,public::get_total_momentum_fractions=>qcd_2_2_get_total_momentum_fractions
!Originäre qcd_2_2_type Methoden
procedure, public::get_color_flow=>qcd_2_2_get_color_flow
procedure, public::get_diagram_color_kind=>qcd_2_2_get_diagram_color_kind
procedure, public::get_io_kind=>qcd_2_2_get_io_kind
procedure, public::get_hyperbolic_fractions=>qcd_2_2_get_hyperbolic_fractions
procedure, public::get_color_correlations=>qcd_2_2_get_color_correlations
procedure, public::qcd_2_2_initialize
generic,public::initialize=>qcd_2_2_initialize
```

#### 3.3.2 muli type

Der Datentyp muli\_type ist eine Sammlung von allen Daten, die für Generierung von mehrfachen Wechselwirkungen relevant sind. Da Instanzen von muli\_type keine Zeiger enthalten, mit Ausnahme von Zeigen auf Komponenten von sich selbst, und nicht auf dynamische Modulkomponenten zugreifen, können beliebig viele Instanzen von muli\_type erzeugt und parallel verwendet werden. Bloß kann LHAPDF nicht parallel aufgerufen werden.

muli\_type erweitert qcd\_2\_2\_type, damit *ist* eine Instanz von muli\_type die aktuelle Wechselwirkung. Die aktuellen Zustände der Remnants sind hingegen Komponenten von muli\_type, sodass andere Varianten von Remnants umgesetzt werden können, ohne diese Modul (entsprechend später den WHIZARD-Core) verändern zu müssen

Neben den aktuellen Zuständen der Wechselwirkung und der Remnants enthält muli\_type auch einen Importance-Sampler für die Impulsanteile  $[\xi_1, \xi_2]$ . Dieser ist derzeit nicht auf dem Stand der Dissertation, wo ein gemeinsames Sampling für alle Strati beschrieben wird. Dieses gemeinsame Sampling wäre dann so generisch, dass es nicht mehr eine Komponente von muli\_type sein sollte. Dann könnten mehrere Instancen von muli\_type dasselbe Sampling verwenden. Derzeit ist das Sampling zweifach redundant, nämlich wird für jedes Stratum für jede Instanz von muli\_type ein eigener Sampler allociert. Bei dem aktuellen Stand ist deswegen davon abzuraten, MulI zu parallelisieren.

```
type, extends (qcd_2_2_type)::muli_type
```

#### Komponenten

```
private
  !Untere Grenze für die Wechselwirkungsskala
  real(kind=double)::GeV2_scale_cutoff
  !Sollen die Strukturfunktionen im Laufe des Algorithmus verändert werden?
  logical::modify_pdfs=muli_default_modify_pdfs
  !Lag die letzte Wechselwirkungsskala unter GeV2_scale_cutoff?
  logical::finished=.false.
  !Wieviel Zeit haben die einzelnen Teile des Algorithmus benötigt?
  real(kind=double)::init_time=0D0
  real(kind=double)::pt_time=0D0
  real(kind=double)::partons_time=0D0
  real(kind=double)::confirm_time=0D0
  !Sind die Monte-Carlo-Generatoren bereit zur Generierung von MPI?
  logical::initialized=.false.
  !Wurde eine härteste Wechselwirkung vorgegeben?
  logical::initial_interaction_given=.false.
  !Der Mittelwert des hadronischen Wirkungsquerschnitts bei der aktuellen Skala.
  !Der Monte-Carlo-Generator für [x_1,x_2] verwendet ein vielfaches dieses Werts
  !als obere Schranke für den Wirkungsquerschnitt.
  real(kind=double)::mean=1D0
  !Die integrierten Wirkungsquerschnitte aller Strati bei der aktuellen Skala.
  !Der Monte-Carlo-Generator für die nächste Skala verwendet diese Integrale anstelle
  !der Skala als Startwerte.
  real(kind=double),dimension(0:16)::start_integrals=&
       !Der Zufallsgenerator für diese Instanz.
```



```
type(tao_random_state)::tao_rnd
!Die Wirkungsquerschnitte und deren Stammfunktionen aller Strati
type(muli_trapezium_tree_type)::dsigma
!Importance-Sampler für alle Strati.
type(sample_inclusive_type)::samples
!Die Remnants der beiden Protonen.
type(pp_remnant_type)::beam
!Ein interner Zeiger auf ein Segment der Stammfunktion dsigma, dass die
!aktuelle Skala umfasst.
class(muli_trapezium_node_class),pointer::node=>null()
end type muli_type
```

#### Methoden

```
contains
  !Überschriebene serializable_class Methoden
  procedure, public::write_to_marker=>muli_write_to_marker
  procedure,public::read_from_marker=>muli_read_from_marker
  procedure, public::print_to_unit=>muli_print_to_unit
  procedure,public,nopass::get_type=>muli_get_type
  !Originare muli_type Methoden
  ! init / final
  procedure, public::muli_initialize
  procedure, public::apply_initial_interaction=>muli_apply_initial_interaction
  procedure,public::finalize=>muli_finalize
  procedure, public::stop_trainer=>muli_stop_trainer
  procedure,public::reset_timer=>muli_reset_timer
  procedure,public::restart=>muli_restart
  generic,public:: initialize=>muli_initialize
  ! status query
  procedure,public::is_initialized=>muli_is_initialized
  procedure, public::is_initial_interaction_given=>muli_is_initial_interaction_given
  procedure,public::is_finished=>muli_is_finished
  ! user interface
  procedure, public::enable_remnant_pdf=>muli_enable_remnant_pdf
  procedure,public::disable_remnant_pdf=>muli_disable_remnant_pdf
  procedure, public::generate_gev2_pt2=>muli_generate_gev2_pt2
  procedure,public::generate_partons=>muli_generate_partons
  procedure,public::generate_flow=>muli_generate_flow
  procedure, public::replace_parton=>muli_replace_parton
  procedure,public::get_parton_pdf=>muli_get_parton_pdf
  procedure, public::get_momentum_pdf=>muli_get_momentum_pdf
  procedure,public::print_timer=>muli_print_timer
  procedure,public::generate_samples=>muli_generate_samples
  ! beam test
  procedure,public::fake_interaction=>muli_fake_interaction
  ! private procedures
  procedure, private::generate_next_scale=>muli_generate_next_scale
  procedure,private::confirm=>muli_confirm
```

## 3.4 Implementierung der Prozeduren

3.4.1 Methoden für qcd 2 2 type

## Überschriebene serializable class Methoden qcd 2 2 write to marker \( \ \) subroutine qcd\_2\_2\_write\_to\_marker(this,marker,status) class(qcd\_2\_2\_type),intent(in)::this class(marker\_type),intent(inout)::marker integer(kind=dik),intent(out)::status call marker%mark\_begin("qcd\_2\_2\_type") call transversal\_momentum\_write\_to\_marker(this,marker,status) call marker%mark("process\_id",this%process\_id) call marker%mark("integrand\_id",this%integrand\_id) call marker%mark("momentum\_fractions",this%momentum\_fractions) call marker%mark("hyperbolic\_fractions",this%hyperbolic\_fractions) call marker%mark\_end("qcd\_2\_2\_type") end subroutine qcd\_2\_2\_write\_to\_marker qcd 2 2 read from marker $\uparrow$ subroutine qcd\_2\_2\_read\_from\_marker(this,marker,status) class(qcd\_2\_2\_type),intent(out)::this class(marker\_type),intent(inout)::marker integer(kind=dik),intent(out)::status call marker%pick\_begin("qcd\_2\_2\_type",status=status) call transversal\_momentum\_read\_from\_marker(this,marker,status) call marker%pick("process\_id",this%process\_id,status) call marker%pick("integrand\_id",this%integrand\_id,status) call marker%pick("momentum\_fractions",this%momentum\_fractions,status) call marker%pick("hyperbolic\_fractions",this%hyperbolic\_fractions,status) call marker%pick\_end("qcd\_2\_2\_type",status=status) end subroutine qcd\_2\_2\_read\_from\_marker qcd 2 2 print to unit $\uparrow$ subroutine qcd\_2\_2\_print\_to\_unit(this,unit,parents,components,peers) class(qcd\_2\_2\_type),intent(in)::this integer, intent(in)::unit integer(kind=dik),intent(in)::parents,components,peers integer, dimension (2,4)::flow integer::index if(parents>zero)& call transversal\_momentum\_print\_to\_unit(this,unit,parents-1,components,peers) write(unit,'("Components of qcd\_2\_2\_type:")') ",I3)')this%get\_process\_id() write(unit,'("Process id is: write(unit,'("Integrand id is: ",I3)')this%get\_integrand\_id() if(this%get\_integrand\_id()>0)then ",4(I3))')this%get\_lha\_flavors() write(unit,'("LHA Flavors are: ",4(I3))')this%get\_pdg\_flavors() write(unit,'("PDG Flavors are:

```
write(unit,'("Parton kinds are:
                                           ",2(I3))')this%get_parton_kinds()
                                           ",2(I3))')this%get_pdf_int_kinds()
       write(unit,'("PDF int kinds are:
       write(unit,'("Diagram kind is:
                                           ",2(I3))')this%get_diagram_kind()
    end if
    call this%get_color_correlations(1,index,flow)
    write(unit, '("Color Permutations: ",4(IO))')this%flow
    write(unit,'("Color Connections:")')
    write(unit,'("(",I0,",",I0,")+(",I0,",",I0,")->(",I0,",",I0,")+(",I0,",",I0,")")')flow
    write(unit,'("Evolution scale is: ",E14.7)')this%get_unit2_scale()
    write(unit,'("Momentum boost is:
                                        ",E14.7)')this%get_momentum_boost()
    write(unit, '("Remant momentum fractions are: ",2(E14.7))')&
    this%get_remnant_momentum_fractions()
    write(unit,'("Total momentum fractions are: ",2(E14.7))')&
    this%get_total_momentum_fractions()
  end subroutine qcd_2_2_print_to_unit
qcd 2 2 get type \uparrow
  pure subroutine qcd_2_2_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="qcd_2_2_type")
  end subroutine qcd_2_2_get_type
Überschriebene qcd 2 2_class Methoden
\operatorname{qcd} 2 get process \operatorname{id} \uparrow
  elemental function qcd_2_2_get_process_id(this) result(id)
    class(qcd_2_2_type),intent(in)::this
    integer::id
    id=this%process_id
  end function qcd_2_2_get_process_id
qcd 2 2 get integrand id \( \ \ \)
  elemental function qcd_2_2_get_integrand_id(this) result(id)
    class(qcd_2_2_type),intent(in)::this
    integer::id
    id=this%integrand_id
  end function qcd_2_2_get_integrand_id
qcd 2 2 get lha flavors \( \ \)
  pure function qcd_2_2_get_lha_flavors(this) result(lha)
    class(qcd_2_2_type),intent(in)::this
    integer, dimension(4)::lha
    lha=valid_processes(1:4,this%process_id)
  end function qcd_2_2_get_lha_flavors
qcd 2 2 get pdg flavors \( \ \)
```

```
pure function qcd_2_2_get_pdg_flavors(this) result(pdg)
    class(qcd_2_2_type),intent(in)::this
    integer,dimension(4)::pdg
    pdg=this%get_lha_flavors()
    where(pdg==0) pdg=21
  end function qcd_2_2_get_pdg_flavors
qcd 2 2 get pdf int kinds \( \)
  pure function qcd_2_2_get_pdf_int_kinds(this) result(kinds)
    class(qcd_2_2_type),intent(in)::this
    integer,dimension(2)::kinds
    kinds=double_pdf_kinds(1:2,this%integrand_id)
  end function qcd_2_2_get_pdf_int_kinds
qcd 2 2 get parton id \( \ \ \)
  elemental function qcd_2_2_get_parton_id(this,n) result(id)
    class(qcd_2_2_type),intent(in)::this
    integer,intent(in)::n
    integer::id
    id=this%parton_ids(n)
  end function qcd_2_2_get_parton_id
qcd 2 2 get parton kinds †
  pure function qcd_2_2_get_parton_kinds(this) result(kinds)
    class(qcd_2_2_type),intent(in)::this
    integer, dimension(2)::kinds
    kinds=this%get_pdf_int_kinds()
    kinds(1)=parton_kind_of_int_kind(kinds(1))
    kinds(2)=parton_kind_of_int_kind(kinds(2))
  end function qcd_2_2_get_parton_kinds
qcd 2 2 get io kind \uparrow
  elemental function qcd_2_2_get_io_kind(this) result(kind)
    class(qcd_2_2_type),intent(in)::this
    integer::kind
    kind=valid_processes(5,this%process_id)
  end function qcd_2_2_get_io_kind
\operatorname{qcd} 2 get diagram kind \uparrow
  elemental function qcd_2_2_get_diagram_kind(this) result(kind)
    class(qcd_2_2_type),intent(in)::this
    integer::kind
    kind=valid_processes(6,this%process_id)
  end function qcd_2_2_get_diagram_kind
```

#### Originäre qcd 2 2 type Methoden

```
qcd 2 2 get diagram color kind \uparrow
```

This is one more hack. Before merging into the interleaved algorithm, muli has only cared for summed cross sections, but not for specific color flows. So two different diagrams with equal cross sections were summed up to diagram kind 1.



Now muli also generates color flows, so we must devide diagram kind 1 into diagram color kind 0 and diagram color kind 1.

```
elemental function qcd_2_2_get_diagram_color_kind(this) result(kind)
  class(qcd_2_2_type),intent(in)::this
  integer::kind
  kind=valid_processes(6,this%process_id)
  if(kind==1)then
    if(product(valid_processes(1:2,this%process_id))>0)then
       kind=0
    end if
end if
end function qcd_2_2_get_diagram_color_kind
```

## $\verb|qcd_2_2_get_momentum_boost| \uparrow$

Noch nicht implementiert



```
elemental function qcd_2_2_get_momentum_boost(this) result(boost)
   class(qcd_2_2_type),intent(in)::this
   real(kind=double)::boost
   boost=-1D0
 end function qcd_2_2_get_momentum_boost
pure function qcd_2_2_get_hyperbolic_fractions(this) result(fractions)
   class(qcd_2_2_type),intent(in)::this
   real(kind=double), dimension(3)::fractions
   fractions=this%hyperbolic_fractions
 end function qcd_2_2_get_hyperbolic_fractions
pure function qcd_2_2_get_remnant_momentum_fractions(this) result(fractions)
   class(qcd_2_2_type),intent(in)::this
   real(kind=double), dimension(2)::fractions
   fractions=this%momentum_fractions(1:2)
 end function qcd_2_2_get_remnant_momentum_fractions
qcd 2 2 get total momentum fractions \( \)
```

Noch nicht implementiert



```
pure function qcd_2_2_get_total_momentum_fractions(this) result(fractions)
    class(qcd_2_2_type),intent(in)::this
    real(kind=double),dimension(2)::fractions
    fractions=[-1D0,-1D0]
    end function qcd_2_2_get_total_momentum_fractions

qcd_2_2_get_color_flow ↑

pure function qcd_2_2_get_color_flow(this) result(flow)
    class(qcd_2_2_type),intent(in)::this
    integer,dimension(4)::flow
    flow=this%flow
    end function qcd_2_2_get_color_flow
```

Diese Methode generiert Farbflussdiagramme aus der internen Darstellung mittels Permutationen, wie sie in muli\_type%generate\_flow generiert werden. Der Interleaved Algorithmus numeriert alle Farbflüsse, deswegen nehmen wir die aktuelle Anzahl von Farbflüssen mit start\_index entgegen und liefern die neue Anzahl mit final\_index zurück. Die Ordnungszahlen der neu generierten Farblinien laufen dann von start index+1 bis einschließlich final index.

flow liefert schießlich das Farbflussdiagramm selbst zurück. Das Format von flow sieht vor, dass der zweite Index die Position des Partons im Diagramm wie in ?? mit  $[1,2,3,4] \rightarrow [a,b,c,d]$  beschreibt. Die beiden Stellen flow[:,a] beinhalten die Ordnungszahlen für eine eventuelle Farblinie bzw. eine eventuelle Antifarblinie oder 0 für keine Farblinie.

Die eingekreisten Zahlen sind die Positionen in flow, die nicht eingekreisten Zahlen sind die Inizes der Farblinien.

```
subroutine qcd_2_2_get_color_correlations(this, start_index, final_index, flow)
  class(qcd_2_2_type),intent(in)::this
  integer,intent(in)::start_index
  integer,intent(out)::final_index
  integer,dimension(2,4),intent(out)::flow
  integer::pos,f_end,f_beginning
  final_index=start_index
  !we set all flows to zero. zero means no connection.
  flow=reshape([0,0,0,0,0,0,0,0],[2,4])
  !look at all four possible ends of color lines.
  do f_end=1,4
     !the beginning of this potential line is stored in flow. zero means no line.
     f_beginning=this%flow(f_end)
     !is there a line beginning at f_beginning and ending at f_end?
     if(f_beginning>0)then
        !yes it is. we get a new number for this new line
        final_index=final_index+1
        !is this line beginning in the initial state?
```

```
if(f_beginning<3)then
             !yes it is. lets connect the color entry of f_begin.
             flow(1,f_beginning)=final_index
          else
             !no, it's the final state. lets connect the anticolor entry of f_begin.
             flow(2,f_beginning)=final_index
          end if
          !is this line ending in the final state?
          if(f_end>2)then
             !yes it is. lets connect the color entry of f_end.
             flow(1,f_end)=final_index
          else
             !no, it's the initial state. lets connect the anticolor entry of f_end.
             flow(2,f_end)=final_index
          end if
       end if
    end do
  end subroutine qcd_2_2_get_color_correlations
qcd 2 2 initialize \uparrow
Gewöhnliche Initialisierung aller Komponenten.
  subroutine qcd_2_2_initialize(this,gev2_s,process_id,integrand_id,parton_ids,flow,hyp,cart)
    class(qcd_2_2_type),intent(out)::this
    real(kind=double),intent(in)::gev2_s
    integer,intent(in)::process_id,integrand_id
    integer, dimension(2), intent(in)::parton_ids
    integer, dimension (4), intent(in)::flow
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(3), intent(in), optional::cart
    !Generischer Aufruf von transversal_momentum_initialize(this,gev2_s).
    call this%initialize(gev2_s)
    this%process_id=process_id
    this%integrand_id=integrand_id
    this%parton_ids=parton_ids
    this%flow=flow
    this%hyperbolic_fractions=hyp
    if(present(cart))then
       this%momentum_fractions=cart
    else
       this%momentum_fractions=h_to_c_param(hyp)
    end if
  end subroutine qcd_2_2_initialize
3.4.2 Methoden für muli type
```

Überschriebene serializable class Methoden

```
muli write to marker \( \ \)
```

```
subroutine muli_write_to_marker(this,marker,status)
    class(muli_type),intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("muli_type")
    call qcd_2_2_write_to_marker(this,marker,status)
    call marker%mark("modify_pdfs",this%modify_pdfs)
    call marker%mark("initialized",this%initialized)
    call marker%mark("initial_interaction_given",this%initial_interaction_given)
    call marker%mark("finished",this%finished)
    call marker%mark("init_time",this%init_time)
    call marker%mark("pt_time",this%pt_time)
    call marker%mark("partons_time",this%partons_time)
    call marker%mark("confirm_time",this%confirm_time)
    call marker%mark_instance(this%dsigma, "dsigma")
    call marker%mark_instance(this%samples, "samples")
    call marker%mark_instance(this%beam, "beam")
    call marker%mark_end("muli_type")
  end subroutine muli_write_to_marker
muli read from marker \( \)
  subroutine muli_read_from_marker(this,marker,status)
    class(muli_type),intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("muli_type",status=status)
    call qcd_2_2_read_from_marker(this,marker,status)
    call marker%pick("modify_pdfs",this%modify_pdfs,status)
    call marker%pick("initialized",this%initialized,status)
    call marker%pick("initial_interaction_given",this%initial_interaction_given,status)
    call marker%pick("finished",this%finished,status)
    call marker%pick("init_time",this%init_time,status)
    call marker%pick("pt_time",this%pt_time,status)
    call marker%pick("partons_time",this%partons_time,status)
    call marker%pick("confirm_time",this%confirm_time,status)
    call marker%pick_instance("dsigma",this%dsigma,status=status)
    call marker%pick_instance("samples",this%samples,status=status)
    call marker%pick_instance("beam",this%beam,status=status)
    call marker%pick_end("muli_type",status)
  end subroutine muli_read_from_marker
muli print to unit \
  subroutine muli_print_to_unit(this,unit,parents,components,peers)
    class(muli_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    if(parents>0)call qcd_2_2_print_to_unit(this,unit,parents-1,components,peers)
    write(unit,fmt="(a)")"Components of muli_type :"
    write(unit,'("Model Parameters:")')
    write(unit,'("GeV2_scale_cutoff : ",E20.10)')this%GeV2_scale_cutoff
```

```
write(unit,'("Modify PDF
                                    : ",L1)')this%modify_pdfs
    write(unit,'("PT Chain Status:")')
    write(unit,'("Initialized
                                    : ",L1)')this%initialized
    write(unit,'("initial_interaction_given: ",L1)')this%initial_interaction_given
   write(unit,'("Finished
                                    : ",L1)')this%finished
    write(unit,'("Exceeded
                                    : ",L1)')this%exceeded
    write(unit,'("Generator Internals:")')
    write(unit,'("Mean Value
                                    : ",E20.10)')this%mean
    if(components>zero)then
       write(unit,'("Start Integrals
                                      : ",16(E20.10))')this%start_integrals(1:16)
       write(unit, '("dsigma Component:")')
       call this%dsigma%print_to_unit(unit, parents, components-1, peers)
       write(unit,'("samples Component:")')
       call this%samples%print_to_unit(unit,parents,components-1,peers)
       write(unit, '("beam Component:")')
       call this%beam%print_to_unit(unit, parents, components-1, peers)
    else
       write(unit, '("Skipping Derived-Type Components.")')
    end if
 end subroutine muli_print_to_unit
muli get type ↑
 pure subroutine muli_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="muli_type")
 end subroutine muli_get_type
```

#### Originäre muli type Methoden

```
muli apply initial interaction \( \ \)
```

MulI kann die härteste Wechselwirkung selbst generieren oder eine bereits generiete Wechselwirkung auf die Remnants übertragen. Mit dieser Methode wird eine extern (üblicherweise durch WHIZARD) generierte Wechselwirkung übertragen.

Vor jedem Aufruf dieser Methode muss \*this\* durch muli\_initialize initialisiert werden. Es sollten zwischen der Initialisierung und diesem Aufruf keine Wechselwirkungen generiert werden.

```
gev2_s invariante Masse des hadronischen Systems vor der Wechselwirkung in GeV² x1 longitudinaler Impulsanteil des ersten Partons x2 longitudinaler Impulsanteil des zweiten Partons pdg_f1 Flavor des ersten Partons im PDG-Schema pdg_f2 Flavor des zweiten Partons im PDG-Schema n1 Ordnungszahl des ersten Partons n2 Ordnungszahl des zweiten Partons subroutine muli_apply_initial_interaction(this,& gev2_s,& x1,& x2,& pdg_f1,&
```

```
pdg_f2,&
      n1,&
      n2)
    class(muli_type),intent(inout)::this
   real(kind=double),intent(in)::Gev2_s,x1,x2
   integer,intent(in)::pdg_f1,pdg_f2,n1,n2
   real(kind=double)::rnd1,rnd2,time
    if(this%initialized)then
       !Timer Start für Benchmarkzwecke.
      call cpu_time(time)
      this%init_time=this%init_time-time
       !Einige Informationen für Debuggingzwecke.
      print *,"muli_apply_initial_interaction:"
      print *,"gev2_s=",gev2_s
      print *,"x1=",x1
      print *,"x2=",x2
      print *,"pdg_f1=",pdg_f1
      print *,"pdg_f2=",pdg_f2
      print *,"n1=",n1
      print *,"n2=",n2
!Aufgrund eines Bugs in gfortran 4.6 konnte ich die tao_state variable nicht an
!andere Module weitergeben und habe stattdessen vorgenerierte Zufallszahlen weitergegeben.
      call tao_random_number(this%tao_rnd,rnd1)
      call tao_random_number(this%tao_rnd,rnd2)
       !Timer Stop für Benchmarkzwecke.
      call cpu_time(time)
      this%init_time=this%init_time+time
       !Die nächste Zeile ist der eigentliche Aufruf für das Anpassen der Remnants.
       !Alles andere in dieser Methode ist Wrapper-Overhead.
```



Muli hat  $p_{\perp}$  als Ordnungsparameter, WHIZARD generiert diese Valiable aber nicht.  $p_{\perp}$  lässt sich auch nicht eindeutig aus den generierten Variablen ermitteln. Es ließe sich bestenfalls eine Verteilung von  $p_{\perp}$  in Abhängigkeit der bekannten Variablen angeben. Hier verwenden wir einen einfacheren Weg und setzen die Obere Schranke  $p_{\perp} \leq \hat{s}/4 = sx_1x_2/4$  für  $p_{\perp}$  ein.

Diese Methode initialisiert eine Instanz vom Typ muli type.

```
\begin{tabular}{lll} GeV2\_scale\_cutoff & Skala in GeV^2, bei der der Algorithmus beendet wird. \\ & GeV2\_s & invariante Masse des hadronischen Systems in GeV^2 \\ & muli\_dir & vollständiger Unix-Pfad zu dem Verzeichnis, in dem MulI-Daten liegen. \\ & random seed & \begin{tabular}{lll} FeV^2 & F
```

Diese Methode sollte für jede Instanz nur einmal aufgerufen werden. Der Hauptzweck ist, den Monte-Carlo-Generator zu initialisieren, nicht etwa die Remnants zu initialisieren. Da hierfür einige Zeiger allociert werden, ist es ratsam, die Instanz mit muli\_finalize aufzuräumen, wenn man sie nicht mehr benötigt.



```
subroutine muli_initialize(this,&
     GeV2_scale_cutoff,&
     gev2_s,&
    muli_dir,&
     random_seed)
  class(muli_type),intent(out)::this
  real(kind=double),intent(in)::gev2_s,GeV2_scale_cutoff
  character(*),intent(in)::muli_dir
  integer,intent(in),optional::random_seed
  real(kind=double)::time
  logical::exist
  type(muli_dsigma_type)::dsigma_aq
  character(3)::lhapdf_member_c
  !Timer Start für Benchmarkzwecke.
  call cpu_time(time)
  this%init_time=this%init_time-time
  !Einige Informationen für Debuggingzwecke.
  print *,"muli_initialize: The MULI modules are still not fully populated, so MULI might &
       &generate some dummy values instead of real Monte Carlo generated interactions."
  print *,"Given Parameters:"
  print *,"GeV2_scale_cutoff=",GeV2_scale_cutoff
  print *,"muli_dir=",muli_dir
  print *,"lhapdf_dir=",""
  print *,"lhapdf_file=",muli_default_lhapdf_file
  print *,"lhapdf_member=",muli_default_lhapdf_member
  print *,""
  !\,p_{\perp} wird auf die invariante Masse normiert.
  call transversal_momentum_initialize(this,gev2_s)
  !Die Remnants werden initialisiert.
  call this % beam % initialize (&
       muli_dir,&
       lhapdf_dir="",&
       lhapdf_file=muli_default_lhapdf_file,&
       lhapdf_member=muli_default_lhapdf_member)
  this%GeV2_scale_cutoff=GeV2_scale_cutoff
  if(present(random_seed))then
     call tao_random_create(this%tao_rnd,random_seed)
  else
     call tao_random_create(this%tao_rnd,1)
  end if
```

!Wir durchsuchen muli\_dir nach vorgenerierten hadronischen Wirkungsquerschnitten.

!Dafür wird eine Zeichenkette generiert, die den Namen der LHAPDF-Datei enthält. !Zusätzlich wird aus der lhapdf\_member Variable eine Zeichenkette lhapdf\_member\_c !generiert, denn in jeder xml-Datei können mehrere Wirkungsquerschnitte für !verschiedene lhapdf\_member liegen.



Ich habe noch nie mehrere Member in einer Datei verwendet. Höchstwahrscheinlich funktioniert es dann auch nicht.

```
print *,"looking for previously generated root function..."
   call integer_with_leading_zeros(muli_default_lhapdf_member,3,lhapdf_member_c)
    inquire(file=muli_dir//"/dsigma_"//muli_default_lhapdf_file//".xml",exist=exist)
    if(exist)then
!Wir haben eine xml Datei zu der richtigen LHAPDF-Datei gefunden. Jetzt
!deserialisieren wir die Wirkungsquerschnitte zu dem gewünschten lhapdf_member.
      print *,"found. Starting deserialization..."
      call this%dsigma%deserialize(&
           name="dsigma_"//muli_default_lhapdf_file//"_"//lhapdf_member_c,&
           file=muli_dir//"/dsigma_"//muli_default_lhapdf_file//".xml")
      print *,"done. Starting generation of plots..."
!Einige Plots für Debuggingzwecke.
      call this%dsigma%gnuplot(muli_dir)
      print *,"done."
    else
!Es wurden keine passenden hadronischen Wirkungsquerschnitte gefunden. Es werden
!welche generiert und in muli_dir geschrieben. dsigma_aq ist nur für die Generierung
!der Wirkungsquerschnitte relevant, aber nicht für die Generierung der Ereignisse.
!dsigma_aq wird nur zu Debugging-Zwecken in muli_dir geschrieben. Die Serialisierung
!von dsigma_aq kann also jederzeit gefahrlos herausgenommen werden.
      print *, "No root function found. Starting generation of root function..."
      call dsigma_aq%generate(GeV2_scale_cutoff,gev2_s,this%dsigma)
      print *,"done. Starting serialization of root function..."
      call this%dsigma%serialize(&
           name="dsigma_"//muli_default_lhapdf_file//"_"//lhapdf_member_c,&
           file=muli_dir//"/dsigma_"//muli_default_lhapdf_file//".xml")
      print *,"done. Starting serialization of generator..."
      call dsigma_aq%serialize(&
           name="dsigma_aq_"//muli_default_lhapdf_file//"_"//lhapdf_member_c,&
           file=muli_dir//"/dsigma_aq_"//muli_default_lhapdf_file//".xml")
      print *,"done. Starting generation of plots..."
      call this%dsigma%gnuplot(muli_dir)
      print *,"done."
   end if
!Es wird noch nach Daten für das Importance-Sampling gesucht. Ohne diese kann MulI
!in seltenen Fällen unendlich langsam werden, wörtlich!
   print *,""
   print *,"looking for previously generated samples..."
   inquire(file=muli_dir//"/samples.xml",exist=exist)
   if(exist)then
      print *,"found. Starting deserialization..."
      call this%samples%deserialize("samples", muli_dir//"/samples.xml")
    else
```

```
print *, "No samples found. Starting with default initialization."
       call this%samples%initialize(4,int_sizes_all,int_all,1D-2)
    end if
    !Jetzt wird MulI startklar gemacht.
    call this%restart()
    this%initialized=.true.
    !Timer Stopp für Benchmarkzwecke.
    call cpu_time(time)
    this%init_time=this%init_time+time
  end subroutine muli initialize
muli finalize ↑
  subroutine muli_finalize(this)
    class(muli_type),intent(inout)::this
    print *,"muli_finalize"
    nullify(this%node)
    call this%dsigma%finalize()
    call this%samples%finalize()
    call this%beam%finalize()
  end subroutine muli_finalize
muli stop trainer \
```

Trainer ist ein Bertiebsmodus von MulI, in dem das Importance-Sampling in jedem Schritt verfeinert wird. Das Sampling ist darauf optimiert, dass es schnell (also mit wenigen Ereignissen) den MCG beschleunigt, aber nicht darauf optimiert, bei vielen Daten den MCG perfekt zu beschleunigen. Deshalb konvergiert die Geschwindigkeit des MCG gegen eine Grenze und der Trainer-Modus kann abgestellt werden.

Das hat in der NAG Variante von MulI bereits funktioniert, allerdings musste ich für die gcc-Kompatiblität so tief in den Sampler eingreifen, dass ich ihn komplett neu geschrieben habe. Den Nicht-Trainer-Modus habe ich in der gcc-Version noch nicht umgesetzt, entsprechend ist diese Methode nur ein Dummy für ein nicht-vorhandenes Feature.



```
subroutine muli_stop_trainer(this)
    class(muli_type),intent(inout)::this
    print *,"muli_stop_trainer: DUMMY!"
    end subroutine muli_stop_trainer

muli_reset_timer \
    subroutine muli_reset_timer(this)
        class(muli_type),intent(inout)::this
        this%init_time=ODO
        this%pt_time=ODO
        this%partons_time=ODO
        this%confirm_time=ODO
    end subroutine muli_reset_timer

muli_restart \
    muli_restart \
```

Wenn mehrere Ereignisse (Ein Ereignis ist eine Hadron-Hadron-Streuung inklusive ISR und MPI) in einem Programmaufruf generiert werden sollen, dann ist diese Methode und eventuell muli apply initial interaction vor jedem neuen Ereignis aufzurufen, aber nicht muli initialize.

```
subroutine muli_restart(this)  {\tt class(muli\_type),intent(inout)::this} \\ {\tt !this\%node wird auf das letzte Blatt aus der Binärbaumdarstellung für die hadronischen} \\ {\tt !Wirkungsquerschnitte gesetzt. Es enthält dann die Wirkungsquerschnitte bei der Startskala} \\ {\tt !für } p_{\perp}. \\ {\tt call this\%dsigma\%get\_rightmost(this\%node)} \\ {\tt !Die Remnants werden zurückgesetzt.} \\ {\tt call this\%beam\%reset()} \\ \\ }
```

Offensichtlich ist der  $p_{\perp}$ -Generator jetzt noch nicht fertig, es können also weitere Werte für  $p_{\perp}$  generiert werden. Alle anderen Komponenten werden auf ungültige Werte gesetzt, damit das Programm tendentiell eher abstürtzt als mit willkürlichen Zahlen zu rechnen, falls etwas schiefgeht, wie z.B. eine Nachfrage nach der aktuellen Wechselwirkung, obwohl noch keine generiert wurde. start\_integrals ist widerum eine gültige Initialisierung, denn die Integrale von der aktuellen (= der maximalen) Skala bis zur maximalen Skala sind offensichtlich gleich Null.

```
this%finished=.false.
   this%process_id=-1
   this%integrand_id=-1
   this%momentum_fractions=[-1D0,-1D0,1D0]
   this%hyperbolic_fractions=[-1D0,-1D0,1D0]
   this%start_integrals=&
    end subroutine muli_restart
muli is initialized \( \ \)
  elemental function muli_is_initialized(this) result(res)
   logical::res
   class(muli_type),intent(in) :: this
   res=this%initialized
  end function muli_is_initialized
muli is initial interaction given \( \ \)
  elemental function muli_is_initial_interaction_given(this) result(res)
    logical::res
   class(muli_type),intent(in) :: this
   res=this%initial_interaction_given
  end function muli_is_initial_interaction_given
muli is finished \
  elemental function muli_is_finished(this) result(res)
    logical::res
   class(muli_type),intent(in) :: this
   res=this%finished
  end function muli_is_finished
```

```
Nur für Debugging-Zwecke
  subroutine muli_enable_remnant_pdf(this)
    class(muli_type),intent(inout)::this
    this%modify_pdfs=.true.
  end subroutine muli_enable_remnant_pdf
muli disable remnant pdf \( \ext{} \)
Nur für Debugging-Zwecke
  subroutine muli_disable_remnant_pdf(this)
    class(muli_type),intent(inout)::this
    this%modify_pdfs=.false.
  end subroutine muli_disable_remnant_pdf
muli generate gev2 pt2 \uparrow
Wrapper für die Generierung der nächsten Skala p_{\perp}, die eigentliche Arbeit wird in muli_{
m type}generate_{
m next}scale
gemacht. Diese Wrapper-Methode nimmt eine beliebige Start-Skala für p_{\perp} entgegen, liefert einen Kan-
didaten für p_{\perp} zurück und misst die Zeit, die die CPU dafür benötigt hat.
  subroutine muli_generate_gev2_pt2(this,gev2_start_scale,gev2_new_scale)
    class(muli_type),intent(inout)::this
    real(kind=double),intent(in)::gev2_start_scale
    real(kind=double),intent(out)::gev2_new_scale
    real(kind=double)::time
    !Timer Start für Benchmark-Zwecke
    call cpu_time(time)
    this%pt_time=this%pt_time-time
    !Die aktuelle Skala wird auf den angegebenen Wert gesetzt
    call this%set_gev2_scale(gev2_start_scale)
    !Mit muli_trapezium_type%approx_integral wird die Stammfunktionen \mathcal{S}\_lphaeta an
    !dieser Skala ausgewertet.
    this%start_integrals=this%node%approx_integral(this%get_unit_scale())
    !Eine neue Wechselwirkungsskala wird MC-generiert.
    call this%generate_next_scale()
    !Die neue Skala wird zurückgegeben.
    gev2_new_scale=this%get_gev2_scale()
    !Timer Stopp
    call cpu_time(time)
    this%pt_time=this%pt_time+time
  end subroutine muli_generate_gev2_pt2
muli generate flow \( \)
Generierung einer internen Darstellung eines Farbflussdiagramms für das aktuelle Feynmandiagramm.
  subroutine muli_generate_flow(this)
    class(muli_type),intent(inout)::this
    integer::rnd
    integer::m,n
    logical, dimension(3)::t
    integer,dimension(4)::tmp_flow
```

muli enable remnant pdf \( \ \)

```
!we initialize with zeros. a zero means no line ends here.
this%flow=[0,0,0,0]
!we randomly pick a color flow
call tao_random_number(this%tao_rnd,rnd)
!the third position of muli_flow_stats is the sum of all flow wheights of
!stratum diagram_kind. so we generate a random number 0 <= m < sum(weights)
m=modulo(rnd,muli_flow_stats(3,this%get_diagram_color_kind()))
!lets visit all color flows of stratum diagram_kind.
!the first and second position of muli_flow_stats
!tell us the index of the first and the last valid color flow.
do n=muli_flow_stats(1,this%get_diagram_color_kind()),&
muli_flow_stats(2,this%get_diagram_color_kind())
   !now we remove the weight of flow n from our random number.
  m=m-muli_flows(0,n)
   !this is how we pick a flow.
   if(m<0)then
      !the actual flow
      this%flow=muli_flows(1:4,n)
   end if
end do
!the diagram kind contains a primitive diagram and all diagramms which can
!be deriven by
!(1) global charge conjugation
!(2) permutation of the initial state particles
!(3) permutation of the final state particles
!lets see, what transformations we have got in our actual interaction.
t=muli_get_state_transformations(this%get_diagram_color_kind(),this%get_lha_flavors())
!now we have to apply these transformations to our flow.
!(1) means: swap beginning and end of a line. flow is a permutation that maps
!ends to their beginnings, so we apply flow to itself:
if(t(1))then
   tmp_flow=this%flow
   this%flow=[0,0,0,0]
   do n=1,4
      if(tmp_flow(n)>0)this%flow(tmp_flow(n))=n
   end do
end if
if(t(2))then
   !we swap the particles 1 and 2
   tmp_flow(1)=this%flow(2)
   tmp_flow(2)=this%flow(1)
   tmp_flow(3:4)=this%flow(3:4)
   !we swap the beginnings assigned to particle 1 and 2
   where(tmp_flow==1)
      this%flow=2
   elsewhere(tmp_flow==2)
      this%flow=1
   elsewhere
      this%flow=tmp_flow
   end where
```

```
!we swap the particles 3 and 4
       tmp_flow(1:2)=this%flow(1:2)
       tmp_flow(3)=this%flow(4)
       tmp_flow(4)=this%flow(3)
       !we swap the beginnings assigned to particle 3 and 4
       where(tmp_flow==3)
          this%flow=4
       elsewhere(tmp_flow==4)
          this%flow=3
       elsewhere
          this%flow=tmp_flow
       end where
    end if
  end subroutine muli_generate_flow
muli generate partons \( \ \)
Generierung der Partonimpulsanteile [\xi_1, \xi_2] sowie der Partonflavor [a, b, c, d], siehe Abschnitt ??.
Im Wesentlichen ist dies ein Wrapper für sample inclusive type%mcgenerate hit und muli type%generate flow
n1, n2: Identifikationsnummern der Partonen. Das shower interface kümmert sich um die Durchnum-
merierung der Partonen, deswegen nimmt muli generate partons diese Nummern entgegen, statt sie
zu erzeugen.
x proton 1,x proton 2: Longitudinale Impulsanteile der Partonen, bezogen auf die ursprünglichen
Protonimpulse, nicht auf die aktuellen Remnantimpulse.
pdg_f1,pdg_f2,pdg_f3,pdg_f4: Die Flavor a,b,c,d der Partonen im PDG-Schema.
  subroutine muli_generate_partons(this,n1,n2,x_proton_1,x_proton_2,pdg_f1,pdg_f2,pdg_f3,pdg_f4)
    class(muli_type),intent(inout)::this
    integer, intent(in)::n1,n2
    real(kind=double),intent(out)::x_proton_1,x_proton_2
    integer,intent(out)::pdg_f1,pdg_f2,pdg_f3,pdg_f4
    integer,dimension(4)::pdg_f
    real(kind=double)::time
    !print *, "muli_generate_partons: n1=", n1, " n2=", n2
```

end if

if(t(3))then

this%parton\_ids(1)=n1
this%parton\_ids(2)=n2
call cpu\_time(time)

this%partons\_time=this%partons\_time-time

Mittels muli\_trapezium\_type%approx\_value\_n wird der Mittelwert  $\overline{S}_{\alpha\beta}$  ausgewertet. Anschließend werden mittels sample\_inclusive\_type%mcgenerate\_hit die Nummer  $process_id$  des Feynandiagramms und die Impulsanteile  $momentum_fractions$  der Partonen generiert.

```
this%tao_rnd,&
this%process_id,&
this%momentum_fractions)
```

Mittels muli\_type%generate\_flow wird ein Farbflussdiagramm generiert.

Wrapper für die eigentliche Routine pp remnant type%momentum pdf

```
call this%generate_flow()
```

Üblichwerweise (Wenn ich nicht debugge) werden die Remnante mittels pp\_remnant\_type%apply\_interaction die Remnants über die neue Wechselwirkung in Kenntnis gesetzt.

```
if(this%modify_pdfs)then
       call cpu_time(time)
       this%partons_time=this%partons_time+time
       this%confirm_time=this%confirm_time-time
       call this%beam%apply_interaction(this)
       call cpu_time(time)
       this%confirm_time=this%confirm_time+time
       this%partons_time=this%partons_time-time
    x_proton_1=this%momentum_fractions(1)
    x_proton_2=this%momentum_fractions(2)
    pdg_f=this%get_pdg_flavors()
    pdg_f1=pdg_f(1)
    pdg_f2=pdg_f(2)
    pdg_f3=pdg_f(3)
    pdg_f4=pdg_f(4)
    call cpu_time(time)
    this%partons_time=this%partons_time-time
    call qcd_2_2_print_to_unit(this,output_unit,100_dik,100_dik,100_dik)
  end subroutine muli_generate_partons
muli replace parton \( \ \)
Wrapper für die eigentliche Routine pp remnant type%replace parton
  subroutine muli_replace_parton(this,proton_id,old_id,new_id,pdg_f,x_proton,gev_scale)
    class(muli_type),intent(inout)::this
    integer,intent(in)::proton_id,old_id,new_id,pdg_f
    real(kind=double),intent(in)::x_proton,gev_scale
    !print *, "muli_replace_parton(", proton_id, old_id, new_id, pdg_f, x_proton, gev_scale, ")"
    if(proton_id==1.or.proton_id==2)then
       call this%beam%replace_parton(proton_id,old_id,new_id,pdg_f,x_proton,gev_scale)
    else
       print *,"muli_replace_parton: proton_id must be 1 or 2, but ",proton_id," was given."
    end if
  end subroutine muli_replace_parton
muli get momentum pdf †
```

```
function muli_get_momentum_pdf(this,x_proton,gev2_scale,n,pdg_f) result(pdf)
    real(kind=double)::pdf
    class(muli_type),intent(in)::this
    real(kind=double),intent(in)::x_proton,gev2_scale
    integer,intent(in)::n,pdg_f
    call this%beam%momentum_pdf(x_proton,gev2_scale,n,pdg_f,pdf)
  end function muli_get_momentum_pdf
muli get parton pdf \( \ \)
Wrapper für die eigentliche Routine pp remnant type%parton pdf
  function muli_get_parton_pdf(this,x_proton,gev2_scale,n,pdg_f) result(pdf)
    real(kind=double)::pdf
    class(muli_type),intent(in)::this
    real(kind=double),intent(in)::x_proton,gev2_scale
    integer,intent(in)::n,pdg_f
    call this%beam%parton_pdf(x_proton,gev2_scale,n,pdg_f,pdf)
  end function muli_get_parton_pdf
muli print timer \
  subroutine muli_print_timer(this)
    class(muli_type),intent(in) :: this
    print('("Init time:
                             ",E20.10)'),this%init_time
    print('("PT gen time: ",E20.10)'),this%pt_time
    print('("Partons time: ",E20.10)'),this%partons_time
    print('("Confirm time: ",E20.10)'),this%confirm_time
    print('("Overall time: ",E20.10)'),&
    this%init_time+this%pt_time+this%partons_time+this%confirm_time
  end subroutine muli_print_timer
muli generate next scale \( \ \)
Hier wird die nächste Wechselwirkungsskala h_3^{(n+1)} generiert. Für jedes Stratum \{\alpha, \beta\} wird die Unter-
funktion generate_single_pts aufgerufen, um einen Wert h_{3\alpha\beta}^{(n+1)} zu generieren. muli_generate_next_scale
setzt dann h_3^{(n+1)} = \max(h_{3\alpha\beta}^{(n+1)}). Intern werden normierte Skalen h_3 = \frac{4p_{\perp}}{s} =pts (pt normiert auf s)
verwendet.
  subroutine muli_generate_next_scale(this,integrand_kind)
    class(muli_type),intent(inout)::this
    integer,intent(in),optional::integrand_kind
    real(kind=double)::pts,tmp_pts,rnd
```

Das optionale Argument integrand\_kind wird nur für interne Testzwecke verwendet, man sollte es gefahrlos samt der nachfolgenden Konstruktion entfernen können. integrand\_kind ist ein Stratum  $\{\alpha, \beta\}$ , das vorgegeben werden kann.

```
if(present(integrand_kind))then
  call tao_random_number(this%tao_rnd,rnd)
  call generate_single_pts(&
```

class(muli\_trapezium\_node\_class),pointer::tmp\_node

integer::tmp\_int\_kind

pts=-1D0

```
integrand_kind,&
    this%start_integrals(integrand_kind),&
    this%beam%get_pdf_int_weights(double_pdf_kinds(1:2,integrand_kind)),&
    rnd,&
    this%dsigma,&
    pts,&
    this%node)
```

Das ist der vorgesehene Weg, hier werden alle Strati mit tmp\_int\_kind durchlaufen. mit pp\_remnant\_type%get\_pdf\_int\_weights werden die Wichtungsfaktoren  $[W_{\alpha}, W_{\beta}]$  angefordert. in muli interactions%double pdf kinds ist eine Abbildung  $[1..16] \rightarrow \{\alpha, \beta\}$  definiert.

Nach jedem Aufruf von generate\_single\_pts wird überprüft, ob tmp\_pts= $h_{3\alpha\beta}^{(n+1)}$  größer als der bisher größte Wert ist. Wenn ja, wird  $h_3^{(n+1)}=h_{3\alpha\beta}^{(n+1)}$  gesetzt.

generate\_single\_pts liefert  $h_{3\alpha\beta}=-1$  zurück, wenn  $p_{\perp\alpha\beta}< p_{\perp}^{\min}$ . Es reicht am Schluss also aus, wenn wir nachsehen, ob  $h_3>0$ . Wenn nicht, dann ist die Skala  $p_{\perp}$  am unteren Ende angekommen und es werden keine weiteren MPI generiert.

tmp\_node zeigt auf das Blatt der approximierten Wirkungsquerschnitte muli\_type%dsigma, das  $p_{\perp\alpha\beta}$  enthält. Dieses Blatt wird später noch benötigt, wenn aus dem hier generierten Kandidaten eine tatsächliche Wechselwirkung generiert wird.

```
do tmp_int_kind=1,16
          call tao_random_number(this%tao_rnd,rnd)
          call generate_single_pts(&
               tmp_int_kind,&
               this%start_integrals(tmp_int_kind),&
               this%beam%get_pdf_int_weights(double_pdf_kinds(1:2,tmp_int_kind)),&
               this%dsigma,&
               tmp_pts,&
               tmp_node)
          if(tmp_pts>pts)then
             pts=tmp_pts
             this%integrand_id=tmp_int_kind
             this%node=>tmp_node
          end if
       end do
   end if
   if(pts>0)then
       call this%set_unit_scale(pts)
   else
       this%finished=.true.
    end if
contains
```

Siehe Abschnitt ??, (??)-(??) mit weight  $\to W_{\alpha}W_{\beta}$ , rnd  $\to z$  und arg  $\to \zeta$ . Wenn  $W_{\alpha}W_{\beta} = 0$ , dann wird keine Skala generiert, weil mindestens einer der beiden beteiligte n Beiträge zur Strukturfunktion gleich Null ist.

Mit muli\_trapezium\_tree\_type%find\_decreasing wird muli\_type%dsigma nach dem Blatt durchsucht, dessen Bildmenge von  $S_{\alpha\beta}$  den Wert  $\zeta$  enthält. Wenn der Funktionswert l\_integral von  $S_{\alpha\beta}$ an der unteren Intervallgrenze kleiner als  $\zeta$  ist, dann liegt  $\zeta$  tatsächlich nicht in der Bildmenge von  $S_{\alpha\beta}$ . Damit ist klar, dass der gesuchte Wert von  $p_{\perp} < p_{\perp}^{\min}$  ist und das Ergebnis wird auf den Wert -1 gesetzt. Andernfalls wird mittels muli\_trapezium\_type%approx\_position\_by\_integral die Umkehrfunktion  $S_{\alpha\beta}^{-1}$  ausgewertet.

subroutine generate\_single\_pts(int\_kind,start\_int,weight,rnd,int\_tree,pts,node)

integer, intent(in)::int\_kind

real(kind=double),intent(in)::start\_int,weight,rnd

```
type(muli_trapezium_tree_type),intent(in)::int_tree
      real(kind=double),intent(out)::pts
      class(muli_trapezium_node_class),pointer,intent(out)::node
      real(kind=double)::arg
      if(weight>0D0)then
         arg=start_int-log(rnd)/weight
         call int_tree%find_decreasing(arg,int_kind,node)
         if(node%get_l_integral(int_kind)>arg)then
            pts=node%approx_position_by_integral(int_kind,arg)
         else
            pts=-1D0
         end if
      else
         pts=-1D0
      end if
    end subroutine generate_single_pts
  end subroutine muli_generate_next_scale
muli confirm \
Wird nur für Debuggingzwecke in Zusammenhang mit muli_type%generate samples verwendet.
  subroutine muli_confirm(this)
    class(muli_type),intent(inout) :: this
    this%mean=this%node%approx_value_n(this%get_unit_scale(),this%integrand_id)
    this%start_integrals=this%node%approx_integral(this%get_unit_scale())
  end subroutine muli_confirm
muli generate samples \( \)
Ein Generator für die Zerlegung des \{h_1, h_2, h_3\}-Einheitsquaders, siehe Abschnitt ??. Diese Methode
wird nur für Debugginzwecke verwendet.
  subroutine muli_generate_samples(this,n_total,n_print,integrand_kind,muli_dir,analyse)
    class(muli_type),intent(inout)::this
    integer(kind=dik),intent(in)::n_total,n_print
    integer, intent(in)::integrand_kind
    character(*),intent(in)::muli_dir
    logical, intent(in)::analyse
    integer(kind=dik)::n_inner
    class(muli_trapezium_node_class),pointer::start_node=>null()
    class(muli_trapezium_node_class),pointer,save::s_node=>null()
    class(muli_trapezium_node_class),pointer,save::node=>null()
```

```
character(2)::prefix
integer,save::t_slice,t_region,t_proc,t_subproc,t_max_n=0
integer(kind=dik)::n_t,n_p,n_m
integer::n,m,u,unit=0
integer(kind=dik)::n_tries=0
integer(kind=dik)::n_hits=0
integer(kind=dik)::n_over=0
integer(kind=dik)::n_miss=0
real(kind=double), save, dimension(3)::cart_hit
integer, save, dimension(4)::t_i_rnd
real(kind=double),dimension(16)::d_rnd
real(kind=double), save::t_area, t_dddsigma, t_rnd, t_weight, t_arg
real(kind=double)::mean=0D0
real(kind=double)::time=ODO
real(kind=double)::timepa=0D0
real(kind=double)::timept=0D0
real(kind=double)::timet=0D0
real(kind=double)::pts,s_pts=1D0
real(kind=double)::pts2=1D0
real(kind=double)::rnd
logical::running
character(3)::num
integer::success=-1
integer::chain_length=0
integer::int_kind
integer::process_id
real(kind=double),dimension(0:16)::integral
call this%print_parents()
n_tries=one
n_inner=n_total/n_print
n_t=zero
print:do while(n_t<n_total)</pre>
   call cpu_time(time)
   timet=-time
   n_p=zero
   inner:do while(n_p<n_print)</pre>
      chain_length=0
      call this%restart()
      this%integrand_id=integrand_kind
      call cpu_time(time)
      timept=timept-time
      call this%generate_next_scale(integrand_kind)
      call cpu_time(time)
      timept=timept+time
      chain:do while(.not.this%is_finished())
         chain_length=chain_length+1
         n_p=n_p+1
         call this%confirm()
         call cpu_time(time)
         timepa=timepa-time
```

```
!
                           print *,this%get_unit2_scale()
             call sample_inclusive_mcgenerate_hit(&
                  this%samples,&
                  this%get_unit2_scale(),&
                  this%mean,&
                  this%integrand_id,&
                  this%tao_rnd,&
                  this%process_id,&
                  this%momentum_fractions)
             call cpu_time(time)
             timepa=timepa+time
             timept=timept-time
             call this%generate_next_scale(integrand_kind)
             call cpu_time(time)
             timept=timept+time
          end do chain
       end do inner
       n_t=n_t+n_p
       call this%samples%sum_up()
       call cpu_time(time)
       timet=timet+time
       print *,n_t,"/",n_total
       print *,"time: ",timet
       print *,"pt time: ",timept
       print *,"pa time: ",timepa
       print *,this%samples%n_tries_sum,this%samples%n_hits_sum,this%samples%n_over_sum
       if(this%samples%n_hits_sum>0)then
          print *,(this%samples%n_hits_sum*10000)/this%samples%n_tries_sum,&
               (this%samples%n_over_sum*10000)/this%samples%n_hits_sum
       else
          print *,"no hits"
       end if
    end do print
    call integer_with_leading_zeros(integrand_kind,2,prefix)
    if(analyse)then
       call this%samples%int_kinds(integrand_kind)%analyse(muli_dir,prefix//"_")
       call this%samples%int_kinds(integrand_kind)%serialize(&
            "sample_int_kind_"//prefix,&
            muli_dir//"/sample_int_kind/"//prefix//".xml")
    end if
    call this%samples%int_kinds(integrand_kind)%serialize(&
         "sample_int_kind_"//prefix,&
         muli_dir//"/sample_int_kind/"//prefix//".xml")
  end subroutine muli_generate_samples
muli fake interaction \( \ \)
Wird ebenfalls zu Debuggingzwecken verwendet. So können Wechselwirkungen ohne Verwendung von
WHIZARD oder das shower interface auf die Remnants übertragen werden.
```

```
real(kind=double),intent(in)::Gev2_scale,x1,x2
    integer,intent(in)::process_id,integrand_id,n1,n2
    integer,dimension(4),intent(in),optional::flow
    call this%set_gev2_scale(Gev2_scale)
    this%process_id=process_id
    this%integrand_id=integrand_id
    this%parton_ids=[n1,n2]
    if(present(flow))then
       this%flow=flow
    else
       this%flow=[0,0,0,0]
    end if
    this%momentum_fractions=[x1,x2,this%get_unit2_scale()]
    call this%beam%apply_interaction(this)
    call this%beam%print_all()
  end subroutine muli_fake_interaction
end module muli
```

# 4 Modul muli momentum

# 4.1 Abhängigkeiten

use muli\_basic

# 4.2 Derived Types

## 4.2.1 transversal momentum type

Dieser Datentyp abstrahiert den Entwicklungsparameter  $p_{\perp}$ . Intern wird  $p_{\perp}$  durch die Komponente momentum dargestellt. Dieser enthält die fünf Einträge  $\left[s,\sqrt{p_{\perp}},p_{\perp},\sqrt{4*p_{\perp}/s},4*p_{\perp}/s\right]$ . Für jeden Eintrag werden get und set Methoden bereitgestellt. Wenn statt eines Werts von  $p_{\perp}$  eine Instanz vom Typ transversal\_momentum\_type übergeben wird, werden Fehler durch falsche Einheiten vermieden.

Nach Mull-Konvention wird die Einheit immer vor den Namen der Variable gestellt, also GeV\_scale für  $\sqrt{p_{\perp}}$  und GeV2\_scale für  $p_{\perp}$  usw. Hier wird bei dimensionslosen Größen  $\sim \sqrt{p_{\perp}}$  das Prefix unit und bei dimensionslosen Größen  $\sim p_{\perp}$  das prefix unit2 vorangestellt, damit immer klar ist, was gemeint ist.

MaxScale ist der größtmögliche Wert für  $p_{\perp}$ , mit  $p_{\parallel}^{\max} = s/2$ .

Die invariante Masse s wird hier initial\_cme genannt. Letzteres ist die invariante Masse des Proton-Proton-Systems vor der ersten (WHIZARD) Wechselwirkung. Das spiegelt die Tatsache wider, dass dynamische Energieen der Remnants noch nicht implementiert sind. Dieser Datentyp ist der richtige Ort, um die aktuelle CME zu speichern. Da alle anderen Module auf die get-Methoden dieses Moduls zurückgreifen, sollte es ausreichen, die interne Darstellung hier anzupassen.



```
implicit none
  type,extends(serializable_class)::transversal_momentum_type
    private
    real(kind=drk),dimension(0:4)::momentum=[0D0,0D0,0D0,0D0,0D0]
contains
   !Überschriebene serializable_class Methoden
    procedure,public::write_to_marker=>transversal_momentum_write_to_marker
    procedure,public::read_from_marker=>transversal_momentum_read_from_marker
    procedure,public::print_to_unit=>transversal_momentum_print_to_unit
    procedure,public,nopass::get_type=>transversal_momentum_get_type
    !Originäre transversal_momentum_type Methodentransversal_momentum_type
    procedure,public::get_gev_initial_cme=>transversal_momentum_get_gev_initial_cme
    procedure,public::get_gev_max_scale=>transversal_momentum_get_gev_max_scale
    procedure,public::get_gev2_max_scale=>transversal_momentum_get_gev2_max_scale
    procedure,public::get_gev_scale=>transversal_momentum_get_gev_scale
```

```
procedure,public::get_gev2_scale=>transversal_momentum_get_gev2_scale
procedure,public::get_unit_scale=>transversal_momentum_get_unit_scale
procedure,public::get_unit2_scale=>transversal_momentum_get_unit2_scale
procedure,public::set_gev_initial_cme=>transversal_momentum_set_gev_initial_cme
procedure,public::set_gev_max_scale=>transversal_momentum_set_gev_max_scale
procedure,public::set_gev2_max_scale=>transversal_momentum_set_gev2_max_scale
procedure,public::set_gev_scale=>transversal_momentum_set_gev2_scale
procedure,public::set_gev2_scale=>transversal_momentum_set_gev2_scale
procedure,public::set_unit_scale=>transversal_momentum_set_unit_scale
procedure,public::set_unit2_scale=>transversal_momentum_set_unit2_scale
procedure,public::transversal_momentum_initialize
generic,public::initialize=>transversal_momentum_initialize
end type transversal_momentum_type
```

## 4.2.2 qcd\_2\_2\_class

Abstrakte Klasse, die eine QCD-2→2-Wechselwirkung abstrahiert. pp\_remnant\_type greift auf Eigenschaften einer solchen Wechselwirkung zurück, allerdings werden die Methoden in dem Modul muli implementiert, auf das muli\_remnant keinen Zugriff hat. Zwar könnte man dieses Problem durch eine andere Hierarchie von Modulen lösen, aber ich nehme an, dass dieses Problem wieder auftaucht, wenn die Remnants als WHIZARD-Strukturfunktionen implementiert werden. Deswegen habe ich diese Lösung gewählt.

```
type,Extendstransversal_momentum_type,abstract::qcd_2_2_class
contains
  procedure(qcd_get_int),deferred::get_process_id
  procedure(qcd_get_int),deferred::get_integrand_id
  procedure(qcd_get_int),deferred::get_diagram_kind
  procedure(qcd_get_int_4),deferred::get_lha_flavors
  procedure(qcd_get_int_4),deferred::get_pdg_flavors
  procedure(qcd_get_int_by_int),deferred::get_parton_id
  procedure(qcd_get_int_2),deferred::get_parton_kinds
  procedure(qcd_get_int_2),deferred::get_pdf_int_kinds
  procedure(qcd_get_drk),deferred::get_momentum_boost
  procedure(qcd_get_drk_2),deferred::get_remnant_momentum_fractions
  procedure(qcd_get_drk_2),deferred::get_total_momentum_fractions
end type qcd_2_2_class
```

#### 4.3 Interfaces

```
abstract interface
subroutine qcd_none(this)
  import qcd_2_2_class
  class(qcd_2_2_class),target,intent(in)::this
end subroutine qcd_none
elemental function qcd_get_drk(this)
  use muli_basic, only: drk
  import qcd_2_2_class
  class(qcd_2_2_class),intent(in)::this
```

```
real(kind=drk)::qcd_get_drk
   end function qcd_get_drk
  pure function qcd_get_drk_2(this)
     use muli_basic, only: drk
     import qcd_2_2_class
     class(qcd_2_2_class),intent(in)::this
     real(kind=drk),dimension(2)::qcd_get_drk_2
   end function qcd_get_drk_2
   pure function qcd_get_drk_3(this)
     use muli_basic, only: drk
     import qcd_2_2_class
     class(qcd_2_2_class),intent(in)::this
     real(kind=drk),dimension(3)::qcd_get_drk_3
   end function qcd_get_drk_3
   elemental function qcd_get_int(this)
     use muli_basic, only: drk
     import qcd_2_2_class
     class(qcd_2_2_class),intent(in)::this
     integer::qcd_get_int
   end function qcd_get_int
   elemental function qcd_get_int_by_int(this,n)
     use muli_basic, only: drk
     import qcd_2_2_class
     class(qcd_2_2_class),intent(in)::this
     integer,intent(in)::n
     integer::qcd_get_int_by_int
   end function qcd_get_int_by_int
   pure function qcd_get_int_2(this)
     use muli_basic, only: drk
     import qcd_2_2_class
     class(qcd_2_2_class),intent(in)::this
     integer,dimension(2)::qcd_get_int_2
   end function qcd_get_int_2
  pure function qcd_get_int_4(this)
     use muli_basic, only: drk
     import qcd_2_2_class
     class(qcd_2_2_class),intent(in)::this
     integer,dimension(4)::qcd_get_int_4
   end function qcd_get_int_4
end interface
```

# 4.4 Implementierung der Prozeduren

#### 4.4.1 Methoden für transversal momentum type

Überschriebene serializable\_class Methoden

```
transversal momentum write to marker \( \)
```

```
subroutine transversal_momentum_write_to_marker(this,marker,status)
    class(transversal_momentum_type),intent(in)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("transversal_momentum_type")
    call marker%mark("gev_momenta",this%momentum(0:1))
    call marker%mark_end("transversal_momentum_type")
  end subroutine transversal_momentum_write_to_marker
transversal momentum read from marker \( \)
  subroutine transversal_momentum_read_from_marker(this,marker,status)
    class(transversal_momentum_type),intent(out)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("transversal_momentum_type",status=status)
    call marker%pick("gev_momenta",this%momentum(0:1),status)
    this%momentum(2:4)=[\&
         this%momentum(1)**2,&
         this%momentum(1)/this%momentum(0),&
         (this%momentum(1)/this%momentum(0))**2]
    call marker%pick_end("transversal_momentum_type", status=status)
  end subroutine transversal_momentum_read_from_marker
transversal momentum print to unit \( \ \)
  subroutine transversal_momentum_print_to_unit(this,unit,parents,components,peers)
    class(transversal_momentum_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    write(unit, '("Components of transversal_momentum_type:")')
    write(unit,fmt='("Actual energy scale:")')
    write(unit,fmt='("Max scale (MeV) :",E20.10)')this%momentum(0)
    write(unit,fmt='("Scale (MeV)
                                       :",E20.10)')this%momentum(1)
    write(unit,fmt='("Scale^2 (MeV^2) :",E20.10)')this%momentum(2)
    write(unit,fmt='("Scale normalized :",E20.10)')this%momentum(3)
    write(unit,fmt='("Scale^2 normalized:",E20.10)')this%momentum(4)
  end subroutine transversal_momentum_print_to_unit
transversal momentum get type †
  pure subroutine transversal_momentum_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="transversal_momentum_type")
  end subroutine transversal_momentum_get_type
Originäre transversal momentum type Methoden
transversal momentum get gev initial cme \( \)
```

```
elemental function transversal_momentum_get_gev_initial_cme(this) result(scale)
    class(transversal_momentum_type),intent(in)::this
    real(kind=drk)::scale
    scale=this%momentum(0)*2D0
  end function transversal_momentum_get_gev_initial_cme
transversal momentum get gev max scale ↑
transversal momentum get gev max scale ↑
  elemental function transversal_momentum_get_gev_max_scale(this) result(scale)
    class(transversal_momentum_type),intent(in)::this
    real(kind=drk)::scale
    scale=this%momentum(0)
  end function transversal_momentum_get_gev_max_scale
transversal momentum get gev2 max scale \( \ \)
  elemental function transversal_momentum_get_gev2_max_scale(this) result(scale)
    class(transversal_momentum_type),intent(in)::this
    real(kind=drk)::scale
    scale=this%momentum(0)**2
  end function transversal_momentum_get_gev2_max_scale
transversal momentum get gev scale †
  elemental function transversal_momentum_get_gev_scale(this) result(scale)
    class(transversal_momentum_type),intent(in)::this
    real(kind=drk)::scale
    scale=this%momentum(1)
  end function transversal_momentum_get_gev_scale
transversal momentum get gev2 scale ↑
  elemental function transversal_momentum_get_gev2_scale(this) result(scale)
    class(transversal_momentum_type),intent(in)::this
    real(kind=drk)::scale
    scale=this%momentum(2)
  end function transversal_momentum_get_gev2_scale
transversal momentum get unit scale ↑
  elemental function transversal_momentum_get_unit_scale(this) result(scale)
    class(transversal_momentum_type),intent(in)::this
    real(kind=drk)::scale
    scale=this%momentum(3)
  end function transversal_momentum_get_unit_scale
transversal momentum get unit2 scale \( \ \)
  elemental function transversal_momentum_get_unit2_scale(this) result(scale)
    class(transversal_momentum_type),intent(in)::this
    real(kind=drk)::scale
    scale=this%momentum(4)
  end function transversal_momentum_get_unit2_scale
```

```
transversal momentum set gev initial cme \( \)
  subroutine transversal_momentum_set_gev_initial_cme(this,new_gev_initial_cme)
    class(transversal_momentum_type),intent(inout)::this
    real(kind=drk),intent(in) :: new_gev_initial_cme
    this%momentum(0) = new_gev_initial_cme/2D0
    this%momentum(3) = this%momentum(1)/this%momentum(0)
    this%momentum(4) = this%momentum(3)**2
  end subroutine transversal_momentum_set_gev_initial_cme
transversal momentum set gev max scale↑
  subroutine transversal_momentum_set_gev_max_scale(this,new_gev_max_scale)
    class(transversal_momentum_type),intent(inout)::this
    real(kind=drk),intent(in) :: new_gev_max_scale
    this%momentum(0) = new_gev_max_scale
    this%momentum(3) = this%momentum(1)/this%momentum(0)
    this%momentum(4) = this%momentum(3)**2
  end subroutine transversal_momentum_set_gev_max_scale
transversal momentum set gev2 max scale ↑
  subroutine transversal_momentum_set_gev2_max_scale(this,new_gev2_max_scale)
    class(transversal_momentum_type),intent(inout)::this
    real(kind=drk),intent(in) :: new_gev2_max_scale
    this%momentum(0) = sqrt(new_gev2_max_scale)
    this%momentum(3) = this%momentum(1)/this%momentum(0)
    this%momentum(4) = this%momentum(3)**2
  end subroutine transversal_momentum_set_gev2_max_scale
transversal momentum set gev scale↑
  subroutine transversal_momentum_set_gev_scale(this,new_gev_scale)
    class(transversal_momentum_type),intent(inout)::this
    real(kind=drk),intent(in) :: new_gev_scale
    this%momentum(1) = new_gev_scale
    this%momentum(2) = new_gev_scale**2
    this%momentum(3) = new_gev_scale/this%momentum(0)
    this%momentum(4) = this%momentum(3)**2
  end subroutine transversal_momentum_set_gev_scale
transversal momentum set gev2 scale ↑
  subroutine transversal_momentum_set_gev2_scale(this,new_gev2_scale)
    class(transversal_momentum_type),intent(inout)::this
    real(kind=drk),intent(in) :: new_gev2_scale
    this%momentum(1) = sqrt(new_gev2_scale)
    this%momentum(2) = new_gev2_scale
    this%momentum(3) = this%momentum(1)/this%momentum(0)
    this%momentum(4) = this%momentum(3)**2
  end subroutine transversal_momentum_set_gev2_scale
transversal momentum set unit scale \( \)
```

```
subroutine transversal_momentum_set_unit_scale(this,new_unit_scale)
    class(transversal_momentum_type),intent(inout)::this
    real(kind=drk),intent(in) :: new_unit_scale
    this%momentum(1) = new_unit_scale*this%momentum(0)
    this%momentum(2) = this%momentum(1)**2
    this%momentum(3) = new_unit_scale
    this%momentum(4) = this%momentum(3)**2
  end subroutine transversal_momentum_set_unit_scale
{
m transversal} {
m momentum} {
m set} {
m unit2} {
m scale} \uparrow
  subroutine transversal_momentum_set_unit2_scale(this,new_unit2_scale)
    class(transversal_momentum_type),intent(inout)::this
    real(kind=drk),intent(in) :: new_unit2_scale
    this%momentum(3) = sqrt(new_unit2_scale)
    this%momentum(4) = new_unit2_scale
    this%momentum(1) = this%momentum(3)*this%momentum(0)
    this%momentum(2) = this%momentum(1)**2
  end subroutine transversal_momentum_set_unit2_scale
transversal momentum initialize \( \)
 subroutine transversal_momentum_initialize(this,gev2_s)
    class(transversal_momentum_type),intent(out)::this
    real(kind=drk),intent(in)::gev2_s
    real(kind=drk)::gev_s
    gev_s=sqrt(gev2_s)
    this%momentum=[gev_s/2D0,gev_s/2D0,gev2_s/4D0,1D0,1D0]
  end subroutine transversal_momentum_initialize
```

4 Modul muli\_momentum

# 5 Modul muli remnant

# 5.1 Allgemeines

#### 5.1.1 Zweck

Das Modul muli\_remnant enthält die vollständige Beschreibung der Remnants. Bislang sind die ursprünglichen Hadronen fest auf Protonen implementiert, allerdings sind Verallgemeinerungen auf größere Klassen teilweise vorbereitet.

#### 5.1.2 Voraussetzungen

Nicht in diesem Modul enthalten sind:

• Die ursprünglichen Strukturfunktionen der ungestörten Hadronen

Diese werden für die Definition der Remnant-PDFs verwendet. Verschiedene PDF-Sets können daher auch zu verschiedene Remnant-PDFs führen. Im Moment werden die LHAPDF-Bibliotheken verwendet. muli\_remnant verlässt sich darauf, dass diese bereits initialisiert sind und initialisiert sie nicht selbst.

In pp\_remnant\_type%initialize werden zwar alle notwendigen LHAPDF Informationen, also Unix-Verzeichnis, Dateiname und Member, entgegengenommen. Diese werden aber nur verwendet, um die passenden integrierten PDFs pp\_remnant\_type%pdf\_norm\_zu\_deserialisieren.

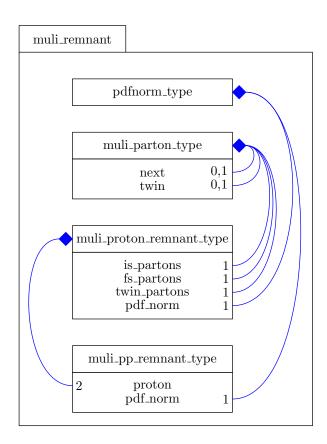
Es wird das Modul pdf builtin eingebunden, aber im aktuellen Status nicht verwendet.

• muli interactions

#### 5.1.3 Schnittstelle

Die meisten Typen und Prozeduren in diesem Modul sind nur für interne Zwecke vorgesehen. Der erweiterte Datentyp muli\_pp\_remnant\_type wurde eigens implementiert, um als Schnittstelle nach außen zu dienen. Er enthält zwei Instanzen vom Typ muli\_proton\_remnant\_type und abstrahiert auf diese Weise die einzelnen Hadron-Remnants. Deshalb sollte es auch ohne Änderung der Schnittstelle möglich sein, andere Hadron-Remnants zu realisieren. muli\_pp\_remnant\_type enthält Wrapper-Methoden für alle momentan benötigten Informationen. Von muli\_type werden verwendet:

- pp remnant type%initialize
- pp remnant type%finalize
- pp remnant type%reset
- pp remnant type%replace parton
- pp remnant type%apply interaction



- pp remnant type%apply initial interaction
- pp\_remnant\_type%momentum\_pdf
- pp\_remnant\_type%parton\_pdf
- pp\_remnant\_type%get\_pdf\_int\_weights

Zusammen mit den überladenen Standardmethoden der Klasse serializable\_class

- pp remnant type%write to marker
- pp remnant type%read from marker
- pp remnant type%print to unit
- pp remnant type%get type

ergeben diese Methoden eine vollständige Schnittstelle für die Remnants. Konsequenterweise sollten alle Modul-Komponenten, alle Modul-Prozeduren und alle bis auf die erwähnten Type-Bound-Prozeduren als privat deklariert werden. Derzeit sind die Prozeduren nur deshalb public, um das Debugging zu erleichtern.

#### 5.1.4 Datentypen

Alle Datentypen sind Erweiterungen von serializable  $\_$  class.

#### • pdfnorm type:

Für die Berechnung der Wichtungsfaktoren  $W_k$  für die einzelnen Beiträge  $f_k(x,\mu_F)$  zur Remnant-Strukturfunktion ist nicht die volle Information  $f_k(x,\mu_F)$  notwendig. Es reicht aus, den Impulsmittelwert  $\langle f_k(\mu_F) \rangle = \int_{x=x_0}^1 x f_k(x,\mu_F)$  zu kennen. pdfnorm\_type liefert eben diesen Impulsmittelwert. Außerdem enthält pdfnorm\_type die Summe über alle Impulsmittelwerte. Idealerweise sollte diese Summe geich Eins sein. Damit aber Abweichungen von Eins die Summenregel (??) nicht beeinflussen, werden alle Impulserwartungswerte auf die Summe normiert, daher auch der Name pdfnorm\_type<sup>1</sup>.

#### • parton type:

Für die Berechnung der Wichtungsfaktoren ist es weiterhin notwendig zu wissen, welche Partonen bereits aus dem Remnant entnommen wurden. parton\_type ist eine Liste von eben diesen Partonen. Für Seequarks ist es außerdem wichtig, die Eigenschaften des Splittingpartners aus dem  $g \to q_S q_Q$  Gluonsplitting zu kennen. parton\_type enthält folglich einen Zeiger parton\_type%twin auf das jeweils andere Quark eines solchen Splittings

• proton remnant type:

Container für alle Eigenschaften eines Proton-Remnants und für spezifische Methoden zur Bestimmung der Wichtungsfaktoren für Proton-Remnants.

• pp remnant type:

Abstrahierung der beiden Remnants und Schnittstelle für das Modul.

# 5.2 Abhängigkeiten

```
use,intrinsic::iso_fortran_env
use pdf_builtin !NODEP!
use tao_random_numbers !NODEP!
use muli_basic
use muli_interactions
use muli_momentum
```

#### 5.3 Parameter

muli\_remnant%nx und muli\_remnant%nq sind Parameter fur die Approximation von  $\langle f_k(\mu) \rangle$ . nx ist die Zahl der Stützstellen für x und nq ist die Zahl der Stützstellen für  $\mu_F = Q$ , bei denen  $f_k(x, \mu_F)$  dafür ausgewertet wird. Da über x integriert wird, nehmen die Werte für x keinen Speicher in Anspruch, sondern nur CPU-Zeit. Die Werte für  $\mu_F$  werden hingegen gespeichert.

muli\_remnant%remnant\_weight\_model und muli\_remnant%gluon\_exp sind Modellparameter für die Behandlung der Remnants. remnant\_weight\_model gibt an, wie die Wichtungsfaktoren durch die einzige Bedingung (??) ausgedrückt werden. In Tabelle ?? ist eine Übersicht angegeben. In proton remnant type%calculate weight werden die Wichtungsfaktoren bestimmt.

 $<sup>^1</sup>$ hängt stark von den Integrationsparametern ab, bei exakterer Integration scheint der Fehler beliebig klein zu werden, dadurch wird die CPU-Last aber zu groß. Renormierung ist eine deutlich billigere Methode. In den aktuellen Einstellung mit einer gut angepassten Verteilung von  $10^7$  Stützstellen ist die Abweichung mit  $< 10^{-4}$  eigentlich irrelevant, dafür dauert es einige Minuten, bis alle Integrationen fertig sind.

gluon\_exp ist ein Parameter für die Approximation der Quasivalenzquarkbeiträge, siehe remnant\_gluon\_pdf\_a

```
implicit none
integer,parameter::nx=10000000
integer,parameter::nq=60
integer,public::remnant_weight_model=2
integer::gluon_exp=4
```

## 5.4 Derived Types

## 5.4.1 pdfnorm type

pdfnorm\_type approximiert die Impulserwartungswerte  $\langle f_k(\mu) \rangle = \int_{x=x_0}^1 x f_k(x,\mu)$  aller Beiträge k zur Strukturfunktion. pdfnorm\_type hat nur zwei neue Methoden, scan und get\_norm. scan Wertet  $f_k(x,\mu)$  an allen  $nx \otimes nq$  Stellen für alle 13 Einträge der LHAPDF-Sets aus und bestimmt daraus die Werte

$$pdf_{norm}(\mu) = \left[ \langle f_{\Sigma}(\mu) \rangle, \frac{\langle f_{g}(\mu) \rangle}{\langle f_{\Sigma}(\mu) \rangle}, \frac{\langle f_{s}(\mu) \rangle}{\langle f_{\Sigma}(\mu) \rangle}, \frac{\langle f_{d^{v}}(\mu) \rangle}{\langle f_{\Sigma}(\mu) \rangle}, \frac{\langle f_{u^{v}}(\mu) \rangle}{\langle f_{\Sigma}(\mu) \rangle} \right]$$
(5.1)

für nq verschiedene Werte von  $\mu_F$ .  $\langle f_{\Sigma}(\mu) \rangle$  bezeichnet die Summe über die Impulsmittelwerte aller 13 Einträge der LHAPDF-Sets. pdf\_int $(k, \mu_F) = \langle f_k(\mu_F) \rangle$ , k = LHAPDF-Flavor, ist ein Zwischenschritt und wird eigentlich nicht benötigt, sobald pdf\_norm bestimmt ist. pdf\_int kann also gefahrlos von der Liste der Komponenten entfernt werden. Es wird nur zu Debugging-Zwecken mitgeführt.

pdfnorm\_type%qmin, pdfnorm\_type%qmax und pdfnorm\_type%dq legen die Abbildung  $j = 1..nq \rightarrow \mu_j$  fest, wobei j der zweite Index von pdf\_int bzw. pdf\_norm ist. Allerdings tragen sie die etwas unübliche Einheit  $\sqrt{GeV}$ . Es gilt:

$$\mu_j = \left(qmin + j \ dq\right)^2 \tag{5.2}$$

```
type,extends(serializable_class)::pdfnorm_type
    real(kind=double)::qmin,qmax,dq
    real(kind=double),dimension(-6:6,0:nq)::pdf_int
    real(kind=double),dimension(0:4,0:nq)::pdf_norm
    contains
    !Überschriebene serializable_class Methoden
    procedure::write_to_marker=>pdfnorm_write_to_marker
    procedure::read_from_marker=>pdfnorm_read_from_marker
    procedure::print_to_unit=>pdfnorm_print_to_unit
    procedure,nopass::get_type=>pdfnorm_get_type
    procedure,nopass::verify_type=>pdfnorm_verify_type
    !Originäre pdfnorm_type Methoden
    procedure::scan=>pdfnorm_scan
    procedure::get_norm=>pdfnorm_get_norm
end type pdfnorm_type
```



## 5.4.2 parton type

parton\_type ist eine Liste von Partonen. Jedes Parton bekommt eine eindeutige parton\_type%id, die mit der id des ISR-Algorithmus übereinstimmt. So können sich ISR und MPI miteinander verständigen, mit welchem Parton etwas geschieht.

parton type%lha flavor ist das Flavor des Partons im LHA-Schema

Handelt es sich nicht um ein Quasivalenzquark, dann ist parton\_type%momentum der Impulsanteil  $\xi$ , bezogen auf den aktuellen Remnantimpuls, des Partons. Bei einem Quasivalenzquark hingegen ist parton type%momentum der ungewichtete Impulserwartungswert des Quasivalenzquarks.



parton\_type%twin ist nur von Bedeutung, wenn das Parton ein Seequark oder ein Quasivalenzquark ist. Dann ist twin der Spittingpartner des vorangegangenen Gluonsplittings.

parton type%next ist das nächste Parton in der Liste.

```
type, Extendsserializable_class::parton_type
   private
   integer::id=-1
   integer::lha_flavor
   real(kind=double)::momentum=-1D0
   class(parton_type), pointer::twin=>null()
   class(parton_type),pointer::next=>null()
contains
   !Überschriebene serializable_class Methoden
   procedure::write_to_marker=>parton_write_to_marker
  procedure::read_from_marker=>parton_read_from_marker
   procedure::print_to_unit=>parton_print_to_unit
  procedure,nopass::get_type=>parton_get_type
   !Originäre parton_type Methoden
   procedure::unweighted_pdf=>twin_unweighted_pdf
  procedure::deallocate=>twin_deallocate
   procedure::push=>parton_push
   procedure::pop_by_id=>parton_pop_by_id
  procedure::pop_by_association=>parton_pop_by_association
   generic::pop=>pop_by_id,pop_by_association
end type parton_type
```

## 5.4.3 proton remnant type

```
proton_remnant_type enthält den aktuellen Status eines Proton-Remnants. Das sind die Anzahl der jeweiligen Valenzquarks proton_remnant_type%valence_content, die Anzahl aller Quasivalenzquarks proton_remnant_type%n_twins, die aktuellen Wichtungsfaktoren proton_remnant_type%pdf_int_weight (siehe (??)), den Remnantimpuls dividiert durch den ursprünglichen Protonimpuls proton_remnant_type%momentum_fraction, die Summe der ungewichteten Impulsmittelwerte der Quasivalenzquarks proton_remnant_type%twin_norm, die Liste der Quasivalenzquarks im Remnant proton_remnant_type%twin_partons,
```

```
die Liste der aktiven Initial State Partonen proton_remnant_type%is_partons,
```

die Liste der aktiven Final State Partonen proton\_remnant\_type%fs\_partons

sowie eine redundante Referenz auf die integrierten LHAPDFs proton\_remnant\_type%pdf\_norm. Redundant bedeutet, dass mehrere Instanzen einen Zeiger auf dasselbe Ziel haben. Die Allokierung der pdf\_norm wird einer Instanz des Datentyps pp\_remnant\_type durchgeführt. Nur diese Instanz sollte auch die Deallokierung durchführen.

```
type, extends (serializable_class)::proton_remnant_type
   integer,dimension(2)::valence_content=[1,2]
   integer::n_twins=0
   ![gluon,sea quark,valence down,valence up,twin]
  real(kind=drk), dimension(5)::pdf_int_weight=[1D0,1D0,1D0,1D0,0D0]
  real(kind=drk)::momentum_fraction=1D0
  real(kind=double)::twin_norm=0D0
  type(parton_type)::twin_partons
  type(parton_type)::is_partons
   type(parton_type)::fs_partons
   ! these pointers shall not be allocated, deallocated, serialized or
   ! deserialized explicitly.
   class(pdfnorm_type),pointer::pdf_norm=>null()
 contains
   !Überschriebene serializable_class Methoden
   procedure::write_to_marker=>proton_remnant_write_to_marker
  procedure::read_from_marker=>proton_remnant_read_from_marker
   procedure::print_to_unit=>proton_remnant_print_to_unit
   procedure,nopass::get_type=>proton_remnant_get_type
   !Originare proton_remnant_type Methoden
   ! manipulating parton content
  procedure::remove_valence_quark=>proton_remnant_remove_valence_quark
  procedure::remove_sea_quark=>proton_remnant_remove_sea_quark
  procedure::remove_gluon=>proton_remnant_remove_gluon
  procedure::remove_valence_up_quark=>proton_remnant_remove_valence_up_quark
  procedure::remove_valence_down_quark=>proton_remnant_remove_valence_down_quark
  procedure::remove_twin=>proton_remnant_remove_twin
   ! getting pdf
  procedure::momentum_twin_pdf=>proton_remnant_momentum_twin_pdf
  procedure::momentum_twin_pdf_array=>proton_remnant_momentum_twin_pdf_array
  procedure::momentum_kind_pdf=>proton_remnant_momentum_kind_pdf
  procedure::momentum_flavor_pdf=>proton_remnant_momentum_flavor_pdf
  procedure::momentum_kind_pdf_array=>proton_remnant_momentum_kind_pdf_array
  procedure::momentum_flavor_pdf_array=>proton_remnant_momentum_flavor_pdf_array
  procedure::parton_twin_pdf=>proton_remnant_parton_twin_pdf
  procedure::parton_twin_pdf_array=>proton_remnant_parton_twin_pdf_array
  procedure::parton_kind_pdf=>proton_remnant_parton_kind_pdf
  procedure::parton_flavor_pdf=>proton_remnant_parton_flavor_pdf
  procedure::parton_kind_pdf_array=>proton_remnant_parton_kind_pdf_array
  procedure::parton_flavor_pdf_array=>proton_remnant_parton_flavor_pdf_array
   ! getting components
  procedure::get_pdf_int_weight=>proton_remnant_get_pdf_int_weight
  procedure::get_valence_down_weight=>proton_remnant_get_valence_down_weight
```

```
procedure::get_valence_up_weight=>proton_remnant_get_valence_up_weight
   procedure::get_valence_weight=>proton_remnant_get_valence_weight
  procedure::get_gluon_weight=>proton_remnant_get_gluon_weight
   procedure::get_sea_weight=>proton_remnant_get_sea_weight
  procedure::get_twin_weight=>proton_remnant_get_twin_weight
  procedure::get_valence_content=>proton_remnant_get_valence_content
   procedure::get_momentum_fraction=>proton_remnant_get_momentum_fraction
   ! misc
   procedure::deallocate=>proton_remnant_deallocate
   procedure::initialize=>proton_remnant_initialize
   procedure::finalize=>proton_remnant_finalize
   procedure::apply_initial_splitting=>proton_remnant_apply_initial_splitting
  procedure::reset=>proton_remnant_reset
   ! private
   procedure, private::calculate_weight=>proton_remnant_calculate_weight
   procedure, private::push_is_parton=>proton_remnant_push_is_parton
   procedure, private::push_twin=>proton_remnant_push_twin
  procedure,private::calculate_twin_norm=>proton_remnant_calculate_twin_norm
  procedure,private::replace_is_parton=>proton_remnant_replace_is_parton
   ! plots
   procedure::gnuplot_momentum_kind_pdf_array=>proton_remnant_gnuplot_momentum_kind_pdf_array
end type proton_remnant_type
```

### 5.4.4 pp remnant type

pp\_remnant\_type abstrahiert die einzelnen Hadron-Remnants und dient als Schnittstelle für das komplette Modul. Aus anderen Modulen heraus sollen keine anderen Methoden, als die hier definierten, aufgerufen werden. Deswegen hat pp\_remnant\_type als einziger Datentyp in diesem Modul eine Komponente "initialized", so dass eine Warnung ausgegeben werden kann, wenn ein Zugriff auf nichtinitialisierte Komponenten versucht wird.

pp\_remnant\_type%gev\_cme\_tot soll die aktuelle invariante Masse des hadronischen Systems zurückgeben. Dynamische invariante Massen sind aber noch nicht implementiert. pp\_remnant\_type%X ist die aktuelle invariante Masse dividiert durch die ursprüngliche invariante Masse des Proton-Proton-Systems, allerdings wird diese Variable (noch) nirgends verwendet.



```
pp_remnant_type%proton sind die beiden Proton-Remnants.

pp_remnant_type%pdfnorm_type sind die Impulsmittelwerte der PDFs.

type,Extendsserializable_class::pp_remnant_type
    logical::initialized=.false.
    real(kind=double),private::gev_initial_cme = gev_cme_tot
    real(kind=double),private::X=1D0
    type(proton_remnant_type),dimension(2)::proton
    class(pdfnorm_type),pointer,private::pdf_norm
    contains
    !Überschriebene serializable_class Methoden
    procedure::write_to_marker=>pp_remnant_write_to_marker
    procedure::read_from_marker=>pp_remnant_read_from_marker
    procedure::print_to_unit=>pp_remnant_print_to_unit
```

```
procedure,nopass::get_type=>pp_remnant_get_type
        !Originare pp_remnant_type Methoden
        ! init /final
       procedure::initialize=>pp_remnant_initialize
       procedure::finalize=>pp_remnant_finalize
       procedure::reset=>pp_remnant_reset
        ! manipulating parton content
       procedure::apply_initial_interaction=>pp_remnant_apply_initial_interaction
       procedure::replace_parton=>pp_remnant_replace_parton
       procedure::apply_interaction=>pp_remnant_apply_interaction
        ! getting pdfs
       procedure::momentum_pdf=>pp_remnant_momentum_pdf
       procedure::parton_pdf=>pp_remnant_parton_pdf
       procedure::get_proton_remnant_momentum_fractions=>pp_remnant_get_proton_remnant_momentum
       procedure::get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_parton_flavor_pdf_arrays=>pp_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_remnant_get_r
        ! getting components
       procedure::get_pdf_int_weights=>pp_remnant_get_pdf_int_weights
       procedure::get_pdf_int_weight=>pp_remnant_get_pdf_int_weight
       procedure::set_pdf_weight=>pp_remnant_set_pdf_weight
       procedure::get_gev_initial_cme=>pp_remnant_get_gev_initial_cme
       procedure::get_gev_actual_cme=>pp_remnant_get_gev_actual_cme
       procedure::get_cme_fraction=>pp_remnant_get_cme_fraction
       procedure::get_proton_remnants=>pp_remnant_get_proton_remnants
end type pp_remnant_type
```

# 5.5 Implementierung der Methoden

## 5.5.1 Methoden für pdfnorm type

```
pdfnorm write to marker \( \ \)
  subroutine pdfnorm_write_to_marker(this,marker,status)
    class(pdfnorm_type),intent(in)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("pdfnorm_type")
    call marker%mark("qmin",this%qmin)
    call marker%mark("qmax",this%qmax)
    call marker%mark("dq",this%dq)
    call marker%mark("pdf_int",this%pdf_int)
    call marker%mark("pdf_norm",this%pdf_norm)
    call marker%mark_end("pdfnorm_type")
  end subroutine pdfnorm_write_to_marker
pdfnorm read from marker \( \)
  subroutine pdfnorm_read_from_marker(this,marker,status)
    class(pdfnorm_type),intent(out)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
```

```
character(:),allocatable::name
    call marker%pick_begin("pdfnorm_type", status=status)
    call marker%pick("qmin",this%qmin,status)
    call marker%pick("qmax",this%qmax,status)
    call marker%pick("dq",this%dq,status)
    call marker%pick("pdf_int",this%pdf_int,status)
    call marker%pick("pdf_norm",this%pdf_norm,status)
    call marker%pick_end("pdfnorm_type",status=status)
  end subroutine pdfnorm_read_from_marker
pdfnorm print to unit \
  recursive subroutine pdfnorm_print_to_unit(this,unit,parents,components,peers)
    class(pdfnorm_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    write(unit, '("Components of pdfnorm_type:")')
    write(unit,'("qmin:
                         ",F7.6)')this%qmin
    write(unit,'("qmax:
                           ",F7.6)')this%qmax
    write(unit,'("dq:
                           ",F7.6)')this%dq
    if(components>0)then
       write(unit,'("pdf_int: ",13(F8.6," "))')this%pdf_int
       write(unit,'("pdf_norm: ",5(F8.6," "))')this%pdf_norm
    else
       write(unit,'("Skipping pdf_int")')
       write(unit, '("Skipping pdf_norm")')
    end if
  end subroutine pdfnorm_print_to_unit
pdfnorm get type \( \ \)
  pure subroutine pdfnorm_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="pdfnorm_type")
  end subroutine pdfnorm_get_type
pdfnorm verify type \( \)
  elemental logical function pdfnorm_verify_type(type) result(match)
    character(*),intent(in)::type
    match=type=="pdfnorm_type"
  end function pdfnorm_verify_type
pdfnorm scan †
```

Für verschiedene Werte  $\mu_j$  von  $\mu_F$  integrieren wir über x und bekommen so eine Approximation von  $\langle f_k(\mu) \rangle = \int_{x=x_0}^1 x f_k(x,\mu)$ . In der Komponente this%pdf\_int[k,j] werden die die Werte  $\langle f_k(\mu_j) \rangle$  gespeichert, mit  $k \in [-6:6] = [\overline{t}^S, \overline{b}^S, \overline{c}^S, \overline{s}^S, \overline{u}^S, \overline{d}^S, g, d^V, u^V, s^S, c^S, b^S, t^S]$ . In der Komponente this%pdf\_norm[m,j] werden normierte Summen dieser Integrale gspeichert.

$$this\%pdf\_norm[m,j] = \frac{\sum_{k \in I_m} \langle f_k(\mu_j) \rangle}{N}$$
 (5.3)

mit

$$N = \sum_{\text{alle } I_m} \langle f_k(\mu_j) \rangle \tag{5.4}$$

und mit I = [gluon, see, valenz-down, valenz-up], genauer:

$$I_1 = g (5.5)$$

$$I_2 = \overline{t}^S, \overline{b}^S, \overline{c}^S, \overline{s}^S, \overline{u}^S, \overline{d}^S, d^S, u^S, s^S, c^S, b^S, t^S$$

$$(5.6)$$

$$I_3 = d^V (5.7)$$

$$I_4 = u^V (5.8)$$

Schließlich wird N in this%pdf\_norm[0,j] gespeichert. Idealerweise sollte N=1 sein, das wird auch bei der Berechnung der Wichtungsfaktoren der Remnant-PDFs in proton\_remnant\_type%calculate\_weight explizit angenommen. Da diese Summenregel durch nummerische Fehler aber nicht exakt erfüllt ist, normieren wir die Beiträge auf deren Summe. Dadurch bekommen wir in proton\_remnant\_type%calculate\_weight Wichtungsfaktorn, die kaum von dem nummerischen Fehler der Gleichung N=1 abhängen.

Die Integration über x wird mit der Trapezregel durchgeführt. LHAPDF liefert bereits die momentumpdfs xf, deswegen tritt der Faktor x hier nicht mehr auf. Die x-Werte sind wie auch die  $\mu$ -Werte nicht äquidistant, sondern deren Abstand ist  $\sim \sqrt{x}$  bzw.  $\sim \sqrt{\mu}$ . Da x>0 und  $\mu>0$  treten keine Koordinaten-divergenzen auf.

```
subroutine pdfnorm_scan(this)
  class(pdfnorm_type),intent(out)::this
  integer::ix,iq
  real(kind=double)::xmin,xmax,dx
  real(kind=double)::q,q2min,q2max
  real(kind=double), dimension(-6:6)::f
  real(kind=double), dimension(0:2)::x
  call getxmin(0,xmin)
  call getxmax(0,xmax)
  call getq2min(0,q2min)
  call getq2max(0,q2max)
  this%qmin=sqrt(sqrt(q2min))
  this%qmax=sqrt(sqrt(q2max))
  this%dq=(this%qmax-this%qmin)/nq
  xmin=sqrt(xmin)
  xmax=sqrt(xmax)
  dx=(xmax-xmin)/nx
  do iq=0,nq
     print *,"iq=",iq,"/",nq
     q=(this%qmin+iq*this%dq)**2
     x(0)=xmin**2
     x(1)=(xmin+dx)**2
     call evolvePDF(x(0),q,f)
     !Valenzbeiträge
     f(1)=f(1)-f(-1)
     f(2)=f(2)-f(-2)
     !Trapezregel: linker Rand
     this pdf_{int}(:, iq) = (x(1) - x(0)) *f
     do ix=2,nx
        x(2)=(xmin+ix*dx)**2
```

```
call evolvePDF(x(1),q,f)
           f(1)=f(1)-f(-1)
           f(2)=f(2)-f(-2)
           !Trapezregel: Die bekannte Form ergibt sich aus einer Umsummierung dieser Beiträge.
           this pdf_int(:,iq) = this pdf_int(:,iq) + f*(x(2)-x(0))
           !Die x-Werte werden nach links geschoben
           x(0)=x(1)
           x(1)=x(2)
       end do
       !Trapezregel: rechter Rand
       call evolvePDF(x(1),q,f)
       f(1)=f(1)-f(-1)
       f(2)=f(2)-f(-2)
       !Hier wird endlich durch 2 dividiert.
       this%pdf_int(:,iq)=(this%pdf_int(:,iq)+f*(x(1)-x(0)))/2D0
       this%pdf_norm(4,iq)=this%pdf_int(2,iq)
       !\langle f_d^v\rangle
       this%pdf_norm(3,iq)=this%pdf_int(1,iq)
       !\langle f_u\rangle
       this%pdf_int(2,iq)=this%pdf_int(2,iq)+this%pdf_int(-2,iq)
       this%pdf_int(1,iq)=this%pdf_int(1,iq)+this%pdf_int(-1,iq)
       this%pdf_norm(1,iq)=this%pdf_int(0,iq)
       !\sum \langle f_q \hat{s}\rangle
       this%pdf_norm(2,iq)=sum(this%pdf_int(-6:-1,iq))+sum(this%pdf_int(-2:-1,iq))+sum(this%pdf_int
       !\sum_{alle\ Partonen} \langle f_k \rangle
       this%pdf_norm(0,iq)=sum(this%pdf_int(:,iq))
       !Normierung auf pdf_norm(0,iq)
       this%pdf_norm(1,iq)=this%pdf_norm(1,iq)/this%pdf_norm(0,iq)
       this%pdf_norm(2,iq)=this%pdf_norm(2,iq)/this%pdf_norm(0,iq)
       this%pdf_norm(3,iq)=this%pdf_norm(3,iq)/this%pdf_norm(0,iq)
       this%pdf_norm(4,iq)=this%pdf_norm(4,iq)/this%pdf_norm(0,iq)
    end do
  end subroutine pdfnorm_scan
pdfnorm get norm \( \ \)
```

Hier habe ich verschiedene Polynome zur Approximation der  $\mu_F$ -Abhängigkeit probiert. Dim ist die Ordnung des Polynoms. Wie auch bei der x-Integration hat die Trapezregel, also dim=1, die besten Resultate gebracht.

```
subroutine pdfnorm_get_norm(this,gev_q,dim,kind,norm)
  class(pdfnorm_type),intent(in)::this
  real(kind=double),intent(in)::gev_q
  integer,intent(in)::dim,kind
  real(kind=double),intent(out)::norm
  integer::iq
  real(kind=double)::x,q,z0,z1,z2,z3,z4
  norm=-1D0
  q=sqrt(gev_q)-this%qmin
```

```
iq=floor(q/this%dq)
 x=q/this%dq-iq
  if(iq<0)then
     print *,"pdfnorm_getnorm: q < q_min ",gev_q,this%qmin**2</pre>
     norm=this%pdf_norm(kind,0)
  else
     if(iq>=nq)then
        print *,"pdfnorm_getnorm: q >= q_max ",gev_q,this%qmax**2
        norm=this%pdf_norm(kind,nq)
        select case(dim)
        case(0)
           norm=this%pdf_norm(kind,iq)
        case(1)
           norm=this%pdf_norm(kind,iq)*(1D0-x)+this%pdf_norm(kind,iq+1)*x
        case(2)
           x=x+mod(iq,2)
           iq=iq-mod(iq,2)
           z0=this%pdf_norm(kind,iq)
           z1=this%pdf_norm(kind,iq+1)
           z2=this%pdf_norm(kind,iq+2)
           norm = ((z0-2D0*z1+z2)*x-(3D0*z0-4D0*z1+z2))*x/2D0+z0
        case(3)
           x=x+mod(iq,3)
           iq=iq-mod(iq,3)
           z0=this%pdf_norm(kind,iq)
           z1=this%pdf_norm(kind,iq+1)
           z2=this%pdf_norm(kind,iq+2)
           z3=this%pdf_norm(kind,iq+3)
           norm = ((-(z0-3*z1+3*z2-z3)*x+3*(2*z0-5*z1+4*z2-z3))*x-(11*z0-18*z1+9*z2-2*z3))*x
        case(4)
           x=x+mod(iq,4)
           iq=iq-mod(iq,4)
           z0=this%pdf_norm(kind,iq)
           z1=this%pdf_norm(kind,iq+1)
           z2=this%pdf_norm(kind,iq+2)
           z3=this%pdf_norm(kind,iq+3)
           z4=this%pdf_norm(kind,iq+4)
           norm = (((((z0-4*z1+6*z2-4*z3+z4)*x\&
                -2*(5*z0-18*z1+24*z2-14*z3+3*z4))*x&
                +(35*z0-104*z1+114*z2-56*z3+11*z4))*x&
                -2*(25*z0-48*z1+36*z2-16*z3+3*z4))*x)/24D0&
                +z0
        case default
           norm=this%pdf_norm(kind,iq)*(1D0-x)+this%pdf_norm(kind,iq+1)*x
        end select
        !
                   print *,iq,x,norm
     end if
  end if
end subroutine pdfnorm_get_norm
```

## 5.5.2 Methoden für parton type

```
parton write to marker \( \ \)
  subroutine parton_write_to_marker(this,marker,status)
    class(parton_type),intent(in)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("parton_type")
    call marker%mark("id",this%id)
    call marker%mark("lha",this%lha_flavor)
    call marker%mark("momentum",this%momentum)
    call marker%mark_end("parton_type")
  end subroutine parton_write_to_marker
parton read from marker \( \)
  subroutine parton_read_from_marker(this,marker,status)
    class(parton_type),intent(out)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    character(:),allocatable::name
    call marker%pick_begin("parton_type",status=status)
    call marker%pick("id",this%id,status)
    call marker%pick("lha",this%lha_flavor,status)
    call marker%pick("momentum",this%momentum,status)
    call marker%pick_end("parton_type",status=status)
  end subroutine parton_read_from_marker
parton print to unit \
  recursive subroutine parton_print_to_unit(this,unit,parents,components,peers)
    class(parton_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    class(serializable_class),pointer::ser
    write(unit,'("Components of parton_type:")')
    write(unit,'("id:
                             ",I7)')this%id
    write(unit,'("lha flavor: ",I7)')this%lha_flavor
    write(unit,'("momentum: ",F7.6)')this%momentum
    ser=>this%next
    call serialize_print_peer_pointer(ser,unit,parents,components,peers-one,"next")
    ser=>this%twin
    call serialize_print_comp_pointer(ser,unit,parents,components,peers-one,"twin")
  end subroutine parton_print_to_unit
parton get type \( \ \)
  pure subroutine parton_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="parton_type")
  end subroutine parton_get_type
```

```
twin unweighted pdf \( \ \)
  pure function twin_unweighted_pdf(this,momentum_fraction) result(pdf)
    !parton pdf
    class(parton_type),intent(in)::this
    real(kind=double),intent(in)::momentum_fraction
    real(kind=double)::pdf
    if(momentum_fraction+this%twin%momentum<1D0)then
       pdf=remnant_twin_pdf_p(momentum_fraction,this%twin%momentum,gluon_exp)
    else
       pdf=0D0
    end if
  end function twin_unweighted_pdf
twin deallocate \
  recursive subroutine twin_deallocate(this)
    class(parton_type)::this
    if(associated(this%next))then
       call this%next%deallocate
       deallocate(this%next)
  end subroutine twin_deallocate
parton push \( \ \)
  subroutine parton_push(this,parton)
    class(parton_type),intent(inout)::this
    class(parton_type),intent(inout),pointer::parton
    parton%next=>this%next
    this%next=>parton
  end subroutine parton_push
parton pop by id \
  subroutine parton_pop_by_id(this,id,parton)
    class(parton_type), target, intent(inout)::this
    integer,intent(in)::id
    class(parton_type),intent(out),pointer::parton
    class(parton_type),pointer::tmp_parton
    tmp parton=>this
    do while(associated(tmp_parton%next))
       if(tmp_parton%next%id==id)exit
       tmp_parton=>tmp_parton%next
    end do
    !Noch wissen wir nicht, ob die Schleife erfolglos durchgelaufen ist.
    if(associated(tmp_parton%next))then
       !Erfolg: Das Parton wird aus der Liste entfernt.
       parton=>tmp_parton%next
       tmp_parton%next=>parton%next
       nullify(parton%next)
    else
       !Kein Erfolg: Das Dummyargument wird deassociiert.
```

```
nullify(parton)
       print *,"parton_pop ",id,"NULL"
    end if
  end subroutine parton_pop_by_id
parton pop by association \( \ \)
  subroutine parton_pop_by_association(this,parton)
    class(parton_type), target, intent(inout)::this
    class(parton_type),intent(inout),target::parton
    class(parton_type),pointer::tmp_parton
    tmp_parton=>this
    do while(associated(tmp_parton%next))
       if(associated(tmp_parton%next,parton))exit
       tmp_parton=>tmp_parton%next
    end do
    !Noch wissen wir nicht, ob die Schleife erfolglos durchgelaufen ist.
    if(associated(tmp_parton%next))then
       !Erfolg: Das Parton wird aus der Liste entfernt.
       tmp_parton%next=>parton%next
       nullify(parton%next)
    else
       !Kein Erfolg
       print *,"parton_pop NULL"
    end if
  end subroutine parton_pop_by_association
5.5.3 Methoden für proton remnant type
! manipulating parton content
proton remnant remove valence quark \( \ \)
  subroutine proton_remnant_remove_valence_quark(this,id,GeV_scale,momentum_fraction,lha_flavor)
    class(proton_remnant_type),intent(inout)::this
    integer,intent(in)::id
    real(kind=double),intent(in)::GeV_scale,momentum_fraction
    integer,intent(in)::lha_flavor !d=1 u=2
    if(lha_flavor==1.or.lha_flavor==2)then
       !q ist die Anzahl der entsprechenden Valenzquarks.
       associate(q=>this%valence_content(lha_flavor))
         if(q>0)then
            q=q-1
            !Das Quark ist ab jetzt ein aktiven Shower-Teilchen.
            call this%push_is_parton(id,lha_flavor,momentum_fraction)
            !Der Remnant-Impuls wird um den Partonimpuls reduziert.
            this%momentum_fraction=this%momentum_fraction*(1D0-momentum_fraction)
            !Die Wichtugsfaktoren werden neu ausgewertet
            call this%calculate_weight(GeV_scale)
         else
            print('("proton_remnant_remove_valence_quark: Cannot remove parton ",I2,": &
```

### proton remnant remove valence up quark \( \extrm{\gamma} \)

q ist die Zahl der Valenz-up-Quarks im Remnant. Wenn keine mehr da sind, dann ist etwas schief gelaufen, sonst wird die Zahl um eins reduziert. Das Parton, das aus dem Remnant entfernt wird, verschwindet natürlich nicht, sondern wird mit proton\_remnant\_type%push\_is\_parton in die perturbative Beschreibung aufgenommen. is\_parton bedeutet Initial-State Parton, genauer gesagt aktives Initial-State Parton.

Selbstverständlich wird der Impuls des Remants aktualisiert und schließlich werden mit proton\_remnant\_type%calculate\_weight die neuen Wichtungsfaktoren  $W_{\alpha}$  bestimmt.

```
subroutine proton_remnant_remove_valence_up_quark(this,id,GeV_scale,momentum_fraction)
    class(proton_remnant_type),intent(inout)::this
    integer,intent(in)::id
    real(kind=double),intent(in)::GeV_scale,momentum_fraction
    associate(q=>this%valence_content(lha_flavor_u))
      if(q>0)then
         q=q-1
         call this "push_is_parton(id,lha_flavor_u,momentum_fraction)
         this%momentum_fraction=this%momentum_fraction*(1D0-momentum_fraction)
         call this%calculate_weight(GeV_scale)
      else
         print('("proton_remnant_remove_valence_up_quark: Cannot remove parton ",I2,": &
              &There are no such partons left.")', lha_flavor_u
         call this%print_all
      end if
    end associate
  end subroutine proton_remnant_remove_valence_up_quark
proton remnant remove valence down quark \( \)
Siehe proton remnant type%remove_valence_up_quark
  subroutine proton_remnant_remove_valence_down_quark(this,id,GeV_scale,momentum_fraction)
    class(proton_remnant_type),intent(inout)::this
    integer,intent(in)::id
    real(kind=double),intent(in)::GeV_scale,momentum_fraction
    associate(q=>this%valence_content(lha_flavor_d))
      if(q>0)then
         q=q-1
         call this%push_is_parton(id,lha_flavor_d,momentum_fraction)
         this%momentum_fraction=this%momentum_fraction*(1D0-momentum_fraction)
         call this%calculate_weight(GeV_scale)
      else
```

Es wird ein Seequark aus dem Remnant genommen und ein Quasivalenzquark hinzugefügt. Wir merken uns, welches Quasivalenzquark zu welchem Seequark gehört und nennen das jeweils andere twin. Mit proton\_remnant\_type%push\_twin erzeugen wir sowohl das neue aktive ISR Seequark als auch das neue Quasivalenzquark.

```
subroutine proton_remnant_remove_sea_quark(this,id,GeV_scale,momentum_fraction&
       &,lha_flavor)
    integer, intent(in)::id
    class(proton_remnant_type),intent(inout)::this
    real(kind=double),intent(in)::GeV_scale,momentum_fraction
    integer,intent(in)::lha_flavor
    if(lha_flavor>-6.and.lha_flavor<6.and.(lha_flavor.ne.0))then
       this%momentum_fraction=this%momentum_fraction*(1D0-momentum_fraction)
       call this %push_twin(id, lha_flavor, momentum_fraction, GeV_scale)
    end if
  end subroutine proton_remnant_remove_sea_quark
proton remnant remove gluon \( \)
Hier ist am wenigsten zu tun. Es wird nur der Remnant-Impuls aktualisiert und mit
proton remnant type%push is parton ein neues aktives ISR-Gluon erzeugt.
  subroutine proton_remnant_remove_gluon(this,id,GeV_scale,momentum_fraction)
    class(proton_remnant_type),intent(inout)::this
    integer, intent(in)::id
    real(kind=double),intent(in)::GeV_scale,momentum_fraction
    this%momentum_fraction=this%momentum_fraction*(1D0-momentum_fraction)
    call this %push_is_parton(id,lha_flavor_g,momentum_fraction)
  end subroutine proton_remnant_remove_gluon
```

#### proton remnant remove twin \

Ein Quasivalenzquark wird aus dem Remnant genommen und in die Liste der aktiven Showerteilchen aufgenommen.

```
subroutine proton_remnant_remove_twin(this,id,GeV_scale)
  class(proton_remnant_type),intent(inout)::this
  integer,intent(in)::id
  real(kind=double),intent(in)::GeV_scale
  class(parton_type),pointer::twin
  call this%twin_partons%pop(id,twin)
  call this%fs_partons%push(twin)
  this%twin_norm=this%twin_norm-twin%momentum
  this%n_twins=this%n_twins-1
```

```
call this%calculate_weight(GeV_scale)
  end subroutine proton_remnant_remove_twin
! getting pdf
proton remnant parton twin pdf \( \ \)
Die Parton-PDFs aller Quasivalenzbeiträge zu dem angegebenen Flavor werden aufaddiert.
  subroutine proton_remnant_parton_twin_pdf(this,lha_flavor,momentum_fraction,pdf)
    class(proton_remnant_type),intent(in)::this
    integer, intent(in)::lha_flavor
    real(kind=double),intent(in)::momentum_fraction
    real(kind=double)::pdf
    class(parton_type),pointer::tmp_twin
    pdf=0D0
    tmp_twin=>this%twin_partons%next
    do while(associated(tmp_twin))
       if(tmp_twin%lha_flavor==lha_flavor)pdf=pdf+tmp_twin%unweighted_pdf(momentum_fraction)
       tmp_twin=>tmp_twin%next
    end do
    pdf=pdf*this%get_twin_weight()
  end subroutine proton_remnant_parton_twin_pdf
proton remnant parton twin pdf array \( \)
Aus der Liste proton remnant type%twin partons wird in ein array von Parton-PDFs erzeugt. Jeder
Eintrag in dem Dummy-Argument pdf entspricht einem Quasivalenzquark.
  subroutine proton_remnant_parton_twin_pdf_array(this,momentum_fraction,pdf)
    class(proton_remnant_type),intent(in)::this
    real(kind=double),intent(in)::momentum_fraction
    real(kind=double), dimension(this%n_twins), intent(out)::pdf
    class(parton_type),pointer::tmp_twin
    integer::1
    tmp_twin=>this%twin_partons%next
    1=0
    do while(associated(tmp_twin))
       pdf(l)=tmp_twin%unweighted_pdf(momentum_fraction)*this%twin_norm
       tmp_twin=>tmp_twin%next
    end do
  end subroutine proton_remnant_parton_twin_pdf_array
proton remnant momentum twin pdf \( \gamma \)
Die Momentum-PDFs aller Quasivalenzbeiträge zu dem angegebenen Flavor werden aufaddiert.
  subroutine proton_remnant_momentum_twin_pdf(this,lha_flavor,momentum_fraction,pdf)
    class(proton_remnant_type),intent(in)::this
    integer, intent(in)::lha_flavor
    real(kind=double),intent(in)::momentum_fraction
    real(kind=double),intent(out)::pdf
    call this%parton_twin_pdf(lha_flavor,momentum_fraction,pdf)
    pdf=pdf*momentum_fraction
  end subroutine proton_remnant_momentum_twin_pdf
```

```
proton remnant momentum twin pdf array \( \)
```

Aus der Liste proton\_remnant\_type%twin\_partons wird in ein array von Momentum-PDFs erzeugt. Jeder Eintrag in dem Dummy-Argument pdf entspricht einem Quasivalenzquark.

```
subroutine proton_remnant_momentum_twin_pdf_array(this,momentum_fraction,pdf)
  class(proton_remnant_type),intent(in)::this
  real(kind=double),intent(in)::momentum_fraction
  real(kind=double),dimension(this%n_twins),intent(out)::pdf
  call this%parton_twin_pdf_array(momentum_fraction,pdf)
  pdf=pdf*momentum_fraction
end subroutine proton_remnant_momentum_twin_pdf_array
```

#### proton\_remnant\_momentum\_kind\_pdf \( \)

Zu dem angegebenen Flavor wird die Momentum-Strukturfunktion nach See- (einschließlich Gluon-), Valenz- und Quasivalenzbeitrag aufgeschlüsselt.

```
subroutine proton_remnant_momentum_kind_pdf(this,GeV_scale,momentum_fraction&
     &,lha_flavor,valence_pdf,sea_pdf,twin_pdf)
  class(proton_remnant_type),intent(in)::this
  real(kind=double),intent(in)::GeV_scale,momentum_fraction
                                                    !g,u,d,etc.
  integer,intent(in)::lha_flavor
  real(kind=double),intent(out)::valence_pdf,sea_pdf,twin_pdf
  real(kind=double), dimension(-6:6)::pdf_array
  call evolvePDF(momentum_fraction,GeV_scale,pdf_array)
  select case (lha_flavor)
  case(0) !gluon
     valence_pdf=0D0
     sea_pdf=pdf_array(0)
  case(1) !down
     valence_pdf=this%get_valence_down_weight()*(pdf_array(1)-pdf_array(-1))
     sea_pdf=pdf_array(-1)
  case(2) !up
     valence_pdf=this%get_valence_up_weight()*(pdf_array(2)-pdf_array(-2))
     sea_pdf=pdf_array(-2)
  case default
     valence_pdf=0D0
     sea_pdf=pdf_array(lha_flavor)
  end select
  sea_pdf=sea_pdf*this%get_sea_weight()
  call this % momentum_twin_pdf(lha_flavor, momentum_fraction, twin_pdf)
end subroutine proton_remnant_momentum_kind_pdf
```

#### $proton\_remnant\_momentum\_flavor\_pdf \uparrow$

Zu dem angegebenen Flavor wird die Momentum-Strukturfunktion zurückgegeben. (Summe über alle Beiträge mit diesem Flavor.)

```
real(kind=double)::valence_pdf,sea_pdf,twin_pdf
call proton_remnant_momentum_kind_pdf(this,GeV_scale,momentum_fraction,lha_flavor&
          &,valence_pdf,sea_pdf,twin_pdf)
pdf=valence_pdf+sea_pdf+twin_pdf
end subroutine proton_remnant_momentum_flavor_pdf
```

```
proton remnant momentum flavor pdf array \( \)
```

Es wird ein array von Momentum-PDFs (Summe über alle Beiträge für jedes Flavor), aufgeschlüsselt nach Partonflavor zurückgegeben.

Es sind (noch) keine Quasivalenzquarks enthalten. Das ist aber nur eine Fleißübung, es gibt keinen technischen Hinderungsgrund.

#### proton remnant momentum kind pdf array \( \)

Es werden See- (einschließlich Gluon-) und Valenzbeiträge zur Momentum-PDF als separate arrays ausgegeben.

 $proton\_remnant\_parton\_kind\_pdf \uparrow$ 

Zu dem angegebenen Flavor wird die Parton-Strukturfunktion nach See- (einschließlich Gluon-), Valenzund Quasivalenzbeitrag aufgeschlüsselt.

```
subroutine proton_remnant_parton_kind_pdf(this,GeV_scale,momentum_fraction&
          &,lha_flavor,valence_pdf,sea_pdf,twin_pdf)
class(proton_remnant_type),intent(in)::this
real(kind=double),intent(in)::GeV_scale,momentum_fraction
integer,intent(in)::lha_flavor !g,u,d,etc.
```

#### proton remnant parton flavor pdf \( \ext{\chi} \)

Zu dem angegebenen Flavor wird die Parton-Strukturfunktion zurückgegeben (Summe über alle Beiträge mit diesem Flavor).

#### proton remnant parton kind pdf array \( \)

Es wird ein array von Parton-PDFs (Summe über alle Beiträge für jedes Flavor), aufgeschlüsselt nach Partonflavor zurückgegeben.

Es sind (noch) keine Quasivalenzquarks enthalten. Das ist aber nur eine Fleißübung, es gibt keinen technischen Hinderungsgrund.



```
subroutine proton_remnant_parton_kind_pdf_array(this,GeV_scale,momentum_fraction&
     &, valence_pdf, sea_pdf)
  class(proton_remnant_type),intent(in)::this
  real(kind=double),intent(in)::GeV_scale,momentum_fraction
  real(kind=double), dimension(2), intent(out)::valence_pdf
  real(kind=double), dimension(-6:6), intent(out)::sea_pdf
  call evolvePDF(momentum_fraction,GeV_scale,sea_pdf)
  sea_pdf=sea_pdf/momentum_fraction
  valence_pdf(1)=(sea_pdf(1)-sea_pdf(-1))*this%valence_content(1)
  valence_pdf(2)=(sea_pdf(2)-sea_pdf(-2))*(this%valence_content(2)/2D0)
  sea_pdf(1)=sea_pdf(-1)
  sea_pdf(2)=sea_pdf(-2)
  valence_pdf=valence_pdf*this%get_valence_weight()
  sea_pdf=sea_pdf*this%get_sea_weight()
  ! no twin yet
end subroutine proton_remnant_parton_kind_pdf_array
```

```
proton remnant parton flavor pdf array \( \)
```

Es werden See- (einschließlich Gluon-) und Valenzbeiträge zur Parton-PDF als separate arrays ausgegeben.

```
subroutine proton_remnant_parton_flavor_pdf_array(this,GeV_scale,momentum_fraction&
       &,pdf)
    class(proton_remnant_type),intent(in)::this
    real(kind=double),intent(in)::GeV_scale,momentum_fraction
    real(kind=double), dimension(-6:6), intent(out)::pdf
    real(kind=double),dimension(2)::valence_pdf
    real(kind=double),dimension(-6:6)::twin_pdf
    print('("proton_remnant_flavor_pdf_array: Not yet implemented.")')
  end subroutine proton_remnant_parton_flavor_pdf_array
! getting components
proton remnant get pdf int weight \
  pure function proton_remnant_get_pdf_int_weight(this) result(weight)
    class(proton_remnant_type),intent(in)::this
    real(kind=double),dimension(5)::weight
    weight=this%pdf_int_weight
  end function proton_remnant_get_pdf_int_weight
proton remnant get valence weight \( \ \)
  pure function proton_remnant_get_valence_weight(this) result(weight)
    class(proton_remnant_type),intent(in)::this
    real(kind=double), dimension(2)::weight
    weight=this%pdf_int_weight(3:4)
  end function proton_remnant_get_valence_weight
{\bf proton\_remnant\_get} \quad {\bf valence} \quad {\bf down} \quad {\bf weight} \uparrow
  elemental function proton_remnant_get_valence_down_weight(this) result(weight)
    class(proton_remnant_type),intent(in)::this
    real(kind=double)::weight
    weight=this%pdf_int_weight(pdf_int_kind_val_down)
  end function proton_remnant_get_valence_down_weight
proton remnant get valence up weight \( \ \)
  elemental function proton_remnant_get_valence_up_weight(this) result(weight)
    class(proton_remnant_type),intent(in)::this
    real(kind=double)::weight
    weight=this%pdf_int_weight(pdf_int_kind_val_up)
  end function proton_remnant_get_valence_up_weight
proton remnant get sea weight \
  elemental function proton_remnant_get_sea_weight(this) result(weight)
    class(proton_remnant_type),intent(in)::this
    real(kind=double)::weight
    weight=this%pdf_int_weight(pdf_int_kind_sea)
  end function proton_remnant_get_sea_weight
proton remnant get gluon weight \
```

```
elemental function proton_remnant_get_gluon_weight(this) result(weight)
    class(proton_remnant_type),intent(in)::this
    real(kind=double)::weight
    weight=this%pdf_int_weight(pdf_int_kind_gluon)
  end function proton_remnant_get_gluon_weight
proton remnant get twin weight \
  elemental function proton_remnant_get_twin_weight(this) result(weight)
    class(proton_remnant_type),intent(in)::this
    real(kind=double)::weight
    weight=this%pdf_int_weight(pdf_int_kind_twin)
  end function proton_remnant_get_twin_weight
proton remnant get valence content \( \ \)
  pure function proton_remnant_get_valence_content(this) result(valence)
    class(proton_remnant_type),intent(in)::this
    integer,dimension(2)::valence
    valence=this%valence_content
  end function proton_remnant_get_valence_content
proton remnant get momentum fraction \( \)
  elemental function proton_remnant_get_momentum_fraction(this) result(momentum)
    class(proton_remnant_type),intent(in)::this
    real(kind=double)::momentum
    momentum=this%momentum_fraction
  end function proton_remnant_get_momentum_fraction
! misc
proton remnant deallocate \( \)
  subroutine proton_remnant_deallocate(this)
    class(proton_remnant_type),intent(inout)::this
    call this%is_partons%deallocate
    call this%fs_partons%deallocate
    call this %twin_partons %deallocate
    this%twin_norm=0D0
    this%n_twins=0
  end subroutine proton_remnant_deallocate
proton remnant initialize \( \)
  subroutine proton_remnant_initialize(this,pdf_norm)
    class(proton_remnant_type),intent(out)::this
    class(pdfnorm_type), target, intent(in)::pdf_norm
    this%pdf_norm=>pdf_norm
  end subroutine proton_remnant_initialize
proton remnant finalize \( \ \)
```

```
subroutine proton_remnant_finalize(this)
  class(proton_remnant_type),intent(inout)::this
  call this%deallocate()
  nullify(this%pdf_norm)
  end subroutine proton_remnant_finalize

proton remnant apply initial splitting ↑
```

Es wird eine WHIZARD-Interaktion auf den Remnant übertragen. Im Falle eines Gluons im Eingangszustand wird einfach die Methode proton\_remnant\_type%remove\_gluon aufgerufen. Im Falle eines Quarks muss noch entschieden werden, ob es sich um ein See- oder ein Valenzquark handelt.

Mit proton\_remnant\_type%parton\_kind\_pdf bekommen wir die Strukturfunktion nach See-, Valenzund Quasivalenzanteil  $(f_{qS}, f_{qV}, f_{qQ})$  aufgeschlüsselt. Durch Vergleich des Verhältnisses  $\frac{f_{qV}}{f_{qV} + f_{qS}}$  mit der Zufallszahl rnd entscheiden wir, ob proton\_remnant\_type%remove\_valence\_up\_quark bzw. proton\_remnant\_type%remove\_valence\_down\_quark oder proton\_remnant\_type%remove\_sea\_quark aufgerufen wird.

```
subroutine proton_remnant_apply_initial_splitting(this,id,pdg_flavor,x,gev_scale,rnd)
    class(proton_remnant_type),intent(inout)::this
    integer,intent(in)::id,pdg_flavor
    real(kind=double),intent(in)::x,gev_scale,rnd
    real(kind=double)::valence_pdf,sea_pdf,twin_pdf
    select case(pdg_flavor)
    case(pdg_flavor_g)
       call this%remove_gluon(id,gev_scale,x)
    case(pdg_flavor_u)
       call this%parton_kind_pdf(gev_scale,x&
            &,pdg_flavor,valence_pdf,sea_pdf,twin_pdf)
       if(valence_pdf/(valence_pdf+sea_pdf)<rnd)then</pre>
          call this%remove_sea_quark(id,gev_scale,x,pdg_flavor)
       else
          call this%remove_valence_up_quark(id,gev_scale,x)
       end if
    case(pdg_flavor_d)
       call this %parton_kind_pdf(gev_scale,x&
            &,pdg_flavor,valence_pdf,sea_pdf,twin_pdf)
       if(valence_pdf/(valence_pdf+sea_pdf)<rnd)then</pre>
          call this%remove_sea_quark(id,gev_scale,x,pdg_flavor)
       else
          call this%remove_valence_down_quark(id,gev_scale,x)
       end if
    case default
       call this%remove_sea_quark(id,gev_scale,x,pdg_flavor)
    this%momentum_fraction=(1D0-x)
  end subroutine proton_remnant_apply_initial_splitting
proton remnant reset \
  subroutine proton_remnant_reset(this)
    class(proton_remnant_type),intent(inout)::this
    call this%deallocate()
```

```
this%valence_content=[1,2]
  this%pdf_int_weight=[1D0,1D0,1D0,1D0,1D0]
  this%momentum_fraction=1D0
  end subroutine proton_remnant_reset
! private
proton remnant push is parton ↑
```

Es wird eine neue Instanz vom Typ parton\_type allokiert und mit parton\_type%push auf den Stapel proton\_remnant\_type%is\_partons der aktiven ISR-Partonen gelegt.

```
subroutine proton_remnant_push_is_parton(this,id,lha_flavor,momentum_fraction)
  class(proton_remnant_type),intent(inout)::this
  integer,intent(in)::id,lha_flavor
  real(kind=double),intent(in)::momentum_fraction
  class(parton_type),pointer::tmp_parton
  allocate(tmp_parton)
  tmp_parton%id=id
  tmp_parton%lha_flavor=lha_flavor
  tmp_parton%momentum=momentum_fraction
  call this%is_partons%push(tmp_parton)
end subroutine proton_remnant_push_is_parton
```

#### proton remnant push twin \

Ein Seequark wird aus dem Remnant entfernt, indem ein neues quark auf den Stapel proton\_remnant\_type%is\_partons der aktiven ISR-Partonen gelegt und ein Quasivalenzquark(twin) in den Remnant aufgenommen wird. Die Quasivalenzquarks im Remnant werden durch den Stapel proton\_remnant\_type%twin\_partons dargestelt. Das Quasivalenzquark bekommt eine negative ID, wodurch es als Quasivalenzquark ausgezeichnet wird. Beide bekommen einen Zeiger twin, der auf das jeweils andere zeigt.

Die Modulfunktion remnant\_twin\_momentum\_4 liefert das Integral über die ungewichtete momentum-PDF des Quasivalenzquarks zurück. new\_twin%momentum ist also der ungewichtete Impulserwartungswert des Quasivalenzquarks, während new\_is%momentum der Impulsanteil  $\xi$  des Partons ist.



Mit parton\_type%push werden die neuen Teichen auf die jeweiligen Stapel gelegt und mit proton remnant type%calculate weight werden die neuen Wichtungsfaktoren ausgewertet.

```
subroutine proton_remnant_push_twin(this,id,lha_flavor,momentum_fraction,gev_scale)
  class(proton_remnant_type),intent(inout)::this
  integer,intent(in)::id,lha_flavor !of IS parton
  real(kind=double),intent(in)::momentum_fraction !of IS parton
  real(kind=double),intent(in)::GeV_scale
  class(parton_type),pointer::new_is,new_twin
  real(kind=double)::norm
  !print *,"proton_remnant_push_twin",momentum_fraction
  allocate(new_is)
  allocate(new_twin)
  !IS initialization
  new_is%id=id
  new_is%lha_flavor=lha_flavor
```

```
new_is%momentum=momentum_fraction
 new_is%twin=>new_twin
  !twin initialization
  new_twin%id=-id
 new_twin%lha_flavor=-lha_flavor
 new_twin%momentum=remnant_twin_momentum_4(momentum_fraction)
 new_twin%twin=>new_is
  !remnant update
  this%n_twins=this%n_twins+1
  this%twin_norm=this%twin_norm+new_twin%momentum
  call this%is_partons%push(new_is)
  call this%twin_partons%push(new_twin)
  call this%calculate_weight(GeV_scale)
end subroutine proton_remnant_push_twin
```

proton remnant calculate twin norm \( \)

Wenn proton remnant type%twin partons Partonen enthält, dann wird die Summe der Impulsmittel-Partonen aus proton remnant type%twin partons  $_{
m in}$  $\operatorname{der}$ proton remnant type%twin normabgelegt. Sonst wird proton remnant type%twin normauf Null gesetzt.

```
subroutine proton_remnant_calculate_twin_norm(this)
    class(proton_remnant_type),intent(inout)::this
    class(parton_type),pointer::twin
    if(associated(this%twin_partons%next))then
       this%twin_norm=0D0
       twin=>this%twin_partons%next
       do while(associated(twin))
          this%twin_norm=this%twin_norm+twin%momentum
          twin=>twin%next
       end do
    else
       this%twin_norm=0D0
    end if
  end subroutine proton_remnant_calculate_twin_norm
proton remnant replace is parton \( \ \)
```

Der ISR-Algorithmus hat ein Splitting eines Teilchens mit der id old id generiert, das zuvor aus dem Remnant entfert wurde. Jetzt wird das alte Remnant-Teilchen wieder in den Remnant zurückgelegt und das neue Teilchen mit der id new id aus dem Remnant entfernt (siehe Abbildung ??). In Abschnitt

5.4.3 meiner Dissertation wird noch einiges zu dieser Prozedur erläutert.

```
subroutine proton_remnant_replace_is_parton&
  (this,&
  old_id,&
 new_id,&
 pdg_f,&
 x_proton,&
  gev_scale)
  class(proton_remnant_type),intent(inout)::this
  integer,intent(in)::old_id,new_id,pdg_f
```

```
real(kind=double),intent(in)::x_proton,gev_scale
class(parton_type),pointer::old_is_parton
integer::lha_flavor
real(kind=double)::momentum_fraction
momentum_fraction=x_proton/this%momentum_fraction()
!convert pdg flavor numbers to lha flavor numbers
if(pdg_f==pdg_flavor_g)then
   lha_flavor=lha_flavor_g
else
   lha_flavor=pdg_f
end if
!we remove the old initial state parton from initial state stack.
call this%is_partons%pop(old_id,old_is_parton)
!this check has no physical meaning, it's just a check for consistency.
if(associated(old_is_parton))then
   !do we emit a gluon?
   if(lha_flavor==old_is_parton%lha_flavor)then
      !has the old initial state parton been a sea quark?
      if(associated(old_is_parton%twin))then
         !the connection of the old is parton with it's twin was provisional.
         !We remove it now
         call this %twin_partons %pop(old_is_parton %twin)
         call this%fs_partons%push(old_is_parton%twin)
         this%n_twins=this%n_twins-1
         !and generate a new initial state parton - twin pair.
         call this%push_twin(new_id,lha_flavor,momentum_fraction,gev_scale)
      else
         !there is no twin, so we just insert the new initial state parton.
         call this%push_is_parton(new_id,lha_flavor,momentum_fraction)
      end if
   else
      !we emit a quark. is this a g->qqbar splitting?
      if(lha_flavor==lha_flavor_g)then
         !we insert the new initial state gloun.
         call this%push_is_parton(new_id,lha_flavor,momentum_fraction)
         !has the old initial state quark got a twin?
         if(associated(old_is_parton%twin))then
            !we assume that this twin is the second splitting particle. so the
            !twin becomes a final state particle now and must be removed from
            !the is stack.
            call this%remove_twin(-old_id,GeV_scale)
         else
            !the old initial state quark has been a valence quark.
            !what should we do now? is this splitting sensible at all?
            !we don't know but allow these splittings.
            !The most trivial treatment is to restore the former valence quark.
            this%valence_content(old_is_parton%lha_flavor)=&
                 this%valence_content(old_is_parton%lha_flavor)+1
         end if
      else
         !this is a q->qg splitting. the new initial state quark emits the
```

```
!preceding initial state gluon. yeah, backward evolution is confusing!
             !the new initial state quark is not part of the proton remnant any longer.
             !how do we remove a quark from the remnant? we add a conjugated twin
             !parton and assume, that this twin is created in a not yet resolved
             !g->qqbar splitting.
             call this%push_twin(new_id,lha_flavor,momentum_fraction,gev_scale)
          end if
       end if
       !everything is done. what shall we do with the old initial state parton?
       !we don't need it any more but we store it anyway for future FSR extension.
       call this%fs_partons%push(old_is_parton)
       !the new initial state parton has taken away momentum, so we update the remnant
       !momentum fraction.
       this%momentum fraction=&
       this%momentum_fraction*(1-momentum_fraction)/(1-old_is_parton%momentum)
    else
       !this indicates a bug.
       print *,"proton_remnant_replace_is_parton: parton #",old_id,&
       " not found on ISR stack."
       if(associated(this%is_partons%next))then
          print *,"actual content of isr stack:"
          call this%is_partons%next%print_peers()
          print *,"isr stack is not associated."
       end if
       STOP
    end if
  end subroutine proton_remnant_replace_is_parton
proton remnant calculate weight \
Die Wichtungsfaktoren [W_G, W_S, W_{d^V}, W_{u^V}, W_Q] aus (??) werden bestimmt.
  subroutine proton_remnant_calculate_weight(this,GeV_scale)
    class(proton_remnant_type),intent(inout)::this
    real(kind=double),intent(in)::GeV_scale
    real(kind=double)::all,gluon,sea,vu,vd,valence,twin,weight
    !Die 1 aus (??)
    call this%pdf_norm%get_norm(GeV_scale,1,0,all)
    !Die Impulsmittelwerte
    call this%pdf_norm%get_norm(GeV_scale,1,pdf_int_kind_gluon,gluon)
    call this%pdf_norm%get_norm(GeV_scale,1,pdf_int_kind_sea,sea)
    call this%pdf_norm%get_norm(GeV_scale,1,pdf_int_kind_val_down,vd)
    call this%pdf_norm%get_norm(GeV_scale,1,pdf_int_kind_val_up,vu)
    !Wir multiplizieren die Valenzbeiträge mit dem Valenz-Inhalt-Faktor.
    valence=&
         vd*this%valence_content(lha_flavor_d)+&
         vu*this%valence_content(lha_flavor_u)/2D0
    !Die Quasivalenzquark-Beiträge werden auf die Summe aller LHAPDF-Mittelwerte normiert.
    !(siehe pdfnorm_type)
    twin=this%twin_norm/all
    !(siehe Tabelle ?? mit w→weight)
```

```
select case(remnant_weight_model)
    case(0) ! no reweighting
       this%pdf_int_weight=[1D0,1D0,1D0,1D0,1D0]
    case(2) !pythia-like, only sea
       weight=(1D0-valence-twin)&
            &/(sea+gluon)
       this%pdf_int_weight=[weight,weight,1D0,1D0,1D0]
    case(3) !only valence and twin
       weight=(1D0-sea-gluon)&
            &/(valence+twin)
       this%pdf_int_weight=[1D0,1D0,weight,weight,weight]
    case(4) !only sea and twin
       weight=(1D0-valence)&
            &/(sea+gluon+twin)
       this%pdf_int_weight=[1D0,weight,1D0,1D0,weight]
    case default !equal weight
       weight=1D0/(valence+sea+gluon+twin)
       this%pdf_int_weight=[weight,weight,weight,weight]
    end select
    this%pdf_int_weight(pdf_int_kind_val_down)=&
      this%pdf_int_weight(pdf_int_kind_val_down)*this%valence_content(1)
    this%pdf_int_weight(pdf_int_kind_val_up)=&
      this%pdf_int_weight(pdf_int_kind_val_up)*this%valence_content(2)*5D-1
  end subroutine proton_remnant_calculate_weight
Überschriebene serializable class Methoden
proton remnant write to marker \( \ext{\chi} \)
  subroutine proton_remnant_write_to_marker(this,marker,status)
    class(proton_remnant_type),intent(in)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("proton_remnant_type")
    call marker%mark("valence_content",this%valence_content)
    call marker%mark("momentum_fraction",this%momentum_fraction)
    call marker%mark("pdf_int_weight",this%pdf_int_weight)
    call marker%mark_end("proton_remnant_type")
  end subroutine proton_remnant_write_to_marker
proton remnant read from marker \( \)
  subroutine proton_remnant_read_from_marker(this,marker,status)
    class(proton_remnant_type),intent(out)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    character(:),allocatable::name
    call marker%pick_begin("proton_remnant_type",status=status)
    call marker%pick("valence_content",this%valence_content,status)
    call marker%pick("momentum_fraction",this%momentum_fraction,status)
    call marker%pick("pdf_int_weight",this%pdf_int_weight,status)
```

```
call marker%pick_end("proton_remnant_type",status=status)
  end subroutine proton_remnant_read_from_marker
proton remnant print to unit \
  subroutine proton_remnant_print_to_unit(this,unit,parents,components,peers)
    class(proton_remnant_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    write(unit, '("Components of proton_remnant_type:")')
    write(unit,'("Valence Content:
                                             ",I1,":",I1)')this&
         &%valence_content
    write(unit, '("N Twins:
                                             ",I1)')this%n_twins
    write(unit,'("INT weights [g,s,d,u,t] ",5(F7.3))')this%pdf_int_weight
    write(unit, '("Total Momentum Fraction: ",F7.3)')this%momentum_fraction
    write(unit,'("Twin Norm:
                                        ",F7.3)')this%twin_norm
  end subroutine proton_remnant_print_to_unit
proton remnant get type †
  pure subroutine proton_remnant_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="proton_remnant_type")
  end subroutine proton_remnant_get_type
proton remnant gnuplot momentum kind pdf array \( \)
```

Außerhalb dieser Prozedur müssen zwei Dateien mit formatiertem, sequentiellen Schreibzugriff geöffnet werden und die assoziierten units an momentum\_unit und parton\_unit übergeben werden. Dann wird  $[x_j, \sum_k f_k(x_j, \mu), \{f_k(x_j, \mu)\}], j = 1..100$  nach parton\_unit und  $[x_j, \sum_k x_j f_k(x_j, \mu), x_j \{f_k(x_j, \mu)\}], j = 1..100$ 1..100 nach momentum\_unit geschrieben. k sind alle einzelnen Beiträge zur Strukturfunktion mit  $k = [v^d, v^u, \overline{\{q\}}, g, \{q\}, \{Q\}], \{q\} \text{ sind alle Flavor und } \{Q\} \text{ alle Quasivalenzquarks.}$ 

```
subroutine proton_remnant_gnuplot_momentum_kind_pdf_array&
  (this, momentum_unit, parton_unit, GeV_scale)
  class(proton_remnant_type),intent(in)::this
  integer,intent(in)::momentum_unit,parton_unit
  real(kind=double),intent(in)::GeV_scale
  real(kind=double), dimension(2)::valence_pdf
  real(kind=double), dimension(-6:6)::sea_pdf
  real(kind=double), dimension(this%n_twins)::twin_pdf
  integer::x
  real(kind=double)::momentum_fraction
  do x=1,100
     momentum_fraction=x*1D-2
     call this%momentum_kind_pdf_array(GeV_scale,momentum_fraction&
          &, valence_pdf, sea_pdf)
     call this % momentum_twin_pdf_array (momentum_fraction, twin_pdf)
     write(momentum_unit,fmt=*)momentum_fraction,&
          sum(valence_pdf)+sum(sea_pdf)+sum(twin_pdf),&
          valence_pdf,&
          sea_pdf,&
          twin_pdf
```

#### 5.5.4 Methoden für pp remnant type

#### pp remnant initialize \

Der Hauptzweck dieser Prozedur ist es, die Impulsmittelwerte  $\langle f \rangle$  ( $\mu$ ) =  $\int dx \ x f(x, \mu)$  bereitzustellen. Im Verzeichnis muli\_dir wird nach integrierten PDFs, passend zu dem verwendeten LHAPDF-Set, gesucht. Wenn sie existierten, werden sie deserialisiert, sonst werden sie neu generiert und serialisiert.

```
subroutine pp_remnant_initialize(&
     this,&
     muli_dir,&
     lhapdf_dir,&
     lhapdf_file,&
     lhapdf_member)
  class(pp_remnant_type),intent(out)::this
  character(*),intent(in)::muli_dir,lhapdf_dir,lhapdf_file
  integer,intent(in)::lhapdf_member
  logical::exist
  allocate(this%pdf_norm)
  print *,"looking for previously generated pdf integrals..."
  inquire(file=muli_dir//"/pdf_norm_"//lhapdf_file//".xml",exist=exist)
  if(exist)then
     print *,"found. Starting deserialization..."
     call this%pdf_norm%deserialize(&
          name="pdf_norm_"//lhapdf_file,&
          file=muli_dir//"/pdf_norm_"//lhapdf_file//".xml")
     print *,"done."
  else
     print *,"No integrals found. Starting generation..."
     call this%pdf_norm%scan()
     print *,"done."
     call this % pdf_norm % serialize (&
          name="pdf_norm_"//lhapdf_file,&
          file=muli_dir//"/pdf_norm_"//lhapdf_file//".xml")
  end if
  call this%proton(1)%initialize(this%pdf_norm)
  call this%proton(2)%initialize(this%pdf_norm)
  this%initialized=.true.
end subroutine pp_remnant_initialize
```

```
pp remnant finalize \( \ \)
```

```
Die Impulsmittelwerte in pp_remnant_type\%pdf_norm werden deallokiert und Zeiger darauf deassoziiert.
```

```
subroutine pp_remnant_finalize(this)
    class(pp_remnant_type),intent(inout)::this
    call this%proton(1)%finalize()
    call this%proton(2)%finalize()
    deallocate(this%pdf_norm)
  end subroutine pp_remnant_finalize
pp remnant apply initial interaction \( \ \)
Wrapper für proton remnant type%apply initial splitting
  subroutine pp_remnant_apply_initial_interaction&
  (this,gev_cme,x1,x2,pdg_f1,pdg_f2,n1,n2,gev_scale,rnd1,rnd2)
    class(pp_remnant_type),intent(inout)::this
    real(kind=double),intent(in)::gev_cme,x1,x2,gev_scale,rnd1,rnd2
    integer,intent(in)::pdg_f1,pdg_f2,n1,n2
    if(this%initialized)then
       call this%proton(1)%apply_initial_splitting(n1,pdg_f1,x1,gev_scale,rnd1)
       call this%proton(2)%apply_initial_splitting(n2,pdg_f2,x2,gev_scale,rnd2)
       this %X = (1D0 - x1) * (1D0 - x2)
       this%gev_initial_cme=gev_cme
    else
       print *,"pp_remnant_apply_initial_interaction:"
       print *,"Not yet initialized, call pp_remnant_initialize first!"
       stop
    end if
  end subroutine pp_remnant_apply_initial_interaction
pp remnant replace parton \( \)
Wrapper für proton remnant type%replace is parton
  subroutine pp_remnant_replace_parton(this,proton_id,old_id,new_id,pdg_f,x_proton,gev_scale
    class(pp_remnant_type),intent(inout)::this
    integer,intent(in)::proton_id,old_id,new_id,pdg_f
    real(kind=double),intent(in)::x_proton,gev_scale
    call this%proton(proton_id)%replace_is_parton(old_id,new_id,pdg_f,x_proton,gev_scale)
  end subroutine pp_remnant_replace_parton
pp remnant momentum pdf \( \ \)
  subroutine pp_remnant_momentum_pdf(this,x_proton,gev2_scale,n,pdg_f,pdf)
    class(pp_remnant_type),intent(in)::this
    real(kind=double),intent(in)::x_proton,gev2_scale
    integer, intent(in)::n,pdg_f
    real(kind=double),intent(out)::pdf
    !Von welchem Remnant wollen wir die Momentum PDF haben?
    !Es muss das erste oder das zweite sein.
    if(n==1.or.n==2)then
       !Der Impulsanteil $x$ ist auf den Impuls des ungestörten Protons bezogen,
```

```
!deswegen darf es nicht zwischen 0 und 1 sein, sondern nur zwischen 0 und $X$.
       if(x_proton<=this%proton(n)%momentum_fraction)then</pre>
          !momentum_flavor_pdf erwartet Flavor im PDG-Schema.
          !Das Gluon muss entsprechend konvertiert werden.
          if(pdg_f==pdg_flavor_g)then
             call this%proton(n)%momentum_flavor_pdf(&
                  sqrt(GeV2_scale),&
                  !momentum_flavor_pdf erwartet Impulsanteile, die auf die Remnantimpulse
                  !bezogen sind.
                  x_proton/this%proton(n)%momentum_fraction,&
                  lha_flavor_g,&
                  pdf&
                  )
          else
             call this%proton(n)%momentum_flavor_pdf(&
                  sqrt(GeV2_scale),x_proton/this%proton(n)%momentum_fraction,pdg_f,pdf&
                  )
          end if
          !Durch die Transformation des Arguments müssen auch die Funktionswerte
          !angepasst werden.
          pdf=pdf*this%proton(n)%momentum_fraction
       else
          pdf=0D0
       end if
    else
       print *,"pp_remnant_momentum_pdf: n must be either 1 or 2, but it is ",n
    end if
  end subroutine pp_remnant_momentum_pdf
pp remnant parton pdf \( \ \)
 subroutine pp_remnant_parton_pdf(this,x_proton,gev2_scale,n,pdg_f,pdf)
    class(pp_remnant_type),intent(in)::this
    real(kind=double),intent(in)::x_proton,gev2_scale
    integer,intent(in)::n,pdg_f
    real(kind=double),intent(out)::pdf
    if(n==1.or.n==2)then
       if(x_proton<=this%proton(n)%momentum_fraction)then
          if(pdg_f==pdg_flavor_g)then
             call this%proton(n)%parton_flavor_pdf(&
                  sqrt(GeV2_scale),&
                  x_proton*(1D0-this%proton(n)%momentum_fraction),&
                  lha_flavor_g,&
                  pdf&
          else
             call this%proton(n)%parton_flavor_pdf(&
                  sqrt(GeV2_scale),&
                  x_proton*(1D0-this%proton(n)%momentum_fraction),&
                  pdg_f,&
```

```
pdf&
    )
    end if
    pdf=pdf/(1D0-this%proton(n)%momentum_fraction)
    else
        pdf=0D0
    end if
    else
        print *,"pp_remnant_parton_pdf: n must be either 1 or 2, but it is ",n stop
    end if
end subroutine pp_remnant_parton_pdf
```

#### pp\_remnant\_apply\_interaction \

Den Remnants wird mitgeteilt, dass eine Wechselwirkung stattgefunden hat. Alle Informationen über diese Wechselwirkung liegen in einer Instanz vom Typ muli\_type. Um sie zu erreichen, wird ein Dummyargument der Klasse qcd\_2\_2\_type, die von muli\_type erweitert wird, deklariert.

Hier geschieht nichts, außer dass das Stratum  $\{\alpha, \beta\}$  explizit als Ganzzahlen-Doublet in  $int\_k$  abgelegt wird und für beide Remnants this%proton(1) und this%proton(2) die entsprechende Methoden aus der Menge  $\{\text{proton\_remnant\_type}\%\text{remove\_valence\_down\_quark}, \text{proton\_remnant\_type}\%\text{remove\_valence\_up} \text{proton\_remnant\_type}\%\text{remove\_sea\_quark}, \text{proton\_remnant\_type}\%\text{remove\_gluon}\}$  aufgerufen wird.

```
subroutine pp_remnant_apply_interaction(this,qcd_2_2)
  class(pp_remnant_type),intent(inout)::this
  class(qcd_2_2_class),intent(in)::qcd_2_2
  integer, dimension (4)::lha_f
  integer, dimension(2)::int_k
  real(kind=double)::gev_pt
  real(kind=double),dimension(2)::mom_f
  integer::n
 mom_f=qcd_2_2%get_remnant_momentum_fractions()
  lha_f=qcd_2_2%get_lha_flavors()
  int_k=qcd_2_2%get_pdf_int_kinds()
  gev_pt=qcd_2_2%get_gev_scale()
  do n=1,2
     select case (int_k(n))
     case(pdf_int_kind_val_down)
        call this%proton(n)%remove_valence_down_quark(&
          qcd_2_2%get_parton_id(n),&
          gev_pt,&
          mom_f(n)
     case(pdf_int_kind_val_up)
        call this%proton(n)%remove_valence_up_quark(&
          qcd_2_2%get_parton_id(n),&
          gev_pt,&
          mom_f(n)
     case(pdf_int_kind_sea)
        call this%proton(n)%remove_sea_quark(&
        qcd_2_2%get_parton_id(n),&
        gev_pt,&
```

```
mom_f(n),&
          lha_f(n))
       case(pdf_int_kind_gluon)
          call this%proton(n)%remove_gluon(&
          qcd_2_2%get_parton_id(n),&
          gev_pt,&
          mom_f(n)
       end select
    end do
    this%X=this%proton(1)%momentum_fraction*this%proton(2)%momentum_fraction
  end subroutine pp_remnant_apply_interaction
pp_remnant reset ↑
  subroutine pp_remnant_reset(this)
    class(pp_remnant_type),intent(inout)::this
    call this%proton(1)%reset()
    call this%proton(2)%reset()
    this%X=1D0
  end subroutine pp_remnant_reset
pp remnant get pdf int weights \
  pure function pp_remnant_get_pdf_int_weights(this,pdf_int_kinds) result(weight)
    class(pp_remnant_type),intent(in)::this
    real(kind=double)::weight
    integer,dimension(2),intent(in)::pdf_int_kinds ! pdf_int_kind
    weight=this%proton(1)%pdf_int_weight(pdf_int_kinds(1))&
          *this%proton(2)%pdf_int_weight(pdf_int_kinds(2))
  end function pp_remnant_get_pdf_int_weights
pp remnant get pdf int weight \
  elemental function pp_remnant_get_pdf_int_weight(this,kind1,kind2) result(weight)
    class(pp_remnant_type),intent(in)::this
    real(kind=double)::weight
    integer,intent(in)::kind1,kind2 ! pdf_int_kind
    weight=this%proton(1)%pdf_int_weight(kind1)&
          *this%proton(2)%pdf_int_weight(kind2)
  end function pp_remnant_get_pdf_int_weight
pp remnant set pdf weight \
  subroutine pp_remnant_set_pdf_weight(this,weights)
    class(pp_remnant_type),intent(inout)::this
    real(kind=double), dimension(10), intent(in)::weights
    this%proton(1)%pdf_int_weight=weights(1:5)
    this%proton(2)%pdf_int_weight=weights(6:10)
  end subroutine pp_remnant_set_pdf_weight
pp remnant get gev initial cme \( \)
```

```
elemental function pp_remnant_get_gev_initial_cme(this) result(cme)
    class(pp_remnant_type),intent(in)::this
    real(kind=double)::cme
    cme=this%gev_initial_cme
  end function pp_remnant_get_gev_initial_cme
pp remnant get gev actual cme \( \)
  elemental function pp_remnant_get_gev_actual_cme(this) result(cme)
    class(pp_remnant_type),intent(in)::this
    real(kind=double)::cme
    cme=this%gev_initial_cme*this%X
  end function pp_remnant_get_gev_actual_cme
pp remnant get cme fraction \( \ \)
  elemental function pp_remnant_get_cme_fraction(this) result(cme)
    class(pp_remnant_type),intent(in)::this
    real(kind=double)::cme
    cme=this%X
  end function pp_remnant_get_cme_fraction
pp remnant get proton remnant momentum fractions \( \)
  pure function pp_remnant_get_proton_remnant_momentum_fractions(this) result(fractions)
    class(pp_remnant_type),intent(in)::this
    real(kind=double), dimension(2)::fractions
    fractions=[&
      this%proton(1)%get_momentum_fraction(),&
      this%proton(2)%get_momentum_fraction()]
  end function pp_remnant_get_proton_remnant_momentum_fractions
pp remnant get proton remnants \( \)
  subroutine pp_remnant_get_proton_remnants(this,proton1,proton2)
    class(pp_remnant_type), target, intent(in)::this
    class(proton_remnant_type),intent(out),pointer::proton1,proton2
    proton1=>this%proton(1)
    proton2=>this%proton(2)
  end subroutine pp_remnant_get_proton_remnants
pp remnant get remnant parton flavor pdf arrays \( \)
  subroutine pp_remnant_get_remnant_parton_flavor_pdf_arrays&
    (this, GeV_scale, momentum1, momentum2, pdf1, pdf2)
    class(pp_remnant_type),intent(in)::this
    real(kind=double),intent(in)::GeV_scale,momentum1,momentum2
    real(kind=double), dimension(-6:6), intent(out)::pdf1,pdf2
    call this%proton(1)%parton_flavor_pdf_array(GeV_scale,momentum1,pdf1)
    call this%proton(2)%parton_flavor_pdf_array(GeV_scale,momentum2,pdf2)
  end subroutine pp_remnant_get_remnant_parton_flavor_pdf_arrays
```

!overridden procedures

```
pp remnant write to marker \( \ \)
  subroutine pp_remnant_write_to_marker(this,marker,status)
    class(pp_remnant_type),intent(in)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("pp_remnant_type")
    call marker%mark("gev_initial_cme",this%gev_initial_cme)
    call marker%mark("X",this%X)
    call this%proton(1)%write_to_marker(marker,status)
    call this%proton(2)%write_to_marker(marker,status)
    call marker%mark_end("pp_remnant_type")
  end subroutine pp_remnant_write_to_marker
pp remnant read from marker \( \ \)
  subroutine pp_remnant_read_from_marker(this,marker,status)
    class(pp_remnant_type),intent(out)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    character(:),allocatable::name
    call marker%pick_begin("pp_remnant_type",status=status)
    call marker%pick("gev_initial_cme",this%gev_initial_cme,status)
    call marker%pick("X",this%X,status)
    call this%proton(1)%read_from_marker(marker,status)
    call this%proton(2)%read_from_marker(marker,status)
    call marker%pick_end("pp_remnant_type",status=status)
  end subroutine pp_remnant_read_from_marker
pp remnant print to unit \ \ \
  subroutine pp_remnant_print_to_unit(this,unit,parents,components,peers)
    class(pp_remnant_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    write(unit,'("Components of pp_remnant_type:")')
    write(unit,'("Initial center of mass energy: ",F10.3)')this%gev_initial_cme
    write(unit,'("Actual center of mass energy: ",F10.3)')this%get_gev_actual_cme()
    write(unit,'("Total Momentum Fraction is:
                                                ",F10.3)')this%X
    if(components>0)then
       write(unit,'("Proton 1:")')
       call this%proton(1)%print_to_unit(unit,parents,components-1,peers)
       write(unit,'("Proton 2:")')
       call this%proton(2)%print_to_unit(unit,parents,components-1,peers)
  end subroutine pp_remnant_print_to_unit
pp remnant_get_type \( \)
  pure subroutine pp_remnant_get_type(type)
    character(:),allocatable,intent(out)::type
```

```
allocate(type,source="pp_remnant_type")
end subroutine pp_remnant_get_type
```

### 5.5.5 Sonstige Prozeduren

```
remnant\_dglap\_splitting\_gqq
```

Der DGLAP-Splitting Kernel für ein  $g \to q\bar{q}$  Splitting.

```
pure function remnant_dglap_splitting_gqq(z) result(p)
  real(kind=double)::p
  real(kind=double),intent(in)::z
  p=(z**2+(1-z)**2)/2D0
end function remnant_dglap_splitting_gqq
```

#### remnant gluon pdf approx

Die Approximation der Gluon-Momentum-PDF. p ist Parameter der Approximation, üblicherweise wird er auf 4 gesetzt. Die Wahl von p wird in muli remnant%gluon exp festgelegt.

```
pure function remnant_gluon_pdf_approx(x,p) result(g)
  real(kind=double)::g
  integer,intent(in)::p
  real(kind=double),intent(in)::x
  g=((1-x)**p)/x
end function remnant_gluon_pdf_approx
```

#### remnant norm 0

Der reziproke Normierungsfaktor der Quasivalenzverteilung für p=0. xs ist der Impulsanteil des Seequarks.

```
pure function remnant_norm_0(xs) result(c0)
  real(kind=double)::c0
  real(kind=double),intent(in)::xs
  c0=6*xs/(2-xs*(3-3*xs+2*xs**2))
end function remnant_norm_0
```

#### $remnant\_norm\_1$

Der reziproke Normierungsfaktor der Quasivalenzverteilung für p=1. xs ist der Impulsanteil des Seequarks.

```
pure function remnant_norm_1(xs) result(c1)
  real(kind=double)::c1
  real(kind=double),intent(in)::xs
  c1=3*xs/(2-xs**2*(3-xs)+3*xs*log(xs))
end function remnant_norm_1
```

#### remnant norm 4

Der reziproke Normierungsfaktor der Quasivalenzverteilung für p=4. xs ist der Impulsanteil des Seequarks.

```
pure function remnant_norm_4(xs) result(c4)
    real(kind=double)::c4
    real(kind=double),intent(in)::xs
    real(kind=double)::y
    if((1D0-xs)>1D-3)then
       c4=3*xs/&
       (1 + 11*xs + 6*xs*log(xs) + 12*xs**3*log(xs) + 18*xs**2*log(xs)&
          + 9*xs**2 - 19*xs**3 - 2*xs**4)
    else
       y=1D0/(1D0-xs)
       c4=&
            &1130D0/11907D0&
            & -10D0 *y**5&
            & -40D0 *y**4/3D0&
            & -160D0*y**3/63D0&
            & +50D0 *y**2/189D0&
            & -565D0*y
                         /3969D0&
            & -186170D0*(1D0-xs)/2750517D0
    end if
  end function remnant_norm_4
remnant norm
Der reziproke Normierungsfaktor der Quasivalenzverteilung für p. xs ist der Impulsanteil des See-
quarks.
  pure function remnant_norm(xs,p) result(c)
    real(kind=double)::c
    real(kind=double),intent(in)::xs
    integer,intent(in)::p
    select case (p)
    case(0)
       c=remnant_norm_0(xs)
    case(1)
       c=remnant_norm_1(xs)
    case default
       c=remnant_norm_4(xs)
    end select
  end function remnant_norm
remnant twin pdf p
Der normierte, aber ungewichtete Quasivalenzbeitrag f_{qQ}(x, \overline{x}) mit xs = \overline{x}.
  pure function remnant_twin_pdf_p(x,xs,p) result(qc)
    real(kind=double)::qc
    real(kind=double),intent(in)::x,xs
```

integer,intent(in)::p
qc=remnant\_norm(xs,p)\*&

end function remnant\_twin\_pdf\_p

remnant\_gluon\_pdf\_approx(xs+x,p)\*&

remnant\_dglap\_splitting\_gqq(xs/(xs+x))/(xs+x)

```
remnant twin momentum 4
```

```
Der Impulsmittelwert des normierten, aber ungewichteten Quasivalenzbeitrags \langle f_{qQ} \rangle(\overline{x}) = \int dx \, x f_{qQ}(x, \overline{x}) mit xs = \overline{x}.
```

#### gnuplot integrated pdf

Zu Debuggingzwecken können die integrierten PDFs geplottet werden.

```
subroutine gnuplot_integrated_pdf(this,momentum_unit,parton_unit)
  class(proton_remnant_type),intent(in)::this
  integer,intent(in)::momentum_unit,parton_unit
  integer, parameter::x_grid=1000000
  integer, parameter::q_grid=100
  integer::n,m,mem
  real(kind=double)::x,q,dx,dq,overall_sum,xmin,xmax,q2min,q2max,qmin,qmax
  real(kind=double),dimension(-6:6)::sea_pdf,sea_momentum_pdf_sum,sea_parton_pdf_sum
 real(kind=double),dimension(2)::valence_pdf,valence_momentum_pdf_sum,valence_parton_pdf_s
  real(kind=double),allocatable,dimension(:)::twin_momentum_pdf_sum
  class(parton_type),pointer::tmp_twin
 mem=1
  call GetXmin(mem,xmin)
  call GetXmax(mem,xmax)
  call GetQ2max(mem,q2max)
  call GetQ2min(mem,q2min)
  qmin=sqrt(q2min)
  qmax=sqrt(q2max)
  print *,"qmin=",qmin,"GeV"
  print *,"qmax=",qmax,"GeV"
  dx=(xmax-xmin)/x_grid
  dq=(qmax-qmin)/q_grid
  q=qmin+dq/2D0
  tmp_twin=>this%twin_partons%next
 n=0
  if(this%n_twins>0)then
     allocate(twin_momentum_pdf_sum(this%n_twins))
     do while(associated(tmp_twin))
        twin_momentum_pdf_sum(n)=tmp_twin%momentum
        tmp_twin=>tmp_twin%next
     end do
  end if
```

```
do m=1,q_grid
    valence_momentum_pdf_sum=[0D0,0D0]
    valence_parton_pdf_sum=[0D0,0D0]
    x=xmin+dx/2D0
    do n=1,x_grid
       call this%parton_kind_pdf_array(Q,x,valence_pdf,sea_pdf)
       valence_parton_pdf_sum=valence_parton_pdf_sum+valence_pdf
       sea_parton_pdf_sum=sea_parton_pdf_sum+sea_pdf
       call this%momentum_kind_pdf_array(Q,x,valence_pdf,sea_pdf)
       valence_momentum_pdf_sum=valence_momentum_pdf_sum+valence_pdf
       sea_momentum_pdf_sum=sea_momentum_pdf_sum+sea_pdf
       x=x+dx
    end do
    valence_parton_pdf_sum=valence_parton_pdf_sum*dx
    sea_parton_pdf_sum=sea_parton_pdf_sum*dx
    valence_momentum_pdf_sum=valence_momentum_pdf_sum*dx
    sea_momentum_pdf_sum=sea_momentum_pdf_sum*dx
    if(this%n_twins>0)then
       write(momentum_unit,fmt=*)q,&
           sum(valence_momentum_pdf_sum)&
            +sum(sea_momentum_pdf_sum)&
            +sum(twin_momentum_pdf_sum),&
           valence_momentum_pdf_sum,&
           sea_momentum_pdf_sum, &
           twin_momentum_pdf_sum
    else
       write(momentum_unit,fmt=*)q,&
           sum(valence_momentum_pdf_sum)+sum(sea_momentum_pdf_sum),&
           valence_momentum_pdf_sum, &
           sea_momentum_pdf_sum
    end if
    write(parton_unit,fmt=*)q,&
         sum(valence_parton_pdf_sum)+sum(sea_parton_pdf_sum),&
         valence_parton_pdf_sum,&
         sea_parton_pdf_sum
    q=q+dq
 end do
end subroutine gnuplot_integrated_pdf
```

 $5\ Modul\ muli\_remnant$ 

# 6 Modul muli dsigma

Hier wird eine Approximation der Stammstrati  $S(p_{\perp})$  aus (??) bereitgestellt. Die Integrationen in (??) werden mit der externen Bibliothek libcuba ausgewertet, die verbleibende Integration in (??) wird mit dem muli-eigenen Modul muli aq ausgewertet.

Zu Beginn hatte ich mit verschiedenen Darstellungen der Wirkungsquerschnitte und mit verschiedenen Integrationsparametern und verschiedenen Einteilungen in Strati experimentiert. Um Codevervielfältigung zu vermeiden hatte ich dann den Code für die Integration von den Wirkungsquerschnitten getrennt. Da die Wirkungsquerschnitte auf Parameter zugreifen müssen, die nicht fur alle Darstellungen gleich sind, konnte ich die Integraden nicht als Funktion an aq\_class übergeben. Stattdessen habe ich mich entschieden, die verschiedenen Varianten durch Überladen der Methode evaluate zu erzeugen. So konnten die Erweiterung von aq\_class komplett verschiedene Methoden zur Auswertung von (??), und dennoch dieselbe Quadratur für (??) verwenden. Heute ist nur noch eine einzige Erweiterung übrig, nämlich muli\_dsigma\_type in diesem Modul. Deswegen ist der Sinn zwischen der Aufteilung der Module muli\_aq und muli\_dsigma nicht mehr offensichtlich.

## 6.1 Abhängigkeiten

```
use muli_momentum
use muli_interactions
use muli_cuba
use muli_aq
```

#### 6.2 Parameter

```
!Die Anzahl der Strati plus 1, für die Summe aller Strati.
integer,parameter,private::dim_f=17
```

## 6.3 Derived Types

## 6.3.1 muli\_dsigma\_type

Der Zweck von muli\_dsigma\_type liegt darin, die abstrakte Methode evaluate von aq\_class zu implementieren und so einen Integradem für die nummerische Integration bereitzustellen. Weiterhin stellt aq\_class die Methode muli\_dsigma\_type%generate zur Verfügung, um die Integration zu starten.

Für das setzten der Faktorisierungsskala wird eine eigene Instanz muli\_dsigma\_type%pt des Datentyps transversal\_momentum\_type verwendet. Eigen bedeutet, dass muli\_dsigma\_type%pt nicht mit der muli-Skala synchronisiert ist, denn diese Integration findet vor der Eventgenerierung mit MULI statt.

```
type,public,extends(aq_class) :: muli_dsigma_type
  private
  type(transversal_momentum_type)::ptpt
   type(cuba_divonne_type) :: cuba_intcuba_int
 contains
   !Überschriebene serializable_class Methoden
  procedure::write_to_marker=>muli_dsigma_write_to_marker
  procedure::read_from_marker=>muli_dsigma_read_from_marker
  procedure::print_to_unit=>muli_dsigma_print_to_unit
  procedure,nopass::get_type=>muli_dsigma_get_type
   !Originäre muli_dsigma_type Methoden
  procedure :: generate=>muli_dsigma_generate
  procedure :: evaluate=>muli_dsigma_evaluate
  procedure :: muli_dsigma_initialize
  generic :: initialize=>muli_dsigma_initialize
end type muli_dsigma_type
```

## 6.4 Implementierung der Prozeduren

```
6.4.1 Methoden für muli dsigma type
```

```
muli dsigma write to marker \( \ \)
  subroutine muli_dsigma_write_to_marker(this, marker, status)
    class(muli_dsigma_type), intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik), intent(out) :: status
    ! local variables
    class(serializable_class),pointer::ser
    call marker%mark_begin("muli_dsigma_type")
    call aq_write_to_marker(this,marker,status)
    call this%cuba_int%serialize(marker, "cuba_int")
    call marker%mark_end("muli_dsigma_type")
  end subroutine muli_dsigma_write_to_marker
muli dsigma read from marker \( \)
  subroutine muli_dsigma_read_from_marker(this,marker,status)
    class(muli_dsigma_type), intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik), intent(out) :: status
    ! local variables
    call marker%pick_begin("muli_dsigma_type",status=status)
    call aq_read_from_marker(this,marker,status)
    call this%cuba_int%deserialize("cuba_int", marker)
    call marker%pick_end("muli_dsigma_type",status)
  end subroutine muli_dsigma_read_from_marker
muli dsigma print to unit \( \ \)
```

```
subroutine muli_dsigma_print_to_unit(this,unit,parents,components,peers)
    class(muli_dsigma_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    integer::ite
    if(parents>0)call aq_print_to_unit(this,unit,parents-1,components,peers)
    write(unit,'("Components of muli_dsigma_type")')
    if(components>0)then
       write(unit,fmt=*)"Printing components of cuba_int:"
       call this%cuba_int%print_to_unit(unit,parents,components-1,peers)
    else
       write(unit,fmt=*)"Skipping components of cuba_int:"
    end if
  end subroutine muli_dsigma_print_to_unit
muli dsigma get type †
  pure subroutine muli_dsigma_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="muli_dsigma_type")
  end subroutine muli_dsigma_get_type
muli dsigma generate \( \)
Initialisierung und Generierung der Stammstrati \mathcal{S}.
Man kann eine Start-Segmentierung des Integrationsbereichs angeben. Dadurch kann die Integration
erheblich beschleunigt werden. Wir wählen eine Segmentierung in initial values so, dass \mu_i = \mu_0 \exp(j),
solange \mu_i < \sqrt{s}/2 und nehmen als letzten Wert \sqrt{s}/2 hinzu.
  subroutine muli_dsigma_generate(this,gev2_scale_cutoff,gev2_s,int_tree)
    class(muli_dsigma_type),intent(inout)::this
    real(kind=drk),intent(in)::gev2_scale_cutoff,gev2_s
    type(muli_trapezium_tree_type),intent(out)::int_tree
    real(kind=drk),dimension(ceiling(log(gev2_s/gev2_scale_cutoff)/2D0))::initial_values
    integer::n
    !Debugging
    print *,gev2_s/gev2_scale_cutoff,ceiling(log(gev2_s/gev2_scale_cutoff)/2D0)
    !Setzen der Start-Segmentierung
    initial_values(1)=sqrt(gev2_scale_cutoff/gev2_s)*2D0
    do n=2, size(initial values)-1
       initial_values(n)=initial_values(n-1)*euler
    end do
    initial_values(n)=1D0
    !Debugging
    print *,initial_values
    !Wir geben dieser Instanz einen Namen und die Nummer 1.
    call identified_initialize(this, one, "dsigma")
    !Die Skala wird initialisiert.
    call this%pt%initialize(gev2_s)
    !Die Genauigkeit der Stammfunktion (??)
    this%abs_error_goal = 0D0
    this%rel_error_goal=scale(1D0,-12)!-12
```

```
this%max_nodes=1000
    !Dimension und Genauigkeit der Integration (??)
    call this%cuba_int%set_common(&
         &dim_f=dim_f,&
         \&dim_x=2,\&
         &eps_rel=scale(this%rel_error_goal,-8),&!-8
         &flags = 0)
    !Die ungefähre Position der Maxima des Integranden
    call this%cuba_int%set_deferred&
      (xgiven_flat=[1D-2,5D-1+epsilon(1D0),1D-2,5D-1-epsilon(1D0)])
    print *,"muli_dsigma_generate:"
    print *,"Overall Error Goal: ",this%rel_error_goal
    !Wir initialisieren die Integration mit der Start-Segmentierung
    call this%init_error_tree(dim_f,initial_values)
    !Die eigentliche Integration
    call this%run()
    !Konvertierung der internen Darstellung mittels fibonacci_root_type
    !in ein bessere Darstellung mittels muli_trapezium_tree_type.
    call this%integrate(int_tree)
    !Aufräumen
    call this%err_tree%deallocate_all()
    deallocate(this%err_tree)
    nullify(this%int_list)
  end subroutine muli_dsigma_generate
muli dsigma evaluate †
Die Wahl der Integrationsroutine und der Darstellung der Wirkungsquerschnitte.
  subroutine muli_dsigma_evaluate(this,x,y)
    class(muli_dsigma_type),intent(inout) :: this
    real(kind=double), intent(in) :: x
    real(kind=double), intent(out),dimension(:):: y
    call this%pt%set_unit_scale(x)
    call this%cuba_int%integrate_userdata(&
         interactions_proton_proton_integrand_param_17_reg,this%pt)
    call this%cuba_int%get_integral_array(y)
  end subroutine muli_dsigma_evaluate
muli dsigma initialize \
    subroutine muli_dsigma_initialize(this,id,name,goal,max_nodes,dim,cuba_goal)
      class(muli_dsigma_type),intent(inout) :: this
      integer(kind=dik),intent(in)::id,max_nodes
      integer,intent(in)::dim
      character(*),intent(in)::name
      real(kind=double),intent(in)::goal,cuba_goal
      call identified_initialize(this,id,name)
      this%rel_error_goal = goal!1d-4
      this%max_nodes=max_nodes
      call this%cuba_int%set_common(&
           &dim_f=dim,&
           \&dim_x=2,\&
```

```
&eps_rel=cuba_goal,&!1d-6
    &flags = 0)
call this%cuba_int%set_deferred&
    (xgiven_flat=[1D-2,5D-1+epsilon(1D0),1D-2,5D-1-epsilon(1D0)])
call this%init_error_tree(dim,(/8D-1/7D3,2D-3,1D-2,1D-1,1D0/))
this%is_deferred_initialised = .true.
end subroutine muli_dsigma_initialize
```

6 Modul muli\_dsigma

# 7 Modul muli aq

aq ist eine Abkürzung für adaptive Quadratur. Mit aq\_class kann für eine beliebige Funktion  $f: \mathbb{R} \to \mathbb{R}^n$  die Quasistammfunktion  $F(x) = \int_x^1 f(y) \, dy$  mittels adaptiver Quadratur ausgewertet und als Binärbaum von Segmenten  $s_j = [x_{j-1}, x_j]$  gespeichert werden. Zu jedem Segment werden  $f(x_j), F(x_j)$  und  $\exp[-F(x_j)]$  gespeichert.

f wird mit der Trapezregel approximiert, entsprechend wird F durch Parabeln approximiert. Dennoch ist die Approximation von F nicht gleich Simpsons Regel, denn wir haben nur zwei Stützstellen  $x_{j-1}$  und  $x_j$  für jede Parabel.

Der Integrationsfehler delta  $\delta'$  bzw.  $\delta'$  ergibt sich bei der Spaltung des Segments  $s_j$  in zwei Untersegmente  $s'_j = [x_{j-1}, y]$  und  $s''_j = [y, x_j]$  durch die Differenz des alten und des neuen Integrals:

$$\delta' = \left| \frac{\left( f(y) - f_j(y) \right) \left( x_{j-1} - y \right)}{2} \right| \tag{7.1}$$

$$\delta'' = \left| \frac{\left( f(y) - f_j(y) \right) \left( x_j - y \right)}{2} \right| \tag{7.2}$$

mit der alten Approximation  $f_j$  des alten Segments j

$$f_j(y) = f(x_j) - y \frac{f(x_j) - f(x_{j-1})}{x_j - x_{j-1}}.$$
(7.3)

## 7.1 Abhängigkeiten

```
use muli_basic
use muli_cuba
use muli_trapezium
use muli_fibonacci_tree
```

## 7.2 Derived Types

#### 7.2.1 aq class

```
type,extends(identified_type),abstract :: aq_class
  ! private
  !Erweiterungen müssen durch is_deferred_initialised signalisieren, dass sie bereit sind.
  logical :: is_deferred_initialised = .false.
  !Ist aq_class%err_tree bereit?
  logical :: is_error_tree_initialised = .false.
  !Wurden die internen Fehlerziele bestimmt?
```

```
logical :: is_goal_set = .false.
!Ist alles bereit zur Integration?
logical :: is_initialised = .false.
!Wurde die Integration durchgeführt?
logical :: is_run = .false.
!Wurde das Fehlerziel erreicht?
logical :: is_goal_reached = .false.
!Wurde aq_class%err_tree nach aq_class%int_list konvertiert?
logical :: is_integrated = .false.
!Die aktuelle Anzahl von Segmenten
integer(kind=dik) :: n_nodes = 0
!Die maximale Anzahl von Segmenten
integer(kind=dik) :: max_nodes = 10000
!Die Dimension von f
integer :: dim_integral = 1
!Das gegebene absolute Fehlerziel
real(kind=double) :: abs_error_goal = 0D0
!Das gegebene relative Fehlerziel
real(kind=double) :: rel_error_goal = 0.1D0
!Das berechnete absolute Fehlerziel, basierend auf der aktuellen
!Schätzung des Integrals
real(kind=double) :: scaled_error_goal = 0.0D0
!Schätzung des Integrals F(x_min)
real(kind=double) :: integral = 1D0
!Aktueller absoluter Integrationsfehler
real(kind=double) :: integral_error = 0D0
!Integrationsintervall
real(kind=double),dimension(2) :: region = (/ODO,1DO/)
!Zu Debuggingzwecken wird die Historie des Integrationsfehlers gespeichert.
!Wenn die Historie oszilliert, dann ist der Fehler in f, also in der
!Cuba-Integration zu groß.
real(kind=double),dimension(:,:),allocatable :: convergence
!time stamps um die Performance des Allgorithmus zu überwachen.
real(kind=double) :: total_time = 0
real(kind=double) :: loop_time = 0
real(kind=double) :: int_time = 0
real(kind=double) :: cuba_time = 0
real(kind=double) :: init_time = 0
real(kind=double) :: cpu_time = 0
!These variables *must* be initialised before the main loop may be called.
!Additionaly the nodes and segments should be preprocessed by first_run
!before the main loop may be called.
!Das tatsächliche Fehlerziel.
real(kind=double) :: error_goal = 0D0
!Während der Integration werden die Segmente des Integranden nach ihrem
!Integrationsfehler sortiert in diesem Binärbaum gespeichert.
class(fibonacci_root_type),pointer ::err_tree=>null()
!Nach erfolgreicher Integration werden die Segmente nach dem Skalenparameter
!sortiert in dieser Liste gespeichert.
```

```
class(muli_trapezium_list_type),pointer ::int_list=>null()
contains
   !Überschriebene serializable_class Methoden
   procedure::write_to_marker=>aq_write_to_marker
  procedure::read_from_marker=>aq_read_from_marker
  procedure::print_to_unit=>aq_print_to_unit
   procedure,nopass::get_type=>aq_get_type
  procedure::deserialize_from_marker=>aq_deserialize_from_marker
   !Originäre aq_class Methoden
  procedure :: aq_initialize
            ::initialize=>aq_initialize
   generic
   procedure ::print_times=>aq_print_times
  procedure ::write_convergence=>aq_write_convergence
   ! init/ de-init
  procedure ::reset=>aq_reset
  procedure ::dealloc_trees=>aq_dealloc_trees
  procedure ::finalize=>aq_dealloc_trees
  procedure ::init_error_tree=>aq_init_error_tree
  procedure ::set_rel_goal=>aq_set_rel_goal
  procedure ::set_abs_goal=>aq_set_abs_goal
   procedure ::set_goal=>aq_set_goal
  procedure ::check_init=>aq_check_init
   ! calculation
   procedure ::main_loop=>aq_main_loop
  procedure ::run=>aq_run
   procedure ::integrate=>aq_integrate
   ! deferred
  procedure(evaluate_if),deferred :: evaluate
end type aq_class
```

#### 7.3 Interfaces

```
interface
   subroutine evaluate_if(this,x,y)
    use kinds!NODEP!
   import aq_class
   class(aq_class),intent(inout) :: this
   real(kind=double), intent(in) :: x
   real(kind=double), intent(out) ,dimension(:):: y
end subroutine evaluate if
```

# 7.4 Implementierung der Prozeduren

```
7.4.1 Methoden für aq_class
Überschriebene serializable_class Methoden
aq_write_to_marker ↑
```

```
subroutine aq_write_to_marker(this,marker,status)
    class(aq_class), intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    class(serializable_class),pointer::ser
    call marker%mark_begin("aq_class")
    call identified_write_to_marker(this,marker,status)
    call marker%mark("is_deferred_initialised",this&
         &%is_deferred_initialised)
    call marker%mark("is_error_tree_initialised",this&
         &%is_error_tree_initialised)
    call marker%mark("is_goal_set",this%is_goal_set)
    call marker%mark("is_initialised",this%is_initialised)
    call marker%mark("is_run",this%is_run)
    call marker%mark("is_goal_reached",this%is_goal_reached)
    call marker%mark("is_integrated",this%is_integrated)
    call marker%mark("n_nodes",this%n_nodes)
    call marker%mark("max_nodes",this%max_nodes)
    call marker%mark("dim_integral",this%dim_integral)
    call marker%mark("abs_error_goal",this%abs_error_goal)
    call marker%mark("rel_error_goal",this%rel_error_goal)
    call marker%mark("scaled_error_goal",this%scaled_error_goal)
    call marker%mark("error_goal",this%error_goal)
    call marker%mark("integral",this%integral)
    call marker%mark("integral_error",this%integral_error)
    call marker%mark("region",this%region(1:2))
    ser=>this%err tree
    call marker%mark_pointer("err_tree",ser)
    ser=>this%int_list
    call marker%mark_pointer("int_list",ser)
    call marker%mark_end("aq_class")
  end subroutine aq_write_to_marker
aq read from marker \( \)
  subroutine aq_read_from_marker(this,marker,status)
    class(aq_class), intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    class(serializable_class),pointer::ser
    call marker%pick_begin("aq_class",status=status)
    call identified_read_from_marker(this,marker,status)
    call marker%pick("is_deferred_initialised",this%is_deferred_initialised&
         &, status)
    call marker%pick("is_error_tree_initialised",this&
         &%is_error_tree_initialised,status)
    call marker%pick("is_goal_set",this%is_goal_set,status)
    call marker%pick("is_initialised",this%is_initialised,status)
    call marker%pick("is_run",this%is_run,status)
    call marker%pick("is_goal_reached",this%is_goal_reached,status)
    call marker%pick("is_integrated",this%is_integrated,status)
```

```
call marker%pick("n_nodes",this%n_nodes,status)
    call marker%pick("max_nodes",this%max_nodes,status)
    call marker%pick("dim_integral",this%dim_integral,status)
    call marker%pick("abs_error_goal",this%abs_error_goal,status)
    call marker%pick("rel_error_goal",this%rel_error_goal,status)
    call marker%pick("scaled_error_goal",this%scaled_error_goal,status)
    call marker%pick("error_goal",this%error_goal,status)
    call marker%pick("integral",this%integral,status)
    call marker%pick("integral_error",this%integral_error,status)
    call marker%pick("region",this%region(1:2),status)
    call marker%pick_pointer("err_tree",ser)
    if(associated(ser))then
       select type(ser)
       class is (fibonacci_root_type)
          this%err_tree=>ser
       class default
          nullify(this%err_tree)
       end select
    end if
    call marker%pick_pointer("int_list",ser)
    if(associated(ser))then
       select type(ser)
       class is (muli_trapezium_list_type)
          this%int_list=>ser
       class default
          nullify(this%int_list)
       end select
    end if
    call marker%pick_end("aq_class", status)
  end subroutine aq_read_from_marker
aq print to unit \
  subroutine aq_print_to_unit(this,unit,parents,components,peers)
    class(aq_class),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    integer::ite
    class(serializable_class),pointer::ser
    if(parents>0)call identified_print_to_unit(this,unit,parents-1,components&
         &, peers)
    write(unit,'("Components of aq_class")')
    write(unit, '(a,L1)') "Deferred class initialised: ",this&
         &%is_deferred_initialised
    write(unit, '(a,L1)')"Error tree initialised:
                                                      ",this&
         &%is_error_tree_initialised
    write(unit, '(a,L1)')"Accuracy goal set:
                                                      ",this%is_goal_set
    write(unit, '(a,L1)')"Ready for run:
                                                      ",this%is_initialised
    write(unit,'(a,L1)')"Is run:
                                                      ",this%is_run
    write(unit,'(a,L1)')"Accuracy goal reached:
                                                      ",this%is_goal_reached
    write(unit,'(a,L1)')"Integral calculated:
                                                      ",this%is_integrated
```

```
write(unit, '(a, I10)')"Number of nodes:
                                                       ",this%n_nodes
    write(unit, '(a, I10)') "Maximal number of nodes:
                                                       ",this%max_nodes
    write(unit, '(a, I10)')"Dimension of integral:
                                                       ",this%dim_integral
    write(unit, '(a, E20.10)') "Given abs. error goal: ",this%abs_error_goal
    write(unit, '(a, E20.10)') "Given rel. error goal: ", this % rel_error_goal
    write(unit, '(a, E20.10)') "Guessed abs error goal: ", this % scaled_error_goal
    write(unit, '(a, E20.10)')"Actual abs error goal: ",this%error_goal
    write(unit, '(a,E20.10)')"Integral
                                                     ",this%integral
    write(unit,'(a,E20.10)')"Estimated abs. error: ",this%integral_error
    write(unit,'(a,E10.5,a,E10.5,a)')"Integration region = (",this%region(1)&
         &," : ",this%region(2),")"
    ser=>this%err_tree
    call serialize_print_comp_pointer(ser,unit,parents,components,peers&
         &, "error tree")
    ser=>this%int_list
    call serialize_print_comp_pointer(ser,unit,parents,components,peers&
         &, "integral list")
  end subroutine aq_print_to_unit
aq get type↑
  pure subroutine aq_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="aq_type")
  end subroutine aq_get_type
aq deserialize from marker \( \ \)
  subroutine aq_deserialize_from_marker(this,name,marker)
    class(aq_class),intent(out)::this
    character(*),intent(in)::name
    class(marker_type),intent(inout)::marker
    class(serializable_class),pointer::ser
    allocate(muli_trapezium_type::ser)
    call marker%push_reference(ser)
    allocate(fibonacci_root_type::ser)
    call marker%push_reference(ser)
    allocate(fibonacci_leave_type::ser)
    call marker%push_reference(ser)
    allocate(fibonacci_node_type::ser)
    call marker%push_reference(ser)
    call serializable_deserialize_from_marker(this,name,marker)
    call marker%pop_reference(ser)
    deallocate(ser)
    call marker%pop_reference(ser)
    deallocate(ser)
    call marker%pop_reference(ser)
    deallocate(ser)
    call marker%pop_reference(ser)
    deallocate(ser)
  end subroutine aq_deserialize_from_marker
```

### Originäre aq class Methoden

```
aq initialize \( \)
  subroutine aq_initialize(this,id,name,goal,max_nodes,dim,init)
    class(aq_class),intent(out) :: this
    integer(kind=dik),intent(in)::id,max_nodes
    integer,intent(in)::dim
    character,intent(in)::name
    real(kind=double)::goal
    real(kind=double), dimension(:), intent(in)::init
    call identified_initialize(this,id,name)
    this%rel_error_goal = goal!1d-4
    this%max_nodes=max_nodes
    call this%init_error_tree(dim,init)
  end subroutine aq_initialize
aq_print_times \uparrow
  subroutine aq_print_times(this)
    class(aq_class),intent(in) :: this
    print '(a,E20.10)',"Initialization time:
                                               ",this%init_time
    print '(a,E20.10)', "Main loop time:
                                               ",this%loop_time
    print '(a,E20.10)',"Integration time:
                                               ",this%int_time
    print '(a,E20.10)',"Overall run time:
                                               ",this%total_time
    print '(a,E20.10)', "Cuba integration time: ",this%cuba_time
  end subroutine aq_print_times
aq write convergence \( \)
  subroutine aq_write_convergence(this,unit)
    class(aq_class),intent(in) :: this
    integer, intent(in)::unit
    integer,dimension(2)::s
    integer::node
    if(allocated(this%convergence))then
       s=shape(this%convergence)
       do node=1,s(2)
          write(unit,fmt=*)node,this%convergence(1:2,node)
       end do
    end if
  end subroutine aq_write_convergence
! init/ de-init
aq reset ↑
  subroutine aq_reset(this)
    class(aq_class) :: this
    this%is_deferred_initialised = .false.
    this%is_error_tree_initialised = .false.
    this%is_goal_set = .false.
    this%is_initialised = .false.
```

```
this%is_run = .false.
    this%is_goal_reached = .false.
    this%is_integrated = .false.
    this%n\_nodes = 0
    this%max_nodes = 10000
    this%dim_integral=1
    this%abs_error_goal = 1D0
    this%rel_error_goal = 0.1D0
    this%scaled_error_goal = 0.0D0
    this%error_goal = 0.0D0
    this%integral = 0D0
    this%integral_error = ODO
    this%region = (/0D0, 1D0/)
    this%total_time = 0
    this%loop_time = 0
    this%int_time = 0
    this%init_time = 0
    call this%dealloc_trees()
  end subroutine aq_reset
aq check init \
  subroutine aq_check_init(this)
    class(aq_class) :: this
    this%is_initialised = this%is_error_tree_initialised .and. this%is_deferred_initialised
  end subroutine aq_check_init
aq dealloc trees ↑
  subroutine aq_dealloc_trees(this)
    class(aq_class) :: this
    if(associated(this%err_tree))then
       call this%err_tree%deallocate_all()
       deallocate(this%err_tree)
    if(associated(this%int_list))then
       call this%int_list%finalize()
       deallocate(this%int_list)
    end if
  end subroutine aq_dealloc_trees
aq init error tree \( \)
  subroutine aq_init_error_tree(this,dim_integral,x_array)
    class(aq_class) :: this
    !Wie viele Einträge hat der Rückgabewert von evaluate?
    integer,intent(in)::dim_integral
    !Eine geordnete Liste von Skalenparametern
    real(kind=double), dimension(:), intent(in) :: x_array
    !(x_j - x_{j-1})/2
    real(kind=double) :: center
    !Die Funktionswerte am linken Rand, in der Mitte und am rechten Rand des Intervalls.
```

```
real(kind=double), dimension(:),allocatable::l_val,c_val,r_val
!Jedes der gegebenen Intervalle wird in zwei Unterintervalle zerlegt, um eine
!Abschätzung des Integrationsfehlees zu bekommen. In left_node und right_node
!werden diese Intervalle gespeichert und in den Binärbaum eingefügt.
class(muli_trapezium_type),pointer :: left_node => null()
class(muli_trapezium_type),pointer :: right_node => null()
!Die Anzahl der gegebenen x-Werte und die Nummer des aktuellen x-Werts.
integer :: x_size,pos
!Timer Start
call cpu_time(this%init_time)
!Signalisieren, dass die Bäume in einem undefinierten Zustand sind.
this%is_initialised=.false.
this%integral=0D0
this%dim_integral=dim_integral
x_size = size(x_array)
if (x_size<2) then
     write (*,'("aq_init_error_tree: I need at least two real values")')
else
   !In der Null-Komponente wird die Summe aller anderen Einträge gespeichert.
   allocate(l_val(0:dim_integral-1))
   allocate(c_val(0:dim_integral-1))
   allocate(r_val(0:dim_integral-1))
   !Der Integrationsbereich wird festgelegt.
   this%region=(/x_array(1),x_array(x_size)/)
   if (x_size<3) then
      !Wir haben nur ein Startsegment, das sich über den gesamten Integrationsbereich
      !erstreckt. Wir Teilen in der Mitte, denn der Binärbaum
      !aq_class%error_tree muss mindestens zwei Blätter haben.
      center=(x_array(2)-x_array(1))/2D0
      !Wir fordern die Funktionswerte an.
      call this%evaluate(x_array(1),l_val)
      call this%evaluate(center,
                                   c_val)
      call this%evaluate(x_array(2),r_val)
      !Wir erzeugen ein neues Segment [x_1,c].
      allocate(left_node)
      call left_node%initialize(&
           &dim=dim_integral,&
           &r_position=center,&
           &d_position=center-x_array(1))
      call left_node%set_r_value(c_val)
      call left_node%set_d_value(c_val-l_val)
      !Wir erzeugen ein neues Segment [c,x_2].
      allocate(right_node)
      call right_node%initialize(&
           &dim=dim_integral,&
           &r_position=x_array(2),&
           &d_position=x_array(2)-center)
      call right_node%set_r_value(r_val)
      call right_node%set_d_value(r_val-c_val)
   else
      !wir haben genügend x-Werte, um einen minimalen Baum
```

```
!aq_class%error_tree mit zwei Blättern zu initialisieren.
   call this%evaluate(x_array(1),l_val)
   call this%evaluate(x_array(2),c_val)
   call this%evaluate(x_array(3),r_val)
   allocate(left_node)
   call left_node%initialize(&
        &dim=dim_integral,&
        &r_position=x_array(2),&
        &d_position=x_array(2)-x_array(1))
   call left_node%set_r_value(c_val)
   call left_node%set_d_value(c_val-l_val)
   allocate(right_node)
   call right_node%initialize(&
        &dim=dim_integral,&
        &r_position=x_array(3),&
        &d_position=x_array(3)-x_array(2))
   call right_node%set_r_value(r_val)
   call right_node%set_d_value(r_val-c_val)
end if
!Die beiden Startblätter des Baums werden bereitgemacht
call left_node%update()
call right_node%update()
!Der Wert für das Integral über diese Blätter wird abgeschätzt.
this%integral=sum(left_node%get_d_integral()+right_node%get_d_integral())
if (.not. associated(this%err_tree)) then
   allocate(this%err tree)
end if
!Debugging
print *,left_node%measure()
print *,right_node%measure()
!Der Baum wird mit den beiden Blättern initialisiert.
call this%err_tree%init_by_content(left_node,right_node)
!Wenn wir noch mehr Segmente haben, dann werden sie in den Baum aufgenommen.
if (x_size > 3) then
   do pos=4,x_size
      !Fortschrittsanzeige. Die Intagrationen können einige Minuten dauern.
      print *,"aq_init_error_tree",pos,"/",x_size
      !Wir merken uns den Funktionswert am rechen Rand des letzten Segments.
      !Das ist der neue linke Funktionswert des neuen Segments.
      l_val=right_node%get_r_value_array()
      !Wir forden den Funktionswert am rechten Rand des neuen Intervalls an.
      call this%evaluate(x_array(pos),r_val)
      !Ein Missbrauch der Variablen, c_val ist jetzt die Intervallänge.
      c_val=r_val-l_val
      allocate(right_node)
      call right_node%initialize(&
           &dim=dim_integral,&
           &r_position=x_array(pos),&
           &d_position=x_array(pos)-x_array(pos-1))
      call right_node%set_r_value(r_val)
      call right_node%set_d_value(c_val)
```

```
call right_node%update()
             call this%err_tree%push_by_content(right_node)
             !Das Gesamtintegral wird um das Integral über das neue Segment erhöht.
             this%integral=this%integral+sum(right_node%get_d_integral())
          !So viele Blätter hat der Baum jetzt.
          this%n_nodes = x_size
       end if
       !Der Baum ist wieder in einem definierten Zustand.
       this%is_error_tree_initialised=.true.
    !Da wir jetzt eine erste Abschätzung für das Integral haben, können wir
    !eine Abschätzung für das absolute Fehlerziel machen.
    call this%set_goal()
    !Damit ist alles Bereit für die adaptive Integration.
    this%is_initialised=.true.
    !Timer Stopp
    call cpu_time(this%cpu_time)
    this%init_time=this%cpu_time-this%init_time
    this%cuba_time=this%init_time
    !Debugging: Ab jetzt schreiben wir den aktuellen Integrationsfehler mit.
    allocate(this%convergence(2,this%n_nodes:this%max_nodes))
  end subroutine aq_init_error_tree
aq set abs goal †
 subroutine aq_set_abs_goal(this,goal)
    class(aq_class) :: this
    real(kind=double) :: goal
    this%abs_error_goal = goal
    call this%set_goal
  end subroutine aq_set_abs_goal
aq set rel goal \( \ \)
 subroutine aq_set_rel_goal(this,goal)
    class(aq_class) :: this
    real(kind=double) :: goal
    this%rel_error_goal = goal
    call this%set_goal
  end subroutine aq_set_rel_goal
aq set goal †
```

Die angegebenen Fehlerziele werden auf Konsistenz geprüft. Aus dem relativen Fehler wird mithilfe der aktuellen Abschätzung des Integrals ein absoluter Fehler scaled\_error\_goal berechnet. Das Minimum aus abs\_error\_goal und scaled\_error\_goal wird das tatsächliche absulute Fehlerziel error\_goal.

```
subroutine aq_set_goal(this)
  class(aq_class) :: this
  this%scaled_error_goal = this%rel_error_goal*abs(this%integral)
  if ((this%scaled_error_goal==0D0).and.(this%abs_error_goal==0D0)) then
    this%is_goal_set = .false.
```

```
this%error_goal = 0D0
    else
       if (this%scaled_error_goal == 0D0) then
          this%error_goal = this%abs_error_goal
       else
          if (this%abs_error_goal == 0D0) then
             this%error_goal = this%scaled_error_goal
             this%error_goal = max(this%scaled_error_goal, this%abs_error_goal)
          end if
       end if
       if (this%error_goal > 0D0) then
          this%is_goal_set = .true.
       else
          this%is_goal_set = .false.
       end if
    end if
  end subroutine aq_set_goal
! calculation
aq main loop \
Die eigentliche adaptive Quadratur findet in dieser Prozedur statt.
  subroutine aq_main_loop(this)
    ! unsafe, when n_nodes < 4
    class(aq_class) :: this
    !Das Blatt mit dem größten Integrationsfehler
    class(fibonacci_leave_type), pointer :: rightmost
    class(measurable_class), pointer :: content
    class(muli_trapezium_type),pointer :: new_node
    !Wurde die maximale Anzahl von Blättern erreicht?
    logical :: limit = .false.
    !Die Stelle, bei der das Segment geteilt wird.
    real(kind=double) :: center
    !Der Funktionswert an dieser Stelle.
    real(kind=double), dimension(:), allocatable::c_val
    allocate(c_val(0:this%dim_integral-1))
       !Wir holen uns das Blatt mit den größten Integrationsfehler.
       call this%err_tree%pop_right(rightmost)
       !Wenn diese Bedingung erfüllt ist, dann ist auch der gesammte Fehler
       !kleiner als this%error_goal
       if (rightmost < this%error_goal/this%n_nodes) then
          this%is_goal_reached = .true.
          exit loop
       else
          !Wir holen uns das Integrationssegment aus dem Blatt.
          call rightmost%get_content(content)
          !Zugriff auf die speziellen Methoden von muli_trapezium_type
          select type (content)
```

```
class is (muli_trapezium_type)
             !Fortschrittsanzeige
             print&
             ('("nodes: ",I5," error: ",E14.7," goal: ",E14.7," node at: ",E14.7,"-",E14.7)'),&
                  this%n_nodes,&
                  rightmost%measure()*this%n_nodes,&
                  this%error_goal,&
                  content%get_l_position(),&
                  content%get_r_position()
             !Debugging: Wir schreiben den Forschritt in den Abbruchbedingung mit.
             this%convergence(1,this%n_nodes)=this%error_goal/this%n_nodes
             this%convergence(2,this%n_nodes)=rightmost%measure()
             !Wir wollen das Segment in der Mitte teilen.
             center = content%get_r_position()-content%get_d_position()/2D0
             call cpu_time(this%cpu_time)
             this%cuba_time=this%cuba_time-this%cpu_time
             !Wir fordern den Funktionswert in der Mitte des Segments an.
             call this%evaluate(center,c_val)
             call cpu_time(this%cpu_time)
             this%cuba_time=this%cuba_time+this%cpu_time
             !Wir teilen das Segment in zwei neue Segmente.
             !Siehe muli_trapezium_type%split
             call content%split(c_val,center,new_node)
             !content ist das rechte Segment und immer noch in rightmost enthalten.
             !Wir können also das Blatt rightmost wieder in den Baum einfügen.
             call this%err_tree%push_by_leave(rightmost)
             !Fur das linke Segment new_node muss noch ein neues Blatt erzeugt werden.
             call this%err_tree%push_by_content(new_node)
          end select
          this%n_nodes=this%n_nodes+1
          !Wenn die maximale Zahl von Blättern erreicht ist, dann müssen wir erfolglos aufhören.
          if (this%n_nodes > this%max_nodes) then
             limit = .true.
             exit loop
          end if
       end if
    end do loop
    !Ein Blatt halten wir noch in der Hand, wir legen es in den Baum zurück.
    call this%err_tree%push_by_leave(rightmost)
  end subroutine aq_main_loop
aq run †
Wrapper für aq main loop.
 subroutine aq_run(this)
    class(aq_class) :: this
    call cpu_time(this%total_time)
    if (.not. this%is_error_tree_initialised) then
      call this%init_error_tree(this%dim_integral,this%region)
    end if
    this%is_run = .false.
```

```
this%is_goal_reached = .false.
  call aq_main_loop(this)
  this%is_run = .true.
  call cpu_time(this%cpu_time)
    this%total_time=this%cpu_time-this%total_time
  end subroutine aq_run
aq_integrate ↑
```

Die eigentliche Integration ist schon fertig, aber die Integrationssegmente sind nach Integrationsfehler sortiert. Wir wollen jetzt einen Binärbaum erzeugen, in dem die Segmente nach den x-Werten sortiert sind.

```
subroutine aq_integrate(this,int_tree)
  class(aq_class) :: this
  class(muli_trapezium_node_class),pointer :: node
  type(muli_trapezium_tree_type),intent(out)::int_tree
  real(kind=double) :: sum
  this%is_integrated=.false.
  this%integral_error=0D0
  if (this%is_run) then
  call cpu_time(this%int_time)
     !Umsortieren
     call fibonacci_tree_resort_and_convert_to_trapezium_list&
       (this%err_tree,this%int_list)
     !Die Integrale über die einzelnen Segmente aufaddieren
     call muli_trapezium_list_integrate(this%int_list,this%integral,this%integral_error)
     !Einen Baum aus der Liste machen
     call this%int_list%to_tree(int_tree)
     this%is_integrated=.true.
     call cpu_time(this%cpu_time)
     this%int_time=this%cpu_time-this%int_time
  end if
end subroutine aq_integrate
```

### 7.4.2 Sonstige Prozeduren

```
fibonacci_tree_resort_and_convert_to_trapezium_list

recursive subroutine fibonacci_tree_resort_and_convert_to_trapezium_list&
    (fib_tree,lin_list)
   !usually, the tree is sorted by the sum of errors.
   !now it shall be sorted by the right position.
   class(fibonacci_node_type),intent(in) :: fib_tree
   class(fibonacci_node_type),pointer :: leave
   class(muli_trapezium_list_type),pointer,intent(out) :: lin_list
   class(muli_trapezium_list_type),pointer :: left_list,right_list
   class(muli_trapezium_node_class),pointer :: left_node,right_node,last_node
   class(measurable_class),pointer :: content
   !When at least one branch of the tree is itself a tree, i.e. each branch has
   !got at least two leaves, then process each branch and merge the results.
   if (fib_tree%depth>1) then
```

```
call fibonacci_tree_resort_and_convert_to_trapezium_list(fib_tree%left,left_list)
   call fibonacci_tree_resort_and_convert_to_trapezium_list(fib_tree%right,right_list)
   !Now we got two sortet lists.
   !Which one's leftmost node has got the lowest value of "r_position"?
   !That one shall be the beginning of the merged list "lin_list".
   if(left_list%is_left_of(right_list))then
      lin_list => left_list
      call left_list%get_right(left_node)
      right_node=>right_list
   else
      lin_list => right_list
      left_node=>left_list
      call right_list%get_right(right_node)
   end if
   last_node=>lin_list
   !Everything is prepared for the algorithm: lin_list is the beginning of the
   !sorted list, last_node is it's end. left_node and right_node are the leftmost
   !nodes of the remainders of left_list and right_list. The latter will get
   !stripped from left to right, until one of them ends.
   do while(associated(left_node).and.associated(right_node))
      if (left_node%is_left_of(right_node)) then
         call last_node%append(left_node)
         call last_node%get_right(last_node)
         call left_node%get_right(left_node)
      else
         call last_node%append(right_node)
         call last_node%get_right(last_node)
         call right_node%get_right(right_node)
      end if
   end do
   !Either left_list or right_list is completely merged into lin_list. The other
   !one gets appended to lin_list.
   if (associated(left_node)) then
      call last_node%append(left_node)
   else
      call last_node%append(right_node)
   end if
   !It's done.
else
   !The tree has got two leaves at most. Is it more than one?
   if (fib_tree%depth == 0) then
      !Here fib_tree is a single leave with an allocated "content" componet of
      !type muli_trapezium_type. If "content" is not type compatible with
      !muli_trapezium_type, then this whole conversion cannot succeed.
      !We allocate a new node of type muli_trapezium_list_type. This list does
      !not contain the content of fib_tree, it *IS* a copy of the content, for
      !muli_trapezium_list_type is an extension of muli_trapezium_type.
      select type (fib_tree)
      class is (fibonacci_leave_type)
         call fib_tree%get_content(content)
         select type (content)
```

```
class is (muli_trapezium_type)
              call muli_trapezium_to_node(content,content%get_r_position(),list=lin_list)
           class default
              print *,"fibonacci_tree_resort_and_convert_to_trapezium_list: &
                   &Content of fibonacci_tree is not type compatible to &
                   &muli_trapezium_type"
           end select
        end select
     else
        !Each branch of fib_tree is a single leave. We could call this soubroutine
        !for each branch, but we do copy and paste for each branch instead.
        leave=>fib_tree%left
        select type (leave)
        class is (fibonacci_leave_type)
           call leave%get_content(content)
           select type (content)
           class is (muli_trapezium_type)
              call muli_trapezium_to_node(content,content%get_r_position(),list=left_list)
           class default
              print *,"fibonacci_tree_resort_and_convert_to_trapezium_list: &
                   &Content of fibonacci_tree is not type compatible to &
                   &muli_trapezium_type"
           end select
        end select
        leave=>fib_tree%right
        select type (leave)
        class is (fibonacci_leave_type)
           call leave%get_content(content)
           select type (content)
           class is (muli_trapezium_type)
              call muli_trapezium_to_node%
                (content,content%get_r_position(),list=right_list)
           class default
              print *,"fibonacci_tree_resort_and_convert_to_trapezium_list: &
                   &Content of fibonacci_tree is not type compatible to &
                   &muli_trapezium_type"
           end select
        end select
        !Finally we append one list to the other, the lowest value of "r_position"
        !comes first.
        if (left_list%is_left_of(right_list)) then
           call left_list%append(right_list)
           lin_list=>left_list
           call right_list%append(left_list)
           lin_list=>right_list
        end if
     end if
  end if
end subroutine fibonacci_tree_resort_and_convert_to_trapezium_list
```

# 8 Modul muli trapezium

In dem Modul muli\_trapezium wird ein Datentyp muli\_trapezium\_type definiert, der eine affin-lineare Approximation von  $\overline{S}_{\alpha\beta}(p_{\perp};s)$ ,  $S_{\alpha\beta}(p_{\perp};s)$ ,  $exp[-S_{\alpha\beta}(p_{\perp};s)]$  und einen Integrationsfehler für  $S_{\alpha\beta}(p_{\perp};s)$  für alle 16 Kombinationen von  $\{\alpha,\beta\}$  für  $\alpha,\beta\in\{g,s,v_d,v_u\}$  bereitstellt.

Weiterhin dir ein abstrakter Datentyp muli\_trapezium\_node\_class definiert, der mehrere Segmente vom Typ muli\_trapezium\_type zusammenfasst und somit eine Approximation der Wirkungsquerschnitte entsprechend der Trapezregel bereitstellt. Daher kommt auch der name des Moduls und der Datentypen.

Für die Auswertung dieser Approximation wird ein Datentyp muli\_trapezium\_tree\_type definiert, der Instanzen der Klasse muli\_trapezium\_node\_class zu einem Binärbaum zusammenstellt. Die Blätter dieses Binärbaums sind jeweils mit ihren linken und rechten Nachbarblättern verbunden, sodass man wahlweise in logarithmischer Zeit ein Blatt von der Wurzel her suchen kann oder die Blätter, sortiert nach  $p_{\perp}$  durchlaufen kann.

Für die Verbindungen unter den Blättern wird der Datentyp muli\_trapezium\_list\_type definiert, der auch ohne Binärbaum als Liste verwendet wird. Jedes Blatt eines Baums ist eine Instanz vom Typ muli\_trapezium\_list\_type.

Die Entscheidung für eine affin-lineare Approximation liegt an der Tatsache, dass höhere Polynome transzendente Funktionen im schlimmsten Fall so deutlich unterschätzen können, dass negative approximierte Funktionswerte bei positiven Funktionen auftreten können. In Abbildung ?? ist das illustriert.

## 8.1 Abhängigkeiten

use muli basic



Abbildung 8.1: Illustration einer quadratischen Approximation von exp(-x)/x. Die Parabel (blau) wird negativ, obwohl die Funktion (rot) streng positiv ist. Mit der Trapezregel kann das nicht passieren.

## 8.2 Parameter

Für jedes Intervall  $[x_l, x_r]$  der approximierten Funktionen g(x) wird deren Funktionswert am rechten Rand r\_value= $f(x_r)$  und die Differenz der Funktionswerte d\_value= $f(x_r) - f(x_l)$  gespeichert. Entsprechend werden die Werte für die negative Stammfunktion (integral) und die daraus berechnete Wahscheinlichkeistfunktion (propability) gespeichert. Schließlich wird ein Integrationsfehler für die Stammfunktion gespeichert. In der Summe macht das value\_dimension=7 Werte, die pro Intervall gespeichert werden müssen. Es wird ein array mit value\_dimension Stellen allokiert, wobei die verschiedenen Werte an der Position \* index abgelegt werden.

```
implicit none
integer,private,parameter::value_dimension=7
integer,private,parameter::r_value_index=1
integer,private,parameter::d_value_index=2
integer,private,parameter::r_integral_index=3
integer,private,parameter::d_integral_index=4
integer,private,parameter::r_propability_index=5
integer,private,parameter::d_propability_index=6
integer,private,parameter::error_index=7
```

## 8.3 Derived Types

## 8.3.1 muli\_trapezium\_type

```
type,extends(measurable_class) :: muli_trapezium_type
```

dim ist die Dimension des Bildraums, also  $\overline{S}:\mathbb{R}\to\mathbb{R}^{\dim}$ . dim ergibt sich aus der Zahl der Strati (=16) plus eins für die Summe über alle Strati. Die Summe wird in der Null-ten Komponente des Funktionswerte-Arrays gespeichert, damit die Strati nach der üblichen Konvention [1..n] indiziert werden.

r position ist der obere Grenze des  $p_{\perp}$ -Intervalls, d position ist die Intervallänge.

measure\_comp ist eine Maßzahl für jedes Intervall, nach der sie in dem Binärbaum sortiert werden. Die Blätter des Baumes sind dann eine geordnete Liste mit aufsteigendem measure\_comp. measure\_comp wird auf r\_position gesetzt.

values ist schließlich die Matrix der Funktionswerte für die verschiedenen Funktionen. Der erste, schnelle Index läuft über die Strati  $\{0..\dim -1\}$ , der zweite, langsame Index läuft über die Menge der Funktionen  $\{r\_value,d\_value,r\_integral,d\_integral,r\_propability,d\_propability,error\}$ 

```
private
integer::dim=0
real(kind=double)::r_position=0D0
real(kind=double)::d_position=0D0
real(kind=double)::measure_comp=0D0
real(kind=double),dimension(:,:),allocatable::values
contains
!Überschriebene serializable_class Methoden
procedure ::write_to_marker=>muli_trapezium_write_to_marker
procedure ::read_from_marker=>muli_trapezium_read_from_marker
procedure ::print_to_unit=>muli_trapezium_print_to_unit
```

```
procedure,nopass ::get_type=>muli_trapezium_get_type
procedure,nopass ::verify_type=>muli_trapezium_verify_type
!Überschriebene measurable_class Methoden
procedure::measure=>muli_trapezium_measure
!Originare muli_trapezium_type Methoden
! init/deinit
procedure::initialize=>muli_trapezium_initialize
! components
procedure,public::get_dimension=>muli_trapezium_get_dimension
procedure, public::get_l_position=>muli_trapezium_get_l_position
procedure, public::get_r_position=>muli_trapezium_get_r_position
procedure,public::get_d_position=>muli_trapezium_get_d_position
procedure,public::get_l_value_array=>muli_trapezium_get_l_value_array
procedure, public::get_l_value_element=>muli_trapezium_get_l_value_element
procedure, public::get_r_value_array=>muli_trapezium_get_r_value_array
procedure, public::get_r_value_element=>muli_trapezium_get_r_value_element
procedure, public::get_d_value_array=>muli_trapezium_get_d_value_array
procedure, public::get_d_value_element=>muli_trapezium_get_d_value_element
procedure, public::get_l_integral_array=>muli_trapezium_get_l_integral_array
procedure,public::get_l_integral_element=>muli_trapezium_get_l_integral_element
procedure, public::get_r_integral_array=>muli_trapezium_get_r_integral_array
procedure, public::get_r_integral_element=>muli_trapezium_get_r_integral_element
procedure, public::get_d_integral_array=>muli_trapezium_get_d_integral_array
procedure, public::get_d_integral_element=>muli_trapezium_get_d_integral_element
procedure, public::get_l_propability_element=>muli_trapezium_get_l_propability_element
procedure,public::get_l_propability_array=>muli_trapezium_get_l_propability_array
procedure, public::get_r_propability_element=>muli_trapezium_get_r_propability_element
procedure, public::get_r_propability_array=>muli_trapezium_get_r_propability_array
procedure, public::get_d_propability_element=>muli_trapezium_get_d_propability_element
procedure,public::get_d_propability_array=>muli_trapezium_get_d_propability_array
procedure,public::get_error=>muli_trapezium_get_error
procedure,public::get_error_sum=>muli_trapezium_get_error_sum
procedure, public::get_integral_sum=>muli_trapezium_get_integral_sum
generic, public::get_l_value=>get_l_value_array,get_l_value_element
generic, public::get_r_value=>get_r_value_array, get_r_value_element
generic, public::get_d_value=>get_d_value_array, get_d_value_element
generic,public::get_l_integral=>get_l_integral_array,get_l_integral_element
generic,public::get_r_integral=>get_r_integral_array,get_r_integral_element
generic, public::get_d_integral=>get_d_integral_array,get_d_integral_element
generic, public::get_l_propability=>get_l_propability_array,get_l_propability_element
generic,public::get_r_propability=>get_r_propability_array,get_r_propability_element
generic,public::get_d_propability=>get_d_propability_array,get_d_propability_element
! interpolations
procedure, public::get_value_at_position=>muli_trapezium_get_value_at_position
procedure::set_r_value=>muli_trapezium_set_r_value
procedure::set_d_value=>muli_trapezium_set_d_value
procedure::set_r_integral=>muli_trapezium_set_r_integral
procedure::set_d_integral=>muli_trapezium_set_d_integral
procedure::set_r_propability=>muli_trapezium_set_r_propability
procedure::set_d_propability=>muli_trapezium_set_d_propability
procedure::set_error=>muli_trapezium_set_error
```

```
! tests
  procedure,public::is_left_of=>muli_trapezium_is_left_of
  procedure,public::includes=>muli_trapezium_includes
   ! convert
  procedure ::to_node=>muli_trapezium_to_node
  procedure ::sum_up=>muli_trapezium_sum_up
   ! approximation
  procedure ::approx_value=>muli_trapezium_approx_value
  procedure ::approx_value_n=>muli_trapezium_approx_value_n
  procedure ::approx_integral=>muli_trapezium_approx_integral
  procedure ::approx_integral_n=>muli_trapezium_approx_integral_n
  procedure ::approx_propability=>muli_trapezium_approx_propability
  procedure ::approx_propability_n=>muli_trapezium_approx_propability_n
  procedure ::approx_position_by_integral=>muli_trapezium_approx_position_by_integral
  procedure ::split=>muli_trapezium_split
  procedure ::update=>muli_trapezium_update
end type muli_trapezium_type
```

## 8.3.2 muli trapezium node class

muli\_trapezium\_node\_class ist eine abstake Klasse, die durch die Komonenten left und right wahlweise ein Binärbaum oder eine doppelt-verknüpften Liste sein kann. Welche dieser Ausprägungen vorliegt, hängt von dem Datentyp ab. Jede Instanz der Klasse muli\_trapezium\_node\_class ist entweder vom Typ muli\_trapezium\_tree\_type oder vom Typ muli\_trapezium\_list\_type. Hier werden alle Methoden definiert, die eine Liste, und ein Baum gemein haben.

```
type, Extendsmuli_trapezium_type, abstract :: muli_trapezium_node_class
```

#### Komponenten

```
private
class(muli_trapezium_node_class), pointer :: left => null()
class(muli_trapezium_node_class), pointer :: right => null()
```

#### Methoden

```
contains
! private
!Überschriebene measurable_class Methoden
procedure,public ::deserialize_from_marker=>muli_trapezium_node_deserialize_from_marker
!Originäre muli_trapezium_node_class Methoden
procedure(muli_trapezium_append_interface),deferred,public::append
procedure(muli_trapezium_final_interface),deferred,public :: finalize
procedure,public ::nullify=>muli_trapezium_node_nullify
procedure,public ::get_left=>muli_trapezium_node_get_left
procedure,public ::get_right=>muli_trapezium_node_get_right
procedure,public ::get_leftmost=>muli_trapezium_node_get_leftmost
procedure,public ::get_rightmost=>muli_trapezium_node_get_rightmost
procedure,public ::decide_by_value=>muli_trapezium_node_decide_by_value
procedure,public ::decide_by_position=>muli_trapezium_node_decide_by_position
```

```
procedure,public ::decide_decreasing=>muli_trapezium_node_decide_decreasing
procedure,public :: muli_trapezium_node_to_tree
procedure,private::untangle=>muli_trapezium_node_untangle
procedure,public ::apply=>muli_trapezium_node_apply
generic,public::decide=>decide_by_value,decide_by_position
end type muli_trapezium_node_class
```

## 8.3.3 muli trapezium tree type

```
muli_trapezium_node_class in der Ausprägung "Binärbaum".

type,extends(muli_trapezium_node_class) :: muli_trapezium_tree_type
```

**Komponenten** down ist ein Zeiger auf das rechteste Blatt von dem linken Nachfolger. Da das Maß eines Blatts gleich r\_position des Blatt ist, gibt down%measure() die obere Grenze des Intervalls des linken Unterbaums wieder. Bei einer Suche nach dem Blatt, das  $p_{\perp}$  enthält, wird also per  $p_{\perp}$  < down%measure() entschieden, ob wir nach links oder nach rechts absteigen.

```
class(muli_trapezium_node_class), pointer :: down => null()
```

#### Methoden

```
contains
   !Überschriebene measurable_class Methoden
   procedure ::write_to_marker=>muli_trapezium_tree_write_to_marker
   procedure ::read_from_marker=>muli_trapezium_tree_read_from_marker
   procedure ::print_to_unit=>muli_trapezium_tree_print_to_unit
  procedure,nopass ::get_type=>muli_trapezium_tree_get_type
   procedure,nopass ::verify_type=>muli_trapezium_tree_verify_type
   !Überschriebene muli_trapezium_node_class Methoden
   procedure,public ::nullify=>muli_trapezium_tree_nullify
  procedure,public ::finalize=>muli_trapezium_tree_finalize
  procedure, public ::decide_by_value=>muli_trapezium_tree_decide_by_value
   procedure, public ::decide_by_position=>muli_trapezium_tree_decide_by_position
  procedure,public ::decide_decreasing=>muli_trapezium_tree_decide_decreasing
   !Originare muli_trapezium_tree_type Methoden
  procedure,public ::get_left_list=>muli_trapezium_tree_get_left_list
  procedure,public ::get_right_list=>muli_trapezium_tree_get_right_list
   procedure, public ::find_by_value=>muli_trapezium_tree_find_by_value
  procedure, public ::find_by_position=>muli_trapezium_tree_find_by_position
   procedure, public ::find_decreasing=>muli_trapezium_tree_find_decreasing
   procedure, public ::approx_by_integral=>muli_trapezium_tree_approx_by_integral
   procedure, public ::approx_by_propability=>muli_trapezium_tree_approx_by_propability
   procedure,public ::to_tree=>muli_trapezium_tree_to_tree
   generic, public::find=>find_by_value,find_by_position
  procedure::append=>muli_trapezium_tree_append
  procedure::gnuplot=>muli_trapezium_tree_gnuplot
end type muli_trapezium_tree_type
```

## 8.3.4 muli trapezium list type

```
muli_trapezium_node_class in der Ausprägung "Liste".

type,extends(muli_trapezium_node_class) :: muli_trapezium_list_type
```

#### Methoden

```
contains
   !Überschriebene measurable_class Methoden
  procedure ::write_to_marker=>muli_trapezium_list_write_to_marker
  procedure ::read_from_marker=>muli_trapezium_list_read_from_marker
  procedure ::read_target_from_marker=>muli_trapezium_list_read_target_from_marker
  procedure ::print_to_unit=>muli_trapezium_list_print_to_unit
  procedure,nopass ::get_type=>muli_trapezium_list_get_type
  procedure,nopass ::verify_type=>muli_trapezium_list_verify_type
   !Originäre muli_trapezium_list_type Methoden
  procedure,public ::finalize=>muli_trapezium_list_finalize
  procedure,public ::insert_right_a=>muli_trapezium_list_insert_right_a
  generic,public ::insert_right=>insert_right_a!,insert_right_b
  procedure,public ::insert_left_a=>muli_trapezium_list_insert_left_a
  generic,public ::insert_left=>insert_left_a!,insert_left_b
  procedure::append=>muli_trapezium_list_append
  procedure,public ::to_tree=>muli_trapezium_list_to_tree
  procedure,public ::gnuplot=>muli trapezium list gnuplot
  procedure,public ::integrate=>muli_trapezium_list_integrate
  procedure,public ::check=>muli_trapezium_list_check
  procedure,public ::apply=>muli_trapezium_list_apply
end type muli_trapezium_list_type
```

## 8.4 Schnittstellen

```
abstract interface
   subroutine muli_trapezium_append_interface(this,right)
   import muli_trapezium_node_class
   class(muli_trapezium_node_class),intent(inout),target :: this,right
   end subroutine muli_trapezium_append_interface
   subroutine muli_trapezium_final_interface(this)
   import muli_trapezium_node_class
   class(muli_trapezium_node_class),intent(inout) :: this
   end subroutine muli_trapezium_final_interface
   end interface
```

## 8.5 Implementierung der Prozeduren

integer, intent(in)::unit

## 8.5.1 Methoden für qcd 2 2 type Überschriebene serializable class Methoden muli trapezium write to marker \ subroutine muli\_trapezium\_write\_to\_marker (this,marker,status) class(muli\_trapezium\_type), intent(in) :: this class(marker\_type),intent(inout)::marker integer(kind=dik),intent(out)::status ! local variables integer::dim call marker%mark\_begin("muli\_trapezium\_type") call marker%mark("dim",this%dim) call marker%mark("r\_position",this%r\_position) call marker%mark("d\_position",this%d\_position) if(allocated(this%values))then call marker%mark("values", this%values) call marker%mark\_null("values") end if call marker%mark\_end("muli\_trapezium\_type") end subroutine muli\_trapezium\_write\_to\_marker muli trapezium read from marker \( \) subroutine muli\_trapezium\_read\_from\_marker (this, marker, status) class(muli\_trapezium\_type), intent(out) :: this class(marker\_type),intent(inout)::marker integer(kind=dik),intent(out)::status ! local variables integer::dim call marker%pick\_begin("muli\_trapezium\_type",status=status) call marker%pick("dim",this%dim,status) call marker%pick("r\_position",this%r\_position,status) call marker%pick("d\_position",this%d\_position,status) if(allocated(this%values))deallocate(this%values) call marker%verify\_nothing("values",status) if(status==serialize\_ok)then allocate(this%values(0:this%dim-1,7)) call marker%pick("values",this%values,status) call marker%pick\_end("muli\_trapezium\_type",status) end subroutine muli\_trapezium\_read\_from\_marker muli trapezium print to unit \( \ \) subroutine muli\_trapezium\_print\_to\_unit(this,unit,parents,components,peers) class(muli\_trapezium\_type),intent(in)::this

```
integer(kind=dik),intent(in)::parents,components,peers
    write(unit,'("Components of muli_trapezium_type:")')
    write(unit,fmt=*)"Dimension:
                                       ",this%dim
    write(unit,fmt=*)"Right position: ",this%r_position
    write(unit,fmt=*)"Position step: ",this%d_position
    if(allocated(this%values))then
       if(components>0)then
                                              ",muli_trapezium_get_r_value_array(this)
          write(unit,fmt=*)"Right values:
          write(unit,fmt=*)"Value step:
                                              ",this%get_d_value()
          write(unit,fmt=*)"Right integrals: ",this%get_r_integral()
          write(unit,fmt=*)"Integral step:
                                              ",this%get_d_integral()
          write(unit,fmt=*)"Right propabilities:",this%get_r_propability()
          write(unit,fmt=*)"Propability step: ",this%get_d_propability()
          write(unit,fmt=*)"Errors:
                                              ",this%get_error()
       else
          write(unit,fmt=*)"Values are allocated."
       end if
    else
       write(unit,fmt=*)"Values are not allocated."
    end if
  end subroutine muli_trapezium_print_to_unit
muli trapezium get type ↑
  pure subroutine muli_trapezium_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="muli_trapezium_type")
  end subroutine muli_trapezium_get_type
muli trapezium verify type \( \)
  elemental logical function muli_trapezium_verify_type(type) result(match)
    character(*),intent(in)::type
    match=type=="muli_trapezium_type"
  end function muli_trapezium_verify_type
Überschriebene measurable type Methoden
muli trapezium measure ↑
  elemental function muli_trapezium_measure(this)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double)::muli_trapezium_measure
    muli_trapezium_measure=this%measure_comp
  end function muli_trapezium_measure
Originäre muli trapezium type Methoden
muli trapezium initialize \( \)
```

```
subroutine muli_trapezium_initialize(this,dim,r_position,d_position)
    class(muli_trapezium_type),intent(inout)::this
    integer, intent(in)::dim
    real(kind=double),intent(in)::r_position,d_position
    integer::dim1,dim2
    this%dim=dim
    this%r_position=r_position
    this%d_position=d_position
    if(allocated(this%values))deallocate(this%values)
    allocate(this%values(0:dim-1,value dimension))
    do dim2=1, value_dimension-1
       do dim1=0, dim-1
          this%values(dim1,dim2)=0D0
       end do
    end do
    do dim1=0,dim-1
       this%values(dim1, value_dimension)=huge(1D0)
    end do
    this%measure_comp=huge(1D0)
  end subroutine muli_trapezium_initialize
!!! components !!!
muli trapezium get dimension †
  elemental function muli_trapezium_get_dimension(this) result(dim)
    class(muli_trapezium_type),intent(in)::this
    integer::dim
    dim=this%dim
  end function muli_trapezium_get_dimension
muli trapezium get l position \( \ \)
  pure function muli_trapezium_get_l_position(this) result(pos)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double)::pos
    pos=this%r_position-this%d_position
  end function muli_trapezium_get_l_position
muli trapezium get r position \( \)
  pure function muli_trapezium_get_r_position(this) result(pos)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double)::pos
    pos=this%r_position
  end function muli_trapezium_get_r_position
muli trapezium get d position \( \ \)
  pure function muli_trapezium_get_d_position(this) result(pos)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double)::pos
    pos=this%d_position
  end function muli_trapezium_get_d_position
```

```
muli trapezium get error sum \( \)
  pure function muli_trapezium_get_error_sum(this) result(error)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double)::error
    error=sum(this%values(0:this%dim-1,error_index))
  end function muli_trapezium_get_error_sum
muli trapezium get integral sum ↑
  pure function muli_trapezium_get_integral_sum(this) result(error)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double)::error
    error=sum(this%values(0:this%dim-1,d_integral_index))
  end function muli_trapezium_get_integral_sum
muli trapezium get l value element \( \ \)
  pure function muli_trapezium_get_l_value_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer, intent(in)::set
    real(kind=double)::element
    element=this%values(set,r_value_index)-this%values(set,d_value_index)
  end function muli_trapezium_get_l_value_element
muli trapezium get l value array \( \)
  pure function muli_trapezium_get_l_value_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double),dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,r_value_index)-this%values(0:this%dim-1,d_value_index)
  end function muli_trapezium_get_l_value_array
muli trapezium get r value element \( \)
  pure function muli_trapezium_get_r_value_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer, intent(in)::set
    real(kind=double)::element
    element=this%values(set,r_value_index)
  end function muli_trapezium_get_r_value_element
muli trapezium get r value array \( \)
  pure function muli_trapezium_get_r_value_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,r_value_index)
  end function muli_trapezium_get_r_value_array
muli trapezium get d value element \( \)
```

```
pure function muli_trapezium_get_d_value_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer,intent(in)::set
    real(kind=double)::element
    element=this%values(set,d_value_index)
  end function muli_trapezium_get_d_value_element
muli trapezium get d value array \( \)
  pure function muli_trapezium_get_d_value_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,d_value_index)
  end function muli_trapezium_get_d_value_array
muli trapezium get l integral element †
  pure function muli_trapezium_get_l_integral_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer,intent(in)::set
    real(kind=double)::element
    element=this%values(set,r_integral_index)-this%values(set,d_integral_index)
  end function muli_trapezium_get_l_integral_element
muli trapezium get l integral array \( \)
  pure function muli_trapezium_get_l_integral_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,r_integral_index)-this%values(0:this%dim-1,d_integral_index)
  end function muli_trapezium_get_l_integral_array
muli trapezium get r integral element †
  pure function muli_trapezium_get_r_integral_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer, intent(in)::set
    real(kind=double)::element
    element=this%values(set,r_integral_index)
  end function muli_trapezium_get_r_integral_element
muli trapezium get r integral array \( \)
  pure function muli_trapezium_get_r_integral_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,r_integral_index)
  end function muli_trapezium_get_r_integral_array
muli trapezium get d integral element \
```

```
pure function muli_trapezium_get_d_integral_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer,intent(in)::set
    real(kind=double)::element
    element=this%values(set,d_integral_index)
  end function muli_trapezium_get_d_integral_element
muli trapezium get d integral array \( \)
  pure function muli_trapezium_get_d_integral_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,d_integral_index)
  end function muli_trapezium_get_d_integral_array
muli trapezium get l propability element \( \ \)
  pure function muli_trapezium_get_l_propability_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer,intent(in)::set
    real(kind=double)::element
    element=this%values(set,r_propability_index)-this%values(set,d_propability_index)
  end function muli_trapezium_get_l_propability_element
muli trapezium get l propability array \( \)
  pure function muli_trapezium_get_l_propability_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
      this%values(0:this%dim-1,r_propability_index)&
     -this%values(0:this%dim-1,d_propability_index)
  end function muli_trapezium_get_l_propability_array
muli trapezium get r propability element \( \ \)
  pure function muli_trapezium_get_r_propability_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer, intent(in)::set
    real(kind=double)::element
    element=this%values(set,r_propability_index)
  end function muli_trapezium_get_r_propability_element
muli trapezium get r propability array \( \)
  pure function muli_trapezium_get_r_propability_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,r_propability_index)
  end function muli_trapezium_get_r_propability_array
muli trapezium get d propability array \( \)
```

```
pure function muli_trapezium_get_d_propability_array(this) result(subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::subarray
    subarray=this%values(0:this%dim-1,d_propability_index)
  end function muli_trapezium_get_d_propability_array
muli trapezium get d propability element \( \)
  pure function muli_trapezium_get_d_propability_element(this,set) result(element)
    class(muli_trapezium_type),intent(in)::this
    integer,intent(in)::set
    real(kind=double)::element
    element=this%values(set,d_propability_index)
  end function muli_trapezium_get_d_propability_element
muli trapezium get error \( \)
  pure function muli_trapezium_get_error(this) result(error)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double), dimension(this%dim)::error
    error=this%values(0:this%dim-1,error_index)
  end function muli_trapezium_get_error
! interpolation
muli trapezium get value at position \( \)
  subroutine muli_trapezium_get_value_at_position(this,pos,subarray)
    class(muli_trapezium_type),intent(in)::this
    real(kind=double),intent(in)::pos
    real(kind=double), dimension(this%dim), intent(out)::subarray
    subarray=this%get_r_value_array()-this%get_d_value()*this%d_position/(this%r_position-pos)
  end subroutine muli_trapezium_get_value_at_position
! write access
muli trapezium set r value \( \)
  subroutine muli_trapezium_set_r_value(this, subarray)
    class(muli_trapezium_type),intent(inout)::this
    real(kind=double),intent(in),dimension(0:this%dim-1)::subarray
    this%values(0:this%dim-1,r_value_index)=subarray
  end subroutine muli_trapezium_set_r_value
muli trapezium set d value \( \)
  subroutine muli_trapezium_set_d_value(this, subarray)
    class(muli_trapezium_type),intent(inout)::this
    real(kind=double),intent(in),dimension(0:this%dim-1)::subarray
    this%values(0:this%dim-1,d_value_index)=subarray
  end subroutine muli_trapezium_set_d_value
muli trapezium set r integral \( \ \)
```

```
subroutine muli_trapezium_set_r_integral(this, subarray)
    class(muli_trapezium_type),intent(inout)::this
    real(kind=double),intent(in),dimension(0:this%dim-1)::subarray
    this%values(0:this%dim-1,r_integral_index)=subarray
  end subroutine muli_trapezium_set_r_integral
muli trapezium set d integral \( \ \)
  subroutine muli_trapezium_set_d_integral(this, subarray)
    class(muli_trapezium_type),intent(inout)::this
    real(kind=double),intent(in),dimension(0:this%dim-1)::subarray
    this%values(0:this%dim-1,d_integral_index)=subarray
  end subroutine muli_trapezium_set_d_integral
muli trapezium set r propability \( \ext{\gamma} \)
  subroutine muli_trapezium_set_r_propability(this, subarray)
    class(muli_trapezium_type),intent(inout)::this
    real(kind=double),intent(in),dimension(0:this%dim-1)::subarray
    this%values(0:this%dim-1,r_propability_index)=subarray
  end subroutine muli_trapezium_set_r_propability
muli trapezium set d propability \( \ \)
  subroutine muli_trapezium_set_d_propability(this, subarray)
    class(muli_trapezium_type),intent(inout)::this
    real(kind=double),intent(in),dimension(0:this%dim-1)::subarray
    this%values(0:this%dim-1,d_propability_index)=subarray
  end subroutine muli_trapezium_set_d_propability
muli trapezium set error \( \)
  subroutine muli_trapezium_set_error(this, subarray)
    class(muli_trapezium_type),intent(inout)::this
    real(kind=double),intent(in),dimension(0:this%dim-1)::subarray
    this%values(0:this%dim-1,error_index)=subarray
    this%measure_comp=sum(subarray)
  end subroutine muli_trapezium_set_error
! tests
muli trapezium is left of \( \ext{\gamma} \)
  pure function muli_trapezium_is_left_of(this,that) result(is_left)
    logical::is_left
    class(muli_trapezium_type),intent(in)::this,that
    is_left=this%r_position<=that%r_position!-that%d_position
  end function muli_trapezium_is_left_of
muli trapezium includes †
```

```
elemental logical function muli_trapezium_includes&
    (this,dim,position,value,integral,propability) result(includes)
    class(muli_trapezium_type),intent(in)::this
    integer, intent(in)::dim
    real(kind=double),intent(in),optional::position,value,integral,propability
    includes=.true.
    if(present(position))then
       if(this%get_l_position()>position.or.position>=this%get_r_position())&
         includes=.false.
    end if
    if(present(value))then
       if(this%get_l_value(dim)>value.or.value>=this%get_r_value(dim))&
         includes=.false.
    end if
    if(present(integral))then
       if(this%get_l_integral(dim)>integral.or.integral>=this%get_r_integral(dim))&
         includes=.false.
    end if
    if(present(propability))then
       if(this%get_l_propability(dim)>propability.or.propability>=this%get_r_propability(dim))&
         includes=.false.
    end if
  end function muli_trapezium_includes
muli_trapezium update ↑
  subroutine muli_trapezium_update(this)
    class(muli_trapezium_type),intent(inout) :: this
    real(kind=double),dimension(:),allocatable :: int
    allocate(int(0:this%dim-1),source=this%get_d_integral())
    call this%set_d_integral(-this%d_position*(this%get_r_value_array()-this%get_d_value()/2D0))
    call this%set_error(abs(this%get_d_integral()-int))
     print('(11(D20.10))'),this%get_d_integral()
  end subroutine muli_trapezium_update
muli trapezium split ↑
  subroutine muli_trapezium_split(this,c_value,c_position,new_node)
    class(muli_trapezium_type),intent(inout) :: this
    real(kind=double),intent(in) :: c_position
    real(kind=double),intent(in),dimension(this%dim) :: c_value
    class(muli_trapezium_type),intent(out),pointer :: new_node
    real(kind=double) :: ndpr,ndpl
    real(kind=double), dimension(:), allocatable::ov,edv
    ndpr=this%r_position-c_position
    ndpl=this%d_position-ndpr
    allocate(ov(0:this%dim-1),&
      source=this%get_r_value_array()-ndpr*this%get_d_value()/this%d_position)
    allocate(edv(0:this%dim-1),source=c_value-ov)
    allocate(new_node)
    call new_node%initialize(dim=this%dim,&
         &r_position=c_position,&
```

```
&d_position=ndpl)
    call new_node%set_r_value(c_value)
    call new_node%set_d_value(this%get_d_value()+c_value-this%get_r_value_array())
    call new_node%set_d_integral(ndpl*(this%get_d_value()-this%get_r_value_array()-c_value)/
    call new_node%set_error(abs((edv*ndpl)/2D0))
    !new_node%measure_comp=sum(abs((edv*ndpl)/2D0))
    this%d_position=ndpr
    call this%set_d_value(this%get_r_value_array()-c_value)
    call this%set_d_integral(-(ndpr*(this%get_r_value_array()+c_value)/2D0))
    call this%set_error(abs(edv*ndpr/2D0))
    !this%measure_comp=sum(abs(edv*ndpr/2D0))
   print ('("muli_trapezium_split: new errors:")')
!
!
    print ('(E14.7)'),this%get_error()
    print ('(E14.7)'), new_node%get_error()
    print('(11(D20.10))'),new_node%get_d_integral()
     print('(11(D20.10))'),this%get_d_integral()
  end subroutine muli_trapezium_split
muli trapezium approx value \( \ \)
  pure function muli_trapezium_approx_value(this,x) result(val)
    ! returns the values at x
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double), dimension(this%dim) :: val
    real(kind=double), intent(in) :: x
    val = this%get_r_value_array()&
          +(x-this%r_position)*this%get_d_value()/this%d_position
  end function muli_trapezium_approx_value
muli\_trapezium\_approx\_value\_n \uparrow
  elemental function muli_trapezium_approx_value_n(this,x,n) result(val)
    ! returns the value at x
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double)::val
    real(kind=double), intent(in) :: x
    integer,intent(in)::n
    val = this%get_r_value_element(n)&
          +(x-this%r_position)*this%get_d_value_element(n)/this%d_position
  end function muli_trapezium_approx_value_n
muli trapezium approx integral \( \)
  pure function muli_trapezium_approx_integral(this,x)
    ! returns the integral from x to r_position
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double),dimension(this%dim) :: muli_trapezium_approx_integral
    real(kind=double), intent(in) :: x
    muli_trapezium_approx_integral = &
         &this%get_r_integral()+&
         &((this\%r_position-x)*\&
         &(-this%get_d_value()*(this%r_position-x)&
```

```
+2*this%d_position*this%get_r_value_array()))/&
         &(2*this%d_position)
  end function muli_trapezium_approx_integral
muli trapezium approx integral n ↑
  elemental function muli_trapezium_approx_integral_n(this,x,n) result(val)
    ! returns the integral from x to r_position
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double)::val
    real(kind=double), intent(in) :: x
    integer,intent(in)::n
    val = &
         &this%get_r_integral_element(n)+&
         &((this%r_position-x)*&
          \& (-this\%get\_d\_value\_element(n)*(this\%r\_position-x) \& \\
           +2*this%d_position*this%get_r_value_element(n)))/&
         &(2*this%d_position)
  end function muli_trapezium_approx_integral_n
muli trapezium approx propability \( \)
   pure function muli_trapezium_approx_propability(this,x) result(prop)
    ! returns the vlaues at x
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double), dimension(this%dim) :: prop
    real(kind=double), intent(in) :: x
    prop=exp(-this%approx_integral(x))
  end function muli_trapezium_approx_propability
muli trapezium approx propability n \
  elemental function muli_trapezium_approx_propability_n(this,x,n) result(val)
    ! returns the integral from x to r_position
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double)::val
    real(kind=double), intent(in) :: x
    integer,intent(in)::n
    val = exp(-this%approx_integral_n(x,n))
  end function muli_trapezium_approx_propability_n
muli_trapezium_approx position by integral \( \)
  elemental function muli_trapezium_approx_position_by_integral(this,dim,int) result(val)
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double)::val
    integer, intent(in)::dim
    real(kind=double),intent(in)::int
    real(kind=double)::dpdv
    dpdv=(this%d_position/this%values(dim,d_value_index))
    val=this%r_position-dpdv*&
         (this%values(dim,r_value_index)-&
           sqrt(((this%values(dim,r_integral_index)-int)*2D0/dpdv)&
```

```
+this%values(dim,r_value_index)**2))
  end function muli_trapezium_approx_position_by_integral
muli trapezium to node ↑
  subroutine muli_trapezium_to_node(this, value, list, tree)
    class(muli_trapezium_type),intent(in) :: this
    real(kind=double),intent(in) :: value
    class(muli_trapezium_list_type),optional,pointer,intent(out) :: list
    class(muli_trapezium_tree_type),optional,pointer,intent(out) :: tree
    if(present(list))then
       allocate(list)
       list%dim=this%dim
       list%r_position=this%r_position
       list%d_position=this%d_position
       allocate(list%values(0:this%dim-1,value_dimension),source=this%values)
    end if
    if(present(tree))then
       allocate(tree)
       tree%dim=this%dim
       tree%r_position=this%r_position
       tree%d_position=this%d_position
       allocate(tree%values(0:this%dim-1,value_dimension),source=this%values)
    end if
  end subroutine muli_trapezium_to_node
muli trapezium sum up \( \)
  subroutine muli_trapezium_sum_up(this)
    class(muli_trapezium_type),intent(inout) :: this
    integer::i
    if(allocated(this%values))then
       do i=1,7
          this%values(0,i)=sum(this%values(1:this%dim-1,i))
       end do
    end if
  end subroutine muli_trapezium_sum_up
8.5.2 Methoden für muli trapezium node class
muli trapezium node deserialize from marker \( \)
  subroutine muli_trapezium_node_deserialize_from_marker(this,name,marker)
    class(muli_trapezium_node_class), intent(out) :: this
    character(*),intent(in)::name
    class(marker_type),intent(inout)::marker
    integer(kind=dik)::status
    class(serializable_class),pointer::ser
    allocate(muli_trapezium_tree_type::ser)
    call marker%push_reference(ser)
    allocate(muli_trapezium_list_type::ser)
```

```
call marker%push_reference(ser)
    call serializable_deserialize_from_marker(this,name,marker)
    call marker%pop_reference(ser)
    deallocate(ser)
    call marker%pop_reference(ser)
    deallocate(ser)
  end subroutine muli_trapezium_node_deserialize_from_marker
muli trapezium node nullify \( \ \)
  subroutine muli_trapezium_node_nullify(this)
    class(muli_trapezium_node_class),intent(out) :: this
    nullify(this%left)
    nullify(this%right)
  end subroutine muli_trapezium_node_nullify
muli trapezium node get left \( \)
  subroutine muli_trapezium_node_get_left(this,left)
    class(muli_trapezium_node_class),intent(in) :: this
    class(muli_trapezium_node_class),pointer,intent(out) :: left
    left=>this%left
  end subroutine muli_trapezium_node_get_left
muli trapezium node get right \
  subroutine muli_trapezium_node_get_right(this,right)
    class(muli_trapezium_node_class),intent(in) :: this
    class(muli_trapezium_node_class),pointer,intent(out) :: right
    right=>this%right
  end subroutine muli_trapezium_node_get_right
muli trapezium node get leftmost †
  subroutine muli_trapezium_node_get_leftmost(this, node)
    class(muli_trapezium_node_class),intent(in) :: this
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    if (associated(this%left)) then
       node=>this%left
       do while (associated(node%left))
          node=>node%left
       end do
    else
       nullify(node)
    end if
  end subroutine muli_trapezium_node_get_leftmost
muli trapezium node get rightmost \( \ \ \ \ \)
  subroutine muli_trapezium_node_get_rightmost(this,right)
    class(muli_trapezium_node_class),intent(in) :: this
    class(muli_trapezium_node_class),pointer,intent(out) :: right
    if (associated(this%right)) then
```

```
right=>this%right
       do while (associated(right%right))
          right=>right%right
       end do
    else
       nullify(right)
    end if
  end subroutine muli_trapezium_node_get_rightmost
muli trapezium node decide by value \( \)
  subroutine muli_trapezium_node_decide_by_value(this,value,dim,record,node)
    class(muli_trapezium_node_class),intent(in) :: this
    real(kind=double),intent(in)::value
    integer,intent(in)::record,dim
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    if (this %values (dim, record) > value) then
       node=>this%left
    else
       node=>this%right
  end subroutine muli_trapezium_node_decide_by_value
muli trapezium node decide by position \( \)
  subroutine muli_trapezium_node_decide_by_position(this,position,node)
    class(muli_trapezium_node_class),intent(in) :: this
    real(kind=double),intent(in)::position
    class(muli_trapezium_node_class), pointer, intent(out) :: node
    if(this%r_position>position)then
       node=>this%left
    else
       node=>this%right
  end subroutine muli_trapezium_node_decide_by_position
muli trapezium node decide decreasing \( \)
  subroutine muli_trapezium_node_decide_decreasing(this,value,dim,record,node)
    class(muli_trapezium_node_class),intent(in) :: this
    real(kind=double),intent(in)::value
    integer, intent(in)::record, dim
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    if(this%values(dim,record) <=value)then
       node=>this%left
    else
       node=>this%right
    end if
  end subroutine muli_trapezium_node_decide_decreasing
muli trapezium node untangle ↑
```

```
subroutine muli_trapezium_node_untangle(this)
    class(muli_trapezium_node_class),intent(inout),target :: this
    if(associated(this%left))then
       if(associated(this%left%right,this))then
          nullify(this%left%right)
          nullify(this%left)
       end if
    end if
  end subroutine muli_trapezium_node_untangle
muli trapezium node apply \( \)
  recursive subroutine muli_trapezium_node_apply(this,proc)
    class(muli_trapezium_node_class),intent(inout) :: this
    interface
       subroutine proc(this)
         import muli_trapezium_node_class
         class(muli_trapezium_node_class),intent(inout) :: this
       end subroutine proc
    end interface
    if(associated(this%right))call proc(this%right)
    if(associated(this%left))call proc(this%left)
    call proc(this)
  end subroutine muli_trapezium_node_apply
8.5.3 Methoden für muli trapezium list type
muli trapezium list write to marker \( \)
  recursive subroutine muli_trapezium_list_write_to_marker (this,marker,status)
    class(muli_trapezium_list_type), intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    ! local variables
    class(serializable_class),pointer::ser
    call marker%mark_begin("muli_trapezium_list_type")
    call muli_trapezium_write_to_marker(this, marker, status)
    ser=>this%right
    call marker%mark_pointer("right",ser)
    call marker%mark_end("muli_trapezium_list_type")
  end subroutine muli_trapezium_list_write_to_marker
muli trapezium list read from marker \( \)
  recursive subroutine muli_trapezium_list_read_from_marker (this,marker,status)
    class(muli_trapezium_list_type), intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    print *,"muli_trapezium_list_read_from_marker:"
    print *, "You cannot deserialize a list with this subroutine."
```

```
print *,"Use muli_trapezium_list_read_target_from_marker instead."
  end subroutine muli_trapezium_list_read_from_marker
muli trapezium list read target from marker \( \)
  recursive subroutine muli_trapezium_list_read_target_from_marker (this,marker,status)
    class(muli_trapezium_list_type), target, intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    ! local variables
    class(serializable_class),pointer::ser
    call marker%pick_begin("muli_trapezium_list_type",status=status)
    call muli_trapezium_read_from_marker(this, marker, status)
    call marker%pick_pointer("right",ser)
    if(associated(ser))then
       select type(ser)
       class is (muli_trapezium_list_type)
          this%right=>ser
          ser%left=>this
       class default
          nullify(this%right)
          print *,"muli_trapezium_list_read_target_from_marker:"
          print *,"Unexpected type for right component."
       end select
    else
       nullify(this%right)
    end if
    call marker%pick_end("muli_trapezium_list_type",status)
  end subroutine muli_trapezium_list_read_target_from_marker
muli trapezium list print to unit \
  recursive subroutine muli_trapezium_list_print_to_unit&
    (this, unit, parents, components, peers)
    class(muli_trapezium_list_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    class(serializable_class),pointer::ser
    if(parents>0)call muli_trapezium_print_to_unit(this,unit,parents-1,components,peers)
    ser=>this%left
    call serialize_print_peer_pointer(ser,unit,-one,-one,-one,"LEFT")
    ser=>this%right
    call serialize_print_peer_pointer(ser,unit,parents,components,peers,"RIGHT")
  end subroutine muli_trapezium_list_print_to_unit
muli trapezium list get type †
  pure subroutine muli_trapezium_list_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="muli_trapezium_list_type")
  end subroutine muli_trapezium_list_get_type
muli trapezium list verify type \( \)
```

```
elemental logical function muli_trapezium_list_verify_type(type) result(match)
    character(*),intent(in)::type
    match=type=="muli_trapezium_list_type"
  end function muli_trapezium_list_verify_type
muli trapezium list finalize \( \)
 recursive subroutine muli_trapezium_list_finalize(this)
    class(muli_trapezium_list_type),intent(inout)::this
    if (associated(this%right)) then
       call this%right%finalize()
       deallocate(this%right)
    end if
    this%dim=0
  end subroutine muli_trapezium_list_finalize
muli trapezium list insert left a \( \)
  subroutine muli_trapezium_list_insert_left_a(this, value, content, new_node)
    class(muli_trapezium_list_type),intent(inout),target :: this
    real(kind=double),intent(in) :: value
    class(muli_trapezium_type),intent(in) :: content
    class(muli_trapezium_list_type),pointer,intent(out) :: new_node
    call content%to_node(value,list=new_node)
    new node%right=>this
    if(associated(this%left))then
       new_node%left=>this%left
       this%left%right=>new_node
    else
      nullify(new_node%left)
    end if
    this%left=>new_node
  end subroutine muli_trapezium_list_insert_left_a
muli trapezium list insert right a \
  subroutine muli_trapezium_list_insert_right_a(this,value,content,new_node)
    class(muli_trapezium_list_type),intent(inout),target :: this
    real(kind=double),intent(in) :: value
    class(muli_trapezium_type),intent(in) :: content
    class(muli_trapezium_list_type),pointer,intent(out) :: new_node
    class(muli_trapezium_list_type),pointer :: tmp_list
    call content%to_node(value,list=tmp_list)
    if(associated(this%right))then
       this%right%left=>tmp_list
       tmp_list%right=>this%right
    else
       nullify(tmp_list%right)
    end if
    this%right=>tmp_list
    tmp_list%left=>this
    new_node=>tmp_list
  end subroutine muli_trapezium_list_insert_right_a
```

```
muli trapezium list append \( \ \)
  subroutine muli_trapezium_list_append(this,right)
    class(muli_trapezium_list_type),intent(inout),target :: this
    class(muli_trapezium_node_class),intent(inout),target :: right
    this%right=>right
    right%left=>this
  end subroutine muli_trapezium_list_append
muli trapezium list to tree \( \)
  subroutine muli_trapezium_list_to_tree(this,out_tree)
    class(muli_trapezium_list_type), target, intent(in) :: this
    class(muli_trapezium_tree_type),intent(out) :: out_tree
    type(muli_trapezium_tree_type),target :: do_list
    class(muli_trapezium_node_class),pointer :: this_entry,do_list_entry,node
    class(muli_trapezium_tree_type),pointer :: tree1,tree2
    integer :: ite,log,n_deep,n_leaves
    n_leaves=0
    this_entry => this
    count: do while(associated(this_entry))
       n_leaves=n_leaves+1
       this_entry=>this_entry%right
    end do count
    call ilog2(n_leaves, log, n_deep)
    this_entry => this
    do_list_entry => do_list
    deep: do ite=0,n_deep-1
       allocate(tree1)
       tree1%down=>this_entry%right
       allocate(tree2)
       tree2%down=>this_entry
       tree2%left=>this_entry
       tree2%right=>this_entry%right
       tree1%left=>tree2
       this_entry => this_entry%right%right
       do_list_entry%right=>tree1
       do_list_entry=>tree1
    end do deep
    rest: do while(associated(this_entry))
       allocate(tree1)
       tree1%down=>this_entry
       tree1%left=>this_entry
       do_list_entry%right => tree1
       do_list_entry => tree1
       this_entry => this_entry%right
       ite=ite+1
    end do rest
    tree: do while(ite>2)
       do_list_entry => do_list%right
       node=>do_list
```

```
level: do while(associated(do_list_entry))
          node%right=>do_list_entry%right
          node=>do_list_entry%right
          do_list_entry%right=>node%left
          node%left=>do_list_entry
          do_list_entry=>node%right
          ite=ite-1
       end do level
    end do tree
    node=>do_list%right
    select type(node)
    type is (muli_trapezium_tree_type)
       call node%to_tree(out_tree)
    class default
       print *,"muli_trapezium_list_to_tree"
       print *,"unexpeted type for do_list%right"
    end select
    out_tree%right=>out_tree%right%left
    if(allocated(out_tree%values))then
       deallocate(out_tree%values)
    end if
    deallocate(do_list%right%right)
    deallocate(do_list%right)
  end subroutine muli_trapezium_list_to_tree
muli trapezium list gnuplot \( \ \)
  subroutine muli_trapezium_list_gnuplot(this,dir)
    class(muli_trapezium_list_type),intent(in),target :: this
    character(len=*),intent(in)::dir
    character(len=*),parameter::val_file="/value.plot"
    character(len=*),parameter::int_file="/integral.plot"
    character(len=*), parameter::err_file="/integral_error.plot"
    character(len=*),parameter::pro_file="/propability.plot"
    character(len=*),parameter::den_file="/density.plot"
    character(len=*),parameter::fmt='(E20.10)'
    class(muli_trapezium_node_class),pointer::list
    integer::val_unit,err_unit,int_unit,pro_unit,den_unit
    call generate_unit(val_unit,100,1000)
    open(val_unit,file=dir//val_file)
    call generate_unit(int_unit,100,1000)
    open(int_unit,file=dir//int_file)
    call generate_unit(err_unit,100,1000)
    open(err_unit,file=dir//err_file)
    call generate_unit(pro_unit,100,1000)
    open(pro_unit,file=dir//pro_file)
    call generate_unit(den_unit,100,1000)
    open(den_unit,file=dir//den_file)
    do while (associated(list))
        print *,list%r_position,list%get_r_value()
!
```

```
write(val_unit,fmt,advance='NO')list%r_position
       call write_array(val_unit,list%get_r_value_array(),fmt)
       write(int_unit,fmt,advance='NO')list%r_position
       call write_array(int_unit,list%get_r_integral(),fmt)
       write(err_unit,fmt,advance='NO')list%r_position
       call write_array(err_unit,list%get_error(),fmt)
       write(pro_unit,fmt,advance='NO')list%r_position
       call write_array(pro_unit,list%get_r_propability(),fmt)
       write(den_unit,fmt,advance='NO')list%r_position
       call write_array(den_unit,list%get_r_propability()*list%get_r_value_array(),fmt)
       list=>list%right
    end do
    close(val_unit)
    close(int_unit)
    close(err_unit)
    close(pro_unit)
    close(den_unit)
    contains
      subroutine write_array(unit,array,form)
        integer, intent(in)::unit
        real(kind=double),dimension(:),intent(in)::array
        character(len=*),intent(in)::form
        integer::n
        do n=1,size(array)
           write(unit,form,ADVANCE='NO')array(n)
           flush(unit)
        end do
        write(unit,'("")')
      end subroutine write_array
  end subroutine muli_trapezium_list_gnuplot
muli trapezium list integrate \( \)
  subroutine muli_trapezium_list_integrate(this,integral_sum,error_sum)
    class(muli_trapezium_list_type),intent(in),target :: this
    real(kind=double),intent(out)::error_sum,integral_sum
    real(kind=double), dimension(:), allocatable::integral
    class(muli_trapezium_node_class),pointer :: node
    allocate(integral(0:this%dim-1))
    call this%get_rightmost(node)
    integral=0D0
    integral_sum=0D0
    error_sum=0D0
    integrate: do while(associated(node))
       node%values(1,r_value_index)=sum(node%values(1:this%dim-1,r_value_index))
       node%values(1,d_value_index)=sum(node%values(1:this%dim-1,d_value_index))
       node%values(1,error_index)=sum(node%values(1:this%dim-1,error_index))
       error_sum=error_sum+node%values(1,error_index)
       call node%set_d_integral(&
         node%get_d_position()*(node%get_d_value()/2D0-node%get_r_value_array()))
       call node%set_r_propability(exp(-integral))
```

```
call node%set_r_integral(integral)
       integral=integral-node%get_d_integral()
       call node%set_d_propability(node%get_r_propability()-exp(-integral))
       call node%get_left(node)
    end do integrate
    integral_sum=integral(1)
  end subroutine muli_trapezium_list_integrate
muli trapezium list check \( \)
  recursive subroutine muli_trapezium_list_check(this)
    class(muli_trapezium_list_type),intent(in),target :: this
    class(muli_trapezium_node_class),pointer::tn,next
    real(kind=double), parameter::eps=1d-10
    logical::test
    if(associated(this%right))then
       next=>this%right
       test=(this%r_position.le.this%right%get_l_position()+eps)
       print *,"position check: ",test
       if(.not.test)then
          call this%print_parents()
          call next%print_parents()
       end if
       select type (next)
       class is (muli_trapezium_list_type)
          tn=>this
          print *,"structure check: ",associated(tn,next%left)
          print *,"class check:
          call next%check()
       class default
          print *,"class check:
                                   F''
       end select
    else
       print *,"end of list at ",this%r_position
  end subroutine muli_trapezium_list_check
muli trapezium list apply \( \ext{} \)
  recursive subroutine muli_trapezium_list_apply(this,proc)
    class(muli_trapezium_list_type),intent(inout) :: this
    interface
       subroutine proc(this)
         import muli_trapezium_node_class
         class(muli_trapezium_node_class),intent(inout) :: this
       end subroutine proc
    end interface
    if(associated(this%right))call this%right%apply(proc)
    call proc(this)
  end subroutine muli_trapezium_list_apply
```

### 8.5.4 Methoden für muli trapezium tree type

```
muli trapezium tree write to marker \( \)
  subroutine muli_trapezium_tree_write_to_marker (this,marker,status)
    class(muli_trapezium_tree_type), intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    ! local variables
    class(muli_trapezium_list_type),pointer::list
    class(serializable_class),pointer::ser
    call marker%mark_begin("muli_trapezium_tree_type")
    call this%get_left_list(list)
    ser=>list
    call marker%mark_pointer("list",ser)
    call marker%mark_end("muli_trapezium_tree_type")
  end subroutine muli_trapezium_tree_write_to_marker
muli trapezium tree read from marker \( \)
  subroutine muli_trapezium_tree_read_from_marker (this,marker,status)
    class(muli_trapezium_tree_type), intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    ! local variables
    class(serializable_class),pointer::ser
    call marker%pick_begin("muli_trapezium_tree_type",status=status)
    call marker%pick_pointer("list",ser)
    if(associated(ser))then
       select type(ser)
       class is (muli_trapezium_list_type)
          call ser%to_tree(this)
       class default
          nullify(this%left)
          nullify(this%right)
          nullify(this%down)
       end select
    else
       nullify(this%left)
       nullify(this%right)
       nullify(this%down)
    end if
    call marker%pick_end("muli_trapezium_tree_type",status)
  end subroutine muli_trapezium_tree_read_from_marker
muli trapezium tree print to unit \( \ \)
  recursive subroutine muli_trapezium_tree_print_to_unit(this,unit,parents,components,peers)
    class(muli_trapezium_tree_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    class(serializable_class),pointer::ser
```

```
if(parents>0)call muli_trapezium_print_to_unit(this,unit,parents-1,components,peers)
    ser=>this%down
    call serialize_print_peer_pointer(ser,unit,one,zero,one,"DOWN")
    if(associated(this%left))then
       select type(sertmp=>this%left)
       class is(muli_trapezium_list_type)
          ser=>sertmp
          call serialize_print_peer_pointer(ser,unit,parents,components,zero,"LEFT")
       class default
          call serialize_print_peer_pointer(ser,unit,parents,components,peers,"LEFT")
       end select
    else
       write(unit,fmt=*)"Left is not associated."
    end if
    if(associated(this%right))then
       select type(sertmp=>this%right)
       class is(muli_trapezium_list_type)
          ser=>sertmp
          call serialize_print_peer_pointer(ser,unit,parents,components,zero,"RIGHT")
       class default
          call serialize_print_peer_pointer(ser,unit,parents,components,peers,"RIGHT")
       end select
    else
       write(unit,fmt=*)"Right is not associated."
    end if
  end subroutine muli_trapezium_tree_print_to_unit
muli trapezium tree get type \( \)
  pure subroutine muli_trapezium_tree_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="muli_trapezium_tree_type")
  end subroutine muli_trapezium_tree_get_type
muli trapezium tree verify type \
  elemental logical function muli_trapezium_tree_verify_type(type) result(match)
    character(*),intent(in)::type
    match=type=="muli_trapezium_tree_type"
  end function muli_trapezium_tree_verify_type
Überschriebene muli trapezium node class Methoden
muli trapezium tree nullify \( \ \)
  subroutine muli_trapezium_tree_nullify(this)
    class(muli_trapezium_tree_type),intent(out) :: this
    call muli_trapezium_node_nullify(this)
    nullify(this%down)
  end subroutine muli_trapezium_tree_nullify
muli trapezium tree get left list \
```

```
subroutine muli_trapezium_tree_get_left_list(this,list)
    class(muli_trapezium_tree_type),intent(in) :: this
    class(muli_trapezium_list_type), pointer, intent(out) :: list
    class(muli_trapezium_node_class),pointer::node
    call this%get_leftmost(node)
    if(associated(node))then
       select type(node)
       class is (muli_trapezium_list_type)
          list=>node
       class default
          nullify(list)
       end select
    else
       nullify(list)
    end if
  end subroutine muli_trapezium_tree_get_left_list
muli trapezium tree get right list \
  subroutine muli_trapezium_tree_get_right_list(this,list)
    class(muli_trapezium_tree_type),intent(in) :: this
    class(muli_trapezium_list_type),pointer,intent(out) :: list
    class(muli_trapezium_node_class),pointer::node
    call this%get_rightmost(node)
    if (associated(node)) then
       select type(node)
       class is (muli_trapezium_list_type)
          list=>node
       class default
          nullify(list)
       end select
    else
       nullify(list)
    end if
  end subroutine muli_trapezium_tree_get_right_list
muli trapezium tree finalize \( \)
  recursive subroutine muli_trapezium_tree_finalize(this)
    class(muli_trapezium_tree_type),intent(inout) :: this
    if (associated(this%right)) then
       call this%right%untangle()
       call this%right%finalize()
       deallocate(this%right)
    if (associated(this%left)) then
       call this%left%untangle()
       call this%left%finalize()
       deallocate(this%left)
    end if
    this%dim=0
  end subroutine muli_trapezium_tree_finalize
```

```
muli trapezium tree decide by value \( \)
  subroutine muli_trapezium_tree_decide_by_value(this,value,dim,record,node)
    class(muli_trapezium_tree_type),intent(in) :: this
    real(kind=double),intent(in)::value
    integer,intent(in)::record,dim
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    if(this%down%values(dim,record)>value)then
       node=>this%left
    else
       node=>this%right
    end if
  end subroutine muli_trapezium_tree_decide_by_value
muli trapezium tree decide by position \( \)
  subroutine muli_trapezium_tree_decide_by_position(this,position,node)
    class(muli_trapezium_tree_type),intent(in) :: this
    real(kind=double),intent(in)::position
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    if (this%down%r_position>position)then
       node=>this%left
    else
       node=>this%right
  end subroutine muli_trapezium_tree_decide_by_position
muli trapezium tree decide decreasing \( \)
  subroutine muli_trapezium_tree_decide_decreasing(this,value,dim,record,node)
    class(muli_trapezium_tree_type),intent(in) :: this
    real(kind=double),intent(in)::value
    integer,intent(in)::record,dim
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    if (this %down % values (dim, record) <= value) then
       node=>this%left
    else
       node=>this%right
  end subroutine muli_trapezium_tree_decide_decreasing
muli trapezium tree find by value \( \extrm{\chi} \)
  subroutine muli_trapezium_tree_find_by_value(this,value,dim,record,node)
    class(muli_trapezium_tree_type),intent(in),target :: this
    real(kind=double),intent(in)::value
    integer,intent(in)::record,dim
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    node=>this
    do while(.not.allocated(node%values))
       call node%decide(value,dim,record,node)
    end do
  end subroutine muli_trapezium_tree_find_by_value
```

```
muli trapezium tree find by position \( \)
  subroutine muli_trapezium_tree_find_by_position(this,position,node)
    class(muli_trapezium_tree_type),intent(in),target :: this
    real(kind=double),intent(in)::position
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    node=>this
    do while(.not.allocated(node%values))
       call node%decide(position, node)
  end subroutine muli_trapezium_tree_find_by_position
muli trapezium tree find decreasing \( \)
  subroutine muli_trapezium_tree_find_decreasing(this, value, dim, node)
    class(muli_trapezium_tree_type),intent(in),target :: this
    real(kind=double),intent(in)::value
    integer,intent(in)::dim
    class(muli_trapezium_node_class),pointer,intent(out) :: node
    node=>this
    do while(.not.allocated(node%values))
       call node%decide_decreasing(value,dim,r_integral_index,node)
  end subroutine muli_trapezium_tree_find_decreasing
muli trapezium tree approx by integral \( \ \)
  subroutine muli_trapezium_tree_approx_by_integral&
    (this,int,dim,in_range,position,value,integral,content)
    class(muli_trapezium_tree_type),intent(in),target :: this
    real(kind=double),intent(in) :: int
    integer,intent(in)::dim
    logical,intent(out) :: in_range
    class(muli_trapezium_node_class),pointer,intent(out),optional :: content
    real(kind=double),intent(out),optional :: position,value,integral
    integer::i
    real(kind=double) :: DINT!,l_prop,r_prop,d_prop
    real(kind=double)::RP,DP,RV,DV,RI!FC = gfortran
    class(muli_trapezium_node_class),pointer :: node
    node=>this
    do while(.not.allocated(node%values))
       call node%decide_decreasing(INT,dim,r_integral_index,node)
    end do
    if(
         int<=node%values(dim,r_integral_index)-node%values(dim,d_integral_index)&
         &int>=node%values(dim,r_integral_index))then
       in_range=.true.
         RP=node%r_position!FC = gfortran
         DP=node%d_position!FC = gfortran
         RV=node%values(dim,r_value_index)!FC = gfortran
         DV=node%values(dim,d_value_index)!FC = gfortran
         RI=node%values(dim,r_integral_index)!FC = gfortran
```

```
if (present(position)) then
            DINT=(ri-int)*2D0*dv/dp
            position=rp-(dp/dv)*(rv-sqrt(dint+rv**2))
         end if
         if (present(value)) then
            value=Sqrt(dp*(-2*dv*int + 2*dv*ri + dp*rv**2))/dp
         end if
         if (present(integral)) then
            integral=int
         if (present(content)) then
            content=>node
         end if
    else
       in_range=.false.
  end subroutine muli_trapezium_tree_approx_by_integral
muli trapezium tree approx by propability \( \)
  subroutine muli_trapezium_tree_approx_by_propability&
    (this,prop,dim,in_range,position,value,integral,content)
    class(muli_trapezium_tree_type),intent(in),target :: this
    real(kind=double),intent(in) :: prop
    integer, intent(in)::dim
    logical,intent(out) :: in_range
    class(muli_trapezium_node_class),pointer,intent(out),optional :: content
    real(kind=double),intent(out),optional :: position,value,integral
    integer::i
    real(kind=double) :: INT,DINT,l_prop,r_prop,d_prop
    class(muli_trapezium_node_class),pointer :: node
    if(ODO<prop.and.prop<1D0)then
       node=>this
       INT=-log(prop)
       call muli_trapezium_tree_approx_by_integral&
         (this, int, dim, in_range, position, value, integral, content)
    else
       in_range=.false.
    end if
  end subroutine muli_trapezium_tree_approx_by_propability
muli trapezium tree to tree \( \)
  subroutine muli_trapezium_tree_to_tree(this,out_tree)
    class(muli_trapezium_tree_type),intent(in) :: this
    class(muli_trapezium_tree_type),intent(out) :: out_tree
    out_tree%left=>this%left
    out_tree%right=>this%right
    out_tree%down=>this%down
  end subroutine muli_trapezium_tree_to_tree
muli trapezium tree append \( \ \)
```

```
subroutine muli_trapezium_tree_append(this,right)
    class(muli_trapezium_tree_type),intent(inout),target :: this
    class(muli_trapezium_node_class),intent(inout),target :: right
    print ('("muli_trapezium_tree_append: Not yet implemented.")')
    end subroutine muli_trapezium_tree_append

muli_trapezium_tree_gnuplot \^
subroutine muli_trapezium_tree_gnuplot(this,dir)
    class(muli_trapezium_tree_type),intent(in) :: this
    character(len=*),intent(in)::dir
    class(muli_trapezium_list_type),pointer::list
    call this%get_left_list(list)
    call list%gnuplot(dir)
end subroutine muli_trapezium_tree_gnuplot
```

# 9 Modul muli fibonacci tree

# 9.1 Abhängigkeiten

```
use muli basic
```

#### 9.2 Parameter

```
character(*),parameter,private :: no_par = "edge=\noparent"
character(*),parameter,private :: no_ret = "edge=\noreturn"
character(*),parameter,private :: no_kid = "edge=\nochild"
character(*),parameter,private :: le_kid = "edge=\childofleave"
```

## 9.3 Derived Types

## 9.3.1 fibonacci node type

```
type,extends(measurable_class) :: fibonacci_node_type
   private
   class(fibonacci_node_type), pointer :: up => null()
   class(measurable_class), pointer :: down => null()
   class(fibonacci_node_type), pointer :: left => null()
   class(fibonacci_node_type), pointer :: right => null()
   integer :: depth = 0
contains
   ! overridden serializable_class procedures
   procedure::write_to_marker=>fibonacci_node_write_to_marker
   procedure::read_from_marker=>fibonacci_node_read_from_marker
  procedure::read_target_from_marker=>fibonacci_node_read_target_from_marker
   procedure::print_to_unit=>fibonacci_node_print_to_unit
  procedure,nopass::get_type=>fibonacci_node_get_type
  procedure::deserialize_from_marker=>fibonacci_node_deserialize_from_marker
   ! overridden measurable_class procedures
   procedure::measure=>fibonacci_node_measure
  procedure,public ::deallocate_tree=>fibonacci_node_deallocate_tree
  procedure,public ::deallocate_all=>fibonacci_node_deallocate_all
   procedure, public ::get_depth=>fibonacci_node_get_depth
   procedure,public ::count_leaves=>fibonacci_node_count_leaves
```

```
! public tests
    procedure,public,nopass ::is_leave=>fibonacci_node_is_leave
    procedure,public,nopass ::is_root=>fibonacci_node_is_root
    procedure,public,nopass ::is_inner=>fibonacci_node_is_inner
! print methods
    procedure, public ::write_association=>fibonacci_node_write_association
    procedure,public ::write_contents=>fibonacci_node_write_contents
    procedure,public ::write_values=>fibonacci_node_write_values
    procedure,public ::write_leaves=>fibonacci_node_write_leaves
    !procedure,public ::write=>fibonacci_node_write_contents
! write methods
    procedure,public ::write_pstricks=>fibonacci_node_write_pstricks
! elaborated functions
    procedure,public ::copy_node=>fibonacci_node_copy_node
    procedure,public ::find_root=>fibonacci_node_find_root
    procedure,public ::find_leftmost=>fibonacci_node_find_leftmost
    procedure,public ::find_rightmost=>fibonacci_node_find_rightmost
    procedure,public ::find=>fibonacci_node_find
    procedure,public ::find_left_leave=>fibonacci_node_find_left_leave
    procedure, public ::find_right_leave=>fibonacci_node_find_right_leave
    procedure,public ::apply_to_leaves=>fibonacci_node_apply_to_leaves
    procedure, public ::apply_to_leaves_rl=>fibonacci_node_apply_to_leaves_rl
! private procedures: these are unsafe!
    procedure ::set_depth=>fibonacci_node_set_depth
    procedure ::append_left=>fibonacci_node_append_left
    procedure ::append_right=>fibonacci_node_append_right
    procedure ::replace=>fibonacci_node_replace
    procedure ::swap=>fibonacci_node_swap_nodes
    procedure ::flip=>fibonacci_node_flip_children
    procedure ::rip=>fibonacci_node_rip
    procedure ::remove_and_keep_parent=>fibonacci_node_remove_and_keep_parent
    procedure ::remove_and_keep_twin=>fibonacci_node_remove_and_keep_twin
    procedure ::rotate_left=>fibonacci_node_rotate_left
    procedure ::rotate_right=>fibonacci_node_rotate_right
    procedure ::rotate=>fibonacci_node_rotate
    procedure ::balance_node=>fibonacci_node_balance_node
    procedure ::update_depth_save=>fibonacci_node_update_depth_save
    procedure ::update_depth_unsave=>fibonacci_node_update_depth_unsave
    procedure ::repair=>fibonacci node repair
! tests: these are save when type is fibonacci_node_type and else unsafe.
    procedure ::is_left_short=>fibonacci_node_is_left_short
    procedure ::is_right_short=>fibonacci_node_is_right_short
    procedure ::is_unbalanced=>fibonacci_node_is_unbalanced
    procedure ::is_left_too_short=>fibonacci_node_is_left_too_short
    procedure ::is_right_too_short=>fibonacci_node_is_right_too_short
    procedure ::is_too_unbalanced=>fibonacci_node_is_too_unbalanced
    procedure ::is_left_child=>fibonacci_node_is_left_child
    procedure ::is_right_child=>fibonacci_node_is_right_child
 end type fibonacci_node_type
```

## 9.3.2 fibonacci leave type

```
type,extends(fibonacci_node_type) :: fibonacci_leave_type
    class(measurable_class),pointer :: content
contains
   ! overridden serializable_class procedures
   procedure::print_to_unit=>fibonacci_leave_print_to_unit
   procedure,nopass::get_type=>fibonacci_leave_get_type
   procedure,public ::deallocate_all=>fibonacci_leave_deallocate_all
   ! new procedures
   procedure,public ::pick=>fibonacci_leave_pick
   procedure,public ::get_left=>fibonacci_leave_get_left
   procedure,public ::get_right=>fibonacci_leave_get_right
   procedure,public ::write_pstricks=>fibonacci_leave_write_pstricks
   procedure,public ::copy_content=>fibonacci_leave_copy_content
   procedure,public ::set_content=>fibonacci_leave_set_content
   procedure,public ::get_content=>fibonacci_leave_get_content
   procedure,public,nopass ::is_inner=>fibonacci_leave_is_inner
   procedure,public,nopass ::is_leave=>fibonacci_leave_is_leave
  procedure ::insert_leave_by_node=>fibonacci_leave_insert_leave_by_node
   procedure ::is_left_short=>fibonacci_leave_is_left_short
   procedure ::is_right_short=>fibonacci_leave_is_right_short
   procedure ::is_unbalanced=>fibonacci_leave_is_unbalanced
   procedure ::is_left_too_short=>fibonacci_leave_is_left_too_short
   procedure ::is_right_too_short=>fibonacci_leave_is_right_too_short
   procedure ::is_too_unbalanced=>fibonacci_leave_is_too_unbalanced
end type fibonacci_leave_type
```

## 9.3.3 fibonacci root type

```
type,extends(fibonacci_node_type) :: fibonacci_root_type
    logical::is_valid_c=.false.
    class(fibonacci_leave_type),pointer ::leftmost=>null()
    class(fibonacci_leave_type),pointer ::rightmost=>null()
 contains
    ! overridden serializable_class procedures
    procedure::write_to_marker=>fibonacci_root_write_to_marker
    procedure::read_target_from_marker=>fibonacci_root_read_target_from_marker
    procedure::print_to_unit=>fibonacci_root_print_to_unit
    procedure, nopass::get_type=>fibonacci_root_get_type
    ! new procedures
    procedure::get_leftmost=>fibonacci_root_get_leftmost
    procedure::get_rightmost=>fibonacci_root_get_rightmost
! public tests
    procedure,public,nopass ::is_root=>fibonacci_root_is_root
    procedure,public,nopass ::is_inner=>fibonacci_root_is_inner
    procedure,public ::is_valid=>fibonacci_root_is_valid
    procedure,public ::count_leaves=>fibonacci_root_count_leaves
    procedure,public ::write_pstricks=>fibonacci_root_write_pstricks
    procedure,public ::copy_root=>fibonacci_root_copy_root
```

```
procedure,public ::push_by_content=>fibonacci_root_push_by_content
  procedure,public ::push_by_leave=>fibonacci_root_push_by_leave
  procedure,public ::pop_left=>fibonacci_root_pop_left
  procedure,public ::pop_right=>fibonacci_root_pop_right
  procedure,public ::merge=>fibonacci_root_merge
  procedure,public ::set_leftmost=>fibonacci_root_set_leftmost
  procedure,public ::set_rightmost=>fibonacci_root_set_rightmost
  procedure,public ::init_by_leave=>fibonacci_root_init_by_leave
  procedure,public ::init_by_content=>fibonacci_root_init_by_content
  procedure,public ::reset=>fibonacci_root_reset
   ! init/final
  procedure,public ::deallocate_tree=>fibonacci_root_deallocate_tree
  procedure,public ::deallocate_all=>fibonacci_root_deallocate_all
  procedure ::is_left_child=>fibonacci_root_is_left_child
  procedure ::is_right_child=>fibonacci_root_is_right_child
end type fibonacci_root_type
```

## 9.3.4 fibonacci stub type

```
type,extends(fibonacci_root_type) :: fibonacci_stub_type
contains
 ! overridden serializable_class procedures
 procedure,nopass::get_type=>fibonacci_stub_get_type
 ! overridden fibonacci_root_type procedures
 procedure,public ::push_by_content=>fibonacci_stub_push_by_content
 procedure,public ::push_by_leave=>fibonacci_stub_push_by_leave
 procedure,public ::pop_left=>fibonacci_stub_pop_left
 procedure,public ::pop_right=>fibonacci_stub_pop_right
end type fibonacci_stub_type
```

## 9.3.5 fibonacci leave list type

```
type fibonacci_leave_list_type
  class(fibonacci_leave_type),pointer ::leave=>null()
  class(fibonacci_leave_list_type),pointer :: next => null()
end type fibonacci_leave_list_type
```

# 9.4 Implementierung der Prozeduren

```
9.4.1 Methoden für fibonacci_node_type

Überschriebene serializable class Methoden
```

```
fibonacci node write to marker \
```

```
recursive subroutine fibonacci_node_write_to_marker(this,marker,status)
    class(fibonacci_node_type), intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
! local variables
    class(serializable_class),pointer::ser
    call marker%mark_begin("fibonacci_node_type")
    ser=>this%left
    call marker%mark_pointer("left",ser)
    ser=>this%right
    call marker%mark_pointer("right",ser)
    ser=>this%xxxx
    call marker%mark_pointer("down",ser)
    call marker%mark_end("fibonacci_node_type")
  end subroutine fibonacci_node_write_to_marker
fibonacci node read from marker \( \)
 recursive subroutine fibonacci_node_read_from_marker (this,marker,status)
    class(fibonacci_node_type), intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    print *, "fibonacci_node_read_from_marker: You cannot deserialize a list with this subroutine."
    print *,"Use fibonacci_node_read_target_from_marker instead."
  end subroutine fibonacci_node_read_from_marker
fibonacci node read target from marker \( \)
recursive subroutine fibonacci_node_read_target_from_marker(this,marker,status)
    class(fibonacci_node_type), target, intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
! local variables
    class(serializable_class),pointer::ser
    call marker%pick_begin("fibonacci_node_type",status=status)
    call marker%pick_pointer("left",ser)
    if(status==0)then
       select type(ser)
       class is (fibonacci_node_type)
          this%left=>ser
          this%left%up=>this
       end select
    end if
    call marker%pick_pointer("right",ser)
    if(status==0)then
       select type(ser)
       class is (fibonacci_node_type)
          this%right=>ser
          this%right%up=>this
       end select
    end if
    call marker%pick_pointer("down",ser)
```

```
if(status==0)then
       select type(ser)
       class is (measurable_class)
          this%xxxx=>ser
       end select
    end if
    call marker%pick_end("fibonacci_node_type",status)
  end subroutine fibonacci_node_read_target_from_marker
fibonacci node get type \( \)
  pure subroutine fibonacci_node_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="fibonacci_node_type")
  end subroutine fibonacci_node_get_type
fibonacci node deserialize from marker \( \)
  subroutine fibonacci_node_deserialize_from_marker(this,name,marker)
    class(fibonacci_node_type),intent(out)::this
    character(*),intent(in)::name
    class(marker_type),intent(inout)::marker
    class(serializable_class),pointer::ser
    allocate(fibonacci_leave_type::ser)
    call marker%push_reference(ser)
    allocate(fibonacci_node_type::ser)
    call marker%push_reference(ser)
    call serializable_deserialize_from_marker(this,name,marker)
    call marker%pop_reference(ser)
    deallocate(ser)
    call marker%pop_reference(ser)
    deallocate(ser)
  end subroutine fibonacci_node_deserialize_from_marker
fibonacci node print to unit \
  recursive subroutine fibonacci_node_print_to_unit(this,unit,parents,components,peers)
    class(fibonacci_node_type),intent(in)::this
    integer,intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    class(serializable_class),pointer::ser
    write(unit,'("Components of fibonacci_node_type:")')
    write(unit, '("Depth: ", I22)')this%depth
    write(unit, '("Value: ",E23.16)')this%measure()
    ser=>this%up
    call serialize_print_comp_pointer(ser, unit, parents, -one, -one, "Up:
    ser=>this%left
    call serialize_print_peer_pointer(ser,unit,parents,components,peers,"Left:
                                                                                   ")
    ser=>this%right
    call serialize_print_peer_pointer(ser,unit,parents,components,peers,"Right:
                                                                                   ")
  end subroutine fibonacci_node_print_to_unit
fibonacci node measure \( \ \)
```

```
elemental function fibonacci_node_measure(this)
    class(fibonacci_node_type),intent(in)::this
    real(kind=double)::fibonacci_node_measure
    fibonacci_node_measure=this%down%measure()
  end function fibonacci_node_measure
! init/final
fibonacci node deallocate tree \uparrow
  recursive subroutine fibonacci_node_deallocate_tree(this)
    class(fibonacci_node_type),intent(inout) :: this
    if (associated(this%left)) then
       call this%left%deallocate_tree()
       deallocate(this%left)
    end if
    if (associated(this%right)) then
       call this%right%deallocate_tree()
       deallocate(this%right)
    end if
    call this%set_depth(0)
  end subroutine fibonacci_node_deallocate_tree
fibonacci node deallocate all \( \ \)
  recursive subroutine fibonacci_node_deallocate_all(this)
    class(fibonacci_node_type),intent(inout) :: this
    if (associated(this%left)) then
       call this%left%deallocate_all()
       deallocate(this%left)
    end if
    if (associated(this%right)) then
       call this%right%deallocate_all()
       deallocate(this%right)
    end if
    call this%set_depth(0)
  end subroutine fibonacci_node_deallocate_all
fibonacci node set depth \uparrow
  subroutine fibonacci_node_set_depth(this,depth)
    class(fibonacci_node_type),intent(inout) :: this
    integer,intent(in) :: depth
    this%depth=depth
  end subroutine fibonacci_node_set_depth
fibonacci node get depth \uparrow
  elemental function fibonacci_node_get_depth(this)
    class(fibonacci_node_type),intent(in) :: this
    integer :: fibonacci_node_get_depth
    fibonacci_node_get_depth = this%depth
  end function fibonacci_node_get_depth
```

```
fibonacci node is leave \( \ \)
  elemental function fibonacci_node_is_leave()
    logical :: fibonacci_node_is_leave
    fibonacci_node_is_leave = .false.
  end function fibonacci_node_is_leave
fibonacci node is root \( \ \)
  elemental function fibonacci_node_is_root()
    logical :: fibonacci_node_is_root
    fibonacci_node_is_root = .false.
  end function fibonacci_node_is_root
fibonacci node is inner \( \)
  elemental function fibonacci_node_is_inner()
    logical :: fibonacci_node_is_inner
    fibonacci_node_is_inner = .true.
  end function fibonacci_node_is_inner
fibonacci node write leaves \
  subroutine fibonacci_node_write_leaves(this,unit)
    class(fibonacci_node_type),intent(in),target :: this
    integer,intent(in),optional :: unit
    call this%apply_to_leaves(fibonacci_leave_write,unit)
  end subroutine fibonacci_node_write_leaves
fibonacci node write contents \
  subroutine fibonacci_node_write_contents(this,unit)
    class(fibonacci_node_type),intent(in),target :: this
    integer,intent(in),optional :: unit
    call this%apply_to_leaves(fibonacci_leave_write_content,unit)
  end subroutine fibonacci_node_write_contents
fibonacci node write values \
  subroutine fibonacci_node_write_values(this, unit)
    class(fibonacci_node_type),intent(in),target :: this
    integer,intent(in),optional :: unit
    call this%apply_to_leaves(fibonacci_leave_write_value,unit)
  end subroutine fibonacci_node_write_values
fibonacci node write association \( \ \)
  subroutine fibonacci_node_write_association(this,that)
    class(fibonacci_node_type),intent(in),target :: this
    class(fibonacci_node_type),intent(in),target :: that
    if (associated(that%left,this)) then
       write(*,'("this is left child of that")')
    if (associated(that%right,this)) then
```

```
write(*,'("this is right child of that")')
    end if
    if (associated(that%up,this)) then
       write(*,'("this is parent of that")')
    end if
    if (associated(this%left,that)) then
       write(*,'("that is left child of this")')
    if (associated(this%right,that)) then
       write(*,'("that is right child of this")')
    if (associated(this%up,that)) then
       write(*,'("that is parent of this")')
    end if
  end subroutine fibonacci_node_write_association
fibonacci node write pstricks \( \)
 recursive subroutine fibonacci_node_write_pstricks(this,unitnr)
    class(fibonacci_node_type),intent(in),target :: this
    integer,intent(in) :: unitnr
    if (associated(this%up)) then
       if (associated(this%up%left,this).neqv.(associated(this%up%right,this))) then
          write(unitnr,'("\beginpsTree\Toval\node",i3,"",f9.3,"")')&
            int(this%depth),this%measure()
       else
          write(unitnr,'("\beginpsTree\Toval[",a,"]\node",i3,"",f9.3,"")')&
            no_ret,int(this%depth),this%measure()
       end if
       write(unitnr,'("\beginpsTree\Toval[",a,"]\node",i3,"",f9.3,"")')&
         no_par,int(this%depth),this%measure()
    if (associated(this%left)) then
       call this%left%write_pstricks(unitnr)
    else
       write(unitnr,'("\Tr[edge=brokenline]")')
    if (associated(this%right)) then
       call this%right%write_pstricks(unitnr)
    else
       write(unitnr,'("\Tr[edge=brokenline]")')
    write(unitnr,'("\endpsTree")')
  end subroutine fibonacci_node_write_pstricks
fibonacci node copy node \( \)
 subroutine fibonacci_node_copy_node(this,primitive)
    class(fibonacci_node_type),intent(out) :: this
    class(fibonacci_node_type),intent(in) :: primitive
    this%up => primitive%up
```

```
this%left => primitive%left
    this%right => primitive%right
    this%depth = primitive%depth
    this%down=> primitive%down
  end subroutine fibonacci_node_copy_node
fibonacci node find root \
  subroutine fibonacci_node_find_root(this,root)
    class(fibonacci_node_type),intent(in),target :: this
    class(fibonacci_root_type),pointer,intent(out) :: root
    class(fibonacci_node_type),pointer :: node
    node=>this
    do while(associated(node%up))
       node=>node%up
    end do
    select type (node)
    class is (fibonacci_root_type)
       root=>node
    class default
       nullify(root)
       print *,"fibonacci_node_find_root: root is not type compatible to&
       & fibonacci_root_type. Retured NULL()."
    end select
  end subroutine fibonacci_node_find_root
fibonacci node find leftmost \
  subroutine fibonacci_node_find_leftmost(this,leave)
    class(fibonacci_node_type),intent(in), target :: this
    class(fibonacci_leave_type), pointer, intent(out) :: leave
    class(fibonacci_node_type), pointer :: node
    node=>this
    do while(associated(node%left))
       node=>node%left
    end do
    select type (node)
    class is (fibonacci_leave_type)
       leave => node
    class default
       leave => null()
    end select
  end subroutine fibonacci_node_find_leftmost
fibonacci node find rightmost \uparrow
  subroutine fibonacci_node_find_rightmost(this,leave)
    class(fibonacci_node_type),intent(in), target
    class(fibonacci_leave_type), pointer, intent(out) :: leave
    class(fibonacci_node_type), pointer :: node
    node=>this
    do while(associated(node%right))
```

```
node=>node%right
    end do
    select type (node)
    class is (fibonacci_leave_type)
       leave => node
    class default
       leave => null()
    end select
  end subroutine fibonacci_node_find_rightmost
fibonacci node find \
  subroutine fibonacci_node_find(this,value,leave)
    class(fibonacci_node_type),intent(in),target :: this
    real(kind=double),intent(in) :: value
    class(fibonacci_leave_type),pointer,intent(out) :: leave
    class(fibonacci_node_type), pointer :: node
    node=>this
    do
       if (node>=value) then
          if (associated(node%left)) then
             node=>node%left
          else
             print *,"fibonacci_node_find: broken tree!"
             leave => null()
             return
          end if
       else
          if (associated(node%right)) then
             node=>node%right
          else
             print *,"fibonacci_node_find: broken tree!"
             leave => null()
             return
          end if
       end if
       select type (node)
       class is (fibonacci_leave_type)
          leave => node
          exit
       end select
    end do
  end subroutine fibonacci_node_find
fibonacci node find left leave \uparrow
  subroutine fibonacci_node_find_left_leave(this,leave)
    class(fibonacci_node_type),intent(in),target :: this
    class(fibonacci_node_type),pointer :: node
    class(fibonacci_leave_type), pointer, intent(out) :: leave
    nullify(leave)
    node=>this
```

```
do while (associated(node%up))
       if (associated(node%up%right,node)) then
          node=>node%up%left
          do while (associated(node%right))
             node=>node%right
          end do
          select type (node)
          class is (fibonacci_leave_type)
          leave=>node
          end select
          exit
       end if
       node=>node%up
    end do
  end subroutine fibonacci_node_find_left_leave
fibonacci node find right leave \( \)
  subroutine fibonacci_node_find_right_leave(this,leave)
    class(fibonacci_node_type),intent(in),target
    class(fibonacci_node_type),pointer :: node
    class(fibonacci_leave_type),pointer,intent(out) :: leave
    nullify(leave)
    node=>this
    do while (associated(node%up))
       if (associated(node%up%left,node)) then
          node=>node%up%right
          do while (associated(node%left))
             node=>node%left
          end do
          select type (node)
          class is (fibonacci_leave_type)
          leave=>node
          end select
          exit
       end if
       node=>node%up
  end subroutine fibonacci_node_find_right_leave
fibonacci node replace \( \ \)
  subroutine fibonacci_node_replace(this,old_node)
    class(fibonacci_node_type),intent(inout),target :: this
    class(fibonacci_node_type),target :: old_node
    if (associated(old_node%up)) then
       if (old_node%is_left_child()) then
          old_node%up%left => this
       else
          if (old_node%is_right_child()) then
             old_node%up%right => this
          end if
```

```
end if
       this%up => old_node%up
    else
       nullify(this%up)
    end if
  end subroutine fibonacci_node_replace
fibonacci node swap nodes †
 subroutine fibonacci_node_swap_nodes(left,right)
    class(fibonacci_node_type), target, intent(inout) :: left, right
    class(fibonacci_node_type),pointer :: left_left,right_right
    class(measurable_class),pointer::down
    ! swap branches
    left_left =>left%left
    right_right=>right%right
    left%left =>right%right
    right%right=>left_left
    ! repair up components
    right_right%up=>left
    left_left%up =>right
    ! repair down components
          down => left%down
    left%down => right%down
    right%down =>
  end subroutine fibonacci_node_swap_nodes
fibonacci node swap nodes †
  subroutine fibonacci_node_swap_nodes(this,that)
     class(fibonacci_node_type),target :: this
!
     class(fibonacci_node_type),pointer,intent(in) :: that
     class(fibonacci_node_type),pointer :: par_i,par_a
    par_i => this%up
    par_a => that%up
!
!
    if (associated(par_i%left,this)) then
!
        par_i%left => that
1
    else
!
        par_i%right => that
    end if
     if (associated(par_a%left,that)) then
!
!
        par_a%left => this
!
    else
!
        par_a%right => this
     end if
    this%up => par_a
     that%up => par_i
  end subroutine fibonacci_node_swap_nodes
fibonacci node flip children †
```

```
subroutine fibonacci_node_flip_children(this)
    class(fibonacci_node_type),intent(inout) :: this
    class(fibonacci_node_type),pointer :: child
    child => this%left
    this%left=>this%right
    this%right => child
  end subroutine fibonacci_node_flip_children
fibonacci node rip \( \)
  subroutine fibonacci_node_rip(this)
    class(fibonacci_node_type),intent(inout),target :: this
    if (this%is_left_child()) then
       nullify(this%up%left)
    if (this%is_right_child()) then
       nullify(this%up%right)
    end if
    nullify(this%up)
  end subroutine fibonacci_node_rip
fibonacci node remove and keep twin \
  subroutine fibonacci_node_remove_and_keep_twin(this,twin)
    class(fibonacci_node_type),intent(inout),target :: this
    class(fibonacci_node_type),intent(out),pointer :: twin
    class(fibonacci_node_type),pointer :: pa
    if (.not. (this%is_root())) then
       pa=>this%up
       if (.not. pa%is_root()) then
          if (this%is_left_child()) then
             twin => pa%right
          else
             twin => pa%left
          end if
          if (pa%is_left_child()) then
             pa%up%left => twin
          else
             pa%up%right => twin
          end if
       end if
       twin%up => pa%up
       if(associated(this%right))then
          this%right%left=>this%left
       if(associated(this%left))then
          this%left%right=>this%right
       end if
       nullify(this%left)
       nullify(this%right)
       nullify(this%up)
       deallocate(pa)
```

```
end if
  end subroutine fibonacci_node_remove_and_keep_twin
fibonacci node remove and keep parent \( \)
 subroutine fibonacci_node_remove_and_keep_parent(this,pa)
    class(fibonacci_node_type),intent(inout),target :: this
    class(fibonacci_node_type),intent(out),pointer :: pa
    class(fibonacci_node_type),pointer :: twin
    if (.not. (this%is_root())) then
       pa=>this%up
       if (this%is_left_child()) then
          twin => pa%right
       else
          twin => pa%left
       end if
       twin%up=>pa%up
       if (associated(twin%left)) then
          twin%left%up => pa
       if (associated(twin%right)) then
          twin%right%up => pa
       end if
       call pa%copy_node(twin)
       select type(pa)
       class is (fibonacci_root_type)
          call pa%set_leftmost()
          call pa%set_rightmost()
       end select
       if(associated(this%right))then
          this%right%left=>this%left
       end if
       if(associated(this%left))then
          this%left%right=>this%right
       end if
       nullify(this%left)
       nullify(this%right)
       nullify(this%up)
       deallocate(twin)
    else
       pa=>this
    end if
  end subroutine fibonacci_node_remove_and_keep_parent
fibonacci leave pick \( \ \)
  subroutine fibonacci_leave_pick(this)
    class(fibonacci_leave_type), target, intent(inout) :: this
    class(fibonacci_node_type),pointer :: other
    class(fibonacci_root_type),pointer :: root
    call this%up%print_parents()
    call this%find_root(root)
```

```
if(associated(this%up,root))then
       if(this%up%depth<2)then
          print *,"fibonacci_leave_pick: Cannot pick leave. &
          &Tree must have at least three leaves."
          return
       else
          call this%remove_and_keep_parent(other)
          call other%repair()
       end if
    else
       call this%remove_and_keep_twin(other)
       call other%up%repair()
    end if
    if(associated(root%leftmost,this))call root%set_leftmost()
    if(associated(root%rightmost,this))call root%set_rightmost()
  end subroutine fibonacci_leave_pick
fibonacci node append left \( \ \)
  subroutine fibonacci_node_append_left(this,new_branch)
    class(fibonacci_node_type),target :: this
    class(fibonacci_node_type),target :: new_branch
    this%left => new_branch
    new_branch%up => this
  end subroutine fibonacci_node_append_left
fibonacci node append right \( \ \)
  subroutine fibonacci_node_append_right(this,new_branch)
    class(fibonacci_node_type),intent(inout),target :: this
    class(fibonacci_node_type),target :: new_branch
    this%right => new_branch
    new_branch%up => this
  end subroutine fibonacci_node_append_right
fibonacci node rotate left \uparrow
  subroutine fibonacci_node_rotate_left(this)
    class(fibonacci_node_type),intent(inout),target :: this
    call this%swap(this%right)
    call this%right%flip()
    call this%right%update_depth_unsave()
   call this%flip()
    value = this%value
    this%value = this%left%value
    this%left%value = value
  end subroutine fibonacci_node_rotate_left
fibonacci node rotate right \
  subroutine fibonacci_node_rotate_right(this)
    class(fibonacci_node_type),intent(inout),target :: this
    call this%left%swap(this)
```

```
call this%left%flip()
    call this%left%update_depth_unsave()
    call this%flip()
    value = this%value
    this%value = this%right%value
     this%right%value = value
  end subroutine fibonacci_node_rotate_right
fibonacci node rotate ↑
 subroutine fibonacci_node_rotate(this)
    class(fibonacci_node_type),intent(inout),target :: this
    if (this%is_left_short()) then
       call this%rotate_left()
    else
       if (this%is_right_short()) then
          call this%rotate_right()
       end if
    end if
  end subroutine fibonacci_node_rotate
fibonacci node balance node \( \)
  subroutine fibonacci_node_balance_node(this,changed)
    class(fibonacci_node_type),intent(inout),target :: this
    logical,intent(out) :: changed
    changed=.false.
    if (this%is_left_too_short()) then
       if (this%right%is_right_short()) then
          call this%right%rotate_right
       end if
       call this%rotate_left()
       changed=.true.
    else
       if (this%is_right_too_short()) then
          if (this%left%is_left_short()) then
             call this%left%rotate_left
          end if
          call this%rotate_right()
          changed=.true.
       end if
    end if
  end subroutine fibonacci_node_balance_node
fibonacci node update depth unsave \uparrow
 subroutine fibonacci_node_update_depth_unsave(this)
    class(fibonacci_node_type),intent(inout) :: this
    this%depth=max(this%left%depth+1,this%right%depth+1)
  end subroutine fibonacci_node_update_depth_unsave
fibonacci node update depth save \( \)
```

```
subroutine fibonacci_node_update_depth_save(this,updated)
    class(fibonacci_node_type),intent(inout) :: this
    logical,intent(out) :: updated
    integer :: left,right,new_depth
    if (associated(this%left)) then
       left=this%left%depth+1
    else
       left=-1
    end if
    if (associated(this%right)) then
       right=this%right%depth+1
    else
       right=-1
    end if
    new_depth=max(left,right)
    if (this%depth == new_depth) then
       updated = .false.
    else
       this%depth=new_depth
       updated = .true.
  end subroutine fibonacci_node_update_depth_save
fibonacci node repair \
  subroutine fibonacci_node_repair(this)
    class(fibonacci_node_type),intent(inout),target :: this
    class(fibonacci_node_type),pointer:: node
    logical :: new_depth,new_balance
    new_depth = .true.
    node=>this
    do while((new_depth .or. new_balance) .and. (associated(node)))
       call node%balance_node(new_balance)
       call node%update_depth_save(new_depth)
       node=>node%up
    end do
  end subroutine fibonacci_node_repair
fibonacci node is left short \( \ \)
  elemental logical function fibonacci_node_is_left_short(this)
    class(fibonacci_node_type),intent(in) :: this
    fibonacci_node_is_left_short = (this%left%depth<this%right%depth)
  end function fibonacci_node_is_left_short
fibonacci node is right short \
  elemental logical function fibonacci_node_is_right_short(this)
    class(fibonacci_node_type),intent(in) :: this
    fibonacci_node_is_right_short = (this%right%depth<this%left%depth)
  end function fibonacci_node_is_right_short
fibonacci node is unbalanced \( \ \)
```

```
elemental logical function fibonacci_node_is_unbalanced(this)
    class(fibonacci_node_type),intent(in) :: this
    fibonacci_node_is_unbalanced = (this%is_left_short() .or. this%is_right_short())
  end function fibonacci_node_is_unbalanced
fibonacci node is left too short \uparrow
  elemental logical function fibonacci_node_is_left_too_short(this)
    class(fibonacci_node_type),intent(in) :: this
    fibonacci_node_is_left_too_short = (this%left%depth+1<this%right%depth)
  end function fibonacci_node_is_left_too_short
fibonacci node is right too short \( \ \)
  elemental logical function fibonacci_node_is_right_too_short(this)
    class(fibonacci_node_type),intent(in) :: this
    fibonacci_node_is_right_too_short = (this%right%depth+1<this%left%depth)
  end function fibonacci_node_is_right_too_short
fibonacci node is too unbalanced \
  elemental logical function fibonacci_node_is_too_unbalanced(this)
    class(fibonacci_node_type),intent(in) :: this
    fibonacci_node_is_too_unbalanced = (this%is_left_too_short() .or. this%is_right_too_short())
  end function fibonacci_node_is_too_unbalanced
fibonacci node is left child \( \)
  elemental logical function fibonacci_node_is_left_child(this)
    class(fibonacci_node_type),intent(in),target :: this
    fibonacci_node_is_left_child = associated(this%up%left,this)
  end function fibonacci_node_is_left_child
fibonacci node is right child \
  elemental logical function fibonacci_node_is_right_child(this)
    class(fibonacci_node_type),intent(in),target :: this
    fibonacci_node_is_right_child = associated(this%up%right,this)
  end function fibonacci_node_is_right_child
fibonacci node apply to leaves \
 recursive subroutine fibonacci_node_apply_to_leaves(node,func,unit)
    class(fibonacci_node_type),intent(in),target :: node
    interface
       subroutine func(this, unit)
         import fibonacci_leave_type
         class(fibonacci_leave_type),intent(in),target :: this
         integer,intent(in),optional :: unit
       end subroutine func
    end interface
    integer,intent(in),optional :: unit
    select type (node)
    class is (fibonacci_leave_type)
```

```
call func(node,unit)
    class default
       call node%left%apply_to_leaves(func,unit)
       call node%right%apply_to_leaves(func,unit)
    end select
  end subroutine fibonacci_node_apply_to_leaves
fibonacci node apply to leaves rl \uparrow
  recursive subroutine fibonacci_node_apply_to_leaves_RL(node,func,unit)
    class(fibonacci_node_type),intent(in),target :: node
    interface
       subroutine func(this,unit)
         import fibonacci_leave_type
         class(fibonacci_leave_type),intent(in),target :: this
         integer,intent(in),optional :: unit
       end subroutine func
    end interface
    integer, intent(in), optional :: unit
    select type (node)
    class is (fibonacci_leave_type)
       call func(node,unit)
    class default
       call node%right%apply_to_leaves_rl(func,unit)
       call node%left%apply_to_leaves_rl(func,unit)
    end select
  end subroutine fibonacci_node_apply_to_leaves_RL
fibonacci node count leaves \
  recursive subroutine fibonacci_node_count_leaves(this,n)
    class(fibonacci_node_type),intent(in) :: this
    integer,intent(out) :: n
    integer::n1,n2
    if(associated(this%left).and.associated(this%right)) then
       call fibonacci_node_count_leaves(this%left,n1)
       call fibonacci_node_count_leaves(this%right,n2)
       n=n1+n2
    else
       n=1
    end if
  end subroutine fibonacci_node_count_leaves
9.4.2 Methoden für fibonacci root type
fibonacci root write to marker \( \)
  SUBROUTINE fibonacci_root_write_to_marker(this,marker,status)
    CLASS(fibonacci_root_type), INTENT(IN) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
```

```
call marker%mark_begin("FIBONACCI_ROOT_TYPE")
    call fibonacci_node_write_to_marker(this,marker,status)
    marker%mark_end("FIBONACCI_ROOT_TYPE")
  end SUBROUTINE fibonacci_root_write_to_marker
fibonacci root read target from marker \( \)
 SUBROUTINE fibonacci_root_read_target_from_marker(this,marker,status)
    CLASS(fibonacci_root_type), target, INTENT(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("FIBONACCI_ROOT_TYPE",status)
    call fibonacci_node_read_from_marker(this,marker,status)
    call this%find_leftmost(this%leftmost)
    call this%find_rightmost(this%rightmost)
     call marker%pick_end("FIBONACCI_ROOT_TYPE",status)
  end SUBROUTINE fibonacci_root_read_target_from_marker
fibonacci root print to unit \
 subroutine fibonacci_root_print_to_unit(this,unit,parents,components,peers)
    class(fibonacci_root_type),intent(in)::this
    integer,intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    class(serializable_class),pointer::ser
    if(parents>0)call fibonacci_node_print_to_unit(this,unit,parents-1,components,peers)
    write(unit,'("Components of fibonacci_root_type:")')
    ser=>this%leftmost
    call serialize_print_peer_pointer(ser,unit,parents,components,min(peers,one),"Leftmost: ")
    ser=>this%rightmost
    call serialize_print_peer_pointer(ser,unit,parents,components,min(peers,one),"Rightmost:")
  end subroutine fibonacci_root_print_to_unit
fibonacci root get type \( \)
 pure subroutine fibonacci_root_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="fibonacci_root_type")
  end subroutine fibonacci_root_get_type
fibonacci root get leftmost \( \ \)
 subroutine fibonacci_root_get_leftmost(this,leftmost)
    class(fibonacci_root_type),intent(in)::this
    class(fibonacci_leave_type),pointer::leftmost
    leftmost=>this%leftmost
  end subroutine fibonacci_root_get_leftmost
fibonacci root get rightmost \( \ \)
 subroutine fibonacci_root_get_rightmost(this,rightmost)
    class(fibonacci_root_type),intent(in)::this
    class(fibonacci_leave_type),pointer::rightmost
```

if (is\_sequential=="Y" .and. is\_formatted=="Y" .and. is\_writeable=="Y") then write(unitnr,'("\beginpsTree\Toval[linecolor=blue]\node",i3,"",f9.3,"")')&

this%depth,this%measure()

if (associated(this%leftmost)) then

call this%leftmost%write\_pstricks(unitnr)

write(unitnr,'("\Tr[",a,"]")') no\_kid

end if

```
if (associated(this%left)) then
             call this%left%write_pstricks(unitnr)
             write(unitnr,'("\Tr[",a,"]")') no_kid
          end if
          if (associated(this%right)) then
             call this%right%write_pstricks(unitnr)
             write(unitnr,'("\Tr[",a,"]")') no_kid
          if (associated(this%rightmost)) then
             call this%rightmost%write_pstricks(unitnr)
          else
             write(unitnr,'("\Tr[",a,"]")') no_kid
          write(unitnr,'("\endpsTree")')
          write(unitnr,'("\\")')
       else
          print '("fibonacci_node_write_pstricks: Unit ",I2," is not opened properly.")',unitnr
          print '("No output is written to unit.")'
       end if
    else
       print '("fibonacci_node_write_pstricks: Unit ",I2," is not opened.")',unitnr
       print '("No output is written to unit.")'
    end if
  end subroutine fibonacci_root_write_pstricks
fibonacci root copy root \( \ \)
 subroutine fibonacci_root_copy_root(this,primitive)
    class(fibonacci_root_type),intent(out) :: this
    class(fibonacci_root_type),intent(in) :: primitive
    call fibonacci_node_copy_node(this,primitive)
    this%leftmost => primitive%leftmost
    this%rightmost => primitive%rightmost
  end subroutine fibonacci_root_copy_root
fibonacci root push by content \( \ \)
 subroutine fibonacci_root_push_by_content(this,content)
    class(fibonacci_root_type), target, intent(inout) :: this
    class(measurable_class),target,intent(in)::content
    class(fibonacci_leave_type),pointer :: node
     print *,"fibonacci_root_push_by_content: ",content%measure()
    allocate(node)
    node%down=>content
    call this%push_by_leave(node)
  end subroutine fibonacci_root_push_by_content
fibonacci root push by leave \( \ \)
```

```
! this is a workaround for BUG 44696. This subroutine is a merge of
! fibonacci_tree_push_by_node
! fibonacci_node_find
! fibonacci_leave_insert_leave_by_node
subroutine fibonacci_root_push_by_leave(this,new_leave)
  class(fibonacci_root_type), target, intent(inout)
  class(fibonacci_leave_type),pointer,intent(inout) :: new_leave
  class(fibonacci_leave_type),pointer :: old_leave
  class(fibonacci_node_type), pointer :: node,new_node,leave_c
  if (new leave<=this%leftmost) then
     old_leave=>this%leftmost
     this%leftmost=>new_leave
     node=>old_leave%up
     call fibonacci_node_spawn&
       (new_node, new_leave, old_leave, old_leave%left, old_leave%right)
     call node%append_left(new_node)
  else
     if (new_leave>this%rightmost) then
        old_leave=>this%rightmost
        this%rightmost=>new_leave
        node=>old_leave%up
        call fibonacci_node_spawn&
          (new_node,old_leave,new_leave,old_leave%left,old_leave%right)
        call node%append_right(new_node)
     else
        node=>this
        do
           if (new_leave<=node) then
              leave_c=>node%left
              select type (leave_c)
              class is (fibonacci_leave_type)
                 if(new_leave<=leave_c)then</pre>
                    call fibonacci_node_spawn&
                      (new_node,new_leave,leave_c,leave_c%left,leave_c%right)
                 else
                    call fibonacci_node_spawn&
                      (new_node,leave_c,new_leave,leave_c%left,leave_c%right)
                 end if
                 call node%append_left(new_node)
                 exit
              class default
                 node=>node%left
              end select
           else
              leave_c=>node%right
              select type (leave_c)
              class is (fibonacci_leave_type)
                 if(new_leave<=leave_c)then</pre>
                    call fibonacci_node_spawn&
                      (new_node,new_leave,leave_c,leave_c%left,leave_c%right)
                 else
```

```
call fibonacci_node_spawn&
                        (new_node,leave_c,new_leave,leave_c%left,leave_c%right)
                   end if
                   call node%append_right(new_node)
                   exit
                class default
                   node=>node%right
                end select
             end if
          end do
       end if
    end if
    call node%repair()
  end subroutine fibonacci_root_push_by_leave
fibonacci root pop left \
 subroutine fibonacci_root_pop_left(this,leave)
    class(fibonacci_root_type),intent(inout),target :: this
    class(fibonacci_leave_type),pointer,intent(out) :: leave
    class(fibonacci_node_type),pointer :: parent,grand
    !write(11,fmt=*)"fibonacci root pop left
                                                             "!PSTRICKS
    !flush(11)!PSTRICKS
    leave => this%leftmost
    if (this%left%depth>=1) then
       parent => leave%up
       grand=>parent%up
       grand%left => parent%right
       parent%right%up=>grand
       deallocate(parent)
       parent=>grand%left
       if (.not.parent%is_leave())then
          parent=>parent%left
       end if
       select type (parent)
       class is (fibonacci_leave_type)
          this%leftmost => parent
       class default
          print *,"fibonacci_root_pop_left: ERROR: leftmost is no leave."
          call parent%print_all()
          STOP
       end select
       !call this%write_pstricks(11)!PSTRICKS
       !flush(11)!PSTRICKS
       !write(11,fmt=*)"fibonacci node repair
                                                             "!PSTRICKS
       !flush(11)!PSTRICKS
       call grand%repair()
    else
       if (this%left%depth==0.and.this%right%depth==1) then
          parent => this%right
          parent%right%up=>this
```

```
parent%left%up=>this
          this%left=>parent%left
          this%right=>parent%right
          this%depth=1
          deallocate(parent)
          parent=>this%left
          select type (parent)
          class is (fibonacci_leave_type)
          this%leftmost => parent
          end select
          this%down=>this%leftmost%down
       end if
    end if
    nullify(leave%right%left)
    nullify(leave%up)
    nullify(leave%right)
    nullify(this%leftmost%left)
    !call this%write_pstricks(11)!PSTRICKS
    !flush(11)!PSTRICKS
  end subroutine fibonacci_root_pop_left
fibonacci root pop right \
  subroutine fibonacci_root_pop_right(this,leave)
    class(fibonacci_root_type),intent(inout),target :: this
    class(fibonacci_leave_type),pointer,intent(out) :: leave
    class(fibonacci_node_type),pointer :: parent,grand
    leave => this%rightmost
    if (this%right%depth>=1) then
       parent => leave%up
       grand=>parent%up
       grand%right => parent%left
       parent%left%up=>grand
       deallocate(parent)
       parent=>grand%right
       if (.not.parent%is_leave())then
          parent=>parent%right
       end if
       select type (parent)
       class is (fibonacci_leave_type)
          this%rightmost => parent
       class default
          print *,"fibonacci_root_pop_left: ERROR: leftmost is no leave."
          call parent%print_all()
          STOP
       end select
       call grand%repair()
    else
       if (this%right%depth==0.and.this%left%depth==1) then
          parent => this%left
          parent%left%up=>this
```

```
parent%right%up=>this
          this%right=>parent%right
          this%left=>parent%left
          this%depth=1
          deallocate(parent)
          parent=>this%right
          select type (parent)
          class is (fibonacci_leave_type)
          this%rightmost => parent
          end select
          this%down=>this%rightmost%down
       end if
    end if
  end subroutine fibonacci_root_pop_right
fibonacci root merge ↑
  subroutine fibonacci_root_merge(this_tree,that_tree,merge_tree)
    ! I neither used nor revised this procedure for a long time, so it might be broken.
    class(fibonacci_root_type),intent(in) :: this_tree
    class(fibonacci_root_type),intent(in) :: that_tree
    class(fibonacci_root_type), pointer, intent(out) :: merge_tree
    class(fibonacci_leave_type),pointer :: this_leave,that_leave,old_leave
    type(fibonacci_leave_list_type),target :: leave_list
    \verb|class(fibonacci_leave_list_type)|, pointer :: last_leave|
    integer :: n_leaves
    if (associated(this_tree%leftmost).and.associated(that_tree%leftmost)) then
       n_{leaves=1}
       this_leave=>this_tree%leftmost
       that_leave=>that_tree%leftmost
       if (this_leave < that_leave) then
          allocate(leave_list%leave, source=this_leave)
          call this_leave%find_right_leave(this_leave)
       else
          allocate(leave_list%leave, source=that_leave)
          call that_leave%find_right_leave(that_leave)
       end if
       last_leave=>leave_list
       do while (associated(this_leave).and.associated(that_leave))
          if (this_leave < that_leave) then
             old_leave=>this_leave
             call this_leave%find_right_leave(this_leave)
          else
             old_leave=>that_leave
             call that_leave%find_right_leave(that_leave)
          end if
          allocate(last_leave%next)
          last_leave=>last_leave%next
          allocate(last_leave%leave,source=old_leave)
          n_leaves=n_leaves+1
       end do
```

```
if (associated(this_leave)) then
          old_leave=>this_leave
       else
          old_leave=>that_leave
       end if
       do while (associated(old_leave))
          allocate(last_leave%next)
          last_leave=>last_leave%next
          allocate(last_leave%leave,source=old_leave)
          n leaves=n leaves+1
          call old_leave%find_right_leave(old_leave)
       end do
       allocate(merge_tree)
       call fibonacci_root_list_to_tree(merge_tree,n_leaves,leave_list)
    else
       n_leaves=0
    end if
    if(associated(leave_list%next)) then
       last_leave=>leave_list%next
       do while (associated(last_leave%next))
          leave_list%next=>last_leave%next
          deallocate(last_leave)
          last_leave=>leave_list%next
       end do
       deallocate(last_leave)
  end subroutine fibonacci_root_merge
fibonacci root set leftmost \
  subroutine fibonacci_root_set_leftmost(this)
    class(fibonacci_root_type) :: this
    call this%find_leftmost(this%leftmost)
  end subroutine fibonacci_root_set_leftmost
fibonacci root set rightmost \
  subroutine fibonacci_root_set_rightmost(this)
    class(fibonacci_root_type) :: this
    call this%find_rightmost(this%rightmost)
  end subroutine fibonacci_root_set_rightmost
fibonacci root init by leave \( \)
  subroutine fibonacci_root_init_by_leave(this,left_leave,right_leave)
    class(fibonacci_root_type), target, intent(out) :: this
    class(fibonacci_leave_type), target, intent(in) :: left_leave, right_leave
    if (left_leave <= right_leave) then</pre>
       this%left => left_leave
       this%right => right_leave
       this%leftmost => left_leave
       this%rightmost => right_leave
```

```
else
       this%left => right_leave
       this%right => left_leave
       this%leftmost => right_leave
       this%rightmost => left_leave
    end if
    this%left%up => this
    this%right%up => this
    this%down=>this%leftmost%down
    this%depth = 1
    this%leftmost%right=>this%rightmost
    this%rightmost%left=>this%leftmost
    this%is_valid_c=.true.
  end subroutine fibonacci_root_init_by_leave
fibonacci root init by content \( \ \)
  subroutine fibonacci_root_init_by_content(this,left_content,right_content)
    class(fibonacci_root_type), target, intent(out) :: this
    class(measurable_class),intent(in),target :: left_content,right_content
    call fibonacci_root_reset(this)
    print *,"fibonacci_root_init_by_content: ",left_content%measure(),right_content%measure()
    if (left_content<right_content) then
       call this%leftmost%set_content(left_content)
       call this%rightmost%set_content(right_content)
    else
       call this%leftmost%set_content(right_content)
       call this%rightmost%set_content(left_content)
    end if
    this%down=>this%leftmost%down
    this%is_valid_c=.true.
  end subroutine fibonacci_root_init_by_content
fibonacci root reset \( \ \)
 subroutine fibonacci_root_reset(this)
    class(fibonacci_root_type), target, intent(inout) :: this
    call fibonacci_root_deallocate_tree(this)
    allocate (this%leftmost)
    allocate (this%rightmost)
    this%depth=1
    this%leftmost%depth=0
    this%rightmost%depth=0
    this%left=>this%leftmost
    this%right=>this%rightmost
    this%left%up=>this
    this%right%up=>this
    this%leftmost%right=>this%rightmost
    this%rightmost%left=>this%leftmost
  end subroutine fibonacci_root_reset
fibonacci root deallocate tree \( \)
```

```
recursive subroutine fibonacci_root_deallocate_tree(this)
    class(fibonacci_root_type),intent(inout) :: this
    call fibonacci_node_deallocate_tree(this)
    nullify(this%leftmost)
    nullify(this%rightmost)
  end subroutine fibonacci_root_deallocate_tree
fibonacci root deallocate all \uparrow
  recursive subroutine fibonacci_root_deallocate_all(this)
    class(fibonacci_root_type),intent(inout) :: this
    call fibonacci_node_deallocate_all(this)
    nullify(this%leftmost)
    nullify(this%rightmost)
  end subroutine fibonacci_root_deallocate_all
fibonacci root is left child \
  elemental logical function fibonacci_root_is_left_child(this)
    class(fibonacci_root_type), target, intent(in) :: this
    fibonacci_root_is_left_child = .false.
  end function fibonacci_root_is_left_child
fibonacci root is right child \
  elemental logical function fibonacci_root_is_right_child(this)
    class(fibonacci_root_type), target, intent(in) :: this
    fibonacci_root_is_right_child = .false.
  end function fibonacci_root_is_right_child
9.4.3 Methoden für fibonacci stub type
fibonacci stub get type \( \)
  pure subroutine fibonacci_stub_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="fibonacci_stub_type")
  end subroutine fibonacci_stub_get_type
fibonacci stub push by content \( \ \)
  subroutine fibonacci_stub_push_by_content(this,content)
    class(fibonacci_stub_type), target, intent(inout) :: this
    class(measurable_class), target, intent(in)::content
    class(fibonacci_leave_type),pointer::leave
    allocate(leave)
    call leave%set_content(content)
    call this%push_by_leave(leave)
  end subroutine fibonacci_stub_push_by_content
fibonacci stub push by leave \( \)
```

```
subroutine fibonacci_stub_push_by_leave(this,new_leave)
    class(fibonacci_stub_type), target, intent(inout)
    class(fibonacci_leave_type),pointer,intent(inout) :: new_leave
    class(fibonacci_leave_type), pointer::old_leave
    if(this%depth<1)then
       if(associated(this%leftmost))then
          old_leave=>this%leftmost
          call this%init_by_leave(old_leave,new_leave)
       else
          this%leftmost=>new leave
       end if
    else
       call fibonacci_root_push_by_leave(this,new_leave)
    end if
  end subroutine fibonacci_stub_push_by_leave
fibonacci stub pop left \( \ \)
 subroutine fibonacci_stub_pop_left(this,leave)
    class(fibonacci_stub_type),intent(inout),target :: this
    class(fibonacci_leave_type),pointer,intent(out) :: leave
    if(this%depth<2)then
       if(this%depth==1)then
          leave=>this%leftmost
          this%leftmost=>this%rightmost
          nullify(this%rightmost)
          nullify(this%right)
          nullify(this%left)
          this%depth=0
          this%is_valid_c=.false.
       else
          if(associated(this%leftmost))then
             leave=>this%leftmost
             nullify(this%leftmost)
          end if
       end if
    else
       call fibonacci_root_pop_left(this,leave)
    end if
  end subroutine fibonacci_stub_pop_left
fibonacci stub pop right \( \ \)
 subroutine fibonacci_stub_pop_right(this,leave)
    class(fibonacci_stub_type),intent(inout),target :: this
    class(fibonacci_leave_type),pointer,intent(out) :: leave
    if(this%depth<2)then
       if(this%depth==1)then
          this%is_valid_c=.false.
          if(associated(this%rightmost))then
             leave=>this%rightmost
             nullify(this%rightmost)
```

```
nullify(this%right)
          else
             if(associated(this%leftmost))then
                leave=>this%leftmost
                nullify(this%leftmost)
                nullify(this%left)
             else
                nullify(leave)
             end if
          end if
       end if
    else
       call fibonacci_root_pop_right(this,leave)
  end subroutine fibonacci_stub_pop_right
9.4.4 Methoden für fibonacci leave type
fibonacci leave get type \( \ \)
  pure subroutine fibonacci_leave_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="fibonacci_leave_type")
  end subroutine fibonacci_leave_get_type
fibonacci leave print to unit \
  subroutine fibonacci_leave_print_to_unit(this,unit,parents,components,peers)
    class(fibonacci_leave_type),intent(in)::this
    integer,intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    class(serializable_class),pointer::ser
    if(parents>0)call fibonacci_node_print_to_unit(this,unit,parents-one,components,-one)
    write(unit, '("Components of fibonacci_leave_type:")')
    ser=>this%down
    call serialize_print_comp_pointer(ser,unit,parents,components,peers,"Content:")
  end subroutine fibonacci_leave_print_to_unit
fibonacci leave get left \uparrow
  subroutine fibonacci_leave_get_left(this,leave)
    class(fibonacci_leave_type),intent(in) :: this
    class(fibonacci_leave_type),intent(out),pointer :: leave
    class(fibonacci_node_type),pointer::node
    node=>this%left
    select type(node)
    class is (fibonacci_leave_type)
       leave=>node
    end select
  end subroutine fibonacci_leave_get_left
```

```
fibonacci leave get right \( \ \)
  subroutine fibonacci_leave_get_right(this,leave)
    class(fibonacci_leave_type),intent(in) :: this
    class(fibonacci_leave_type),intent(out),pointer :: leave
    class(fibonacci_node_type),pointer::node
    print *,"fibonacci_leave_get_right"
    call this%down%print_little
    if(associated(this%right))then
       node=>this%right
        call node%down%print_little
Ţ
       select type(node)
       class is (fibonacci_leave_type)
          leave=>node
       end select
    else
1
        print *,"no right leave"
      nullify(leave)
    end if
  end subroutine fibonacci_leave_get_right
fibonacci leave deallocate all \( \)
 subroutine fibonacci_leave_deallocate_all(this)
    class(fibonacci_leave_type),intent(inout) :: this
    if (associated(this%down)) then
       deallocate(this%down)
    end if
  end subroutine fibonacci_leave_deallocate_all
fibonacci leave write pstricks \( \)
 subroutine fibonacci_leave_write_pstricks(this,unitnr)
    class(fibonacci_leave_type),intent(in),target :: this
    integer,intent(in) :: unitnr
    write(unitnr,'("\beginpsTree\Toval[linecolor=green]\node",i3,"",f9.3,"")')&
      this%depth,this%measure()
    if (associated(this%left)) then
       write(unitnr,'("\Tr[",a,"]")') le_kid
    end if
    if (associated(this%right)) then
      write(unitnr,'("\Tr[",a,"]")') le_kid
    end if
    write(unitnr,'("\endpsTree")')
  end subroutine fibonacci_leave_write_pstricks
fibonacci leave insert leave by node \( \)
  subroutine fibonacci_leave_insert_leave_by_node(this,new_leave)
    class(fibonacci_leave_type),target,intent(inout) :: this,new_leave
    class(fibonacci_node_type),pointer :: parent,new_node
    parent=>this%up
    !print *,associated(this%left),associated(this%right)
```

```
if(this<new_leave)then
       call fibonacci_node_spawn(new_node, this, new_leave, this%left, this%right)
       !print *,"Repair! ",this%measure(),new_leave%measure()
       call fibonacci_node_spawn(new_node,new_leave,this,this%left,this%right)
    end if
    if(associated(parent%left,this))then
       call parent%append_left(new_node)
    else
       call parent%append_right(new_node)
    end if
    call parent%repair()
  end subroutine fibonacci_leave_insert_leave_by_node
fibonacci leave copy content \( \ \)
  subroutine fibonacci_leave_copy_content(this,content)
    class(fibonacci_leave_type) :: this
    class(measurable_class),intent(in) :: content
    allocate(this%down, source=content)
  end subroutine fibonacci_leave_copy_content
fibonacci leave set content \( \)
  subroutine fibonacci_leave_set_content(this,content)
    class(fibonacci_leave_type) :: this
    class(measurable_class),target,intent(in) :: content
    this%down => content
  end subroutine fibonacci_leave_set_content
fibonacci leave get content \( \ \)
  subroutine fibonacci_leave_get_content(this,content)
    class(fibonacci_leave_type),intent(in) :: this
    class(measurable_class),pointer :: content
    content => this%down
  end subroutine fibonacci_leave_get_content
fibonacci leave is inner \( \)
  elemental logical function fibonacci_leave_is_inner()
    fibonacci_leave_is_inner = .false.
  end function fibonacci_leave_is_inner
fibonacci leave is leave \( \ \)
  elemental logical function fibonacci_leave_is_leave()
    fibonacci_leave_is_leave = .true.
  end function fibonacci_leave_is_leave
fibonacci leave is left short \( \ \)
```

```
elemental logical function fibonacci_leave_is_left_short(this)
    class(fibonacci_leave_type),intent(in) :: this
    fibonacci_leave_is_left_short = .false.
  end function fibonacci_leave_is_left_short
fibonacci leave is right short \( \ \)
  elemental logical function fibonacci_leave_is_right_short(this)
    class(fibonacci_leave_type),intent(in) :: this
    fibonacci_leave_is_right_short = .false.
  end function fibonacci_leave_is_right_short
fibonacci leave is unbalanced \( \)
  elemental logical function fibonacci_leave_is_unbalanced(this)
    class(fibonacci_leave_type),intent(in) :: this
    fibonacci_leave_is_unbalanced = .false.
  end function fibonacci_leave_is_unbalanced
fibonacci leave is left too short \( \ \)
  elemental logical function fibonacci_leave_is_left_too_short(this)
    class(fibonacci_leave_type),intent(in) :: this
    fibonacci_leave_is_left_too_short = .false.
  end function fibonacci_leave_is_left_too_short
fibonacci leave is right too short \( \ \)
  elemental logical function fibonacci_leave_is_right_too_short(this)
    class(fibonacci_leave_type),intent(in) :: this
    fibonacci_leave_is_right_too_short = .false.
  end function fibonacci_leave_is_right_too_short
fibonacci leave is too unbalanced \( \ \)
  elemental logical function fibonacci_leave_is_too_unbalanced(this)
    class(fibonacci_leave_type),intent(in) :: this
    fibonacci_leave_is_too_unbalanced = .false.
  end function fibonacci_leave_is_too_unbalanced
9.4.5 Sonstige Prozeduren
fibonacci leave write content
  subroutine fibonacci_leave_write_content(this,unit)
    class(fibonacci_leave_type),intent(in),target :: this
    integer,optional,intent(in)::unit
    call this%down%print_all(unit)
```

end subroutine fibonacci\_leave\_write\_content

fibonacci leave write

```
subroutine fibonacci_leave_write(this,unit)
    class(fibonacci_leave_type),intent(in),target :: this
    integer, optional, intent(in)::unit
    call this%print_all(unit)
  end subroutine fibonacci_leave_write
fibonacci leave write value
  subroutine fibonacci_leave_write_value(this,unit)
    class(fibonacci_leave_type),intent(in),target :: this
    integer,intent(in),optional::unit
    if(present(unit))then
       write(unit,fmt=*)this%measure()
    else
       print *,this%measure()
    end if
     call this%print_little(unit)
  end subroutine fibonacci_leave_write_value
fibonacci node spawn
  subroutine fibonacci_node_spawn&
    (new_node,left_leave,right_leave,left_left_leave,right_right_leave)
    class(fibonacci_node_type),pointer,intent(out) :: new_node
    class(fibonacci_leave_type),target,intent(inout) :: left_leave,right_leave
    class(fibonacci_node_type),pointer,intent(inout) :: left_left_leave,right_right_leave
    allocate(new node)
    new_node%depth=1
    if(associated(left_left_leave))then
       left_left_leave%right=>left_leave
       left_leave%left=>left_left_leave
    else
       nullify(left_leave%left)
    end if
    if(associated(right_right_leave))then
       right_right_leave%left=>right_leave
       right_leave%right=>right_right_leave
       nullify(right_leave%right)
    end if
    new_node%left=>left_leave
    new_node%right=>right_leave
    new_node%down=>left_leave%down
    new_node%depth=1
    left_leave%up=>new_node
    right_leave%up=>new_node
    left_leave%right=>right_leave
    right_leave%left=>left_leave
  end subroutine fibonacci_node_spawn
fibonacci root list to tree
```

```
subroutine fibonacci_root_list_to_tree(this,n_leaves,leave_list_target)
  class(fibonacci_root_type),target :: this
  integer,intent(in) :: n_leaves
  type(fibonacci_leave_list_type),target,intent(in) :: leave_list_target
   class(fibonacci_root_type),pointer,intent(out) :: tree
  integer:: depth,n_deep,n_merge
  class(fibonacci_node_type),pointer :: node
  class(fibonacci_leave_list_type),pointer :: leave_list
  class(fibonacci_leave_type),pointer::content
  real(kind=double) :: up_value
  leave_list=>leave_list_target
  call ilog2(n_leaves,depth,n_deep)
  n_deep=n_deep*2
  n_merge=0
  this%depth=depth
  node=>this
  outer: do
     do while(depth>1)
        depth=depth-1
        allocate(node%left)
        node%left%up=>node
        node=>node%left
        node%depth=depth
     end do
     node%left=>leave_list%leave
     node%down=>leave_list%leave%down
     leave list=>leave list%next
     node%right=>leave_list%leave
     content => leave_list%leave
     leave_list=>leave_list%next
     n_merge=n_merge+2
     inner: do
        if (associated(node%up)) then
           if (node%is_left_child()) then
              if (n_merge==n_deep.and.depth==1) then
                 node=>node%up
                 node%right=>leave_list%leave
                 node%right%up=>node
                 node%down=>content%down
                 content=>leave_list%leave
                 leave_list=>leave_list%next
                 n_merge=n_merge+1
                 cycle
              end if
              exit inner
           else
              node=>node%up
              depth=depth+1
           end if
        else
           exit outer
```

```
end if
end do inner
node=>node%up
node%down=>content%down
allocate(node%right)
node%right%up => node
node=>node%right
if (n_deep==n_merge) then
    depth=depth-1
end if
node%depth=depth
end do outer
call this%set_leftmost
call this%set_rightmost
end subroutine fibonacci_root_list_to_tree
```

# 10 Modul muli interactions

## 10.1 Abhängigkeiten

use muli\_momentum

#### 10.2 Parameter

```
implicit none
!process parameters
integer,parameter::hadron_A_kind=2212 ! Proton
integer,parameter::hadron_B_kind=-2212 ! Anti Proton
integer, dimension(4), parameter::parton_kind_of_int_kind=[1,1,2,2]
real(kind=double), parameter :: b_sigma_tot_all = 100 !mb PDG
real(kind=double), parameter :: b_sigma_tot_nd = 0.5*b_sigma_tot_all !phys.rev.d v49 n5 1994
real(kind=double), parameter :: gev_cme_tot = 14000 !total center of mass energie
real(kind=double), parameter :: gev2_cme_tot = gev_cme_tot**2 !s
real(kind=double), parameter :: gev_pt_max = gev_cme_tot/2D0
real(kind=double), parameter :: gev2_pt_max = gev2_cme_tot/4D0
!model parameters
real(kind=double), parameter :: gev_pt_min = 8D-1
real(kind=double), parameter :: gev2_pt_min = gev_pt_min**2
real(kind=double), parameter :: pts_min = gev_pt_min/gev_pt_max
real(kind=double), parameter :: pts2_min = gev2_pt_min/gev2_pt_max
real(kind=double), parameter :: gev_p_t_0 = 2.0
real(kind=double), parameter :: gev2_p_t_0 = gev_p_t_0**2
real(kind=double), parameter :: norm_p_t_0 = gev_p_t_0/gev_pt_max
real(kind=double), parameter :: norm2_p_t_0 = gev2_p_t_0/gev2_pt_max
!mathematical constants
real(kind=double), private, parameter :: pi = 3.14159265
real(kind=double), parameter
                            :: euler = exp(1D0)
!physical constants
real(kind=double), parameter :: gev2_mbarn = 0.389379304D0
real(kind=double), parameter :: const_pref=pi*gev2_mbarn/(gev2_cme_tot*b_sigma_tot_nd)
  !parton kind parameters
integer,parameter,public::lha_flavor_at=-6
integer, parameter, public::lha_flavor_ab=-5
integer, parameter, public::lha_flavor_ac=-4
integer,parameter,public::lha_flavor_as=-3
integer, parameter, public::lha_flavor_au=-2
integer,parameter,public::lha_flavor_ad=-1
integer,parameter,public::lha_flavor_g=0
```

```
integer,parameter,public::lha_flavor_d=1
integer,parameter,public::lha_flavor_u=2
integer,parameter,public::lha_flavor_s=3
integer, parameter, public::lha_flavor_c=4
integer,parameter,public::lha_flavor_b=5
integer,parameter,public::lha_flavor_t=6
integer,parameter,public::pdg_flavor_at=-6
integer,parameter,public::pdg_flavor_ab=-5
integer, parameter, public::pdg_flavor_ac=-4
integer, parameter, public::pdg_flavor_as=-3
integer, parameter, public::pdg_flavor_au=-2
integer,parameter,public::pdg_flavor_ad=-1
integer,parameter,public::pdg_flavor_g=21
integer,parameter,public::pdg_flavor_d=1
integer,parameter,public::pdg_flavor_u=2
integer,parameter,public::pdg_flavor_s=3
integer, parameter, public::pdg_flavor_c=4
integer,parameter,public::pdg_flavor_b=5
integer,parameter,public::pdg_flavor_t=6
integer,parameter,public::parton_kind_sea=1
integer, parameter, public::parton_kind_valence=2
integer, parameter, public::parton_kind_sea_and_valence=3
integer, parameter, public::parton_kind_twin=4
integer,parameter,public::parton_kind_sea_and_twin=5
integer,parameter,public::parton_kind_valence_and_twin=6
integer,parameter,public::parton_kind_all=7
integer, parameter, public::pdf_int_kind_undef=0
integer,parameter,public::pdf_int_kind_gluon=1
integer,parameter,public::pdf_int_kind_sea=2
integer,parameter,public::pdf_int_kind_val_down=3
integer, parameter, public::pdf_int_kind_val_up=4
integer,parameter,public::pdf_int_kind_twin=5
character(len=2),dimension(-6:6),parameter :: integer_parton_names = &
     &["-6","-5","-4","-3","-2","-1","00","+1","+2","+3","+4","+5","+6"]
character,dimension(-6:6),parameter :: traditional_parton_names = &
     &["T", "B", "C", "S", "U", "D", "g", "d", "u", "s", "c", "b", "t"]
!ps polynom coefficients
! evolution variable is pt2s/(x1*x2)
real(kind=double),dimension(1:4,1:5),parameter :: phase_space_coefficients_in&
  = reshape(source=[&
     & 6144D0, -4608D0, +384D0,
                                    ODO,&
     & 6144D0, -5120D0, +384D0,
                                    ODO,&
     & 6144D0, -2048D0, +128D0, -576D0,&
     &13824D0, -9600D0, +1056D0,
     &31104D0, -19872D0, +2160D0, +486D0],&
     &shape=[4,5])
! evolution variable is pt2s/(x1*x2)
real(kind=double),dimension(1:4,1:8),parameter :: phase_space_coefficients_inout&
  = reshape(source=[&
     &3072, -2304, +192,
                              0, &
```

```
&6144, -5120, +384,
                                0, &
      &O,
                   0,
                      192, -96, &
      &3072,
             -2048, +192, -96, &
      &O,
               2048, -2176, +576, &
                 288, -306, +81, &
      &O,
      &6912, -4800, +528,
                                0, &
      &31104,-23328, +5832, -486],&
      &shape=[4,8])
integer,dimension(1:4,0:8),parameter :: inout_signatures = reshape(source=[&
       1, 1, 1, 1, &!1a
      -1, 1, -1, 1, &! 1b
       1, 1, 1, 1, &!2
       1,-1, 1,-1,&!3
       1,-1, 1,-1,&!4
       1,-1, 0, 0, &!5
       0, 0, 1,-1,&!6
       1, 0, 1, 0, &!7
       0, 0, 0, 0],&
       shape=[4,9])
integer, dimension(6, -234:234), parameter::valid_processes=reshape([&
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          -6,
               -6,
                      2,
                           2, &! -234
     -5,
          -6,
               -5,
                           1,&!-233
-6,
                      1,
-6,
     -5,
          -5,
               -6,
                      1,
                           1,&!-232
     -4,
          -6,
               -4,
-6,
                      1,
                           1,&!-231
-6,
    -4,
          -4,
               -6,
                           1,&!-230
                      1,
     -3,
-6,
          -6,
               -3,
                      1,
                           1,&!-229
     -3,
          -3,
               -6,
                           1,&!-228
-6,
                      1,
     -2,
-6,
          -6,
               -2,
                      1,
                           1,&!-227
                      1,
-6,
     -2,
          -2,
               -6,
                           1,&!-226
    -1,
                           1,&!-225
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          -6,
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                      1,
                      1,
-6,
    -1,
          -1,
               -6,
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-6,
          -6,
                Ο,
                      4,
                           7,&!-223
          Ο,
-6,
      0,
               -6,
                      4,
                           7,&!-222
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          -6,
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                           3, &! -210
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      6,
         -4,
                4,
                      3,
                           3, &! -209
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-6,
                3,
                           3,&!-208
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         -2,
                      3,
                           3,&!-207
-6,
                2,
-6,
      6, -1,
                1,
                      3,
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```

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	0,			4,	7,&!-150
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-3,	3,	-2,	2,	3,	3,&!-105
-3,	3,	-1,	1,	3,	3,&!-104

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-3,	3,	4,	-4,	3,		-99
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-3,	3,	6,	-6,	3,	3,&!	
-3,	4,	-3,	4,	1,	1,&!	-96
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	4,				1,&!	-95
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-3,	5,	5,	-3,	1,	1,&!	-93
-3,	6,	-3,	6,	1,	1,&!	-92
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-2,	-1,	-1,	-2,	1,	1,&!	-80
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		-2,			7,&!	-79
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-2,	4,	-2,	4,	1,	1,&!	-60 E0
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-2,	6,	-2,	6,	1,	1,&!	-56
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ο,	-5,		ο,	4,	7,&!	-16
0,	-5,	0,	-5,	4,	7,&!	-15
0,	-4,	-4,	0,	4,	7,&!	-14
	-4, -4,					
0,		0,	-4,	4,	7,&!	-13
0,	-3,	-3,	0,	4,	7,&!	-12
Ο,	-3,	Ο,	-3,	4,	7,&!	-11
Ο,	-2,	-2,	Ο,	4,	7,&!	-10
Ο,	-2,	Ο,	-2,	4,	7,&!	-9
Ο,	-1,	-1,	Ο,	4,	7,&!	-8
Ο,	-1,	Ο,	-1,	4,	7,&!	-7
Ο,	Ο,	-6,	6,	5,	6,&!	-6
0,	0,	-5 <b>,</b>	5,	5,	6,&!	
0,	0,	-4,	4,	5,	6,&!	
0,	0,	-3,	3,	5,	6,&!	-3
0,	0,	-2,	2,	5,	6,&!	-2
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Ο,	Ο,	1,	-1,	5,	6,&!	1
Ο,	Ο,	2,	-2,	5,	6,&!	2
Ο,	Ο,	3,	-3,	5,	6,&!	3
Ο,	Ο,	4,	-4,	5,	6,&!	4
Ο,	Ο,	5,	-5,	5,	6,&!	5
Ο,	Ο,	6,	-6,	5,	6,&!	6
Ο,	1,	Ο,	1,	4,	7,&!	7
Ο,	1,	1,	Ο,	4,	7,&!	8
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Ο,	2,	2,	Ο,	4,	7,&!	10
Ο,	3,	Ο,	3,	4,	7,&!	11
Ο,	3,	3,	Ο,	4,	7,&!	12
Ο,	4,	Ο,	4,	4,	7,&!	13
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Ο,	6,	Ο,	6,	4,	7,&!	17
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1,	-6,	1,	-6,	1,	1,&!	20
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1,	-5,	1,	-5,	1,	1,&!	22
1,	-4,	-4,	1,	1,	1,&!	23
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1,	-1,	1,	-1,	3,	4,&!	36
1,	-1,	2,	-2,	3,	3,&!	37
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3, -3, 6, -6, 3, 1, 1,&! 109         3, -2, -2, 3, 1, 1,&! 110         3, -2, 3, -2, 1, 1,&! 111         3, -1, -1, 3, 1, 1,&! 112         3, -1, 3, -1, 1, 1,&! 113         3, 0, 0, 3, 4, 7,&! 114         3, 0, 3, 0, 4, 7,&! 115         3, 1, 1, 3, 1, 1,&! 116         3, 1, 3, 1, 1, 1,&! 117         3, 2, 2, 3, 1, 1,&! 118         3, 2, 3, 2, 1, 1,&! 119         3, 3, 3, 3, 2, 2,&! 120         3, 4, 3, 4, 1, 1,&! 121         3, 5, 5, 3, 5, 1, 1,&! 122         3, 6, 3, 6, 1, 1,&! 124         3, 6, 3, 6, 1, 1,&! 125         3, 6, 6, 6, 3, 1, 1,&! 126         4, -6, -6, 4, -6, 1, 1,&! 128         4, -5, -5, 4, 1, 1,&! 129         4, -6, 4, -6, 6, 1, 1,&! 129         4, -7, -5, 5, 3, 3,&! 131         4, -4, -4, 4, 3, 4,&! 133         4, -4, -5, 5, 3, 3,&! 131         4, -4, -5, 5, 3, 3,&! 132         4, -4, -1, 1, 3, 3,&! 136         4, -4, -2, 2, 3, 3,&! 135         4, -4, -4, 4, 3, 3, 3,&! 134         4, -4, -5, 5, 3, 3,&! 134         4, -4, -5, 5, 3, 3,&! 134         4, -4, -1, 1, 3, 3,&! 136         4, -4, -1, 1, 3, 3,&! 136         4, -4, 5, -5, 3, 3,&! 139         4, -4, 0, 0, 3, 5,&! 137         4, -4, 3, -3, 1, 1,&! 141	3.		5.	-5.			
3, -2, -2, 3, -2, 1, 1,&! 110         3, -2, 3, -2, 1, 1,&! 111         3, -1, -1, 3, 1, 1,&! 112         3, -1, 3, -1, 1, 1,&! 113         3, 0, 0, 3, 4, 7,&! 114         3, 0, 3, 0, 4, 7,&! 115         3, 1, 1, 3, 1, 1,&! 116         3, 1, 3, 1, 1, 1,&! 117         3, 2, 2, 3, 1, 1,&! 118         3, 2, 3, 2, 1, 1,&! 119         3, 3, 3, 3, 2, 2,&! 120         3, 4, 3, 4, 1, 1,&! 121         3, 5, 3, 5, 1, 1,&! 122         3, 6, 3, 6, 1, 1,&! 125         3, 6, 3, 6, 1, 1,&! 125         3, 6, 6, 3, 1, 1,&! 126         4, -6, -6, 4, -6, 1, 1,&! 128         4, -5, -5, 4, 1, 1,&! 129         4, -4, -6, 6, 3, 3,&! 131         4, -4, -6, 6, 3, 3,&! 131         4, -4, -4, 4, 3, 4,&! 133         4, -4, -5, 5, 3, 3,&! 134         4, -4, -1, 1, 3, 3,&! 136         4, -4, -2, 2, 3, 3,&! 135         4, -4, -4, 4, 3, 3, 3,&! 136         4, -4, -5, 5, 3, 3,&! 139         4, -4, 5, -5, 3, 3,&! 134         4, -4, -1, 1, 3, 3,&! 136         4, -4, -1, 1, 3, 3,&! 136         4, -4, -1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1							
3, -2, 3, -2, 1, 1,&! 111         3, -1, -1, 3, 1, 1,&! 112         3, -1, 3, -1, 1, 1,&! 113         3, 0, 0, 3, 4, 7,&! 114         3, 0, 3, 0, 4, 7,&! 115         3, 1, 1, 3, 1, 1,&! 116         3, 1, 3, 1, 1, 1,&! 117         3, 2, 2, 3, 1, 1,&! 118         3, 2, 3, 2, 1, 1,&! 119         3, 3, 3, 3, 2, 2,&! 120         3, 4, 3, 4, 1, 1,&! 121         3, 5, 3, 5, 1, 1,&! 123         3, 5, 3, 5, 1, 1,&! 124         3, 6, 3, 6, 1, 1,&! 125         3, 6, 6, 3, 1, 1,&! 126         4, -6, -6, 4, 1, 1,&! 127         4, -6, -6, 4, 1, 1,&! 129         4, -5, -5, 4, 1, 1,&! 129         4, -4, -6, 6, 3, 3,&! 131         4, -4, -5, 5, 3, 3,&! 134         4, -4, -4, 4, 3, 4,&! 133         4, -4, -5, 5, 3, 3,&! 135         4, -4, -1, 1, 3, 3,&! 136         4, -4, -1, 1, 3, 3,&! 136         4, -4, -4, 4, 3, 3, 3, 139         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, -1, 1, 3, 3,&! 136         4, -4, -1, 1, 1, 3, 3,&! 136         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, 5, -5, 3, 3, 3,! 140         4, -4, 5, -5, 3, 3, 3,! 140         4, -4, 5, -5, 3, 3, 3,! 140							
3, -1, -1, 3, 1, 1,&! 112         3, -1, 3, -1, 1, 1,&! 113         3, 0, 0, 3, 4, 7,&! 114         3, 0, 3, 0, 4, 7,&! 115         3, 1, 1, 3, 1, 1,&! 116         3, 1, 3, 1, 1, 1,&! 117         3, 2, 2, 3, 1, 1,&! 118         3, 2, 3, 2, 1, 1,&! 119         3, 3, 3, 3, 2, 2,&! 120         3, 4, 3, 4, 1, 1,&! 121         3, 5, 3, 5, 1, 1,&! 123         3, 6, 3, 6, 1, 1,&! 124         3, 6, 6, 3, 1, 1,&! 125         3, 6, 6, 3, 1, 1,&! 127         4, -6, -6, 4, 1, 1,&! 129         4, -5, -5, 4, 1, 1,&! 129         4, -4, -6, 6, 3, 3,&! 130         4, -4, -4, 4, 3, 4,&! 133         4, -4, -4, 4, 3, 4,&! 133         4, -4, -1, 1, 3, 3,&! 136         4, -4, 1, -1, 3, 3,&! 136         4, -4, 5, -5, 3, 3, 3,! 130         4, -4, -5, 5, 3, 3, 3,! 134         4, -4, -5, 5, 3, 3, 3,! 134         4, -4, -5, 5, 3, 3, 3,! 136         4, -4, -5, 5, 3, 3, 3,! 136         4, -4, -1, 1, 3, 3,&! 136         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, 5, -5, 3, 3, 3,! 134         4, -4, 1, -1, 3, 3, 3,! 136         4, -4, 1, -1, 3, 3, 3,! 139         4, -4, 5, -5, 3, 3, 3,! 140	3,	-2,	-2,	3,	1,	1,&!	110
3,       -1,       3,       -1,       1,       1,&!       113         3,       0,       0,       3,       4,       7,&!       114         3,       0,       3,       4,       7,&!       115         3,       1,       1,       3,       1,       1,&!       116         3,       1,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       118         3,       2,       3,       1,       1,&!       118         3,       2,       3,       1,       1,&!       119         3,       3,       3,       2,       2,&!       120         3,       4,       3,       4,       1,       1,&!       122         3,       4,       3,       4,       1,       1,&!       122         3,       5,       5,       3,       1,       1,&!       122         3,       6,       6,       3,       1,       1,&!       124         4,       -6,	3,	-2,	3,	-2,	1,	1,&!	111
3,       -1,       3,       -1,       1,       1,&!       113         3,       0,       0,       3,       4,       7,&!       114         3,       0,       3,       4,       7,&!       115         3,       1,       1,       3,       1,       1,&!       116         3,       1,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       118         3,       2,       3,       1,       1,&!       118         3,       2,       3,       1,       1,&!       119         3,       3,       3,       2,       2,&!       120         3,       4,       3,       4,       1,       1,&!       122         3,       4,       3,       4,       1,       1,&!       122         3,       5,       5,       3,       1,       1,&!       122         3,       6,       6,       3,       1,       1,&!       124         4,       -6,	3,	-1,	-1,	3,	1,	1.&!	112
3,       0,       3,       4,       7,&!       114         3,       0,       3,       0,       4,       7,&!       115         3,       1,       1,       3,&!       11,&!       116         3,       1,       3,       1,       1,&!       117         3,       1,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       118         3,       2,       2,       3,       1,       1,&!       119         3,       3,       3,       2,       2,&!       120         3,       4,       3,       4,       1,       1,&!       121         3,       4,       3,       4,       1,       1,&!       122         3,       5,       5,       3,       1,       1,&!       122         3,       5,       5,       3,       1,       1,&!       122         3,       6,       6,       3,       1,       1,&!       122         4,       -6,       4,       -1,       1,&!       122         4,       -6,       4,							
3,       0,       3,       7,&!       115         3,       1,       1, &!       116         3,       1,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       118         3,       2,       3,       2,       1,       1,&!       119         3,       3,       3,       2,       2,&!       120         3,       4,       3,       4,       1,       1,&!       121         3,       4,       3,       4,       1,       1,&!       122         3,       5,       3,       5,       1,       1,&!       122         3,       6,       3,       6,       1,       1,&!       122         3,       6,       3,       6,       1,       1,&!       125         3,       6,       6,       3,       1,       1,&!       126         4,       -6,       4,       1,       1,&!       127         4,       -6,       4,       1,       1,&!							
3,       1,       1,       3,       1,       1,&!       116         3,       1,       3,       1,       1,&!       117         3,       2,       2,       3,       1,       1,&!       118         3,       2,       3,       2,       1,&!       119         3,       3,       3,       2,       2,&!       120         3,       4,       3,       4,       1,       1,&!       121         3,       4,       3,       1,       1,&!       122         3,       5,       3,       5,       1,       1,&!       122         3,       5,       5,       3,       1,       1,&!       122         3,       6,       3,       1,       1,&!       122         3,       6,       3,       1,       1,&!       122         3,       6,       6,       3,       1,       1,&!       125         3,       6,       6,       3,       1,       1,&!       126         4,       -6,       4,       1,       1,&!       127         4,       -6,       4,       1,							
3,       1,       3,       1,       1, &! 117         3,       2,       2,       3,       1,       1,&! 118         3,       2,       3,       2,       2,&! 120         3,       3,       3,       2,       2,&! 120         3,       4,       3,       1,       1,&! 121         3,       4,       4,       3,       1,       1,&! 122         3,       5,       3,       5,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 125         3,       6,       6,       3,       1,       1,&! 126         4,       -6,       6,       3,       1,       1,&! 127         4,       -6,       4,       1,       1,&! 128       122         4,       -6,       4,       1,       1,&! 129       124         4,       -5,       4,       -5,       1,	3,	Ο,	3,	Ο,	4,	7,&!	115
3,       1,       3,       1,       1, &! 117         3,       2,       2,       3,       1,       1,&! 118         3,       2,       3,       2,       2,&! 120         3,       3,       3,       2,       2,&! 120         3,       4,       3,       1,       1,&! 121         3,       4,       4,       3,       1,       1,&! 122         3,       5,       3,       5,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 122         3,       6,       3,       6,       1,       1,&! 125         3,       6,       6,       3,       1,       1,&! 126         4,       -6,       6,       3,       1,       1,&! 127         4,       -6,       4,       1,       1,&! 128       122         4,       -6,       4,       1,       1,&! 129       124         4,       -5,       4,       -5,       1,	3,	1,	1,	3,	1,	1,&!	116
3,       2,       2,       3,       1,       1, &!       118         3,       2,       3,       2,       1,       1, &!       119         3,       3,       3,       2,       2, &!       120         3,       4,       3,       1,       1, &!       121         3,       4,       4,       3,       1,       1, &!       122         3,       5,       3,       5,       1,       1, &!       123         3,       5,       5,       3,       1,       1, &!       123         3,       6,       3,       6,       1,       1, &!       122         3,       6,       6,       3,       1,       1, &!       123         3,       6,       6,       3,       1,       1, &!       124         4,       -6,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       127         4,       -6,       4,       1,       1, &!       126         4,       -6,       4,       1,       1, &!       129 <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>							
3,       2,       3,       2,       1,       1, &!       119         3,       3,       3,       2,       2,&!       120         3,       4,       3,       1,       1,&!       121         3,       4,       4,       3,       1,       1,&!       122         3,       5,       3,       5,       1,       1,&!       123         3,       6,       3,       1,       1,&!       123         3,       6,       3,       1,       1,&!       123         3,       6,       3,       1,       1,&!       124         3,       6,       3,       1,       1,&!       124         4,       -6,       -6,       3,       1,       1,&!       125         3,       6,       6,       3,       1,       1,&!       126         4,       -6,       -6,       4,       1,       1,&!       127         4,       -6,       -6,       1,       1,&!       127         4,       -6,       -6,       3,       3,&!       130         4,       -1,       -5,       5,       3, </td <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>							
3,       3,       3,       4,       1,       1, &!       120         3,       4,       3,       1,       1, &!       121         3,       4,       4,       3,       1,       1, &!       122         3,       5,       3,       5,       1,       1, &!       123         3,       6,       3,       1,       1, &!       124         3,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       126         4,       -6,       -6,       4,       1,       1, &!       127         4,       -6,       -6,       4,       1,       1, &!       128         4,       -6,       -6,       1,       1, &!       128         4,       -6,       -6,       1,       1, &!       129         4,       -5,       -5,       1,       1, &!       129         4,       -6,       -6,       3,       3, &!       130         4,       -4,       -6, <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>							
3,       4,       3,       1,       1,&!       121         3,       4,       4,       3,       1,       1,&!       122         3,       5,       3,       5,       1,       1,&!       124         3,       6,       3,       1,       1,&!       125         3,       6,       6,       3,       1,       1,&!       125         3,       6,       6,       3,       1,       1,&!       126         4,       -6,       -6,       4,       1,       1,&!       126         4,       -6,       -6,       4,       1,       1,&!       127         4,       -6,       -6,       1,       1,&!       128         4,       -6,       4,       1,       1,&!       129         4,       -6,       4,       1,       1,&!       129         4,       -6,       4,       1,       1,&!       129         4,       -5,       -5,       1,       1,&!       129         4,       -6,       6,       3,       3,&!       130         4,       -4,       -5,       5,       3	3,	2,	3,	2,	1,	1,&!	119
3,       4,       4,       3,       1,       1, &!       122         3,       5,       3,       5,       1,       1, &!       123         3,       5,       5,       3,       1,       1, &!       124         3,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       126         4,       -6,       -6,       4,       1,       1, &!       126         4,       -6,       -6,       1,       1, &!       127         4,       -6,       -6,       1,       1, &!       126         4,       -6,       -6,       1,       1, &!       128         4,       -5,       -5,       4,       1, &!       129         4,       -6,       -6,       1,       1, &!       130         4,       -4,       -6,       6,       3,       3, &!       131         4,       -4,       -6,       6,       3,       3, &!       132         4,       -4,	3,	3,	3,	3,	2,	2,&!	120
3,       4,       4,       3,       1,       1, &!       122         3,       5,       3,       5,       1,       1, &!       123         3,       5,       5,       3,       1,       1, &!       124         3,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       126         4,       -6,       -6,       4,       1,       1, &!       126         4,       -6,       -6,       1,       1, &!       127         4,       -6,       -6,       1,       1, &!       126         4,       -6,       -6,       1,       1, &!       128         4,       -5,       -5,       4,       1, &!       129         4,       -6,       -6,       1,       1, &!       130         4,       -4,       -6,       6,       3,       3, &!       131         4,       -4,       -6,       6,       3,       3, &!       132         4,       -4,	3.	4.	3.	4.	1.	1.&!	121
3,       5,       3,       5,       1,       1, &!       123         3,       5,       5,       3,       1,       1, &!       124         3,       6,       3,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       126         4,       -6,       -6,       4,       1,       1, &!       127         4,       -6,       -6,       1,       1, &!       127         4,       -6,       4,       1,       1, &!       127         4,       -6,       4,       1,       1, &!       128         4,       -6,       4,       1,       1, &!       129         4,       -5,       4,       1,       1, &!       129         4,       -5,       4,       1,       1, &!       129         4,       -5,       4,       1,       1, &!       129         4,       -6,       6,       3,       3, &!       130         4,       -4,       -5,       5,       3,       3, &!       132         4,       -4,       -2,       2,       3, </td <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>							
3,       5,       5,       3,       1,       1, &!       124         3,       6,       3,       6,       1,       1, &!       125         3,       6,       6,       3,       1,       1, &!       126         4,       -6,       -6,       4,       1,       1, &!       127         4,       -6,       4,       1,       1, &!       127         4,       -6,       4,       1,       1, &!       127         4,       -6,       4,       1,       1, &!       127         4,       -6,       4,       1,       1, &!       128         4,       -6,       4,       1,       1, &!       129         4,       -6,       4,       1,       1, &!       129         4,       -5,       4,       1,       1, &!       129         4,       -6,       6,       3,       3, &!       130         4,       -4,       -6,       6,       3,       3, &!       131         4,       -4,       -2,       2,       3,       3, &!       133         4,       -4,       -1,       1,<							
3,       6,       3,       6,       1,       1,&!       125         3,       6,       6,       3,       1,       1,&!       126         4,       -6,       -6,       4,       1,       1,&!       127         4,       -6,       4,       -6,       1,       1,&!       129         4,       -5,       -5,       4,       1,&!       129         4,       -5,       4,       -5,       1,       1,&!       129         4,       -5,       4,       -5,       1,       1,&!       129         4,       -6,       6,       3,       3,&!       130         4,       -4,       -6,       6,       3,       3,&!       131         4,       -4,       -5,       5,       3,       3,&!       132         4,       -4,       -4,       4,       3,       4,&!       133         4,       -4,       -3,       3,       3,&!       132         4,       -4,       -1,       1,       3,       3,&!       133         4,       -4,       -1,       1,       3,       3,&!       133							
3,       6,       6,       3,       1,       1, &!       126         4,       -6,       -6,       4,       1,       1, &!       127         4,       -6,       4,       -6,       1,       1, &!       128         4,       -5,       -5,       4,       1,       1, &!       129         4,       -5,       4,       1,       1, &!       130         4,       -4,       -6,       6,       3,       3, &!       131         4,       -4,       -6,       6,       3,       3, &!       132         4,       -4,       -5,       5,       3,       3, &!       132         4,       -4,       -4,       4,       3,       4, &!       133         4,       -4,       -3,       3,       3, &!       134         4,       -4,       -2,       2,       3,       3, &!       135         4,       -4,       -1,       1,       3,       3, &!       136         4,       -4,       -1,       1,       3,       3, &!       136         4,       -4,       1,       -1,       3, <td< td=""><td>3,</td><td>5,</td><td>5,</td><td>3,</td><td>1,</td><td>1,&amp;!</td><td>124</td></td<>	3,	5,	5,	3,	1,	1,&!	124
3,       6,       6,       3,       1,       1, &!       126         4,       -6,       -6,       4,       1,       1, &!       127         4,       -6,       4,       -6,       1,       1, &!       128         4,       -5,       -5,       4,       1,       1, &!       129         4,       -5,       4,       1,       1, &!       130         4,       -4,       -6,       6,       3,       3, &!       131         4,       -4,       -6,       6,       3,       3, &!       132         4,       -4,       -5,       5,       3,       3, &!       132         4,       -4,       -4,       4,       3,       4, &!       133         4,       -4,       -3,       3,       3, &!       134         4,       -4,       -2,       2,       3,       3, &!       135         4,       -4,       -1,       1,       3,       3, &!       136         4,       -4,       -1,       1,       3,       3, &!       136         4,       -4,       1,       -1,       3, <td< td=""><td>3,</td><td>6,</td><td>3,</td><td>6,</td><td>1,</td><td>1,&amp;!</td><td>125</td></td<>	3,	6,	3,	6,	1,	1,&!	125
4, -6, -6, 4, 1, 1, &! 127         4, -6, 4, -6, 1, 1, &! 128         4, -5, -5, 4, 1, 1, &! 129         4, -5, 4, -5, 1, 1, &! 130         4, -4, -6, 6, 3, 3, &! 131         4, -4, -5, 5, 3, 3, &! 132         4, -4, -4, 4, 3, 4, &! 133         4, -4, -3, 3, 3, 3, &! 134         4, -4, -1, 1, 3, 3, &! 136         4, -4, 0, 0, 3, 5, &! 137         4, -4, 1, -1, 3, 3, &! 138         4, -4, 2, -2, 3, 3, &! 139         4, -4, 3, -3, 3, 3, &! 140         4, -4, 5, -5, 3, 3, &! 141         4, -4, 6, -6, 3, 3, &! 142         4, -4, 6, -6, 3, 3, &! 143         4, -2, 4, -2, 4, 1, 1, &! 144         4, -2, 4, -2, 1, 1, &! 145         4, -2, 4, -2, 1, 1, &! 147         4, -1, 4, -1, 4, 1, 1, &! 148         4, -1, 4, -1, 1, 1, &! 149         4, -1, 4, -1, 1, 1, &! 149							
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4,       -5,       -5,       4,       1,       1,&!       129         4,       -5,       4,       -5,       1,       1,&!       130         4,       -4,       -6,       6,       3,       3,&!       131         4,       -4,       -5,       5,       3,       3,&!       132         4,       -4,       -4,       4,       3,       4,&!       133         4,       -4,       -3,       3,       3,&!       134         4,       -4,       -2,       2,       3,       3,&!       135         4,       -4,       -2,       2,       3,       3,&!       136         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       1,       -1,       3,       3,&!       138         4,       -4,       3,       -3,       3,&!							
4,       -5,       4,       -5,       1,       1,&!       130         4,       -4,       -6,       6,       3,       3,&!       131         4,       -4,       -5,       5,       3,       3,&!       132         4,       -4,       -4,       3,       4,&!       133         4,       -4,       -3,       3,&!       134         4,       -4,       -2,       2,       3,       3,&!       134         4,       -4,       -2,       2,       3,       3,&!       135         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       0,       0,       3,       5,&!       137         4,       -4,       1,       -1,       3,       3,&!       138         4,       -4,       2,       -2,       3,       3,&!       139         4,       -4,       3,       3,&!       140         4,				-6,	1,		
4, -4, -6, 6, 3, 3,&! 131         4, -4, -5, 5, 3, 3,&! 132         4, -4, -4, 4, 3, 4,&! 133         4, -4, -3, 3, 3, 3,&! 134         4, -4, -1, 1, 3, 3,&! 135         4, -4, 0, 0, 3, 5,&! 137         4, -4, 1, -1, 3, 3,&! 138         4, -4, 2, -2, 3, 3,&! 139         4, -4, 3, -3, 3, 3,&! 140         4, -4, 5, -5, 3, 3,&! 141         4, -4, 6, -6, 3, 3,&! 142         4, -3, 4, -3, 1, 1,&! 144         4, -2, -2, 4, 1, 1,&! 145         4, -2, 4, -2, 1, 1,&! 147         4, -1, 4, -1, 1, 1,&! 148         4, -1, 4, -1, 1, 1,&! 149         4, 0, 0, 4, 4, 7,&! 150	4,	-5,	-5,	4,	1,	1,&!	129
4, -4, -6, 6, 3, 3,&! 131         4, -4, -5, 5, 3, 3,&! 132         4, -4, -4, 4, 3, 4,&! 133         4, -4, -3, 3, 3, 3,&! 134         4, -4, -1, 1, 3, 3,&! 135         4, -4, 0, 0, 3, 5,&! 137         4, -4, 1, -1, 3, 3,&! 138         4, -4, 2, -2, 3, 3,&! 139         4, -4, 3, -3, 3, 3,&! 140         4, -4, 5, -5, 3, 3,&! 141         4, -4, 6, -6, 3, 3,&! 142         4, -3, 4, -3, 1, 1,&! 144         4, -2, -2, 4, 1, 1,&! 145         4, -2, 4, -2, 1, 1,&! 147         4, -1, 4, -1, 1, 1,&! 148         4, -1, 4, -1, 1, 1,&! 149         4, 0, 0, 4, 4, 7,&! 150	4,	-5,	4,	-5,	1,	1,&!	130
4, -4, -5, 5, 3, 3,&! 132         4, -4, -4, 4, 3, 4,&! 133         4, -4, -3, 3, 3, 3,&! 134         4, -4, -2, 2, 3, 3,&! 135         4, -4, -1, 1, 3, 3,&! 136         4, -4, 0, 0, 3, 5,&! 137         4, -4, 1, -1, 3, 3,&! 138         4, -4, 2, -2, 3, 3,&! 139         4, -4, 3, -3, 3, 3,&! 140         4, -4, 4, -4, 3, 4,&! 141         4, -4, 5, -5, 3, 3,&! 142         4, -3, 4, -3, 4, 1, 1,&! 144         4, -3, 4, -3, 1, 1,&! 145         4, -2, 4, -2, 1, 1,&! 147         4, -1, 4, -1, 1, 1,&! 148         4, -1, 4, -1, 1, 1,&! 149         4, 0, 0, 4, 4, 7,&! 150							
4,       -4,       -4,       4,       3,       4, &!       133         4,       -4,       -3,       3,       3, &!       134         4,       -4,       -2,       2,       3,       3, &!       135         4,       -4,       -1,       1,       3,       3, &!       136         4,       -4,       0,       0,       3,       5, &!       137         4,       -4,       1,       -1,       3,       3, &!       138         4,       -4,       1,       -1,       3,       3, &!       138         4,       -4,       1,       -2,       3,       3, &!       139         4,       -4,       2,       -2,       3,       3, &!       139         4,       -4,       3,       -3,       3, &!       139         4,       -4,       3,       -3,       3, &!       139         4,       -4,       3,       3, &!       139         4,       -4,       3,       3, &!       140         4,       -4,       3,       3, &!       140         4,       -4,       5,       -5,							
4,       -4,       -3,       3,       3, &!       134         4,       -4,       -2,       2,       3,       3,&!       135         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       0,       0,       3,       5,&!       137         4,       -4,       1,       -1,       3,       3,&!       138         4,       -4,       1,       -1,       3,       3,&!       138         4,       -4,       2,       -2,       3,       3,&!       138         4,       -4,       3,       -3,&!       138       138       138       138       138       138       138       149       140       140       140       140       140       140       140       140       141							
4,       -4,       -2,       2,       3,       3,&!       135         4,       -4,       -1,       1,       3,       3,&!       136         4,       -4,       0,       0,       3,       5,&!       137         4,       -4,       1,       -1,       3,       3,&!       138         4,       -4,       2,       -2,       3,       3,&!       139         4,       -4,       3,       -3,&!       140         4,       -4,       3,       3,&!       140         4,       -4,       4,       -4,       3,       4,&!       141         4,       -4,       4,       -4,       3,       4,&!       142         4,       -4,       5,       -5,       3,       3,&!       142         4,       -4,       6,       -6,       3,       3,&!       143         4,       -3,       -3,       4,       1,       1,&!       145         4,       -3,       -4,       -3,       1,       1,&!       145         4,       -2,       -2,       4,       1,       1,&!       147 <tr< td=""><td></td><td>-4,</td><td></td><td></td><td>3,</td><td></td><td></td></tr<>		-4,			3,		
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4, -4, -1, 1, 3, 3,&! 136         4, -4, 0, 0, 0, 3, 5,&! 137         4, -4, 1, -1, 3, 3,&! 138         4, -4, 2, -2, 3, 3,&! 139         4, -4, 3, -3, 3, 3,&! 140         4, -4, 5, -5, 3, 3,&! 141         4, -4, 6, -6, 3, 3,&! 142         4, -3, 4, -3, 1, 1,&! 144         4, -2, -2, 4, 1, 1,&! 145         4, -2, 4, -2, 1, 1,&! 147         4, -1, 4, -1, 1, 1,&! 148         4, -1, 4, -1, 1, 1,&! 149         4, 0, 0, 4, 4, 7,&! 150	4,	-4,	-2,	2,	3,	3,&!	135
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4,       -4,       1,       -1,       3,       3,&!       138         4,       -4,       2,       -2,       3,       3,&!       139         4,       -4,       3,       3,&!       140         4,       -4,       4,       -4,       3,       4,&!       141         4,       -4,       5,       -5,       3,       3,&!       142         4,       -4,       6,       -6,       3,       3,&!       143         4,       -3,       -3,       4,       1,       1,&!       144         4,       -3,       4,       -3,       1,       1,&!       145         4,       -2,       -2,       4,       1,       1,&!       146         4,       -2,       4,       -2,       1,       1,&!       147         4,       -1,       -1,       4,       1,       1,&!       148         4,       -1,       4,       -1,       1,&!       149         4,       0,       0,       4,       4,       7,&!       150							
4,       -4,       2,       -2,       3,       3,&!       139         4,       -4,       3,       -3,       3, &!       140         4,       -4,       4,       -4,       3,       4,&!       141         4,       -4,       5,       -5,       3,       3,&!       142         4,       -4,       6,       -6,       3,       3,&!       143         4,       -3,       -3,       4,       1,       1,&!       144         4,       -3,       4,       -3,       1,       1,&!       145         4,       -2,       -2,       4,       1,       1,&!       146         4,       -2,       4,       -2,       1,       1,&!       147         4,       -1,       -1,       4,       1,       1,&!       148         4,       -1,       4,       -1,       1,&!       149         4,       0,       0,       4,       4,       7,&!       150							
4,       -4,       3,       -3,       3,       3, &!       140         4,       -4,       4,       -4,       3,       4, &!       141         4,       -4,       5,       -5,       3,       3, &!       142         4,       -4,       6,       -6,       3,       3, &!       143         4,       -3,       -3,       4,       1,       1, &!       144         4,       -3,       4,       -3,       1,       1, &!       145         4,       -2,       -2,       4,       1,       1, &!       146         4,       -2,       4,       -2,       1,       1, &!       147         4,       -1,       -1,       4,       1,       1, &!       148         4,       -1,       -1,       1,       1, &!       149         4,       0,       0,       4,       4,       7, &!       150							
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4, -4, 4, -4, 3, 4,&! 141         4, -4, 5, -5, 3, 3,&! 142         4, -4, 6, -6, 3, 3,&! 143         4, -3, -3, 4, 1, 1,&! 144         4, -2, -2, 4, 1, 1,&! 145         4, -2, 4, -2, 1, 1,&! 147         4, -1, -1, 4, 1, 1,&! 148         4, -1, 4, -1, 1, 1,&! 149         4, 0, 0, 4, 4, 7,&! 150	4,	-4,	3,	-3,	3,	3,&!	140
4,       -4,       5,       -5,       3,       3,&!       142         4,       -4,       6,       -6,       3,       3,&!       143         4,       -3,       -3,       1,       1,&!       144         4,       -3,       4,       -3,       1,       1,&!       145         4,       -2,       -2,       4,       1,       1,&!       146         4,       -2,       4,       -2,       1,       1,&!       147         4,       -1,       -1,       4,       1,       1,&!       148         4,       -1,       4,       -1,       1,&!       149         4,       0,       0,       4,       4,       7,&!       150							
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4,       -3,       4,       -3,       1,       1,&!       145         4,       -2,       -2,       4,       1,       1,&!       146         4,       -2,       4,       -2,       1,       1,&!       147         4,       -1,       -1,       4,       1,       1,&!       148         4,       -1,       4,       -1,       1,&!       149         4,       0,       0,       4,       4,       7,&!       150	4,	-3,	-3,	4,	1,	1,&!	144
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4, -2, 4, -2, 1, 1,&! 147 4, -1, -1, 4, 1, 1,&! 148 4, -1, 4, -1, 1, 1,&! 149 4, 0, 0, 4, 4, 7,&! 150							
4, -1, -1, 4, 1, 1,&! 148 4, -1, 4, -1, 1, 1,&! 149 4, 0, 0, 4, 4, 7,&! 150							
4, -1, 4, -1, 1, 1, &! 149 4, 0, 0, 4, 4, 7, &! 150							
4, 0, 0, 4, 4, 7,&! 150	4,	-1,	-1,	4,	1,	1,&!	148
4, 0, 0, 4, 4, 7,&! 150	4,	-1,	4,	-1,	1,	1,&!	149
τ, Ο, τ, Ο, τ, Γ,α: 151							
	ᡸ,	Ο,	4,	Ο,	Ψ,	ι,α:	101

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4,
                               1,&! 152
      1,
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                  4,
                        1,
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4,
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            4,
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                               1,&! 155
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                  5,
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           -6,
     -5,
                               4,&! 166
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           -5,
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                        3,
                               3,&! 167
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     -5,
           -3,
                  3,
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                               3,&! 168
     -5,
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                               3,&! 169
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                               3,&! 170
           -1,
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            1,
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     -5,
                 -3,
                        3,
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                               4,&! 176
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                 -6,
                               3,&! 177
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    -4,
           -4,
                  5,
                               1,&! 178
                        1,
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     -4,
            5,
                 -4,
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                               1,&! 179
     -3,
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                  5,
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                               1,&! 183
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     -2,
            5,
                 -2,
                        1,
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     -1,
           -1,
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                        1,
                               1,&! 184
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            5,
                 -1,
                        1,
                               1,&! 185
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                        4,
                               7,&! 186
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                               7,&! 187
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      0,
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                               1,&! 188
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                  5,
                               1,&! 190
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            5,
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                               1,&! 191
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                               1,&! 195
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                               1,&! 197
            6,
                               1,&! 198
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      6,
                  5,
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                        3,
                               4,&! 199
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     -6,
           -5,
                  5,
                        3,
                               3,&! 200
     -6,
           -4,
                  4,
                        3,
                               3,&! 201
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     -6,
           -3,
                  3,
                        3,
                               3,&! 202
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6,
       -6,
             -2,
                    2,
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                                3,&! 204
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       -6,
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       -6,
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              3,
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        3,
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              4,
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        4,
              6,
                    4,
                                1,&! 231
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        5,
                    6,
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                                 1,&! 232
  6,
        5,
              6,
                    5,
                          1,
                                 1,&! 233
        6,
                    6,
                          2,
                                 2&! 234
  6,
              6,
],[6,469])
```

```
integer,dimension(2,0:16),parameter::double_pdf_kinds=reshape([&
     &0,0,&
     &1,1,&
     &1,2,&
     &1,3,&
     &1,4,&
     &2,1,&
     &2,2,&
     &2,3,&
     &2,4,&
     &3,1,&
     &3,2,&
     &3,3,&
     &3,4,&
     &4,1,&
     &4,2,&
```

```
&4,3,&
     &4,4&
     &],[2,17])
integer, parameter, dimension (371)::int_all=[&
                -5,
                             -3,
                                                                2,
                                                                                            6,
                                                                                               -14,
                                                                                                       -13,
     & -6,
                      -4,
                                    -2,
                                           -1,
                                                   0,
                                                         1,
                                                                       3,
                                                                              4,
                                                                                     5,
     & -9,
               -8,
                      -7,
                              7,
                                     8,
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                                                               12,
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                                                               79,
              -79,
                     -78,
                            -43,
                                   -42,
                                           42,
                                                 43,
                                                        78,
                                                                     114,
                                                                           115,
                                                                                  150,
                                                                                         151, -158, -157, -
     &-114,
     &-153, -152, -149, -148, -147, -146, -145, -144, -143, -142, -141, -140, -139, -138, -137, -
     &-133, -132, -131, -122, -121, -120, -119, -118, -117, -116, -113, -112, -111, -110, -109, -
     \&-105, -104, -103, -102, -101, -100,
                                                -99,
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     & -77,
              -76,
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                                   -47,
     & -59,
              -50,
                     -49,
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     & -31,
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     & 32.
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     & 106,
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     & 134,
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              135,
                     136,
                                                              142,
                                                                                   145,
                                                                                                       148,
     & 154,
              155,
                     156,
                            157,
                                   158, -149, -148, -113, -112,
                                                                     -77,
                                                                            -76,
                                                                                   -41,
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                                   -30,
                                          -29,
                                                                                   152,
                                                                                         153, -147, -146, -
     & -34,
              -33,
                     -32,
                            -31,
                                                 44,
                                                        80,
                                                               81,
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     \& -74,
              -73,
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     & 119,
              154,
                     155,
                             42,
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     & 77,
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                             82,
                                    83,
                                           84,
                                                 85,
                                                        86,
                                                               80,
                                                                      81,
                                                                             82]
integer, parameter, dimension (16)::int_sizes_all=[13,16,2,2,16,208,26,26,26,2,26,1,2,2,26,2,1]
integer, parameter, dimension (3,0:8)::muli_flow_stats=&
     reshape([&
      1, 2,4,&
      3, 4,4,&
      5, 6,8,&
      7, 8,4,&
      9,10,8,&
     11,16,16,&
     17,22,16,&
     23,28,16,&
     29,52,96],&
     [3,9])
integer, parameter, dimension (0:4,52)::muli_flows=&
     reshape([&
     3,0,0,1,2,&!1a
     1,0,0,2,1,&
     1,2,0,0,3,&!1b
     3,3,0,0,2,&
     4,0,0,1,2,&!2
```

4,0,0,2,1,& 3,2,0,0,3,&!3 1,3,0,0,2,&

4,2,0,0,3,&!4 4,3,0,0,2,& 4,0,1,3,4,&!5 4,0,1,4,3,& 2,0,3,1,4,& 2,0,4,1,3,& 2,0,3,4,1,& 2,0,4,3,1,& 4,1,2,4,0,&!6 2,1,4,2,0,& 4,2,1,4,0,& 2,4,1,2,0,& 2,2,4,1,0,& 2,4,2,1,0,& 2,0,1,2,4,&!7 2,0,1,4,2,& 4,0,2,1,4,& 4,0,4,1,2,& 2,0,2,4,1,& 2,0,4,2,1,& 9,1,2,3,4,&!8 5,1,2,4,3,& 5,1,3,2,4,& 3,1,4,2,3,& 3,1,3,4,2,& 5,1,4,3,2,& 5,2,1,3,4,& 5,2,1,4,3,& 3,3,1,2,4,& 3,4,1,2,3,& 3,3,1,4,2,& 3,4,1,3,2,& 3,2,3,1,4,& 3,2,4,1,3,& 5,3,2,1,4,& 3,4,2,1,3,& 5,3,4,1,2,& 3,4,3,1,2,& 3,2,3,4,1,& 3,2,4,3,1,& 3,3,2,4,1,& 5,4,2,3,1,& 3,3,4,2,1,& 5,4,3,2,1],&

## 10.3 Interfaces

[5,52])

```
abstract interface
   function trafo_in(in)
     use kinds!NODEP!
     real(kind=double), dimension(3)::trafo_in
     real(kind=double),dimension(3),intent(in)::in
   end function trafo_in
end interface
abstract interface
   pure function coord_scalar_in(hyp)
     use kinds!NODEP!
     real(kind=double)::coord_scalar_in
     real(kind=double), dimension(3), intent(in)::hyp
   end function coord_scalar_in
end interface
abstract interface
   subroutine coord_hcd_in(hyp,cart,denom)
     use kinds!NODEP!
     real(kind=double), dimension(3), intent(in)::hyp
     real(kind=double), dimension(3), intent(out)::cart
     real(kind=double),intent(out)::denom
   end subroutine coord_hcd_in
end interface
interface
   pure function alphaspdf(Q)
     use kinds!NODEP!
     real(kind=double)::alphaspdf
     real(kind=double),intent(in)::Q
   end function alphaspdf
end interface
interface
   pure subroutine evolvepdf(x,q,f)
     use kinds!NODEP!
     real(kind=double),intent(in)::x,q
     real(kind=double),intent(out),dimension(-6:6)::f
   end subroutine evolvepdf
end interface
real(kind=double)::pts2_scale
```

## 10.4 Implementierung der Prozeduren

```
muli_get_state_transformations(inout_kind,lha_flavors) result

pure function muli_get_state_transformations(inout_kind,lha_flavors) result(transformations)
  integer,intent(in)::inout_kind
  integer,dimension(4),intent(in)::lha_flavors
  integer,dimension(4)::signature
  logical,dimension(3)::transformations
  where(lha_flavors>0)
    signature=1
```

```
elsewhere(lha_flavors<0)
       signature=-1
    elsewhere
       signature=0
    end where
    !print *,"inout_kind=",inout_kind
    !print *,"lha_flavors=",lha_flavors
    !print *, "signature", signature
    if(&
         (sum(inout_signatures(1:2,inout_kind)) == sum(signature(1:2))).and.&
         (sum(inout_signatures(3:4,inout_kind)) == sum(signature(3:4)))&
         )then
       transformations(1)=.false.
    else
       transformations(1)=.true.
       signature=-signature
    end if
    if(all(inout_signatures(1:2,inout_kind)==signature(1:2)))then
       transformations(2)=.false.
    else
       transformations(2)=.true.
    end if
    if(all(inout_signatures(3:4,inout_kind)==signature(3:4)))then
       transformations(3)=.false.
    else
       transformations(3)=.true.
    end if
    !print *, "signature", signature
    !print *,"transformations=",transformations
  end function muli_get_state_transformations
id
  pure function id(a)
    real(kind=double),dimension(:),intent(in)::a
    real(kind=double), dimension(size(a))::id
    id=a
  end function id
h to c ort
  pure function h_to_c_ort(hyp)
    real(kind=double), dimension(3)::h_to_c_ort
    real(kind=double), dimension(3), intent(in)::hyp
    h_to_c_ort=&
         \&[sqrt(sqrt(((hyp(1)*(1D0-hyp(3)))+hyp(3))**2+(hyp(2)-(5D-1))**2)\&
                      -(hyp(2)-(5D-1))&
         &, sqrt(sqrt(((hyp(1)*(1D0-hyp(3)))+hyp(3))**2+(hyp(2)-(5D-1))**2)&
                     +(hyp(2)-(5D-1)))&
         &,hyp(3)]
  end function h_to_c_ort
```

```
c_to h ort
 pure function c_to_h_ort(cart)
    real(kind=double), dimension(3)::c_to_h_ort
    real(kind=double), dimension(3), intent(in)::cart
    c_{to}_{-h_{ort}} = [(cart(3) - (cart(1) * cart(2))) / (cart(3) - 1D0), &
                (1D0 - cart(1)**2 + cart(2)**2)/2D0, cart(3)]
  end function c_to_h_ort
h to c noparam
 pure function h_to_c_noparam(hyp)
    real(kind=double), dimension(2)::h_to_c_noparam
    real(kind=double), dimension(2), intent(in)::hyp
    h_to_c_noparam=&
         &[sqrt(sqrt(hyp(1)**8+(((hyp(2)-(5D-1))**3)*4)**2)-((hyp(2)-(5D-1))**3)*4)&
         \&, sqrt(sqrt(hyp(1)**8+(((hyp(2)-(5D-1))**3)*4)**2)+((hyp(2)-(5D-1))**3)*4)]
  end function h_to_c_noparam
c to h noparam
 pure function c_to_h_noparam(cart)
    real(kind=double), dimension(2)::c_to_h_noparam
    real(kind=double), dimension(2), intent(in)::cart
    c_to_h_noparam=&
        &[sqrt(sqrt(cart(1)*cart(2)))&
         &,(1D0+sign(abs((cart(2)**2) - (cart(1)**2))**(1/3D0),cart(2)-cart(1)))/2D0]
  end function c_to_h_noparam
h to c param
 pure function h_to_c_param(hyp)
    real(kind=double), dimension(3)::h_to_c_param
    real(kind=double), dimension(3), intent(in)::hyp
    h_to_c_param=&
        -((hyp(2)-(5D-1))**3)*4)&
        \&, sqrt(sqrt((((hyp(1)**4)*(1D0-hyp(3)))+hyp(3))**2+(((hyp(2)-(5D-1))**3)*4)**2)\&
                    +((hyp(2)-(5D-1))**3)*4)&
         &,hyp(3)]
  end function h_to_c_param
c to h param
 pure function c_to_h_param(cart)
    real(kind=double), dimension(3)::c_to_h_param
    real(kind=double), dimension(3), intent(in)::cart
    c_to_h_param=&
        \&[(((cart(1)*cart(2)) - cart(3))/(1D0 - cart(3)))**(1/4D0)\&]
         \&,(1D0+sign(abs((cart(2)**2) - (cart(1)**2))**(1/3D0),cart(2)-cart(1)))/2D0\&
         &, cart(3)]
  end function c_to_h_param
h to c smooth
```

```
pure function h_to_c_smooth(hyp)
    real(kind=double), dimension(3)::h_to_c_smooth
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double)::h2
   h2=(((hyp(2)-5D-1)**3)*4D0+hyp(2)-5D-1)/2D0
   h_to_c_smooth=&
        &, sqrt(sqrt((((hyp(1)**4)*(1D0-hyp(3)))+hyp(3))**2+h2**2)+h2)&
        &,hyp(3)]
  end function h_to_c_smooth
c to h smooth
 pure function c_to_h_smooth(cart)
    real(kind=double), dimension(3)::c_to_h_smooth
   real(kind=double), dimension(3), intent(in)::cart
    c_to_h_smooth=&
         [((product(cart(1:2))-cart(3))/(1D0-cart(3)))**(1/4D0),&
        (3D0-3D0**(2D0/3)/&
        (-9D0*cart(1)**2 + 9D0*cart(2)**2 + sqrt(3D0+81D0*(cart(1)**2-cart(2)**2)**2))
          **(1D0/3)&
        + 3**(1D0/3)*(-9D0*cart(1)**2 + 9D0*cart(2)**2 + sqrt(3D0 + 81D0*(cart(1)**2&
        - cart(2)**2)**2))**(1D0/3))/6D0, cart(3)]
  end function c_to_h_smooth
h to c ort def
  pure function h_to_c_ort_def(hyp)
    real(kind=double), dimension(3)::h_to_c_ort_def
    real(kind=double), dimension(3), intent(in)::hyp
   h_to_c_ort_def=h_to_c_ort([hyp(1),hyp(2),pts2_scale])
  end function h_to_c_ort_def
c to h ort def
  pure function c_to_h_ort_def(cart)
    real(kind=double), dimension(3)::c_to_h_ort_def
   real(kind=double),dimension(3),intent(in)::cart
    c_to_h_ort_def=c_to_h_ort([cart(1),cart(2),pts2_scale])
  end function c_to_h_ort_def
h to c param def
  pure function h_to_c_param_def(hyp)
    real(kind=double), dimension(3)::h_to_c_param_def
    real(kind=double), dimension(3), intent(in)::hyp
   h_to_c_param_def=h_to_c_param([hyp(1),hyp(2),pts2_scale])
  end function h_to_c_param_def
c to h param def
```

```
pure function c_to_h_param_def(cart)
    real(kind=double), dimension(3)::c_to_h_param_def
    real(kind=double), dimension(3), intent(in)::cart
    if(product(cart(1:2))>=pts2_scale)then
       c_to_h_param_def=c_to_h_param([cart(1),cart(2),pts2_scale])
    else
       c_to_h_param_def=[-1D0,-1D0,-1D0]
    end if
  end function c_to_h_param_def
h to c smooth def
  pure function h_to_c_smooth_def(hyp)
    real(kind=double), dimension(3)::h_to_c_smooth_def
    real(kind=double), dimension(3), intent(in)::hyp
    h_to_c_smooth_def=h_to_c_smooth([hyp(1),hyp(2),pts2_scale])
  end function h_to_c_smooth_def
c to h smooth def
  pure function c_to_h_smooth_def(cart)
    real(kind=double), dimension(3)::c_to_h_smooth_def
    real(kind=double), dimension(3), intent(in)::cart
    if(product(cart(1:2))>=pts2_scale)then
       c_to_h_smooth_def=c_to_h_smooth([cart(1), cart(2), pts2_scale])
    else
       c_{to}_{n-1D0}
    end if
  end function c_to_h_smooth_def
voxel h to c ort
  pure function voxel_h_to_c_ort(hyp)
    real(kind=double)::voxel_h_to_c_ort
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double)::T,TH1
    T=1D0-hyp(3)
    TH1=T*(1DO-hyp(1))
    voxel_h_to_c_ort=Sqrt(T**2/(5D0-4D0*(1D0-hyp(2))*hyp(2)-4D0*(2D0-TH1)*TH1))
  end function voxel_h_to_c_ort
voxel c to h ort
  pure function voxel_c_to_h_ort(cart)
    real(kind=double)::voxel_c_to_h_ort
    real(kind=double), dimension(3), intent(in)::cart
    real(kind=double)::P
    P=product(cart(1:2))
    if(P>cart(3))then
       voxel_c_{to_h_ort} = (cart(1)**2 + cart(2)**2)/(1D0-cart(3))
    else
       voxel_c_to_h_ort=0D0
```

```
end if
  end function voxel_c_to_h_ort
voxel h to c noparam
  pure function voxel_h_to_c_noparam(hyp)
    real(kind=double)::voxel_h_to_c_noparam
    real(kind=double),dimension(3),intent(in)::hyp
    voxel_h_to_c_noparam=&
      12D0*Sqrt((hyp(1)**6*(1D0-2D0*hyp(2))**4)/(4*hyp(1)**8+(1D0-2D0*hyp(2))**6))
  end function voxel_h_to_c_noparam
voxel c to h noparam
  pure function voxel_c_to_h_noparam(cart)
    real(kind=double)::voxel_c_to_h_noparam
    real(kind=double), dimension(3), intent(in)::cart
    real(kind=double)::P
    voxel_c_to_h_noparam = (cart(1)**2+cart(2)**2)/(12D0*(cart(1)*cart(2))**(3D0/4D0)&
         *(cart(2)**2+cart(1)**2)**(2D0/3D0))
  end function voxel_c_to_h_noparam
voxel h to c param
  pure function voxel_h_to_c_param(hyp)
    real(kind=double)::voxel_h_to_c_param
    real(kind=double), dimension(3), intent(in)::hyp
    voxel_h_to_c_param=12*Sqrt((hyp(1)**6*(1D0-2D0*hyp(2))**4*(hyp(3)-1D0)**2)&
         /((1D0-2D0*hyp(2))**6+4D0*(hyp(3)-(hyp(1)**4*(hyp(3)-1D0)))**2))
  end function voxel_h_to_c_param
voxel c to h param
  pure function voxel_c_to_h_param(cart)
    real(kind=double)::voxel_c_to_h_param
    real(kind=double), dimension(3), intent(in)::cart
    real(kind=double)::P,T,CP,CM
    P=product(cart(1:2))
    if(P>cart(3))then
       P=P-cart(3)
      CP=cart(1)**2+cart(2)**2
       CM=abs(cart(2)**2-cart(1)**2)
      T=1-cart(3)
       voxel_c_to_h_param=(Cp*sqrt(sqrt(P/T)))/(12*Cm**(2D0/3D0)*P)
       voxel_c_to_h_param=0D0
    end if
  end function voxel_c_to_h_param
voxel h to c smooth
```

```
pure function voxel_h_to_c_smooth(hyp)
    real(kind=double)::voxel_h_to_c_smooth
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double)::T
    T=1D0-hyp(3)
    voxel_h_to_c_smooth=&
         \&8D0*(hyp(1)**3*(1D0+3D0*(hyp(2)-1D0)*hyp(2))*T)\&
         \frac{1}{2} &/sqrt((1D0-2D0*hyp(2)*(2D0+hyp(2)*(2D0*hyp(2)-3D0)))**2+4D0*(1D0+(hyp(1)**4-1D0)*T)**2)
  end function voxel_h_to_c_smooth
voxel c to h smooth
 pure function voxel_c_to_h_smooth(cart)
    real(kind=double)::voxel_c_to_h_smooth
    real(kind=double), dimension(3), intent(in)::cart
    real(kind=double)::P,S,T,CM,CP
    P=product(cart(1:2))
    if(P>cart(3))then
       P=P-cart(3)
       CP=cart(1)**2+cart(2)**2
       CM = cart(2) **2 - cart(1) **2
       T=1-cart(3)
       S = sqrt(3D0 + 81D0 * cm * * 2)
       voxel_c_to_h_smooth=(3D0**(1D0/3D0)*Cp*(3D0**(1D0/3D0)+(9D0*Cm+S)**(2D0/3D0))&
            *sqrt(sqrt(P/T)))/(4D0*P*S*(9D0*Cm+S)**(1D0/3D0))
    else
       voxel_c_to_h_smooth=0D0
    end if
end function voxel_c_to_h_smooth
voxel h to c ort def
 pure function voxel_h_to_c_ort_def(hyp)
    real(kind=double)::voxel_h_to_c_ort_def
    real(kind=double), dimension(3), intent(in)::hyp
    voxel_h_to_c_ort_def=voxel_h_to_c_ort(hyp)
  end function voxel_h_to_c_ort_def
voxel c to h ort def
 pure function voxel_c_to_h_ort_def(cart)
    real(kind=double)::voxel_c_to_h_ort_def
    real(kind=double), dimension(3), intent(in)::cart
    voxel_c_to_h_ort_def=voxel_c_to_h_ort(cart)
  end function voxel_c_to_h_ort_def
voxel h to c param def
 pure function voxel_h_to_c_param_def(hyp)
    real(kind=double)::voxel_h_to_c_param_def
    real(kind=double), dimension(3), intent(in)::hyp
```

```
voxel_h_to_c_param_def=voxel_h_to_c_param(hyp)
  end function voxel_h_to_c_param_def
voxel c to h param def
  pure function voxel_c_to_h_param_def(cart)
    real(kind=double)::voxel_c_to_h_param_def
    real(kind=double), dimension(3), intent(in)::cart
    voxel_c_to_h_param_def=voxel_c_to_h_param(cart)
  end function voxel_c_to_h_param_def
voxel h to c smooth def
  pure function voxel_h_to_c_smooth_def(hyp)
    real(kind=double)::voxel_h_to_c_smooth_def
    real(kind=double), dimension(3), intent(in)::hyp
    voxel_h_to_c_smooth_def=voxel_h_to_c_smooth(hyp)
  end function voxel_h_to_c_smooth_def
voxel c to h smooth def
  pure function voxel_c_to_h_smooth_def(cart)
    real(kind=double)::voxel_c_to_h_smooth_def
    real(kind=double), dimension(3), intent(in)::cart
    voxel_c_to_h_smooth_def=voxel_c_to_h_smooth(cart)
  end function voxel_c_to_h_smooth_def
denom cart
  pure function denom_cart(cart)
    real(kind=double)::denom_cart
    real(kind=double), dimension(3), intent(in)::cart
    denom_cart=1D0/(864D0*Sqrt(cart(3)**3*(1D0-cart(3)/product(cart(1:2)))))
  end function denom_cart
denom ort
  pure function denom_ort(hyp)
    real(kind=double)::denom_ort
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double)::Y,P
    Y = (1D0 - 2D0 * hyp(2)) * * 2
    P=1D0-hyp(3)
    if(hyp(1)>0D0.and.hyp(3)>0D0)then
       denom_ort=sqrt((P + (-1 + Hyp(1))*P**2)&
                      /(746496*hyp(1)*hyp(3)**3*(4*(1 + (-1 + hyp(1))*P)**2 + Y)))
    else
       denom_ort=0D0
    end if
  end function denom_ort
denom param
```

```
pure function denom_param(hyp)
               real(kind=double)::denom_param
               real(kind=double), dimension(3), intent(in)::hyp
               real(kind=double)::X,Y,P
               X = hyp(1) **4
               Y=1D0-2D0*hyp(2)
               P=1DO-hyp(3)
               if(hyp(3)>0D0)then
                           denom\_param=sqrt((P*(1+P*(X-1))*Sqrt(X)*Y**4)/(5184*(4*(1+P*(X-1))**2+Y**6)*hyp(3)**3))
               else
                           denom_param=0D0
               end if
       end function denom_param
denom param reg
       pure function denom_param_reg(hyp)
               real(kind=double)::denom_param_reg
               real(kind=double), dimension(3), intent(in)::hyp
               real(kind=double)::X,Y,P
               X = hyp(1) **4
               Y=1D0-2D0*hyp(2)
               P=1D0-hyp(3)
               if(hyp(3)>0D0)then
                           denom_param_reg=sqrt((P*(1+P*(X-1))*Sqrt(X)*Y**4)&
                                                                                                            /(5184*(4*(1+P*(X-1))**2+Y**6)*(hyp(3)+norm2_p_t_0)**3))
               else
                           denom_param_reg=0D0
               end if
       end function denom_param_reg
denom smooth
       pure function denom_smooth(hyp)
               real(kind=double)::denom_smooth
               real(kind=double), dimension(3), intent(in)::hyp
               real(kind=double)::X,Y,P
               X=hyp(1)**2
               Y = (1D0 - 2D0 * hyp(2)) * * 2
               P=1D0-hyp(3)
               if(hyp(3)>0D0)then
                           \label{eq:denom_smooth} $$\operatorname{denom\_smooth} = \operatorname{sqrt}((P*X*(1 + P*(-1 + X**2))*(1 + 3*Y)**2)/(46656*hyp(3)**3\&) = \operatorname{denom\_smooth} = \operatorname{deno
                                               *(16*(1 + P*(-1 + X**2))**2 + Y + 2*Y**2 + Y**3)))
               else
                           denom_smooth=0D0
               end if
       end function denom_smooth
denom smooth reg
       pure function denom_smooth_reg(hyp)
               real(kind=double)::denom_smooth_reg
```

```
real(kind=double),dimension(3),intent(in)::hyp
    real(kind=double)::X,Y,P
    X = hyp(1) **2
    Y=(1D0-2D0*hyp(2))**2
    P=1D0-hyp(3)
    if(hyp(3)>0D0)then
       denom_smooth_reg=&
         sqrt((P*X*(1 + P*(-1 + X**2))*(1 + 3*Y)**2)&
              /(46656*(hyp(3)+norm2_p_t_0)**3&
                *(16*(1 + P*(-1 + X**2))**2 + Y + 2*Y**2 + Y**3)))
    else
       denom_smooth_reg=0D0
    end if
  end function denom_smooth_reg
denom cart save
   pure function denom_cart_save(cart)
    real(kind=double)::denom_cart_save
    real(kind=double), dimension(3), intent(in)::cart
    if(product(cart(1:2))>cart(3))then
       denom_cart_save=denom_cart(cart)
    else
       denom_cart_save=0D0
    end if
  end function denom_cart_save
denom ort save
  pure function denom_ort_save(hyp)
    real(kind=double)::denom_ort_save
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double)::Y,Z,W
    real(kind=double), dimension(3)::cart
    cart=h_to_c_ort(hyp)
    if(cart(1)>1D0.or.cart(2)>1D0)then
       denom ort save=0D0
    else
       denom_ort_save=denom_ort(hyp)
    end if
  end function denom_ort_save
denom param save
  pure function denom_param_save(hyp)
    real(kind=double)::denom_param_save
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double)::Y,Z,W
    real(kind=double),dimension(3)::cart
    cart=h_to_c_param(hyp)
    if(cart(1)>1D0.or.cart(2)>1D0)then
       denom_param_save=0D0
```

```
else
       denom_param_save=denom_param(hyp)
    end if
  end function denom_param_save
! pure denom smooth save
  function denom_smooth_save(hyp)
    real(kind=double)::denom_smooth_save
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double)::Y,Z,W
    real(kind=double), dimension(3)::cart
    cart=h_to_c_smooth(hyp)
    if(cart(1)>1D0.or.cart(2)>1D0)then
       denom_smooth_save=0D0
       denom_smooth_save=denom_smooth(hyp)
    end if
  end function denom_smooth_save
denom cart cuba int
  subroutine denom_cart_cuba_int(d_cart,cart,d_denom,denom,pt2s)
    real(kind=double), dimension(3), intent(in)::cart
    real(kind=double), dimension(1), intent(out)::denom
    real(kind=double),intent(in) :: pt2s
    integer,intent(in)::d_cart,d_denom
    denom(1)=denom_cart_save([cart(1),cart(2),pt2s])
  end subroutine denom_cart_cuba_int
denom ort cuba int
  subroutine denom_ort_cuba_int(d_hyp,hyp,d_denom,denom,pt2s)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(1), intent(out)::denom
    real(kind=double),intent(in) :: pt2s
    integer,intent(in)::d_hyp,d_denom
    denom(1)=denom_ort_save([hyp(1),hyp(2),pt2s])
  end subroutine denom_ort_cuba_int
denom param cuba int
  subroutine denom_param_cuba_int(d_hyp,hyp,d_denom,denom,pt2s)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(1), intent(out)::denom
    real(kind=double),intent(in) :: pt2s
    integer,intent(in)::d_hyp,d_denom
    denom(1)=denom_param_save([hyp(1),hyp(2),pt2s])
  end subroutine denom_param_cuba_int
denom smooth cuba int
```

```
subroutine denom_smooth_cuba_int(d_hyp,hyp,d_denom,denom,pt2s)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(1), intent(out)::denom
    real(kind=double),intent(in) :: pt2s
    integer, intent(in)::d_hyp,d_denom
    denom(1)=denom_smooth_save([hyp(1),hyp(2),pt2s])
  end subroutine denom_smooth_cuba_int
coordinates hcd cart
  subroutine coordinates_hcd_cart(hyp,cart,denom)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(3), intent(out)::cart
    real(kind=double),intent(out)::denom
    cart=hyp
    denom=denom_cart_save(cart)
  end subroutine coordinates_hcd_cart
coordinates hcd ort
  subroutine coordinates_hcd_ort(hyp,cart,denom)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double),dimension(3),intent(out)::cart
    real(kind=double),intent(out)::denom
    cart=h_to_c_ort(hyp)
    denom=denom_ort(hyp)
  end subroutine coordinates_hcd_ort
coordinates hcd param
  subroutine coordinates_hcd_param(hyp,cart,denom)
    real(kind=double),dimension(3),intent(in)::hyp
    real(kind=double), dimension(3), intent(out)::cart
    real(kind=double),intent(out)::denom
    cart=h_to_c_param(hyp)
    denom=denom_param(hyp)
  end subroutine coordinates_hcd_param
coordinates hcd param reg
  subroutine coordinates_hcd_param_reg(hyp,cart,denom)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(3), intent(out)::cart
    real(kind=double),intent(out)::denom
    cart=h_to_c_param(hyp)
    denom=denom_param_reg(hyp)
  end subroutine coordinates_hcd_param_reg
coordinates hcd smooth
  subroutine coordinates_hcd_smooth(hyp,cart,denom)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(3), intent(out)::cart
```

```
real(kind=double),intent(out)::denom
    cart=h_to_c_smooth(hyp)
    denom=denom_smooth(hyp)
  end subroutine coordinates_hcd_smooth
coordinates hcd smooth reg
  subroutine coordinates_hcd_smooth_reg(hyp,cart,denom)
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(3), intent(out)::cart
    real(kind=double),intent(out)::denom
    cart=h_to_c_smooth(hyp)
    denom=denom_smooth_reg(hyp)
  end subroutine coordinates_hcd_smooth_reg
pdf in in kind
 pure function pdf_in_in_kind(process_id,double_pdf_id,c1,c2,gev_pt)
    real(kind=double)::pdf_in_in_kind
    real(kind=double),intent(in)::c1,c2,gev_pt
    integer,intent(in)::process_id,double_pdf_id
    real(kind=double)::pdf1,pdf2
    call single_pdf(valid_processes(1,process_id),&
                    double_pdf_kinds(1,double_pdf_id),&
                    c1,&
                    gev_pt,&
                    pdf1)
    call single_pdf(valid_processes(2,process_id),&
                    double_pdf_kinds(2,double_pdf_id),&
                    c2,&
                    gev_pt,&
                    pdf2)
    pdf_in_in_kind=pdf1*pdf2
  contains
    pure subroutine single_pdf(flavor,pdf_kind,c,gev_pt,pdf)
      integer, intent(in)::flavor, pdf_kind
     real(kind=double),intent(in)::c,gev_pt
     real(kind=double),intent(out)::pdf
     real(kind=double),dimension(-6:6)::lha_pdf
     call evolvePDF(c,gev_pt,lha_pdf)
     select case(pdf_kind)
     case(1)
         pdf=lha_pdf(0)
     case(2)
         if(flavor==1.or.flavor==2)then
            pdf=lha_pdf(-flavor)
         else
            pdf=lha_pdf(flavor)
         end if
     case(3)
         pdf=lha_pdf(1)-lha_pdf(-1)
     case(4)
```

```
pdf=lha_pdf(2)-lha_pdf(-2)
      end select
    end subroutine single_pdf
  end function pdf_in_in_kind
ps io pol
  elemental function ps_io_pol(process_io_id,pt2shat)
    real(kind=double)::ps_io_pol
    integer,intent(in)::process_io_id
    real(kind=double),intent(in)::pt2shat
    ps_io_pol=dot_product(&
         [1D0,pt2shat,pt2shat**2,pt2shat**3]&
         ,phase_space_coefficients_inout(1:4,valid_processes(6,process_io_id)))
  end function ps_io_pol
interactions dddsigma
  pure subroutine interactions_dddsigma(process_id,double_pdf_id,hyp,cart,dddsigma)
    real(kind=double),intent(out)::dddsigma
    integer,intent(in)::process_id,double_pdf_id
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(3), intent(out)::cart
    real(kind=double)::a,pt2shat,gev_pt
    cart=h_to_c_param(hyp)
    a=product(cart(1:2))
    if(cart(1) \le 1D0.and.cart(2) \le 1D0)then
       pt2shat=hyp(3)/a
       gev_pt=sqrt(hyp(3))*gev_pt_max
!
        print *,process_id,pt2shat
       dddsigma=&
            &const_pref&
            &*alphasPDF(gev_pt)**2&
            &*ps_io_pol(process_id,pt2shat)&
            &*pdf_in_in_kind(process_id,double_pdf_id,cart(1),cart(2),gev_pt)&
            &*denom_param(hyp)&
            &/a
    else
       dddsigma=0D0
  end subroutine interactions_dddsigma
interactions dddsigma reg
  pure subroutine interactions_dddsigma_reg(process_id,double_pdf_id,hyp,cart,dddsigma)
    real(kind=double),intent(out)::dddsigma
    integer, intent(in)::process_id, double_pdf_id
    real(kind=double), dimension(3), intent(in)::hyp
    real(kind=double), dimension(3), intent(out)::cart
    real(kind=double)::a,pt2shat,gev_pt,gev2_pt
    cart=h_to_c_param(hyp)
    a=product(cart(1:2))
```

```
if(cart(1) \le 1D0.and.cart(2) \le 1D0)then
       pt2shat=hyp(3)/a
       gev_pt=sqrt(hyp(3))*gev_pt_max
       gev2_pt=hyp(3)*gev2_pt_max
        print *,process_id,pt2shat
       dddsigma=&
            &const_pref&
            &*alphasPDF(sqrt(gev2_pt+gev2_p_t_0))**2&
            &*ps_io_pol(process_id,pt2shat)&
            &*pdf_in_in_kind(process_id,double_pdf_id,cart(1),cart(2),gev_pt)&
            &*denom_param_reg(hyp)&
            &/a
    else
       dddsigma=0D0
    end if
  end subroutine interactions_dddsigma_reg
interactions dddsigma print
  subroutine interactions_dddsigma_print(process_id,double_pdf_id,hyp,cart,dddsigma)
    real(kind=double),intent(out)::dddsigma
    integer,intent(in)::process_id,double_pdf_id
    real(kind=double),dimension(3),intent(in)::hyp
    real(kind=double),dimension(3),intent(out)::cart
    real(kind=double)::a,pt2shat,gev_pt
    cart=h_to_c_param(hyp)
    a=product(cart(1:2))
    if(cart(1) \le 1D0.and.cart(2) \le 1D0)then
       pt2shat=hyp(3)/a
       gev_pt=sqrt(hyp(3))*gev_pt_max
!
        print *,process_id,pt2shat
       dddsigma=&
            &const_pref&
             &*alphasPDF(gev_pt)**2&
            &*ps_io_pol(process_id,pt2shat)&
            &*pdf_in_in_kind(process_id,double_pdf_id,cart(1),cart(2),gev_pt)&
            &*denom_param(hyp)&
            &/a
    else
       dddsigma=0D0
    end if
    write(11,fmt=*)dddsigma,pt2shat,&
         pdf_in_in_kind(process_id,double_pdf_id,cart(1),cart(2),&
         gev_pt),ps_io_pol(process_id,pt2shat),const_pref,denom_param(hyp),a
    flush(11)
  end subroutine interactions_dddsigma_print
interactions dddsigma cart
  pure subroutine interactions_dddsigma_cart(process_id,double_pdf_id,cart,dddsigma)
    real(kind=double),intent(out)::dddsigma
    integer,intent(in)::process_id,double_pdf_id
```

```
real(kind=double), dimension(3), intent(in)::cart
    real(kind=double)::a,pt2shat,gev_pt
    a=product(cart(1:2))
    if(cart(1) \le 1D0.and.cart(2) \le 1D0)then
       pt2shat=cart(3)/a
       gev_pt=sqrt(cart(3))*gev_pt_max
Ţ
        print *,process_id,pt2shat
       dddsigma=&
            &const_pref&
            &*alphasPDF(gev_pt)**2&
            &*ps_io_pol(process_id,pt2shat)&
            &*pdf_in_in_kind(process_id,double_pdf_id,cart(1),cart(2),gev_pt)&
            &*denom_cart(cart)&
            &/a
    else
       dddsigma=0D0
    end if
  end subroutine interactions_dddsigma_cart
cuba gg me smooth
  subroutine cuba_gg_me_smooth(d_hyp,hyp,d_me,me,pt2s)
    integer, intent(in)::d_hyp,d_me
    real(kind=double), dimension(d_hyp), intent(in)::hyp
    real(kind=double),dimension(1),intent(out)::me
    real(kind=double),dimension(3)::cart
    real(kind=double),intent(in)::pt2s
    real(kind=double)::p,p2
    if(d_hyp==3)then
       p=hyp(3)
       p2=hyp(3)**2
    else
       if (d_hyp==2)then
          p=sqrt(pt2s)
          p2=pt2s
       end if
    end if
    cart=h_to_c_smooth([hyp(1),hyp(2),p2])
    if(p>pts_min.and.product(cart(1:2))>p2)then
       me(1)=&
            &const_pref&
            &*alphasPDF(p*gev_pt_max)**2&
            &*ps_io_pol(109,p2)&
            &*pdf_in_in_kind(109,11,cart(1),cart(2),p2)&
            &*denom_smooth([hyp(1),hyp(2),p2])&
            &/product(cart(1:2))
    else
       me(1) = ODO
    end if
  end subroutine cuba_gg_me_smooth
cuba gg me param
```

```
subroutine cuba_gg_me_param(d_hyp,hyp,d_me,me,pt2s)
    integer,intent(in)::d_hyp,d_me
    real(kind=double),dimension(d_hyp),intent(in)::hyp
    real(kind=double), dimension(1), intent(out)::me
    real(kind=double),dimension(3)::cart
    real(kind=double),intent(in)::pt2s
    real(kind=double)::p,p2
    if(d_hyp==3)then
       p=hyp(3)
      p2=hyp(3)**2
    else
       if(d_hyp==2)then
          p=sqrt(pt2s)
          p2=pt2s
       end if
    end if
    cart=h_to_c_param([hyp(1),hyp(2),p2])
    if(p>pts_min.and.product(cart(1:2))>p2)then
      me(1)=&
            &const_pref&
            &*alphasPDF(p*gev_pt_max)**2&
            &*ps_io_pol(109,p2)&
            &*pdf_in_in_kind(109,11,cart(1),cart(2),p2)&
            &*denom_param([hyp(1),hyp(2),p2])&
            &/product(cart(1:2))
    else
      me(1)=ODO
    end if
  end subroutine cuba_gg_me_param
cuba gg me ort
  subroutine cuba_gg_me_ort(d_hyp,hyp,d_me,me,pt2s)
    integer,intent(in)::d_hyp,d_me
    real(kind=double), dimension(d_hyp), intent(in)::hyp
    real(kind=double), dimension(1), intent(out)::me
    real(kind=double),dimension(3)::cart
    real(kind=double),intent(in)::pt2s
    real(kind=double)::p,p2
    if(d_hyp==3)then
       p=hyp(3)
      p2=hyp(3)**2
    else
       if(d_hyp==2)then
          p=sqrt(pt2s)
          p2=pt2s
       end if
    end if
    cart=h_to_c_ort([hyp(1),cart(2),p2])
    if(p>pts_min.and.product(cart(1:2))>p2)then
      me(1)=&
```

```
&const_pref&
            &*alphasPDF(p*gev_pt_max)**2&
            &*ps_io_pol(109,p2)&
            &*pdf_in_in_kind(109,11,cart(1),cart(2),p2)&
            &*denom_ort([hyp(1),hyp(2),p2])&
            &/product(cart(1:2))
    else
       me(1)=ODO
    end if
  end subroutine cuba_gg_me_ort
cuba_gg me cart
  subroutine cuba_gg_me_cart(d_cart,cart,d_me,me,pt2s)
    integer, intent(in)::d_cart,d_me
    real(kind=double),dimension(d_cart),intent(in)::cart
    real(kind=double), dimension(1), intent(out)::me
    real(kind=double),intent(in)::pt2s
    real(kind=double)::a,p,p2
    if(d_cart==3)then
       p=cart(3)
       p2=cart(3)**2
    else
       if(d_cart==2)then
          p=sqrt(pt2s)
          p2=pt2s
       end if
    end if
    a=product(cart(1:2))
    if(p>pts_min.and.a>p2)then
       me(1)=&
            &const_pref&
            &*alphasPDF(p*gev_pt_max)**2&
            &*ps_io_pol(109,p2)&
            &*pdf_in_in_kind(109,11,cart(1),cart(2),p2)&
            &*denom_cart([cart(1),cart(2),p2])&
            &/a
    else
       me(1)=0D0
    end if
  end subroutine cuba_gg_me_cart
interactions proton proton integrand generic 17 reg
  subroutine interactions_proton_proton_integrand_generic_17_reg(hyp_2,trafo,f,pt)
    real(kind=double), dimension(2), intent(in)::hyp_2
    procedure(coord_hcd_in)::trafo
    real(kind=double), dimension(17), intent(out)::f
    class(transversal_momentum_type), intent(in) :: pt
    real(kind=double), dimension(3)::cart, hyp_3
    real(kind=double), dimension(5)::psin
    real(kind=double),dimension(-6:6)::c,d
```

```
real(kind=double)::gev_pt,gev2_pt,pts,pt2s,pt2shat,a,&
              pdf_seaquark_seaquark,pdf_seaquark_gluon,pdf_gluon_gluon,&
              pdf_up_seaquark,pdf_up_gluon,pdf_down_seaquark,pdf_down_gluon,&
              v1u, v1d, v2u, v2d, denom
pts=pt%get_unit_scale()
pt2s=pt%get_unit2_scale()
gev_pt=pt%get_gev_scale()
gev2_pt=pt%get_gev2_scale()
hyp_3(1:2)=hyp_2
hyp_3(3)=pt2s
call trafo(hyp_3,cart,denom)
a=product(cart(1:2))
if(cart(1) \le 1D0.and.cart(2) \le 1D0.and.a > pt2s)then
        pt2shat=pt2s/a
         ! phase space polynom
         psin=matmul([1D0,pt2shat,pt2shat**2,pt2shat**3],phase_space_coefficients_in)
         ! pdf
         call evolvepdf(cart(1),gev_pt,c)
         call evolvepdf(cart(2),gev_pt,d)
         !c=[1,1,1,1,1,1,1,1,1,1,1,1,1]*1D0
         !d=c
        v1d=c(1)-c(-1)
         v1u=c(2)-c(-2)
        v2d=d(1)-d(-1)
         v2u=d(2)-d(-2)
        c(1)=c(-1)
        c(2)=c(-2)
        d(1)=d(-1)
        d(2)=d(-2)
        f(1) = 0D0
         !gluon_gluon
         f(2)=(&
                        !type5
                        c(0)*d(0)&
                        )*psin(5)
         !gluon_seaquark
         f(3)=(&
                        c(0)*d(-4)+c(0)*d(-3)+c(0)*d(-2)+c(0)*d(-1)+c(0)*d(1)+c(0)*d(2)+c(0)*d(3)+c(0)*d(4)\& \\ c(0)*d(-4)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)+c(0)*d(-3)
                        )*psin(4)
         !gluon_down
         f(4)=(&
                        !type4
                        c(0)*v2d&
                        )*psin(4)
         !gluon_up
         f(5)=(&
                        !type4
```

```
c(0)*v2u&
                           )*psin(4)
 !seaquark_gluon
f(6)=(&
                            !type4
                          c(-4)*d(0)+c(-3)*d(0)+c(-2)*d(0)+c(-1)*d(0)&
                          +c(1)*d(0)+c(2)*d(0)+c(3)*d(0)+c(4)*d(0)&
                          )*psin(4)
 !seaquark_seaquark
f(7)=&
                            !type1
                            (c(-4)*d(-3)+c(-4)*d(-2)+c(-4)*d(-1)+c(-4)*d(-1)+c(-4)*d(-2)+c(-4)*d(-3)+&
                                c(-3)*d(-4)+c(-3)*d(-2)+c(-3)*d(-1)+c(-3)*d(-1)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3)*d(-2)+c(-3
                                c(-2)*d(-4)+c(-2)*d(-3)+c(-2)*d(-1)+c(-2)*d(-1)+c(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2)*d(-2
                                c(-1)*d(-4)+c(-1)*d(-3)+c(-1)*d(-2)+c(-1)*d(-2)+c(-1)*d(-3)+c(-1)*d(-4)+&
                                 \verb|c(1)*d(-4)+c(1)*d(-3)+c(1)*d(-2)+c(1)*d(2)+c(1)*d(3)+c(1)*d(4)+& \\
                                c(2)*d(-4)+c(2)*d(-3)+c(2)*d(-1)+c(2)*d(1)+c(2)*d(3)+c(2)*d(4)+&
                                c(3)*d(-4)+c(3)*d(-2)+c(3)*d(-1)+c(3)*d(1)+c(3)*d(2)+c(3)*d(4)+&
                                c(4)*d(-3)+c(4)*d(-2)+c(4)*d(-1)+c(4)*d(1)+c(4)*d(2)+c(4)*d(3))&
                                *psin(1)&
                            !type2
                                +(c(-4)*d(-4)+c(-3)*d(-3)+c(-2)*d(-2)+c(-1)*d(-1)&
                                           +c(4)*d(4)+c(3)*d(3)+c(2)*d(2)+c(1)*d(1))&
                                *psin(2)&
                                !type3
                                +(c(-4)*d(4)+c(-3)*d(3)+c(-2)*d(2)+c(-1)*d(1)&
                                           +c(4)*d(-4)+c(3)*d(-3)+c(2)*d(-2)+c(1)*d(-1))&
                                *psin(3)
 !seaquark_down
f(8)=&
                            (c(-4)*v2d+c(-3)*v2d+c(-2)*v2d+c(2)*v2d+c(3)*v2d+c(4)*v2d)&
                           *psin(1)&
                            !type2
                          +c(1)*v2d&
                          *psin(2)&
                            !type3
                          +c(-1)*v2d&
                           *psin(3)
 !seaquark_up
f(9)=&
                            !type1
                            (c(-4)*v2u+c(-3)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-1)*v2u+c(-
                            *psin(1)&
                            !type2
                          +c(2)*v2u&
                           *psin(2)&
                            !type3
                          +c(-2)*v2u&
                          *psin(3)
 !down_gluon
```

```
f(10) = (&
         !type4
         v1d*d(0)&
         )*psin(4)
     !down_seaquark
    f(11)=&
         !type1
         (v1d*d(-4)+v1d*d(-3)+v1d*d(-2)+v1d*d(-2)+v1d*d(-3)+v1d*d(-4))&
         *psin(1)&
         !type2
         +v1d*d(1)&
         *psin(2)&
         !type3
         +v1d*d(-1)&
         *psin(3)
     !down_down
    f(12)=v1d*v2d*psin(2)
    !down_up
    f(13)=v1d*v2u*psin(1)
    !up_gluon
    f(14) = (&
         !type4
         &v1u*d(0)&
         &)*psin(4)
     !up_seaquark
    f(15)=&
         !type1
         (v1u*d(-4)+v1u*d(-3)+v1u*d(-1)+v1u*d(-1)+v1u*d(-3)+v1u*d(-4))&
         *psin(1)&
         !type2
         +v1u*d(2)&
         *psin(2)&
         !type3
         +v1u*d(-2)&
         *psin(3)
    !up_down
    f(16)=v1u*v2d*psin(1)
    !up_up
    f(17)=v1u*v2u*psin(2)
    f=f&
    *const_pref&
         *alphasPDF(sqrt(gev2_pt+gev2_p_t_0))**2&
         *denom&
         /a
     !
            print *,const_pref,alphasPDF(gev_pt)**2,denom_smooth(hyp),a
  else
    end if
  print *,pt2shat,c(0)*d(0),psin(5),const_pref,alphasPDF(gev_pt)**2,denom,a
end subroutine interactions_proton_proton_integrand_generic_17_reg
```

```
interactions proton proton integrand param 17 reg
  subroutine interactions_proton_proton_integrand_param_17_reg(d_hyp,hyp_2,d_f,f,pt)
    integer,intent(in)::d_hyp,d_f
    real(kind=double), dimension(2), intent(in)::hyp_2
    real(kind=double), dimension(17), intent(out)::f
    class(transversal_momentum_type), intent(in) :: pt
    call interactions_proton_proton_integrand_generic_17_reg&
      (hyp_2,coordinates_hcd_param_reg,f,pt)
         write (53,*)hyp_2,momentum_get_pts_scale(),f
  end subroutine interactions_proton_proton_integrand_param_17_reg
interactions proton proton integrand smooth 17 reg
  subroutine interactions_proton_proton_integrand_smooth_17_reg(d_hyp,hyp_2,d_f,f,pt)
    integer,intent(in)::d_hyp,d_f
    real(kind=double), dimension(2), intent(in)::hyp_2
    real(kind=double),dimension(17),intent(out)::f
    class(transversal_momentum_type), intent(in) :: pt
    call interactions_proton_proton_integrand_generic_17_reg&
      (hyp_2,coordinates_hcd_smooth_reg,f,pt)
         write (53,*)hyp_2,momentum_get_pts_scale(),f
  end subroutine interactions_proton_proton_integrand_smooth_17_reg
```

# 11 Modul muli mcint

# 11.1 Abhängigkeiten

```
use muli_basic
use tao_random_numbers !NODEP!
use muli_interactions
```

## 11.2 Parameter

```
integer,private,parameter::max_n=2**30
real(kind=double),private,parameter::max_d=1D0*max_n
real(kind=double),private,parameter,dimension(2,2)::unit_square=reshape([0D0,0D0,1D0,1D0],[2,2])
```

# 11.3 Derived Types

## 11.3.1 sample region type

```
type, extends(serializable_class)::sample_region_type
   integer::n_hits=0
   integer::n_alloc=0
   real(kind=double), dimension(2,2)::corners=unit_square
  real(kind=double),dimension(:,:),allocatable::hyp_hits
contains
   !Überschriebene serializable_class Methoden
   procedure ::write_to_marker=>sample_region_write_to_marker
   procedure ::read_from_marker=>sample_region_read_from_marker
   procedure ::print_to_unit=>sample_region_print_to_unit
  procedure,nopass ::get_type=>sample_region_get_type
   !Originare sample_region_type Methoden
  procedure ::initialize=>sample_region_initialize
   procedure ::generate_hit=>sample_region_generate_hit
  procedure ::confirm_hit=>sample_region_confirm_hit
   procedure ::split=>sample_region_split
   procedure ::write_hits=>sample_region_write_hits
  procedure ::is_full=>sample_region_is_full
  procedure ::move_components=>sample_region_move_components
  procedure ::mean=>sample_region_mean
   procedure ::area=>sample_region_area
   procedure ::density=>sample_region_density
```

```
procedure ::contains=>sample_region_contains
  procedure ::to_generator=>sample_region_to_generator
end type sample_region_type
```

## 11.3.2 sample 2d type

```
type, extends (serializable_class)::sample_2d_type
   integer::n_regions=0
   integer::n_alloc=0
   integer::n_hits=0
  real(kind=double),dimension(2)::range=[0,1]
  type(sample_region_type),dimension(:),allocatable::regions
 contains
   !Überschriebene serializable_class Methoden
  procedure ::write_to_marker=>sample_2d_write_to_marker
  procedure ::read_from_marker=>sample_2d_read_from_marker
  procedure ::print_to_unit=>sample_2d_print_to_unit
  procedure,nopass ::get_type=>sample_2d_get_type
   !Originäre sample_2d_type Methoden
  procedure ::initialize=>sample_2d_initialize
  procedure ::contains=>sample_2d_contains
  procedure ::generate_hit=>sample_2d_generate_hit
  procedure ::confirm_hit=>sample_2d_confirm_hit
  procedure ::split=>sample_2d_split
  procedure ::push=>sample_2d_push
  procedure ::write_hits=>sample_2d_write_hits
  procedure ::is_full=>sample_2d_is_full
  procedure ::move_components=>sample_2d_move_components
  procedure ::thickness=>sample_2d_thickness
  procedure ::analyse=>sample_2d_analyse
  procedure ::to_generator=>sample_2d_to_generator
   procedure ::mean=>sample_2d_mean
end type sample_2d_type
```

#### 11.3.3 sample 3d type

```
type,extends(serializable_class)::sample_3d_type
  integer::n_slices=0
  integer::n_alloc=0
  type(sample_2d_type),dimension(:),allocatable::slices
contains
  !Überschriebene serializable_class Methoden
  procedure ::write_to_marker=>sample_3d_write_to_marker
  procedure ::read_from_marker=>sample_3d_read_from_marker
  procedure ::print_to_unit=>sample_3d_print_to_unit
  procedure,nopass ::get_type=>sample_3d_get_type
  ! overridden measurable_class procedures
  procedure ::measure=>sample_3d_measure
  !Originäre sample_3d_type Methoden
```

```
procedure ::to_generator=>sample_3d_to_generator
procedure :: sample_3d_initialize
procedure :: sample_3d_generate_hit
procedure :: sample_3d_confirm_hit
procedure ::enlarge=>sample_3d_enlarge
generic::initialize=>sample_3d_initialize
generic::generate_hit=>sample_3d_generate_hit
generic::confirm_hit=>sample_3d_confirm_hit
end type sample_3d_type
```

## 11.3.4 sample int kind type

```
type, extends(sample_3d_type)::sample_int_kind_type
   integer::n_proc=0
   integer(kind=i64)::n_tries=0
   integer::n_hits=0
   integer::n_over=0
   integer,dimension(:),allocatable::hits,weights,processes
  real(kind=double)::overall_boost=1D-1
   !Überschriebene serializable_class Methoden
   procedure ::write_to_marker=>sample_int_kind_write_to_marker
   procedure ::read_from_marker=>sample_int_kind_read_from_marker
  procedure ::print_to_unit=>sample_int_kind_print_to_unit
   procedure,nopass ::get_type=>sample_int_kind_get_type
   ! overridden sample_3d_type procedures
   procedure ::to_generator=>sample_int_kind_to_generator
   !Originare sample_int_kind_type Methoden
   procedure ::process_id=>sample_int_kind_process_id
   procedure :: sample_int_kind_initialize
  procedure :: sample_int_kind_generate_hit
   procedure ::mcgenerate_hit=>sample_int_kind_mcgenerate_hit
   procedure :: sample_int_kind_confirm_hit
  procedure ::analyse=>sample_int_kind_analyse
   generic::initialize=>sample_int_kind_initialize
  generic::generate_hit=>sample_int_kind_generate_hit
   generic::confirm_hit=>sample_int_kind_confirm_hit
end type sample_int_kind_type
```

## 11.3.5 sample\_inclusive\_type

```
type,extends(serializable_class)::sample_inclusive_type
   integer::n_alloc=0
   integer(kind=i64)::n_tries_sum=zero
   integer(kind=i64)::n_over_sum=zero
   integer(kind=i64)::n_hits_sum=zero
   type(sample_int_kind_type),dimension(:),allocatable::int_kinds
   contains
   !Überschriebene serializable_class Methoden
```

```
procedure ::write_to_marker=>sample_inclusive_write_to_marker
  procedure ::read_from_marker=>sample_inclusive_read_from_marker
  procedure ::print_to_unit=>sample_inclusive_print_to_unit
  procedure,nopass ::get_type=>sample_inclusive_get_type
   !Originare sample_inclusive_type Methoden
  procedure ::process_id=>sample_inclusive_process_id
  procedure ::initialize=>sample_inclusive_initialize
  procedure ::finalize=>sample_inclusive_finalize
  procedure ::generate_hit=>sample_inclusive_generate_hit
  procedure ::mcgenerate_hit=>sample_inclusive_mcgenerate_hit
  procedure ::confirm_hit=>sample_inclusive_confirm_hit
  procedure ::sum_up=>sample_inclusive_sum_up
  procedure ::analyse=>sample_inclusive_analyse
  procedure ::to_generator=>sample_inclusive_to_generator
  procedure ::allocate=>sample_inclusive_allocate
end type sample_inclusive_type
```

# 11.4 Implementierung der Prozeduren

### 11.4.1 Methoden für sample region type

```
sample region write to marker \( \)
  subroutine sample_region_write_to_marker(this,marker,status)
    class(sample_region_type),intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    integer::n
    call marker%mark_begin("sample_region_type")
    call marker%mark("n_hits",this%n_hits)
    call marker%mark("n_alloc",this%n_alloc)
    call marker%mark("lower_corner",this%corners(1:2,1))
    call marker%mark("upper_corner",this%corners(1:2,2))
    if(allocated(this%hyp_hits))then
       call marker%mark("hyp_hits",this%hyp_hits(1:3,:this%n_hits))
    else
       call marker%mark_nothing("hyp_hits")
    end if
    call marker%mark_end("sample_region_type")
  end subroutine sample_region_write_to_marker
sample region read from marker \( \ \)
  subroutine sample_region_read_from_marker(this,marker,status)
    class(sample_region_type),intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    integer::n
    call marker%pick_begin("sample_region_type",status=status)
    call marker%pick("n_hits",this%n_hits,status)
```

```
call marker%pick("n_alloc",this%n_alloc,status)
    call marker%pick("lower_corner",this%corners(1:2,1),status)
    call marker%pick("upper_corner",this%corners(1:2,2),status)
    if(allocated(this%hyp_hits))deallocate(this%hyp_hits)
    call marker%verify_nothing("hyp_hits",status)
    if(.not.status==serialize_nothing)then
       allocate(this%hyp_hits(3,this%n_alloc))
       call marker%pick("hyp_hits",this%hyp_hits(1:3,:this%n_hits),status)
    end if
    call marker%pick_end("sample_region_type",status)
  end subroutine sample_region_read_from_marker
sample region print to unit \( \ext{\gamma} \)
 subroutine sample_region_print_to_unit(this,unit,parents,components,peers)
    class(sample_region_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    write(unit,fmt=*)"components of sample_region_type"
   write(unit,'("n_hits:
                                    ",i10)')this%n_hits
   write(unit,'("n_alloc:
                                    ",i10)')this%n_alloc
    write(unit,'("corners:
                                    ",4(e20.10))')this%corners
    if(allocated(this%hyp_hits).and.this%n_hits>0)then
       if(components>0)then
          write(unit,'("hits:")')
          print *,shape(this%hyp_hits)
          write(unit,fmt='(3(e20.10))')this%hyp_hits(1:3,this%n_hits)
          write(unit,fmt=*)"skipping hits."
       end if
    else
       write(unit,fmt=*)"hits are not allocated."
  end subroutine sample_region_print_to_unit
sample region get type \( \ \)
 pure subroutine sample_region_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="sample_region_type")
  end subroutine sample_region_get_type
sample region initialize \( \)
  subroutine sample_region_initialize(this,n_alloc)
    class(sample_region_type),intent(out)::this
    integer,intent(in)::n_alloc
    if(allocated(this%hyp_hits))deallocate(this%hyp_hits)
    allocate(this%hyp_hits(3,n_alloc))
    this%n_alloc=n_alloc
  end subroutine sample_region_initialize
sample region generate hit \( \ \)
```

```
pure subroutine sample_region_generate_hit(this,rnd,area,hit)
    class(sample_region_type),intent(in)::this
    integer,intent(in),dimension(2)::rnd
    real(kind=double), dimension(2), intent(out)::hit
    real(kind=double),intent(out)::area
    call muli_mcint_generate_hit(rnd, this%corners, hit)
    area=this%area()
  end subroutine sample_region_generate_hit
sample region confirm hit \uparrow
  subroutine sample_region_confirm_hit(this,hit)
    class(sample_region_type),intent(inout)::this
    real(kind=double), dimension(3), intent(in)::hit
    print *,"sample_region_confirm_hit: ",this%n_hits,this%n_alloc,hit
    this%n_hits=this%n_hits+1
    if(this%n_hits<=this%n_alloc)then
       this%hyp_hits(1:3,this%n_hits)=hit
    else
       print *,"sample_region_confirm_hit: Region is already full."
  end subroutine sample_region_confirm_hit
sample region split \( \ \)
  subroutine sample_region_split(this,pos,dimX,n_alloc,lower,upper)
    class(sample_region_type),intent(in)::this
    type(sample_region_type),intent(out)::lower,upper
    real(kind=double), dimension(3)::hit
    real(kind=double),intent(in)::pos
    integer,intent(in)::dimX,n_alloc
    integer::n_hit
    call lower%initialize(n_alloc)
    call upper%initialize(n_alloc)
    do n_hit=1,this%n_hits
       hit=this%hyp_hits(1:3,n_hit)
       if(hit(dimX)<pos)then
          call lower%confirm_hit(hit)
       else
          call upper%confirm_hit(hit)
       end if
    end do
    lower%corners=this%corners
    upper%corners=this%corners
    if(dimX<3)then
       lower%corners(dimX,2)=pos
       upper%corners(dimX,1)=pos
    end if
  end subroutine sample_region_split
sample region write hits \
```

```
subroutine sample_region_write_hits(this,unit)
    class(sample_region_type),intent(in)::this
    integer, intent(in)::unit
    integer::n
    do n=1,this%n_hits
       write(unit,fmt=*)this%hyp_hits(1:3,n)
    end do
  end subroutine sample_region_write_hits
sample region is full \( \ \)
  elemental logical function sample_region_is_full(this)
    class(sample_region_type),intent(in)::this
    sample_region_is_full=this%n_alloc==this%n_hits
  end function sample_region_is_full
sample region move components \
  subroutine sample_region_move_components(this,that)
    class(sample_region_type),intent(inout)::this
    class(sample_region_type),intent(out)::that
    that%n_alloc=this%n_alloc
    that%n_hits=this%n_hits
    that%corners=this%corners
    call move_alloc(this%hyp_hits,that%hyp_hits)
    this%n_alloc=0
    this%n hits=0
  end subroutine sample_region_move_components
sample region mean \( \)
  elemental function sample_region_mean(this,dim)
    real(kind=double)::sample_region_mean
    class(sample_region_type),intent(in)::this
    integer, intent(in)::dim
    sample_region_mean=sum(this%hyp_hits(dim,1:this%n_hits))/this%n_hits
  end function sample_region_mean
sample region area \( \)
  elemental function sample_region_area(this)
    real(kind=double)::sample_region_area
    class(sample_region_type),intent(in)::this
    sample_region_area=product(this%corners(1:2,2)-this%corners(1:2,1))
  end function sample_region_area
sample region density \( \ \)
  elemental function sample_region_density(this)
    real(kind=double)::sample_region_density
    class(sample_region_type),intent(in)::this
    sample_region_density=this%n_hits/this%area()
  end function sample_region_density
```

```
sample region contains \( \ \)
  pure logical function sample_region_contains(this,hit)
    class(sample_region_type),intent(in)::this
    real(kind=double),intent(in),dimension(3)::hit
    sample_region_contains=(this%corners(1,1)<=hit(1)&</pre>
         .and.hit(1) <= this%corners(1,2)&
         .and.this%corners(2,1)<=hit(2)&
         .and.hit(2)<=this%corners(2,2))
  end function sample_region_contains
sample region to generator \( \)
  subroutine sample_region_to_generator(this)
    class(sample_region_type),intent(inout)::this
    if(allocated(this%hyp_hits))deallocate(this%hyp_hits)
    this%n_alloc=0
  end subroutine sample_region_to_generator
11.4.2 Methoden für sample 2d type
sample 2d write to marker \( \ \)
  subroutine sample_2d_write_to_marker(this,marker,status)
    class(sample_2d_type),intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    integer::n
    call marker%mark_begin("sample_2d_type")
    call marker%mark("n_regions",this%n_regions)
    call marker%mark("n_alloc",this%n_alloc)
    call marker%mark("n_hits",this%n_hits)
    call marker%mark("range",this%range)
    if(this%n_regions>0)then
       call marker%mark_instance_begin(this%regions(1),name="sample_2d_type",shape=shape(this
       do n=1,this%n_regions
          call sample_region_write_to_marker(this%regions(n),marker,status)
       end do
       call marker%mark_instance_end()
    end if
    call marker%mark_end("sample_2d_type")
  end subroutine sample_2d_write_to_marker
sample 2d read from marker \uparrow
  subroutine sample_2d_read_from_marker(this,marker,status)
    class(sample_2d_type),intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    integer::n
    call marker%pick_begin("sample_2d_type",status=status)
```

```
call marker%pick("n_regions",this%n_regions,status)
    call marker%pick("n_alloc",this%n_alloc,status)
    call marker%pick("n_hits",this%n_hits,status)
    call marker%pick("range",this%range,status)
    if(this%n_regions>0)then
       call marker%pick_begin("regions",status=status)
       allocate(this%regions(this%n_regions))
       do n=1,this%n_regions
          call sample_region_read_from_marker(this%regions(n),marker,status)
       call marker%pick_end("regions", status)
    end if
    call marker%pick_end("sample_2d_type",status)
  end subroutine sample_2d_read_from_marker
sample 2d print to unit \( \ \)
  subroutine sample_2d_print_to_unit(this,unit,parents,components,peers)
    class(sample_2d_type),intent(in)::this
    integer,intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    integer::n
    write(unit,fmt=*)"components of sample_2d_type"
    write(unit,'("n_regions:
                                     ",i10)')this%n_regions
    write(unit,'("n_alloc:
                                     ",i10)')this%n_alloc
                                     ",2(e20.10))')this%range
    write(unit,'("range:
    if(allocated(this%regions))then
       if(components>0)then
          write(unit,'("regions:")')
          do n=1,this%n_regions
             call this%regions(n)%print_to_unit(unit, parents, components-1, peers)
          end do
          write(unit,fmt=*)"skipping regions."
       end if
    else
       write(unit,fmt=*)"regions are not allocated."
  end subroutine sample_2d_print_to_unit
sample 2d get type \uparrow
  pure subroutine sample_2d_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="sample_2d_type")
  end subroutine sample_2d_get_type
sample 2d initialize \( \ \)
  subroutine sample_2d_initialize(this,n_alloc)
    class(sample_2d_type),intent(out)::this
    integer,intent(in)::n_alloc
```

```
integer::n
    if(allocated(this%regions))deallocate(this%regions)
    allocate(this%regions(n_alloc))
    this%n_alloc=n_alloc
    this%n_regions=1
    call this%regions(1)%initialize(n_alloc)
!
    do n=1,n_alloc
!
        call this%regions(n)%initialize(n_alloc)
     end do
  end subroutine sample_2d_initialize
sample\_2d contains \uparrow
  pure logical function sample_2d_contains(this,pts2)
    class(sample_2d_type),intent(in)::this
    real(kind=double),intent(in)::pts2
    sample_2d_contains=this%range(1)<=pts2.and.pts2<=this%range(2)</pre>
  end function sample_2d_contains
sample 2d generate hit \uparrow
  pure subroutine sample_2d_generate_hit(this,rnd,boost,hit,region)
    class(sample_2d_type),intent(in)::this
    integer, dimension(3), intent(in)::rnd
    integer,intent(out)::region
    integer::n,sum
    real(kind=double), dimension(2), intent(out)::hit
    real(kind=double),intent(out)::boost
    if(0<this%n_hits.and.this%n_hits<10)then
       sum=modulo(rnd(1),this%n_hits)+1!this should be improved
       region=0
       do while(sum>0)
          region=region+1
          sum=sum-this%regions(region)%n_hits
       end do
       call this%regions(region)%generate_hit(rnd(2:3),boost,hit)
       boost=boost*this%n_hits/this%regions(region)%n_hits
    else
       if(this%n_regions>1)then
          region=modulo(rnd(1),this%n_regions)+1!this should be improved
          call this%regions(region)%generate_hit(rnd(2:3),boost,hit)
          boost=boost*this%n_regions
       else
          region=1
          call this%regions(1)%generate_hit(rnd(2:3),boost,hit)
       end if
    end if
  end subroutine sample_2d_generate_hit
sample 2d confirm hit \
```

```
subroutine sample_2d_confirm_hit(this,hit,region,full)
    class(sample_2d_type),intent(inout)::this
    integer,intent(in)::region
    real(kind=double), dimension(3), intent(in)::hit
    type(sample_region_type),allocatable::old_region
    real(kind=double), dimension(2)::mean, var, diff, cm, cv, c
    integer::n,n_alloc,dim
    logical,intent(out)::full
    this%n_hits=this%n_hits+1
    if(region<=this%n_alloc)then
       full=.false.
       call this%regions(region)%confirm_hit(hit)
       n_alloc=this%regions(region)%n_alloc
       if(this%regions(region)%is_full())then
          if(this%is_full())then
             full=.true.
          else
             this%n_regions=this%n_regions+1
             allocate(old_region)
             call this%regions(region)%move_components(old_region)
             mean=sum(old_region%hyp_hits(1:2,:),dim=2)/n_alloc
             var=0D0
             do n=1,n_alloc
                var=var+abs(mean-old_region%hyp_hits(1:2,n))
             end do
             var=var/n_alloc
             diff=old_region%corners(1:2,2)-old_region%corners(1:2,1)
             cm=abs([0.5D0,0.5D0]-(old_region\%corners(1:2,2)-mean)/diff)
             cv=abs(2*([0.25D0,0.25D0]-var/diff))
             c=max(cm,cv)
             if(c(1) < c(2))then
                dim=2
             else
                dim=1
             end if
             call old_region%split(&
               mean(dim),&
               dim,&
               this%n alloc,&
               this%regions(region),&
               this%regions(this%n_regions))
          end if
       end if
    else
       print *,"sample_2d_confirm_hit: Region ",region," not allocated."
  end subroutine sample_2d_confirm_hit
sample 2d is full \( \ \)
```

```
elemental logical function sample_2d_is_full(this)
    class(sample_2d_type),intent(in)::this
    sample_2d_is_full=this%n_alloc==this%n_regions
  end function sample_2d_is_full
sample 2d split \
  recursive subroutine sample_2d_split(this,n_alloc,pos,lower,upper)
    class(sample_2d_type),intent(in)::this
    integer,intent(in)::n_alloc
    real(kind=double),intent(in)::pos
    type(sample_2d_type),intent(out)::lower,upper
    integer::n_r,n_h
    real(kind=double), dimension(3)::hit
    !print *, "sample_2d_split: ", pos, this % range
    call lower%initialize(4*n_alloc)
    call upper%initialize(4*n_alloc)
    do n_r=this%n_regions,1,-1
       do n_h=1,this%regions(n_r)%n_hits
          hit=this%regions(n_r)%hyp_hits(1:3,n_h)
          if(hit(3)>pos)then
             call upper%push(hit)
          else
             call lower%push(hit)
          end if
       end do
    end do
    lower%range=[this%range(1),pos]
    upper%range=[pos,this%range(2)]
  end subroutine sample_2d_split
sample 2d push \uparrow
  subroutine sample_2d_push(this,hit)
    class(sample_2d_type),intent(inout)::this
    real(kind=double), dimension(3), intent(in)::hit
    integer::region
    logical::full
    do region=1,this%n_regions
       if (this%regions(region)%contains(hit))then
          call this%confirm_hit(hit,region,full)
           call this%regions(region)%confirm_hit(hit)
!
          if(full)print *,"sample_2d_push: region is full now"
          exit
       end if
    end do
    if(region>this%n_regions)print *,"sample_2d_push: no region contains ",hit
  end subroutine sample_2d_push
sample 2d write hits \( \ \)
```

```
subroutine sample_2d_write_hits(this,unit)
    class(sample_2d_type),intent(in)::this
    integer, intent(in)::unit
    integer::n
    do n=1,this%n_regions
       call this%regions(n)%write_hits(unit)
    end do
  end subroutine sample_2d_write_hits
sample 2d move components \( \ \)
  subroutine sample_2d_move_components(this,that)
    class(sample_2d_type),intent(inout)::this
    class(sample_2d_type),intent(out)::that
    that%n_alloc=this%n_alloc
    that%n_regions=this%n_regions
    that%n_hits=this%n_hits
    that%range=this%range
    call move_alloc(this%regions,that%regions)
    this%n_alloc=0
    this%n_regions=0
    this%n_hits=0
    this%range=[0D0,0D0]
  end subroutine sample_2d_move_components
sample 2d thickness \uparrow
  elemental function sample_2d_thickness(this)
    class(sample_2d_type),intent(in)::this
    real(kind=double)::sample_2d_thickness
    sample_2d_thickness=this%range(2)-this%range(1)
  end function sample_2d_thickness
sample 2d analyse \uparrow
  subroutine sample_2d_analyse(this,dir,file)
    class(sample_2d_type),intent(in)::this
    character(*),intent(in)::dir,file
    integer::u
    real(kind=double), dimension(1:2,0:100,0:100)::grid
    integer, dimension(0:100,0:100)::i_grid
    integer::r,x,y
    integer, dimension(2,2)::i
    call generate_unit(u)
    print *,"sample_2d_analyse: ",dir//"/"/file
    open(u,file=dir//"/"//file)
    do x=0,100
       do y=0,100
          grid(1:2,x,y)=[-1D0,-1D0]
       end do
    end do
    do r=1,this%n_regions
```

```
i=int(this%regions(r)%corners*1D2)
       do x=i(1,1),i(1,2)
          do y=i(2,1),i(2,2)
             i_grid(x,y)=this%regions(r)%n_hits
             grid(1,x,y)=1D0/this%regions(r)%area()
             grid(2,x,y)=this%regions(r)%density()
          end do
       end do
    end do
    do x=0,100
       do y=0,100
          write(u,fmt=*)x,y,i_grid(x,y),grid(1:2,x,y)
       end do
       write(u,fmt=*)""
    end do
    close(u)
  end subroutine sample_2d_analyse
sample 2d to generator \( \ \)
  subroutine sample_2d_to_generator(this)
    class(sample_2d_type),intent(inout)::this
    integer::region
    do region=1,this%n_regions
       call this%regions(region)%to_generator()
  end subroutine sample_2d_to_generator
sample 2d mean \uparrow
  elemental function sample_2d_mean(this,dim) result(mean)
    class(sample_2d_type),intent(in)::this
    integer,intent(in)::dim
    real(kind=double)::mean
    integer::region,hit
   mean=0D0
    do region=1,this%n_regions
       do hit=1,this%regions(region)%n_hits
          mean=mean+this%regions(region)%hyp_hits(dim,hit)
       end do
    end do
    mean=mean/this%n_hits
  end function sample_2d_mean
11.4.3 Methoden für sample 3d type
sample 3d write to marker \( \ \)
  subroutine sample_3d_write_to_marker(this,marker,status)
    class(sample_3d_type),intent(in) :: this
    class(marker_type),intent(inout)::marker
```

```
integer(kind=dik),intent(out)::status
    integer::n
    call marker%mark_begin("sample_3d_type")
    call marker%mark("n_slices",this%n_slices)
    call marker%mark("n_alloc",this%n_alloc)
    if(this%n_slices>0)then
       call marker%mark_instance_begin&
         (this%slices(1), "slices", shape=shape(this%slices))
       do n=1,this%n_slices
          call sample_2d_write_to_marker(this%slices(n),marker,status)
       call marker%mark_instance_end()
    end if
    call marker%mark_end("sample_3d_type")
  end subroutine sample_3d_write_to_marker
sample 3d read from marker \( \)
  subroutine sample_3d_read_from_marker(this,marker,status)
    class(sample_3d_type),intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    integer::n
    call marker%pick_begin("sample_3d_type",status=status)
    call marker%pick("n_slices",this%n_slices,status)
    call marker%pick("n_alloc",this%n_alloc,status)
    if(this%n_slices>0)then
       call marker%pick_instance_begin("slices",status=status)
       allocate(this%slices(this%n_slices))
       do n=1,this%n_slices
          call sample_2d_read_from_marker(this%slices(n),marker,status)
       call marker%pick_instance_end(status)
    end if
    call marker%pick_end("sample_3d_type",status)
  end subroutine sample_3d_read_from_marker
sample 3d print to unit \uparrow
  subroutine sample_3d_print_to_unit(this,unit,parents,components,peers)
    class(sample_3d_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    integer::n
    write(unit,fmt=*)"components of sample_3d_type"
                                    ",i10)')this%n_slices
    write(unit,'("n_slices:
    write(unit,'("n_alloc:
                                    ",i10)')this%n_alloc
    if(allocated(this%slices))then
       if(components>0)then
          do n=1,this%n_slices
             call this%slices(n)%print_to_unit(unit,parents,components-1,peers)
          end do
```

```
else
          write(unit,fmt=*)"skipping slices."
       end if
    else
       write(unit,fmt=*)"slices are not allocated."
    end if
  end subroutine sample_3d_print_to_unit
sample 3d get type \uparrow
  pure subroutine sample_3d_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="sample_3d_type")
  end subroutine sample_3d_get_type
sample 3d measure \( \ \)
  elemental function sample_3d_measure(this)
    real(kind=double)::sample_3d_measure
    class(sample_3d_type),intent(in)::this
    sample_3d_measure=1D0
  end function sample_3d_measure
sample 3d to generator \( \ \)
  subroutine sample_3d_to_generator(this)
    class(sample_3d_type),intent(inout)::this
    integer::slice
    do slice=1,this%n_slices
       call this%slices(slice)%to_generator()
    end do
  end subroutine sample_3d_to_generator
sample 3d initialize \( \)
  subroutine sample_3d_initialize(this,n_alloc)
    class(sample_3d_type),intent(out)::this
    integer,intent(in)::n_alloc
    if(allocated(this%slices))deallocate(this%slices)
    if(n alloc>0)then
       allocate(this%slices(n_alloc))
       this%n_alloc=n_alloc
       this%n_slices=1
       call this%slices(1)%initialize(n_alloc)
    else
       this%n_alloc=0
    end if
  end subroutine sample_3d_initialize
sample 3d generate hit \( \ \)
```

```
pure subroutine sample_3d_generate_hit(this,rnd,pts2,boost,hit,region,slice)
    class(sample_3d_type),intent(in)::this
    integer,intent(in),dimension(3)::rnd
    real(kind=double),intent(in)::pts2
    integer,intent(out)::slice,region
    real(kind=double), dimension(3), intent(out)::hit
    real(kind=double),intent(out)::boost
    if(this%n_slices==0)then
       call muli_mcint_generate_hit(rnd,unit_square,hit(1:2))
       boost=1D0
       slice=1
       region=1
    else
       do slice=1,this%n_slices
          if(this%slices(slice)%contains(pts2))exit
       call this%slices(slice)%generate_hit(rnd,boost,hit(1:2),region)
    end if
    hit(3)=pts2
  end subroutine sample_3d_generate_hit
sample 3d confirm hit \
  subroutine sample_3d_confirm_hit(this, hit, region, slice)
    class(sample_3d_type),intent(inout)::this
    integer,intent(in)::slice,region
    real(kind=double),intent(in),dimension(3)::hit
    type(sample_2d_type),allocatable::old_slice
    integer::n
    logical::full
    if(this%n_alloc<slice)then
       print *,"sample_3d_confirm_hit: Slice ",slice," not allocated."
    !if(.not.allocated(this%slices))call this%initialize(2)
       call this%slices(slice)%confirm_hit(hit,region,full)
       if(full)then
          if(this%n_alloc==this%n_slices)call this%enlarge()
          this%n_slices=this%n_slices+1
          allocate(old slice)
          call this%slices(slice)%move_components(old_slice)
          call sample_2d_split(&
               old_slice,&
               this%n_alloc,&
               old_slice%mean(3),&
               this%slices(slice),&
               this%slices(this%n_slices))
       end if
    end if
  end subroutine sample_3d_confirm_hit
sample 3d enlarge \( \)
```

```
subroutine sample_3d_enlarge(this)
    class(sample_3d_type),intent(inout)::this
    type(sample_2d_type),allocatable,dimension(:)::old_slices
    integer::n
    print *,"sample_3d_enlarge"
    call move_alloc(this%slices,old_slices)
    this%n_alloc=this%n_alloc*2
    allocate(this%slices(this%n_alloc))
    do n=1,size(old_slices)
       call old_slices(n)%move_components(this%slices(n))
  end subroutine sample_3d_enlarge
11.4.4 Methoden für sample int kind type
sample\_int\_kind\_write \ to \ marker \uparrow
  subroutine sample_int_kind_write_to_marker(this,marker,status)
    class(sample_int_kind_type),intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("sample_int_kind_type")
    call sample_3d_write_to_marker(this,marker,status)
    call marker%mark("n_hits",this%n_hits)
    call marker%mark("n_proc",this%n_proc)
    call marker%mark("boost",this%overall_boost)
    if(this%n_hits>0)then
       call marker%mark("hits",this%hits)
    end if
    if(this%n_proc>0)then
       call marker%mark("processes", this%processes)
       call marker%mark("weights",this%weights)
    end if
    call marker%mark_end("sample_int_kind_type")
  end subroutine sample_int_kind_write_to_marker
sample int kind read from marker \( \)
  subroutine sample int kind read from marker(this, marker, status)
    class(sample_int_kind_type),intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("sample_int_kind_type",status=status)
    call sample_3d_read_from_marker(this,marker,status)
    call marker%pick("n_hits",this%n_hits,status)
    call marker%pick("n_proc",this%n_proc,status)
    call marker%pick("boost",this%overall_boost,status)
    if(this%n_hits>0)then
       allocate(this%hits(this%n_hits))
       call marker%pick("hits",this%hits,status)
    end if
```

```
if(this%n_proc>0)then
       allocate(this%processes(this%n_proc))
       call marker%pick("processes",this%processes,status)
       allocate(this%weights(this%n_proc))
       call marker%pick("weights",this%weights,status)
    end if
    call marker%pick_end("sample_int_kind_type",status)
  end subroutine sample_int_kind_read_from_marker
sample int kind print to unit \
  subroutine sample_int_kind_print_to_unit(this,unit,parents,components,peers)
    class(sample_int_kind_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    integer::n
    if(parents>0)call sample_3d_print_to_unit(this,unit,parents,components,peers)
    write(unit,fmt=*)"components of sample_int_kind_type"
    write(unit,'("n_hits:
                                   ",i10)')this%n_hits
                                  ",i10)')this%n_proc
    write(unit,'("n_proc:
    write(unit,'("overall_boost: ",e14.7)')this%overall_boost
    write(unit,'("hits:")')
    write(unit,'(10(i0," "))')this%hits(1:this%n_hits)
    write(unit,'("weights:")')
    write(unit, '(10(i0, " "))')this%weights
    write(unit,'("processes:")')
    write(unit, '(2(i0, " "))')this%processes
  end subroutine sample_int_kind_print_to_unit
sample int kind get type \( \)
  pure subroutine sample_int_kind_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="sample_int_kind_type")
  end subroutine sample_int_kind_get_type
sample int kind to generator \( \)
  subroutine sample_int_kind_to_generator(this)
    class(sample_int_kind_type),intent(inout)::this
    integer::int_kind
    if(allocated(this%hits))deallocate(this%hits)
    call sample_3d_to_generator(this)
  end subroutine sample_int_kind_to_generator
sample int kind process id \( \ext{\gamma} \)
  elemental integer function sample_int_kind_process_id(this,subprocess)
    class(sample_int_kind_type),intent(in)::this
    integer,intent(in)::subprocess
    sample_int_kind_process_id=this%processes(subprocess)
  end function sample_int_kind_process_id
```

```
sample int kind initialize \
    subroutine sample_int_kind_initialize(this,n_alloc,processes,overall_boost)
         class(sample_int_kind_type),intent(out)::this
         integer,intent(in)::n_alloc
         integer,intent(in),dimension(:)::processes
         real(kind=double),optional,intent(in)::overall_boost
         integer::s,n
         s=size(processes)
         call sample_3d_initialize(this,n_alloc)
         if(allocated(this%hits))deallocate(this%hits)
         allocate(this%hits(n_alloc))
         if(allocated(this%weights))deallocate(this%weights)
         allocate(this%weights(s))
         if(allocated(this%processes))deallocate(this%processes)
         allocate(this%processes(s),source=processes)
         do n=1,s
               this%weights(n)=0
         end do
         this%n_alloc=n_alloc
         this%n_hits=0
         this%n_proc=s
         if(present(overall_boost))this%overall_boost=overall_boost
        this \% overall\_boost = this \% overall\_boost * this \% n\_procedure the procedure of the pro
           print *,this%weights
    end subroutine sample_int_kind_initialize
sample int kind generate hit \( \ \)
    pure subroutine sample_int_kind_generate_hit&
         (this, rnd, pts2, boost, hit, region, slice, subprocess)
         class(sample_int_kind_type),intent(in)::this
         integer, dimension (4), intent (in)::rnd
         real(kind=double),intent(in)::pts2
         real(kind=double), dimension(3), intent(out)::hit
         integer,intent(out)::region,slice,subprocess
        real(kind=double),intent(out)::boost
        integer::n_n
         print *,rnd,pts2,boost,hit,region,slice,subprocess
         call sample_3d_generate_hit(this,rnd(2:4),pts2,boost,hit,region,slice)
         n_n=modulo(rnd(1),this%n_hits+size(this%weights))+1
         if(n_n>this%n_hits)then
                subprocess=n_n-this%n_hits
                subprocess=this%hits(n_n)
        boost=boost*this%overall_boost*(this%n_proc+this%n_hits)&
                      /(this%n_proc*(this%weights(subprocess)+1))
    end subroutine sample_int_kind_generate_hit
sample int kind mcgenerate hit \
```

```
subroutine sample_int_kind_mcgenerate_hit&
    (this, pts2, mean, integrand_kind, tao_rnd, process_id, cart_hit)
    class(sample_int_kind_type),intent(inout)::this
    integer, intent(in)::integrand_kind
    real(kind=double),intent(in)::pts2,mean
    type(tao_random_state),intent(inout)::tao_rnd
    real(kind=double),dimension(3),intent(out)::cart_hit
    integer,intent(out)::process_id
    real(kind=double)::boost
    integer::region,slice,subprocess
    integer, dimension (4)::i_rnd
    real(kind=double)::dddsigma,d_rnd
    real(kind=double), dimension(3)::hyp_hit
   MC:do
       this%n_tries=this%n_tries+1
       call tao_random_number(tao_rnd,i_rnd)
       call tao_random_number(tao_rnd,d_rnd)
       !print *,pts2,mean,integrand_kind,process_id,cart_hit
       call this%generate_hit(i_rnd,pts2,boost,hyp_hit,region,slice,subprocess)
       process_id=this%process_id(subprocess)
       call interactions_dddsigma_reg(process_id,integrand_kind,hyp_hit,cart_hit,dddsigma)
       dddsigma=dddsigma*boost
       if (d_rnd*mean<dddsigma) then
          exit MC
       end if
    end do MC
    if (mean < dddsigma) then
       call this%confirm_hit(hyp_hit,region,slice,subprocess,.true.)
    else
       call this%confirm_hit(hyp_hit,region,slice,subprocess,.false.)
    end if
  end subroutine sample_int_kind_mcgenerate_hit
sample int kind confirm hit \
  subroutine sample_int_kind_confirm_hit(this,hit,region,slice,subprocess,over)
    class(sample_int_kind_type),intent(inout)::this
    real(kind=double), dimension(3), intent(in)::hit
    integer,intent(in)::region,slice,subprocess
    integer,dimension(:),allocatable::tmp_hits
    logical, optional, intent(in)::over
    this%n_hits=this%n_hits+1
    if(present(over))then
       if(over)then
          this%n_over=this%n_over+1
          this%overall_boost=this%overall_boost/1.1D0
       else
          this%overall_boost=this%overall_boost*1.0001D0
       end if
    end if
    if(0<size(this%hits))then
```

```
if(this%n_hits>size(this%hits))then
          call move_alloc(this%hits,tmp_hits)
          allocate(this%hits(2*size(tmp_hits)))
          this%hits(1:size(tmp_hits))=tmp_hits
       end if
       this%hits(this%n_hits)=subprocess
    end if
    this%weights(subprocess)=this%weights(subprocess)+1
    call sample_3d_confirm_hit(this,hit,region,slice)
  end subroutine sample_int_kind_confirm_hit
sample int kind analyse \( \ \)
  subroutine sample_int_kind_analyse(this,dir,prefix)
    class(sample_int_kind_type),intent(in)::this
    character(*),intent(in)::dir,prefix
    integer::slices_unit,subprocs_unit
    integer::n,slice
    character(3)::slice_name
    integer, dimension(:), allocatable::int_a
    real(kind=double),dimension(:),allocatable::real_a
    call generate_unit(slices_unit)
    print *,"sample_int_kind_analyse: ",dir//"/"/prefix//"slice_distribution.plot"
    open(slices_unit,file=dir//"/"//prefix//"slice_distribution.plot")
    call generate_unit(subprocs_unit)
    print *,"sample_int_kind_analyse: ",dir//"/"/prefix//"subproc_distribution.plot"
    open(subprocs_unit,file=dir//"/"//prefix//"subproc_distribution.plot")
    allocate(real_a(this%n_slices))
    allocate(int_a(this%n_slices))
    do n=1,this%n_slices
       real_a(n)=this%slices(n)%range(1)
    end do
    call misc_sort(real_a,int_a)
    do n=1,size(this%weights)
       if(this%n_hits>0)then
          write(subprocs_unit,fmt=*)&
          real(this%weights(n)),real(this%weights(n)+1)/this%n_hits
          write(subprocs_unit,fmt=*)0,0
       end if
    end do
    do n=1,this%n_slices
       slice=int_a(n)
       call integer_with_leading_zeros(n,3,slice_name)
       call sample_2d_analyse(this%slices(slice),dir,prefix//slice_name//".plot")
       print *,this%n_hits,this%slices(slice)%range(2)-this%slices(slice)%range(1)
       if (this%n_hits>0)then
          write(slices_unit,fmt=*)&
               &this%slices(slice)%range(1),&
               &this%slices(slice)%range(2),&
               &this%slices(slice)%n_hits,&
```

```
&real(this%slices(slice)%n_hits)/&
               (this%n_hits*(this%slices(slice)%range(2)-this%slices(slice)%range(1)))
       else
          write(slices_unit,fmt=*)&
               &this%slices(slice)%range(1),&
               &this%slices(slice)%range(2),&
               &this%slices(slice)%n_hits,&
               &ODO
       end if
    end do
    write(slices_unit,fmt=*)1D0,0D0,0D0,0D0
    close(slices_unit)
    close(subprocs_unit)
  end subroutine sample_int_kind_analyse
11.4.5 Methoden für sample inclusive type
sample inclusive write to marker \( \)
  subroutine sample_inclusive_write_to_marker(this, marker, status)
    class(sample_inclusive_type),intent(in) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    integer::n
    call marker%mark_begin("sample_inclusive_type")
    call marker%mark("n_alloc",this%n_alloc)
    if(allocated(this%int_kinds))then
       call marker%mark_begin(tag="int_kinds",shape=shape(this%int_kinds))
       do n=1,size(this%int_kinds)
          call this%int_kinds(n)%write_to_marker(marker,status)
       end do
       call marker%mark instance end()
    else
       call marker%mark_empty(tag="int_kinds",shape=[0])
    end if
    call marker%mark_end("sample_inclusive_type")
  end subroutine sample_inclusive_write_to_marker
sample inclusive read from marker \( \)
  subroutine sample_inclusive_read_from_marker(this,marker,status)
    class(sample_inclusive_type),intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    integer::n
    integer,dimension(:),allocatable::s
    call marker%pick_begin("sample_inclusive_type",status=status)
    call marker%pick("n_alloc",this%n_alloc,status)
    call marker%pick_begin("int_kinds",shape=s,status=status)
    if(s(1)>0)then
       do n=1,size(this%int_kinds)
```

```
call this%int_kinds(n)%read_from_marker(marker,status)
       end do
       call marker%pick_end("int_kinds",status)
    end if
    call marker%pick_end("sample_inclusive_type",status)
  end subroutine sample_inclusive_read_from_marker
sample inclusive print to unit \( \ \)
  subroutine sample_inclusive_print_to_unit(this,unit,parents,components,peers)
    class(sample_inclusive_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    integer::n
    write(unit,fmt=*)"components of sample_inclusive_type"
    write(unit,'("n_alloc:
                                    ",i10)')this%n_alloc
    if(allocated(this%int_kinds))then
       if(components>0)then
          write(unit,'("int_kinds:")')
          do n=1,this%n_alloc
             call this%int_kinds(n)%print_to_unit(unit,parents,components-1,peers)
          end do
       else
          write(unit,fmt=*)"skipping int_kinds."
       end if
    else
       write(unit,fmt=*)"int_kinds are not allocated."
  end subroutine sample_inclusive_print_to_unit
sample inclusive get type \( \ \)
  pure subroutine sample_inclusive_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="sample_inclusive_type")
  end subroutine sample_inclusive_get_type
sample inclusive process id \
  elemental integer function sample_inclusive_process_id(this,subprocess,int_kind)
    class(sample_inclusive_type),intent(in)::this
    integer,intent(in)::subprocess,int_kind
    sample_inclusive_process_id=this%int_kinds(int_kind)%processes(subprocess)
  end function sample_inclusive_process_id
sample inclusive initialize \( \)
  subroutine sample_inclusive_initialize(this,n_alloc,sizes,processes,overall_boost)
    class(sample_inclusive_type),intent(out)::this
    integer,intent(in)::n_alloc
    integer,dimension(:),intent(in)::sizes,processes
    real(kind=double),optional,intent(in)::overall_boost
    integer::n,sum
```

```
this%n_tries_sum=zero
    this%n_over_sum=0
    this%n_alloc=size(sizes)
    if(allocated(this%int_kinds))deallocate(this%int_kinds)
    allocate(this%int_kinds(this%n_alloc))
    sum=0
    do n=1,this%n_alloc
       call this%int_kinds(n)%initialize(n_alloc,processes(sum+1:sum+sizes(n)),overall_boost)
       sum=sum+sizes(n)
    end do
  end subroutine sample_inclusive_initialize
sample inclusive finalize \( \)
  subroutine sample_inclusive_finalize(this)
    class(sample_inclusive_type),intent(inout)::this
    deallocate(this%int_kinds)
    this%n_alloc=0
  end subroutine sample_inclusive_finalize
sample inclusive generate hit \( \ \)
  pure subroutine sample_inclusive_generate_hit&
    (this, rnd, pts2, int_kind, hit, region, boost, slice, process)
    class(sample_inclusive_type),intent(in)::this
    integer, dimension(4), intent(in)::rnd
    real(kind=double),intent(in)::pts2
    integer, intent(in)::int_kind
    real(kind=double), dimension(3), intent(out)::hit
    integer,intent(out)::region,slice,process
    real(kind=double),intent(out)::boost
    call this%int_kinds(int_kind)%generate_hit(rnd,pts2,boost,hit,region,slice,process)
  end subroutine sample_inclusive_generate_hit
sample inclusive mcgenerate hit \
  subroutine sample_inclusive_mcgenerate_hit&
    (this, pts2, mean, integrand_kind, tao_rnd, process_id, cart_hit)
    class(sample_inclusive_type),intent(inout)::this
    real(kind=double),intent(in)::pts2,mean
    integer,intent(in)::integrand_kind
    type(tao_random_state),intent(inout)::tao_rnd
    real(kind=double),dimension(3),intent(out)::cart_hit
    integer, intent(out)::process_id
    call sample_int_kind_mcgenerate_hit(&
         this%int_kinds(integrand_kind),pts2,mean,integrand_kind,tao_rnd,process_id,cart_hit)
  end subroutine sample_inclusive_mcgenerate_hit
sample inclusive confirm hit \
  subroutine sample_inclusive_confirm_hit(this,hit,int_kind,region,slice,process,over)
    class(sample_inclusive_type),intent(inout)::this
    real(kind=double), dimension(3), intent(in)::hit
```

```
integer,intent(in)::int_kind,region,slice,process
    logical, optional, intent(in)::over
    call this%int_kinds(int_kind)%confirm_hit(hit,region,slice,process,over)
  end subroutine sample_inclusive_confirm_hit
sample inclusive sum up \( \)
  subroutine sample_inclusive_sum_up(this)
    class(sample_inclusive_type),intent(inout)::this
    integer::n
    this%n_tries_sum=zero
    this%n hits sum=zero
    this%n over sum=zero
    do n=1,this%n_alloc
       this%n_tries_sum=this%n_tries_sum+this%int_kinds(n)%n_tries
       this%n_hits_sum=this%n_hits_sum+this%int_kinds(n)%n_hits
       this%n_over_sum=this%n_over_sum+this%int_kinds(n)%n_over
  end subroutine sample_inclusive_sum_up
sample inclusive analyse \( \)
  subroutine sample_inclusive_analyse(this,dir,subdirs)
    class(sample_inclusive_type),intent(in)::this
    character(*),intent(in)::dir
    logical,intent(in)::subdirs
    integer::inclusive_unit
    integer::n,n_hits
    character(2)::sample_name
    call generate_unit(inclusive_unit)
    open(inclusive_unit,file=dir//"/int_kinds.plot")
    n hits=0
    do n=1,size(this%int_kinds)
       n_hits=n_hits+this%int_kinds(n)%n_hits
    end do
    do n=1,size(this%int_kinds)
       write(inclusive_unit,fmt=*)n,real(this%int_kinds(n)%n_hits)/n_hits
       call integer_with_leading_zeros(n,2,sample_name)
       if(subdirs)then
          call sample int kind analyse(&
               this%int_kinds(n),&
               dir//"/"//sample_name,&
       else
          call sample_int_kind_analyse(&
               this%int_kinds(n),&
               dir,&
               sample_name//"_")
       end if
    end do
    close(inclusive_unit)
  end subroutine sample_inclusive_analyse
```

```
sample inclusive to generator \( \)
 subroutine sample_inclusive_to_generator(this)
    class(sample_inclusive_type),intent(inout)::this
    integer::int_kind
    do int_kind=1,size(this%int_kinds)
       call this%int_kinds(int_kind)%to_generator()
  end subroutine sample_inclusive_to_generator
sample inclusive allocate \( \)
  subroutine sample_inclusive_allocate(this,n_alloc)
    class(sample_inclusive_type),intent(out)::this
    integer,intent(in)::n_alloc
    allocate(this%int_kinds(n_alloc))
    this%n_alloc=n_alloc
  end subroutine sample_inclusive_allocate
11.4.6 Sonstige Prozeduren
muli mcint_generate_hit
 pure subroutine muli_mcint_generate_hit(rnd,corners,hit)
    real(kind=double), dimension(2), intent(out)::hit
    integer,intent(in),dimension(2)::rnd
    real(kind=double), dimension(2,2), intent(in)::corners
    !print *,hit
    !print *,corners
    !print *,(corners(1:2,2)-corners(1:2,1))
    hit=(rnd/max_d)*(corners(1:2,2)-corners(1:2,1))+corners(1:2,1)
  end subroutine muli_mcint_generate_hit
plot pstvue3d
  subroutine plot_pstvue3d(unit,corners,density)
    integer, intent(in)::unit
    real(kind=double), dimension(2,2), intent(in)::corners
    real(kind=double),intent(in)::density
    real(kind=double), dimension(2)::width, mean
    real(kind=double),dimension(3,3)::plot
    width=(corners(:,2)-corners(:,1))/2D0
   mean=(corners(:,1)+corners(:,2))/2D0
    plot(1,1)=width(1)
    plot(2,1)=width(2)
    plot(3,1)=density/2D0
    plot(1,2)=mean(1)
    plot(2,2)=mean(2)
    plot(3,2)=density/2D0
    call log_color_code(density,plot(1:3,3))
    if(density>1D0)then
```

```
write(unit,fmt='("
                                      mybigcube",F14.7,"",F14.7,"",F14.7,"&
            &",F14.7,"",F14.7,"",F14.7,"",F14.7,"",F14.7,"",F14.7,"")')plot
       return
    end if
                                      mycube",F14.7,"",F14.7,"",F14.7,"&
    write(unit,fmt='("
         &",F14.7,"",F14.7,"",F14.7,"",F14.7,"",F14.7,"",F14.7,"")')plot
  end subroutine plot_pstvue3d
log color code
  subroutine log_color_code(number,rgb)
    real(kind=double),intent(in)::number
    real(kind=double), dimension(3), intent(out)::rgb
    if(number<exp(-5D0))then
       rgb=[0D0,0D0,exp(5D0)*number]
    else
       if(number<exp(-4D0))then
          rgb=[0D0, (number-exp(-5D0))/(exp(-4D0)-exp(-5D0)), 1D0]
       else
          if(number<exp(-3D0))then
             rgb=[0D0,1D0,1D0-((number-exp(-4D0))/(exp(-3D0)-exp(-4D0)))]
          else
             if(number<exp(-2D0))then
                rgb = [(number - exp(-3D0))/(exp(-2D0) - exp(-3D0)), 1D0, 0D0]
                if(number<exp(-1D0))then
                   rgb=[1D0,1D0-(number-exp(-2D0))/(exp(-1D0)-exp(-2D0)),0D0]
                   if(number<1D0)then
                      rgb=[1D0,0D0,(number-exp(-3D0))/(1D0-exp(-3D0))]
                      rgb=[exp(1D0), 1D0, 1D0]*exp(-number)
                      return
                   end if
                end if
             end if
          end if
       end if
    end if
  end subroutine log_color_code
misc sort
  recursive subroutine misc_sort(in,out)
    real(kind=double), dimension(:), intent(in)::in
    integer, dimension(:), intent(out)::out
    integer,dimension(:),allocatable::tmp
    integer::n,k,l,cut
    if(size(in)==1)then
       out=[1]
    else
       if(size(in)==2)then
```

```
if(in(1) \le in(2))then
           out=[1,2]
        else
           out=[2,1]
        end if
     else
        cut=size(in)/2
        k=1
        1=cut+1
        allocate(tmp(size(in)))
        call misc_sort(in(1:cut),tmp(1:cut))
        call misc_sort(in(cut+1:),tmp(cut+1:))
        do n=cut+1,size(in)
           tmp(n)=tmp(n)+cut
        end do
        do n=1,size(in)
           if(k>cut)then
              out(n)=tmp(1)
              1=1+1
           else
              if(l>size(tmp))then
                 out(n)=tmp(k)
                 k=k+1
              else
                  if(in(tmp(k)) < in(tmp(1)))then
                     out(n)=tmp(k)
                     k=k+1
                 else
                     out(n)=tmp(1)
                     1=1+1
                 end if
              end if
           end if
        end do
     end if
  end if
end subroutine misc_sort
```

# 12 Modul muli\_cuba

# 12.1 Abhängigkeiten

```
use muli_momentum
```

### 12.2 Parameter

```
integer, parameter :: max_maxeval = huge(1)
```

# 12.3 Derived Types

## 12.3.1 cuba class

```
type,extends(serializable_class), abstract :: cuba_class
   ! private
  real(kind=drk) :: start_time=0D0
  real(kind=drk) :: stop_time=0D0
  real(kind=drk) :: run_time=0D0
   ! common input
   integer :: dim_x = 2
   integer :: dim_f = 1
   type(transversal_momentum_type) :: userdata
   real(kind=drk) :: eps_rel = 1D-3
   real(kind=drk) :: eps_abs = 0D0
   integer :: flags = 0
   integer :: seed = 1
   integer :: min_eval = 0
   integer :: max_eval = max_maxeval
   ! common output
   integer :: neval = 0
   integer, public :: fail = -1
   integer :: nregions = 0
   real(kind=drk), dimension(:), allocatable :: integral
   real(kind=drk), dimension(:), allocatable :: error
  real(kind=drk), dimension(:), allocatable :: prob
  procedure(integrand_interface), nopass, pointer::integrand
 contains
   !Überschriebene serializable_class Methoden
```

```
procedure::write_to_marker=>cuba_write_to_marker
  procedure::read_from_marker=>cuba_read_from_marker
  procedure::print_to_unit=>cuba_print_to_unit
   !Originäre cuba_class Methoden
  procedure ::get_integral_array=>cuba_get_integral_array
  procedure ::get_integral_1=>cuba_get_integral_1
            ::get_integral=>get_integral_array,get_integral_1
  procedure ::copy_common=>cuba_copy_common
  procedure ::set_common=>cuba_set_common
  procedure ::set dim f=>cuba set dim f
  procedure ::set_dim_x=>cuba_set_dim_x
  procedure ::reset_timer=>cuba_reset_timer
  procedure ::integrate_with_timer=>cuba_integrate_with_timer
  procedure ::integrate_associated=>cuba_integrate_associated
  procedure(integrate_interface), deferred :: integrate_nd
  procedure(integrate_userdata_interface), deferred :: integrate_userdata
  procedure(cuba_copy_interface), deferred :: copy
  procedure ::dealloc_dim_f=>cuba_dealloc_dim_f
  procedure ::alloc_dim_f=>cuba_alloc_dim_f
  procedure ::dealloc=>cuba_dealloc
  procedure ::alloc=>cuba_alloc
  generic ::integrate=>integrate_nd,integrate_userdata
end type cuba_class
```

## 12.3.2 cuba cuhre type

```
type,extends(cuba_class) :: cuba_cuhre_type
    private
    integer :: key = 13

contains
    !Überschriebene serializable_class Methoden
    procedure::write_to_marker=>cuba_cuhre_write_to_marker
    procedure::read_from_marker=>cuba_cuhre_read_from_marker
    procedure::print_to_unit=>cuba_cuhre_print_to_unit
    procedure,nopass::get_type=>cuba_cuhre_get_type
    !Überschriebene cuba_class Methoden
    procedure ::integrate_nd=>integrate_cuhre
    procedure ::integrate_userdata=>integrate_cuhre_userdata
    procedure ::copy=>cuba_cuhre_copy
    procedure ::set_deferred=>cuba_cuhre_set_deferred
end type cuba_cuhre_type
```

### 12.3.3 cuba suave type

```
type,extends(cuba_class) :: cuba_suave_type
  private
  integer :: nnew = 10000 !1000
  integer :: flatness = 5 !50
```

```
contains
  !Überschriebene serializable_class Methoden
  procedure::write_to_marker=>cuba_suave_write_to_marker
  procedure::read_from_marker=>cuba_suave_read_from_marker
  procedure::print_to_unit=>cuba_suave_print_to_unit
  procedure,nopass::get_type=>cuba_suave_get_type
  !Überschriebene cuba_class Methoden
  procedure ::integrate_nd=>integrate_suave
  procedure ::integrate_userdata=>integrate_suave_userdata
  procedure ::copy=>cuba_suave_copy
end type cuba_suave_type
```

## 12.3.4 cuba divonne type

```
type,extends(cuba_class) :: cuba_divonne_type
  private
   integer :: key1 = 13
   integer :: key2 = 13
   integer :: key3 = 13
   integer :: maxpass = 2
  real(kind=drk) :: border = 0D0
  real(kind=drk) :: maxchisq = 10D0
  real(kind=drk) :: mindeviation = .25D0
   integer :: ngiven = 0
   integer :: ldxgiven = 0
  real(kind=drk), dimension(:,:), allocatable :: xgiven
   integer :: nextra = 0
contains
   !Überschriebene serializable_class Methoden
   procedure::write_to_marker=>cuba_divonne_write_to_marker
  procedure::read_from_marker=>cuba_divonne_read_from_marker
   procedure::print_to_unit=>cuba_divonne_print_to_unit
   procedure,nopass::get_type=>cuba_divonne_get_type
   !Überschriebene cuba_class Methoden
   procedure ::integrate_nd=>integrate_divonne
  procedure ::integrate_userdata=>integrate_divonne_userdata
   procedure ::copy=>cuba_divonne_copy
   procedure ::set_deferred=>cuba_divonne_set_deferred
end type cuba_divonne_type
```

### 12.3.5 cuba vegas type

```
type,extends(cuba_class) :: cuba_vegas_type
  private
  integer :: nstart = 500
  integer :: nincrease = 1000
  integer :: nbatch = 1000
  integer :: gridno = 0
  character(len=8),pointer :: statefile => null()
```

```
!Überschriebene serializable_class Methoden
procedure::write_to_marker=>cuba_vegas_write_to_marker
procedure::read_from_marker=>cuba_vegas_read_from_marker
procedure::print_to_unit=>cuba_vegas_print_to_unit
procedure,nopass::get_type=>cuba_vegas_get_type
!Überschriebene cuba_class Methoden
procedure ::integrate_nd=>integrate_vegas
procedure ::integrate_userdata=>integrate_vegas_userdata
procedure ::copy=>cuba_vegas_copy
procedure ::set_deferred=>cuba_vegas_set_deferred
end type cuba_vegas_type
```

### 12.4 Interfaces

```
interface
  subroutine integrand_interface(dim_x, x, dim_f, f,userdata)
     use kinds !NODEP!
     use muli_momentum
     integer, intent(in) :: dim_x, dim_f
     real(kind=drk), dimension(dim_x), intent(in) :: x
     real(kind=drk), dimension(dim_f), intent(out) :: f
     class(transversal_momentum_type), intent(in) :: userdata
   end subroutine integrand_interface
end interface
interface
  subroutine cuba_copy_interface(this,source)
     import :: cuba_class
     class(cuba_class),intent(out)::this
     class(cuba_class),intent(in)::source
   end subroutine cuba_copy_interface
   subroutine ca_plain(this)
     import :: cuba class
     class(cuba_class) :: this
   end subroutine ca_plain
   subroutine integrate_interface(this, integrand)
     import :: cuba class
     class(cuba_class),intent(inout) :: this
     interface
       subroutine integrand(dim_x, x, dim_f, f,userdata)
          use kinds !NODEP!
          use muli_momentum
          integer, intent(in) :: dim_x, dim_f
          real(kind=drk), dimension(dim_x), intent(in) :: x
          real(kind=drk), dimension(dim_f), intent(out) :: f
          class(transversal_momentum_type), intent(in) :: userdata
        end subroutine integrand
     end interface
   end subroutine integrate_interface
```

```
end interface
interface
   subroutine integrate_userdata_interface(this, integrand,userdata)
     use muli_momentum
     import :: cuba_class
     class(cuba_class),intent(inout) :: this
     interface
        subroutine integrand(dim_x, x, dim_f, f,userdata)
          use kinds !NODEP!
          use muli momentum
          integer, intent(in) :: dim_x, dim_f
          real(kind=drk), dimension(dim_x), intent(in) :: x
          real(kind=drk), dimension(dim_f), intent(out) :: f
          class(transversal_momentum_type), intent(in) :: userdata
        end subroutine integrand
     end interface
     class(transversal_momentum_type),intent(in)::userdata
   end subroutine integrate_userdata_interface
end interface
```

# 12.5 Implementierung der Prozeduren

### 12.5.1 Methoden für cuba class

Überschriebene serializable class Methoden

```
cuba write to marker \( \ \)
 subroutine cuba_write_to_marker(this,marker,status)
    class(cuba_class),intent(in)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("cuba_class")
    call marker%mark("dim_x",this%dim_x)
    call marker%mark("dim_f",this%dim_f)
    call marker%mark("eps_rel",this%eps_rel)
    call marker%mark("eps_abs",this%eps_abs)
    call marker%mark("flags",this%flags)
    call marker%mark("min_eval",this%min_eval)
    call marker%mark("max_eval",this%max_eval)
    call marker%mark("neval",this%neval)
    call marker%mark("fail",this%fail)
    call marker%mark("nregions",this%nregions)
    if(allocated(this%integral))then
       call marker%mark("integral",this%integral)
    else
       call marker%mark_null("integral")
    if(allocated(this%error))then
```

```
call marker%mark("error",this%error)
    else
       call marker%mark_null("error")
    end if
    if(allocated(this%prob))then
       call marker%mark("prob",this%prob)
       call marker%mark_null("prob")
    end if
    call marker%mark_null("cuba_class")
  end subroutine cuba_write_to_marker
cuba read from marker \( \)
  subroutine cuba_read_from_marker(this,marker,status)
    class(cuba_class),intent(out) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("CUBA_CLASS",status=status)
    call marker%pick("dim_x",this%dim_x,status)
    call marker%pick("dim_f",this%dim_f,status)
    call marker%pick("eps_rel",this%eps_rel,status)
    call marker%pick("eps_abs",this%eps_abs,status)
    call marker%pick("flags",this%flags,status)
    call marker%pick("min_eval",this%min_eval,status)
    call marker%pick("max_eval",this%max_eval,status)
    call marker%pick("neval",this%neval,status)
    call marker%pick("fail",this%fail,status)
    call marker%pick("nregions",this%nregions,status)
    call marker%verify_nothing("integral", status)
    if(allocated(this%integral))deallocate(this%integral)
    if(status==serialize_ok)then
       allocate(this%integral(this%dim_f))
       call marker%pick("integral",this%integral,status)
    end if
    call marker%verify_nothing("error",status)
    if(allocated(this%error))deallocate(this%error)
    if(status==serialize ok)then
       allocate(this%error(this%dim_f))
       call marker%pick("error",this%error,status)
    end if
    call marker%verify_nothing("prob",status)
    if(allocated(this%prob))deallocate(this%prob)
    if(status==serialize_ok)then
       allocate(this%prob(this%dim_f))
       call marker%pick("prob",this%prob,status)
    call marker%pick_end("cuba_class",status)
  END SUBROUTINE cuba_read_from_marker
cuba print to unit \
```

```
subroutine cuba_print_to_unit(this,unit,parents,components,peers)
    class(cuba_class),intent(in) :: this
    INTEGER, INTENT(IN) :: unit
    integer(kind=dik),intent(in)::parents,components,peers
    character(11)::n
    write(n,'("(",I2,"(E12.4))")')this%dim_f
    write(unit,'("Components of cuba_class:")')
    write(unit,'("Parameters:")')
    write(unit,'("dim_f:
                              ",I10)')
                                         this%dim_f
    write(unit, '("dim_x:
                              ",I10)')
                                         this%dim x
    call this%userdata%print_to_unit(unit,parents,components-1,peers)
    write(unit,'("eps_rel:
                             ",E10.4)') this%eps_rel
    write(unit,'("eps_abs:
                              ",E10.4)') this%eps_abs
    write(unit,'("flags:
                              ",I10)')
                                         this%flags
    write(unit,'("seed:
                              ",I10)')
                                         this%seed
                              ",I10)')
    write(unit,'("min_eval:
                                         this%min_eval
    write(unit,'("max_eval:
                             ",I10)')
                                         this%max_eval
    write(unit,'("Results:")')
    write(unit,'("neval:
                              ",I10)')
                                         this%neval
                              ",I10)')
    write(unit,'("fail:
                                         this%fail
    write(unit,'("integral:
                             ")',advance="no")
    write(unit,fmt=n)this%integral
                              ")',advance="no")
    write(unit,'("error:
    write(unit,fmt=n)this%error
    write(unit,'("prob:
                              ")',advance="no")
    write(unit,fmt=n)this%prob
    write(unit,'("time:
                             ",E10.4)') this%stop_time-this%start_time
         write(unit,'("time:
                                   ",E10.4)') this%run_time
  end subroutine cuba_print_to_unit
Originäre cuba class Methoden
cuba integrate associated \( \ \)
  subroutine cuba_integrate_associated(this)
    class(cuba_class),intent(inout)::this
    call cuba_integrate_with_timer(this,this%integrand)
  end subroutine cuba_integrate_associated
cuba integrate with timer \uparrow
  subroutine cuba_integrate_with_timer(this,integrand)
    class(cuba_class),intent(inout)::this
    procedure(integrand_interface)::integrand
    call cpu_time(this%start_time)
    call this%integrate(integrand)
    call cpu_time(this%stop_time)
    this%run_time=this%run_time+this%stop_time-this%start_time
  end subroutine cuba_integrate_with_timer
cuba reset timer \( \)
```

```
subroutine cuba_reset_timer(this)
    class(cuba_class),intent(inout)::this
    this%start_time=ODO
    this%stop_time=ODO
    this%run_time=0D0
  end subroutine cuba_reset_timer
cuba get integral array \( \)
  subroutine cuba_get_integral_array(this,integral)
    class(cuba_class) :: this
    real(kind=drk),intent(out),dimension(:) :: integral
    integral=this%integral
  end subroutine cuba_get_integral_array
cuba get integral 1 \(\ext{\gamma}\)
  subroutine cuba_get_integral_1(this,integral)
    class(cuba_class) :: this
    real(kind=drk),intent(out) :: integral
    integral=this%integral(1)
  end subroutine cuba_get_integral_1
cuba dealloc dim f \( \ \)
  subroutine cuba_dealloc_dim_f(this)
    class(cuba_class) :: this
           print '("cuba_dealloc_dim_f...")'
    if (allocated(this%integral)) then
       deallocate(this%integral)
    end if
    if (allocated(this%error)) then
       deallocate(this%error)
    if (allocated(this%prob)) then
       deallocate(this%prob)
    end if
           print '("done")'
  end subroutine cuba_dealloc_dim_f
cuba dealloc ↑
  subroutine cuba_dealloc(this)
    class(cuba_class) :: this
    call this%dealloc_dim_f
  end subroutine cuba_dealloc
cuba alloc dim f \( \ \)
  subroutine cuba_alloc_dim_f(this)
    class(cuba_class) :: this
    call this%dealloc_dim_f()
    allocate(this%integral(this%dim_f))
```

```
allocate(this%error(this%dim_f))
    allocate(this%prob(this%dim_f))
  end subroutine cuba_alloc_dim_f
cuba alloc †
 subroutine cuba_alloc(this)
    class(cuba_class) :: this
    call this%alloc_dim_f
  end subroutine cuba_alloc
cuba set common↑
 subroutine cuba_set_common&
    (this,dim_x,dim_f,eps_rel,eps_abs,flags,seed,min_eval,max_eval,integrand,userdata)
    class(cuba_class),intent(inout) :: this
    integer,intent(in),optional :: dim_x,dim_f,flags,min_eval,max_eval,seed
    real(kind=drk),intent(in),optional :: eps_rel,eps_abs
    type(transversal_momentum_type),intent(in),optional :: userdata
    procedure(integrand_interface),optional::integrand
    if(present(dim_x))then
       call this%set_dim_x(dim_x)
    end if
    if(present(dim_f))then
       call this%set_dim_f(dim_f)
    end if
    if(present(flags))then
       this%flags=flags
    end if
    if(present(seed))then
       this%seed=seed
    if(present(min_eval))then
       this%min_eval=min_eval
    end if
    if(present(max_eval))then
       if(max_eval<max_maxeval)then
          this%max_eval=max_eval
       else
          print '("cuba_set_common: Value of max_eval is too large.")'
          this%max_eval=max_maxeval
       end if
    end if
    if(present(eps_rel))then
       this%eps_rel=eps_rel
    end if
    if(present(eps_abs))then
       this%eps_abs=eps_abs
    end if
    if(present(integrand))this%integrand=>integrand
    if(present(userdata))this%userdata=userdata
  end subroutine cuba_set_common
```

```
cuba set dim f \uparrow
  subroutine cuba_set_dim_f(this,new_dim_f)
    class(cuba_class) :: this
    integer,intent(in) :: new_dim_f
    if (new_dim_f>0) then
      this%dim_f = new_dim_f
      call this%alloc_dim_f
       write (*,'("cuba_set_dim_f: New value for dim_f is negative. dim_f is not set.")')
    end if
  end subroutine cuba_set_dim_f
cuba set dim x \uparrow
  subroutine cuba_set_dim_x(this,new_dim_x)
    class(cuba_class) :: this
    integer,intent(in) :: new_dim_x
    if (new_dim_x>0) then
       this%dim_x = new_dim_x
       write (*,'("cuba_set_dim_x: New value for dim_x is negative. dim_x is not set.")')
    end if
  end subroutine cuba_set_dim_x
cuba copy common ↑
  subroutine cuba_copy_common(this,source)
    class(cuba_class),intent(out) :: this
    class(cuba_class),intent(in) :: source
    this%dim_x = source%dim_x
    this%dim_f = source%dim_f
    this%eps_rel = source%eps_rel
    this%eps_abs = source%eps_abs
    this%flags = source%flags
    this%min_eval = source%min_eval
    this%max_eval = source%max_eval
    call this%alloc()
  end subroutine cuba_copy_common
12.5.2 Methoden für cuba vegas type
Überschriebene serializable class Methoden
cuba vegas write to marker \( \ \)
  subroutine cuba_vegas_write_to_marker(this,marker,status)
    class(cuba_vegas_type),intent(in) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("cuba_vegas_type")
```

```
call cuba_write_to_marker(this,marker,status)
    call marker%mark("nstart",this%nstart)
    call marker%mark("nincrease",this%nincrease)
    call marker%mark_null("cuba_vegas_type")
  end subroutine cuba_vegas_write_to_marker
cuba vegas read from marker \( \)
  subroutine cuba_vegas_read_from_marker(this,marker,status)
    class(cuba_vegas_type),intent(out) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("cuba_vegas_type",status=status)
    call cuba_read_from_marker(this,marker,status)
    call marker%pick("nstart",this%nstart,status)
    call marker%pick("nincrease",this%nincrease,status)
    call marker%pick_end("cuba_vegas_type",status)
  end subroutine cuba_vegas_read_from_marker
cuba vegas print to unit \
  subroutine cuba_vegas_print_to_unit(this,unit,parents,components,peers)
    class(cuba_vegas_type),intent(in) :: this
    INTEGER, INTENT(IN) :: unit
    integer(kind=dik),intent(in)::parents,components,peers
    if(parents>0)call cuba_print_to_unit(this,unit,parents-1,components,peers)
    write(unit,'("Components of cuba_vegas_type:")')
    write(unit,'("nstart:
                             ",I10)')
                                      this%nstart
    write(unit, '("nincrease: ", I10)') this%nincrease
                            ",I10)')
   write(unit,'("nbatch:
                                      this%nbatch
   write(unit,'("gridno:
                            ",I10)')
                                        this%gridno
    if(associated(this%statefile))then
      write(unit,'("statefile:",a)')
                                      this%statefile
    else
      write(unit,'("statefile:",a)')
                                      "not associated"
    end if
  end subroutine cuba_vegas_print_to_unit
cuba vegas get type↑
 pure subroutine cuba_vegas_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="cuba_vegas_type")
  end subroutine cuba_vegas_get_type
Überschriebene cuba class Methoden
cuba vegas set deferred \( \)
```

```
subroutine cuba_vegas_set_deferred(this,n_start,n_increase,nbatch,gridno,statefile)
    class(cuba_vegas_type),intent(inout) :: this
    integer,intent(in),optional :: n_start,n_increase,nbatch,gridno
    character(len=*),intent(in),target,optional::statefile
    if(present(n_start))this%nstart=n_start
    if(present(n_increase))this%nincrease=n_increase
    if(present(nbatch))this%nbatch=nbatch
    if(present(gridno))this%gridno=gridno
    if(present(statefile))this%statefile=>statefile
  end subroutine cuba_vegas_set_deferred
cuba vegas copy↑
  subroutine cuba_vegas_copy(this,source)
    class(cuba_vegas_type),intent(out) :: this
    class(cuba_class),intent(in) :: source
    select type(source)
    class is (cuba_vegas_type)
       call this%copy_common(source)
       this%nstart=source%nstart
       this%nincrease=source%nincrease
    class default
       print *,"cuba_vegas_copy: type of source is not type compatible with &
       &cuba_vegas_type."
    end select
  end subroutine cuba_vegas_copy
integrate vegas †
  subroutine integrate_vegas(this,integrand)
    class(cuba_vegas_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
           print '("vegas")'
    call vegas(&
         this%dim_x, &
         this%dim_f, &
         integrand, &
         this%userdata, &
         this%eps_rel, &
         this%eps_abs, &
         this%flags, &
         this%seed, &
         this%min_eval, &
         this%max_eval, &
         this%nstart, &
         this%nincrease, &
         this%nbatch, &
         this%gridno, &
         this%statefile, &
         this%neval, &
         this%fail, &
         this%integral, &
```

```
this%error, &
         this%prob)
  end subroutine integrate_vegas
integrate vegas userdata †
  subroutine integrate_vegas_userdata(this,integrand,userdata)
    class(cuba_vegas_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
    class(transversal_momentum_type),intent(in)::userdata
           print '("vegas")'
    call vegas(&
         this%dim_x, &
         this%dim_f, &
         integrand, &
         userdata, &
         this%eps_rel, &
         this%eps_abs, &
         this%flags, &
         this%seed, &
         this%min_eval, &
         this%max_eval, &
         this%nstart, &
         this%nincrease, &
         this%nbatch, &
         this%gridno, &
         this%statefile, &
         this%neval, &
         this%fail, &
         this%integral, &
         this%error, &
         this%prob)
  end subroutine integrate_vegas_userdata
12.5.3 Methoden für cuba suave type
Überschriebene serializable class Methoden
cuba suave write to marker \uparrow
  subroutine cuba_suave_write_to_marker(this,marker,status)
    class(cuba_suave_type),intent(in) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("cuba_suave_type")
    call cuba_write_to_marker(this,marker,status)
    call marker%mark("nnew",this%nnew)
    call marker%mark("flatness",this%flatness)
    call marker%mark_null("cuba_suave_type")
  end subroutine cuba_suave_write_to_marker
```

```
cuba suave read from marker \( \ \)
  subroutine cuba_suave_read_from_marker(this, marker, status)
    class(cuba_suave_type),intent(out) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("cuba_suave_type",status=status)
    call cuba_read_from_marker(this,marker,status)
    call marker%pick("nnew",this%nnew,status)
    call marker%pick("flatnes",this%flatness,status)
    call marker%pick_end("cuba_suave_type",status)
  end subroutine cuba_suave_read_from_marker
cuba suave print to unit \
  subroutine cuba_suave_print_to_unit(this,unit,parents,components,peers)
    class(cuba_suave_type),intent(in) :: this
    INTEGER, INTENT(IN) :: unit
    integer(kind=dik),intent(in)::parents,components,peers
    if(parents>0)call cuba_print_to_unit(this,unit,parents-1,components,peers)
    write(unit,'("Components of cuba_suave_type:")')
    write(unit,'("nnew:
                             ",I10)')
                                        this%nnew
    write(unit,'("flatness: ",I10)')
                                        this%flatness
  end subroutine cuba_suave_print_to_unit
cuba suave get type \( \)
  pure subroutine cuba_suave_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="cuba_suave_type")
  end subroutine cuba_suave_get_type
Überschriebene cuba class Methoden
integrate suave \( \)
  subroutine integrate_suave(this,integrand)
    class(cuba_suave_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
           print '("suave")'
    call suave(&
         this%dim_x, &
         this%dim_f, &
         integrand, &
         this%userdata, &
         this%eps_rel, &
         this%eps_abs, &
         this%flags, &
         this%seed, &
         this%min_eval, &
         this%max_eval, &
```

```
this%nnew, &
         this%flatness, &
         this%nregions, &
         this%neval, &
         this%fail, &
         this%integral, &
         this%error, &
         this%prob)
  end subroutine integrate_suave
integrate suave userdata ↑
   subroutine integrate_suave_userdata(this,integrand,userdata)
    class(cuba_suave_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
    class(transversal_momentum_type),intent(in)::userdata
           print '("suave")'
    call suave(&
         this%dim_x, &
         this%dim_f, &
         integrand, &
         userdata, &
         this%eps_rel, &
         this%eps_abs, &
         this%flags, &
         this%seed, &
         this%min_eval, &
         this%max_eval, &
         this%nnew, &
         this%flatness, &
         this%nregions, &
         this%neval, &
         this%fail, &
         this%integral, &
         this%error, &
         this%prob)
  end subroutine integrate_suave_userdata
cuba suave copy ↑
  subroutine cuba_suave_copy(this,source)
    class(cuba_suave_type),intent(out) :: this
    class(cuba_class),intent(in) :: source
    select type(source)
    class is (cuba_suave_type)
       call this%copy_common(source)
       this%nnew = source%nnew
       this%flatness = source%flatness
    class default
       print *,"cuba_suave_copy: type of source is not type compatible with cuba_suave_type."
    end select
  end subroutine cuba_suave_copy
```

## 12.5.4 Methoden für cuba divonne type

### Überschriebene serializable class Methoden

```
cuba divonne write to marker \( \ \)
  subroutine cuba_divonne_write_to_marker(this,marker,status)
    class(cuba_divonne_type),intent(in) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("cuba_divonne_type")
    call cuba_write_to_marker(this,marker,status)
    call marker%mark("key1",this%key1)
    call marker%mark("key2",this%key2)
    call marker%mark("key3",this%key3)
    call marker%mark("maxpass",this%maxpass)
    call marker%mark("border",this%border)
    call marker%mark("maxchisq",this%maxchisq)
    call marker%mark("mindeviation",this%mindeviation)
    call marker%mark("ngiven",this%ngiven)
    call marker%mark("ldxgiven",this%ldxgiven)
    call marker%mark("nextra",this%nextra)
    call marker%mark("xgiven",this%xgiven)
    call marker%mark_null("cuba_divonne_type")
  end subroutine cuba_divonne_write_to_marker
cuba divonne read from marker \( \ \)
  subroutine cuba_divonne_read_from_marker(this,marker,status)
    class(cuba_divonne_type),intent(out) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("cuba_divonne_type",status=status)
    call cuba_read_from_marker(this,marker,status)
    call marker%pick("key1",this%key1,status)
    call marker%pick("key2",this%key2,status)
    call marker%pick("key3",this%key3,status)
    call marker%pick("maxpass",this%maxpass,status)
    call marker%pick("border",this%border,status)
    call marker%pick("maxchisq",this%maxchisq,status)
    call marker%pick("mindeviation",this%mindeviation,status)
    call marker%pick("ngiven",this%ngiven,status)
    call marker%pick("ldxgiven",this%ldxgiven,status)
    call marker%pick("nextra",this%nextra,status)
    if(allocated(this%xgiven))deallocate(this%xgiven)
    allocate(this%xgiven(this%ldxgiven,this%ngiven))
    call marker%pick("xgiven",this%xgiven,status)
    call marker%pick_end("cuba_divonne_type",status)
  end subroutine cuba_divonne_read_from_marker
cuba divonne print to unit \ \
```

```
subroutine cuba_divonne_print_to_unit(this,unit,parents,components,peers)
    class(cuba_divonne_type),intent(in) :: this
    INTEGER, INTENT(IN) :: unit
    integer(kind=dik),intent(in)::parents,components,peers
    if(parents>0)call cuba_print_to_unit(this,unit,parents-1,components,peers)
    write(unit,'("Components of cuba_divonne_type:")')
    write(unit,'("key1:
                             ",I10)')
                                        this%key1
                             ",I10)')
    write(unit,'("key2:
                                        this%key2
                             ",I10)')
    write(unit,'("key3:
                                        this%key3
    write(unit,'("maxpass:
                             ",I10)')
                                        this%maxpass
    write(unit,'("ngiven:
                             ",I10)')
                                        this%ngiven
                             ",I10)')
    write(unit,'("ldxgiven:
                                        this%ldxgiven
    write(unit,'("nextra:
                             ",I10)')
                                       this%nextra
    write(unit,'("border:
                             ",E10.4)') this%border
    write(unit, '("maxchisq: ",E10.4)') this%maxchisq
    write(unit, '("mindeviation:", E10.4)') this%mindeviation
    write(unit,'("xgiven:
                             ",2(E10.4))') this%xgiven
  end subroutine cuba_divonne_print_to_unit
cuba divonne get type↑
 pure subroutine cuba_divonne_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type, source="cuba_divonne_type")
  end subroutine cuba_divonne_get_type
Überschriebene cuba class Methoden
integrate divonne \( \ \)
  subroutine integrate_divonne(this,integrand)
    class(cuba_divonne_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
           call this%reset_output()
         print '("divonne")'
    call divonne(&
         & this%dim_x, &
         & this%dim_f, &
         & integrand, &
         & this%userdata,&
         & this%eps_rel, &
         & this%eps_abs, &
         & this%flags, &
         & this%seed, &
         & this%min_eval, &
         & this%max_eval, &
         & this%key1, &
         & this%key2, &
         & this%key3, &
         & this%maxpass, &
         & this%border, &
```

```
& this%maxchisq, &
         & this%mindeviation, &
         & this%ngiven, &
         & this%ldxgiven, &
         & this%xgiven, &
         & this%nextra, &
                                           & this%peakfinder, &
         & 0,&
         & this%nregions, &
         & this%neval, &
         & this%fail, &
         & this%integral, &
         & this%error, &
         & this%prob)
  end subroutine integrate_divonne
integrate\_divonne\_userdata \uparrow
subroutine integrate_divonne_userdata(this,integrand,userdata)
    class(cuba_divonne_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
    class(transversal_momentum_type),intent(in)::userdata
           call this%reset_output()
         print '("divonne")'
    call divonne(&
         & this%dim_x, &
         & this%dim_f, &
         & integrand, &
         & userdata,&
         & this%eps_rel, &
         & this%eps_abs, &
         & this%flags, &
         & this%seed, &
         & this%min_eval, &
         & this%max_eval, &
         & this%key1, &
         & this%key2, &
         & this%key3, &
         & this%maxpass, &
         & this%border, &
         & this%maxchisq, &
         & this%mindeviation, &
         & this%ngiven, &
         & this%ldxgiven, &
         & this%xgiven, &
         & this%nextra, &
                                           & this%peakfinder, &
         & 0,&
         & this%nregions, &
         & this%neval, &
         & this%fail, &
```

```
& this%integral, &
         & this%error, &
         & this%prob)
  end subroutine integrate_divonne_userdata
cuba divonne copy \( \)
  subroutine cuba_divonne_copy(this,source)
    class(cuba_divonne_type),intent(out) :: this
    class(cuba_class),intent(in) :: source
    select type(source)
    class is (cuba_divonne_type)
       call this%copy_common(source)
       call this%set_deferred(&
       &source%key1,&
       &source%key2,&
       &source%key3,&
       &source%maxpass,&
       &source%border,&
       &source%maxchisq,&
       &source%mindeviation,&
       &source%xgiven&
       &)
    class default
       print *, "cuba_divonne_copy: type of source is not type compatible with cuba_divonne_type."
    end select
  end subroutine cuba_divonne_copy
cuba divonne set deferred \( \)
  subroutine cuba_divonne_set_deferred&
    (this, key1, key2, key3, maxpass, border, maxchisq, mindeviation, xgiven, xgiven_flat)
    class(cuba_divonne_type) :: this
    integer,optional,intent(in)::key1,key2,key3,maxpass
    real(kind=drk),optional,intent(in)::border,maxchisq,mindeviation
    real(kind=drk), dimension(:,:), optional, intent(in)::xgiven
    real(kind=drk),dimension(:),optional,intent(in)::xgiven_flat
    integer,dimension(2)::s
    if(present(key1))this%key1=key1
    if(present(key2))this%key2=key2
    if(present(key3))this%key3=key3
    if(present(maxpass))this%maxpass=maxpass
    if(present(border))this%border=border
    if(present(maxchisq))this%maxchisq=maxchisq
    if(present(mindeviation))this%mindeviation=mindeviation
    if(present(xgiven))then
       if(allocated(this%xgiven))deallocate(this%xgiven)
       s=shape(xgiven)
       if(s(1)==this%dim_x)then
          allocate(this%xgiven(s(1),s(2)),source=xgiven)
          this%ldxgiven=s(1)
          this%ngiven=s(2)
```

```
else
        print *,"cuba_divonne_set_deferred: shape of xgiven is not [dim_x,:]."
        this%ngiven=0
     end if
  end if
  if(present(xgiven_flat))then
     if(allocated(this%xgiven))deallocate(this%xgiven)
     if(mod(size(xgiven_flat),this%dim_x)==0)then
        this%ngiven=size(xgiven_flat)/this%dim_x
        this%ldxgiven=this%dim_x
        allocate(this%xgiven(this%ldxgiven,this%ngiven),&
                 source=reshape(xgiven_flat,[this%ldxgiven,this%ngiven]))
        print *,"cuba_divonne_set_deferred: size of xgiven_flat is no multiple of dim_x."
        this%ngiven=0
     end if
  end if
end subroutine cuba_divonne_set_deferred
```

## 12.5.5 Methoden für cuba vegas type

Überschriebene serializable class Methoden

```
cuba cuhre write to marker \( \)
  subroutine cuba_cuhre_write_to_marker(this,marker,status)
    class(cuba_cuhre_type),intent(in) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("cuba_cuhre_type")
    call cuba_write_to_marker(this, marker, status)
    call marker%mark("key",this%key)
    call marker%pick_end("cuba_cuhre_type",status)
  end subroutine cuba_cuhre_write_to_marker
cuba cuhre read from marker \( \)
  subroutine cuba_cuhre_read_from_marker(this,marker,status)
    class(cuba_cuhre_type),intent(out) :: this
    class(marker_type), intent(inout) :: marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("cuba_cuhre_type",status=status)
    call cuba_read_from_marker(this,marker,status)
    call marker%pick("key",this%key,status)
    call marker%pick_end("cuba_cuhre_type",status)
  end subroutine cuba_cuhre_read_from_marker
cuba cuhre print to unit \( \ \)
```

```
subroutine cuba_cuhre_print_to_unit(this,unit,parents,components,peers)
    class(cuba_cuhre_type),intent(in) :: this
    integer, intent(in) :: unit
    integer(kind=dik),intent(in)::parents,components,peers
    if(parents>0)call cuba_print_to_unit(this,unit,parents-1,components,peers)
    write(unit, '("Components of cuba_cuhre_type:")')
    write(unit,'("key:
                             ",I10)')
                                        this%key
  end subroutine cuba_cuhre_print_to_unit
cuba cuhre get type↑
  pure subroutine cuba_cuhre_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="cuba_cuhre_type")
  end subroutine cuba_cuhre_get_type
Überschriebene cuba class Methoden
integrate cuhre \( \)
  subroutine integrate_cuhre(this,integrand)
    class(cuba_cuhre_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
    ! c
            print '("cuhre")'
    call cuhre(&
         this%dim_x, &
         this%dim_f, &
         integrand, &
         this%userdata, &
         this%eps_rel, &
         this%eps_abs, &
         this%flags, &
          this%seed, &
         this%min_eval, &
         this%max_eval, &
         this%key, &
         this%nregions, &
         this%neval, &
         this%fail, &
         this%integral, &
         this%error, &
         this%prob)
  end subroutine integrate_cuhre
integrate cuhre userdata ↑
  subroutine integrate_cuhre_userdata(this,integrand,userdata)
    class(cuba_cuhre_type),intent(inout) :: this
    procedure(integrand_interface)::integrand
    class(transversal_momentum_type),intent(in)::userdata
            print '("cuhre")'
    ! c
```

```
call cuhre(&
         this%dim_x, &
         this%dim_f, &
         integrand, &
         userdata, &
         this%eps_rel, &
         this%eps_abs, &
         this%flags, &
!
          this%seed, &
         this%min_eval, &
         this%max_eval, &
         this%key, &
         this%nregions, &
         this%neval, &
         this%fail, &
         this%integral, &
         this%error, &
         this%prob)
  end subroutine integrate_cuhre_userdata
cuba cuhre copy↑
  subroutine cuba_cuhre_copy(this,source)
    class(cuba_cuhre_type),intent(out) :: this
    class(cuba_class),intent(in) :: source
    select type(source)
    class is (cuba_cuhre_type)
       call this%copy_common(source)
       this%key=source%key
    class default
       print *,"cuba_cuhre_copy: type of source is not type compatible with &
       &cuba_cuhre_type."
    end select
  end subroutine cuba_cuhre_copy
cuba cuhre set deferred \uparrow
  subroutine cuba_cuhre_set_deferred(this,key)
    class(cuba_cuhre_type),intent(inout) :: this
    integer, intent(in) :: key
    this%key = key
  end subroutine cuba_cuhre_set_deferred
```

# 13 Modul muli basic

# 13.1 Abhängigkeiten

```
use,intrinsic::iso_fortran_env
use kinds !NODEP!
use iso_varying_string, string_t=>varying_string !NODEP!
```

### 13.2 Parameter

```
! bitmodel parameters
integer, public, parameter::drk=double
integer, public, parameter::dik=i64
integer(kind=dik), public, parameter::one=int(1, kind=dik)
integer(kind=dik),public,parameter::zero=int(0,kind=dik)
! serialization parameters
integer(kind=dik),public,parameter::serialize_page_size=1024
integer(kind=dik),public,parameter::serialize_ok=0000
integer(kind=dik), public, parameter::serialize_syntax_error=1001
integer(kind=dik), public, parameter::serialize_wrong_tag=1002
integer(kind=dik), public, parameter::serialize_wrong_id=1003
integer(kind=dik), public, parameter::serialize_wrong_type=1004
integer(kind=dik), public, parameter::serialize_wrong_name=1005
integer(kind=dik), public, parameter::serialize_no_target=1006
integer(kind=dik), public, parameter::serialize_no_pointer=1007
integer(kind=dik), public, parameter::serialize_wrong_action=1008
integer(kind=dik),public,parameter::serialize_unexpected_content=1009
integer(kind=dik),public,parameter::serialize_null=1010
integer(kind=dik), public, parameter::serialize_nothing=1011
logical, public, parameter::serialize_default_indent=.true.
logical, public, parameter::serialize_default_line_break=.true.
logical, public, parameter::serialize_default_asynchronous=.false.
! private components
integer(kind=dik),private::last_id=0
character(len=*), private, parameter::serialize_integer_characters="-0123456789"
```

# 13.3 Derived Types

# 13.3.1 serializable\_class

```
type, public, abstract::serializable_class
 contains
  procedure(ser_write_if),deferred::write_to_marker
  procedure(ser_read_if),deferred::read_from_marker
  procedure(ser_unit),deferred::print_to_unit
  procedure(ser_type),nopass,deferred::get_type
  procedure,nopass::verify_type=>serializable_verify_type
  procedure::read_target_from_marker=>serializable_read_target_from_marker
  procedure::write_type=>serializable_write_type
  procedure::print=>serializable_print
  procedure::print_error=>serializable_print_error
  procedure::print_all=>serializable_print_all
  procedure::print_little=>serializable_print_little
  procedure::print_parents=>serializable_print_parents
  procedure::print_components=>serializable_print_components
  procedure::print_peers=>serializable_print_peers
  procedure::serialize_to_file=>serializable_serialize_to_file
  procedure::serialize_to_unit=>serializable_serialize_to_unit
  procedure::serialize_to_marker=>serializable_serialize_to_marker
  procedure::deserialize_from_file=>serializable_deserialize_from_file
  procedure::deserialize_from_unit=>serializable_deserialize_from_unit
  procedure::deserialize_from_marker=>serializable_deserialize_from_marker
  generic::serialize=>serialize_to_file,serialize_to_unit,serialize_to_marker
   generic::deserialize=>deserialize_from_file,deserialize_from_unit,deserialize_from_mark
end type serializable_class
```

### 13.3.2 measurable class

```
type,public,abstract,extends(serializable_class)::measurable_class
contains
   procedure(measure_int),public,deferred::measure
end type measurable_class
```

### 13.3.3 identified type

```
type,public,extends(serializable_class)::identified_type
    private
    integer(kind=dik)::id
    type(string_t)::name
contains
    ! overridden serializable_class procedures
    procedure,public::write_to_marker=>identified_write_to_marker
    procedure,public::read_from_marker=>identified_read_from_marker
    procedure,public::print_to_unit=>identified_print_to_unit
    procedure,public;nopass::get_type=>identified_get_type
    procedure,nopass::verify_type=>identified_verify_type
    ! new procedures
    procedure,public::identified_initialize
    procedure,public::get_id=>identified_get_id
```

```
procedure,public::get_name=>identified_get_name
  generic,public::initialize=>identified_initialize
end type identified_type
```

## 13.3.4 unique type

```
type,public,extends(identified_type)::unique_type
    private
    integer(kind=dik)::unique_id

contains
    ! overridden serializable_class procedures
    procedure,public,nopass::get_type=>unique_get_type
    procedure,nopass::verify_type=>unique_verify_type
    procedure,public::write_to_marker=>unique_write_to_marker
    procedure,public::read_from_marker=>unique_read_from_marker
    procedure,public::print_to_unit=>unique_print_to_unit
    ! overridden identified_type procedures
    procedure,public::identified_initialize=>unique_initialize
    ! new procedures
    procedure,public::get_unique_id=>unique_get_unique_id
end type unique_type
```

### 13.3.5 serializable ref type

```
type,private::serializable_ref_type
   private
   integer(kind=dik)::id
   class(serializable_class),pointer::ref=>null()
   class(serializable_ref_type),pointer::next=>null()
   contains
    procedure,public::finalize=>serializable_ref_finalize
end type serializable_ref_type
```

# 13.3.6 position\_stack\_type

```
type::position_stack_type
   private
   integer(kind=dik),dimension(2)::position
   class(position_stack_type),pointer::next=>null()
contains
   procedure,public::push_head=>position_stack_push_head
   procedure,public::push_given=>position_stack_push_given
   procedure,public::position_stack_pop
   procedure,public::position_stack_drop
   procedure,public::nth_position=>position_stack_nth_position
   procedure,public::first=>position_stack_first
   procedure,public::last=>position_stack_last
   procedure,public::range=>position_stack_range
```

```
generic,public::push=>push_head
generic,public::push=>push_given
generic,public::pop=>position_stack_pop
generic,public::push=>position_stack_drop
end type position_stack_type
```

### 13.3.7 page ring type

```
type, public::page_ring_type
  logical::asynchronous=serialize_default_asynchronous
  logical::eof_reached=.false.
  integer::unit=-1
  integer(kind=dik)::ring_size=2
  integer(kind=dik)::action=0
  integer(kind=dik)::eof_int=-1
  integer(kind=dik)::out_unit=output_unit
  integer(kind=dik)::err_unit=error_unit
  integer(kind=dik),dimension(2)::active_pages=[0,-1]
  integer(kind=dik),dimension(2)::eof_pos=[-1,-1]
  type(string_t)::eof_string
  type(position_stack_type)::position_stack
   character(serialize_page_size),dimension(:),allocatable::ring
 contains
   ! read access only procedures:
  procedure,public::open_for_read_access=>page_ring_open_for_read_access
  procedure,public::read_page=>page_ring_read_page
   ! write access only procedures:
  procedure,public::open_for_write_access=>page_ring_open_for_write_access
  procedure,public::flush=>page_ring_flush
  procedure,public::break=>page_ring_break
   ! comparing
  procedure,public::str_equal=>page_ring_str_equal
   ! searching:
  procedure,public::find_pure=>page_ring_find_pure
  generic, public::find=>page_ring_find,page_ring_find_default
   ! positioning:
  procedure, public::set_position=>page_ring_set_position
  procedure,public::turn_page=>page_ring_turn_page
  procedure, public::proceed=>page_ring_proceed
  generic, public::push_position=>push_actual_position,push_given_position
  generic, public::pop_position=>pop_actual_position,pop_given_position
  generic, public::get_position=>page_ring_get_position1,page_ring_get_position2
   ! printing:
  procedure,public::print_to_unit=>page_ring_print_to_unit
  procedure,public::print_ring=>page_ring_print_ring
  procedure,public::print_position=>page_ring_print_position
   ! writing:
  procedure,public::put=>page_ring_put
  generic, public::push=>push_string,push_integer,push_integer_dik,push_double,push_integer
```

```
! reading:
procedure,public::get_character=>page_ring_get_character
procedure, public::allocate_substring=>page_ring_allocate_substring
procedure, public::pop_character=>page_ring_pop_character
procedure, public::pop_by_keys=>page_ring_pop_by_keys
generic, public::substring=>page_ring_substring1,page_ring_substring2
generic, public::substring_by_keys=>page_ring_character_by_keys,page_ring_positions_by_keys
generic, public::pop=>pop_string,pop_integer,pop_integer_dik,pop_double,pop_logical,pop_integer
! misc:
procedure, public::close=>page_ring_close
procedure, public::ring_index=>page_ring_ring_index
! private:
procedure,private::activate_next_page=>page_ring_activate_next_page
procedure,private::enlarge=>page_ring_enlarge
! specific names for generic procedures:
procedure, private::page_ring_substring1
procedure, private::page_ring_substring2
procedure,private::page_ring_character_by_keys
procedure,private::page_ring_positions_by_keys
procedure,private::push_string=>page_ring_push_string
procedure, private::push_integer=>page_ring_push_integer
procedure, private::push_integer_dik=>page_ring_push_integer_dik
procedure,private::push_integer_array=>page_ring_push_integer_array
procedure, private::push_integer_array_dik=>page_ring_push_integer_array_dik
procedure,private::push_double=>page_ring_push_double
procedure, private::push_double_array=>page_ring_push_double_array
procedure,private::pop_string=>page_ring_pop_string
procedure, private::pop_integer=>page_ring_pop_integer
procedure, private::pop_integer_dik=>page_ring_pop_integer_dik
procedure,private::pop_logical=>page_ring_pop_logical
procedure,private::pop_integer_array=>page_ring_pop_integer_array
procedure, private::pop_integer_array_dik=>page_ring_pop_integer_array_dik
procedure, private::pop_double=>page_ring_pop_double
procedure, private::pop_double_array=>page_ring_pop_double_array
procedure, private::page_ring_find
procedure,private::page_ring_find_default
procedure, private::actual_index=>page_ring_actual_index
procedure, private::actual_page=>page_ring_actual_page
procedure, private::actual_offset=>page_ring_actual_offset
procedure,private::actual_position=>page_ring_actual_position
procedure,private::first_index=>page_ring_first_index
procedure,private::first_page=>page_ring_first_page
procedure,private::last_index=>page_ring_last_index
procedure,private::last_page=>page_ring_last_page
procedure, private::push_actual_position=>page_ring_ring_push_actual_position
procedure, private::push_given_position=>page_ring_ring_push_given_position
procedure, private::pop_actual_position=>page_ring_ring_pop_actual_position
procedure, private::pop_given_position=>page_ring_ring_pop_given_position
procedure,private::page_ring_get_position1
procedure, private::page_ring_get_position2
```

```
end type page_ring_type
```

### 13.3.8 marker type

```
type,public,extends(page_ring_type)::marker_type
  private
  integer(kind=dik)::indentation=0
   integer(kind=dik)::n_instances=0
  logical::do break=.true.
   logical::do_indent=.false.
   class(serializable_ref_type), pointer::heap=>null()
   class(serializable_ref_type),pointer::references=>null()
 contains
  procedure::mark_begin=>marker_mark_begin
  procedure::mark_instance_begin=>marker_mark_instance_begin
  procedure::mark_end=>marker_mark_end
  procedure::mark_instance_end=>marker_mark_instance_end
  procedure::mark_logical=>marker_mark_logical
  procedure::mark_integer=>marker_mark_integer
  procedure::mark_integer_array=>marker_mark_integer_array
  procedure::mark_integer_matrix=>marker_mark_integer_matrix
  procedure::mark_integer_dik=>marker_mark_integer_dik
  procedure::mark_integer_array_dik=>marker_mark_integer_array_dik
  procedure::mark_integer_matrix_dik=>marker_mark_integer_matrix_dik
  procedure::mark_double=>marker_mark_double
  procedure::mark_double_array=>marker_mark_double_array
  procedure::mark_double_matrix=>marker_mark_double_matrix
  procedure::mark_string=>marker_mark_string
  procedure::mark_instance=>marker_mark_instance
  procedure::mark_target=>marker_mark_target
  procedure::mark_allocatable=>marker_mark_allocatable
  procedure::mark_pointer=>marker_mark_pointer
  procedure::mark_null=>marker_mark_null
  procedure::mark_nothing=>marker_mark_nothing
  procedure::mark_empty=>marker_mark_empty
  procedure::pick_begin=>marker_pick_begin
  procedure::query_instance_begin=>marker_query_instance_begin
  procedure::pick_instance_begin=>marker_pick_instance_begin
  procedure::pick_end=>marker_pick_end
  procedure::pick_instance_end=>marker_pick_instance_end
  procedure::pick_instance=>marker_pick_instance
  procedure::pick_target=>marker_pick_target
  procedure::pick_allocatable=>marker_pick_allocatable
  procedure::pick_pointer=>marker_pick_pointer
  procedure::pick_logical=>marker_pick_logical
  procedure::pick_integer=>marker_pick_integer
  procedure::pick_integer_array=>marker_pick_integer_array
  procedure::pick_integer_matrix=>marker_pick_integer_matrix
  procedure::pick_integer_dik=>marker_pick_integer_dik
  procedure::pick_integer_array_dik=>marker_pick_integer_array_dik
```

```
procedure::pick_integer_matrix_dik=>marker_pick_integer_matrix_dik
   procedure::pick_double=>marker_pick_double
  procedure::pick_double_array=>marker_pick_double_array
   procedure::pick_double_matrix=>marker_pick_double_matrix
   procedure::pick_string=>marker_pick_string
   generic,public::mark=>mark_logical,&
        mark_integer,mark_integer_array,mark_integer_matrix,&
        mark_integer_dik,mark_integer_array_dik,mark_integer_matrix_dik,&
        mark_double,mark_double_array,mark_double_matrix,mark_string
   generic, public::pick=>pick_logical,&
        pick_integer, pick_integer_array, pick_integer_matrix, &
        pick_integer_dik,pick_integer_array_dik,pick_integer_matrix_dik,&
        pick_double,pick_double_array,pick_double_matrix,pick_string
   procedure::verify_nothing=>marker_verify_nothing
   procedure::indent=>marker_indent
   procedure::push_heap=>marker_push_heap
   procedure::pop_heap=>marker_pop_heap
  procedure::search_heap_by_id=>marker_search_heap_by_id
   procedure::search_heap_by_ref=>marker_search_heap_by_ref
  procedure::push_reference=>marker_push_reference
   procedure::pop_reference=>marker_pop_reference
   procedure::reset_references=>marker_reset_references
  procedure::search_reference=>marker_search_reference
   procedure::reset_heap=>marker_reset_heap
  procedure::finalize=>marker_finalize
   generic::search_heap=>search_heap_by_id
  generic::search_heap=>search_heap_by_ref
end type marker_type
```

### 13.4 Interfaces

```
abstract interface
   elemental function measure int(this)
     import measurable_class
     import drk
     class(measurable_class),intent(in)::this
     real(kind=drk)::measure int
   end function measure int
end interface
interface operator(<)</pre>
   module procedure measurable_less_measurable
   module procedure measurable_less_double
end interface
interface operator(<=)</pre>
   module procedure measurable_less_or_equal_measurable
   module procedure measurable_less_or_equal_double
end interface
interface operator(==)
   module procedure measurable_equal_measurable
```

```
module procedure measurable_equal_double
end interface
interface operator(>=)
  module procedure measurable_equal_or_greater_measurable
  module procedure measurable_equal_or_greater_double
end interface
interface operator(>)
  module procedure measurable_greater_measurable
  module procedure measurable_greater_double
end interface
abstract interface
   subroutine ser_write_if(this,marker,status)
     import serializable_class
     import marker_type
     import dik
     class(serializable_class),intent(in)::this
     class(marker_type),intent(inout)::marker
     integer(kind=dik),intent(out)::status
   end subroutine ser_write_if
end interface
abstract interface
   subroutine ser_read_if(this,marker,status)
     import serializable_class
     import marker_type
     import dik
     class(serializable_class),intent(out)::this
     class(marker_type),intent(inout)::marker
     integer(kind=dik),intent(out)::status
   end subroutine ser_read_if
end interface
abstract interface
   subroutine ser_unit(this, unit, parents, components, peers)
     import serializable_class
     import dik
     class(serializable_class),intent(in)::this
     integer,intent(in)::unit
     integer(kind=dik),intent(in)::parents,components,peers
   end subroutine ser_unit
end interface
abstract interface
  pure subroutine ser_type(type)
     character(:),allocatable,intent(out)::type
   end subroutine ser_type
end interface
interface page_ring_position_is_before
  module procedure &
        page_ring_position_is_before_int_pos,&
        page_ring_position_is_before_pos_pos,&
        page_ring_position_is_before_pos_int
end interface
```

## 13.5 Operators

```
public operator(<),operator(<=),operator(>=),operator(>)
public serialize_print_comp_pointer,serialize_print_peer_pointer&
        &,serialize_print_allocatable
public identified_initialize,identified_print_to_unit&
        &,identified_read_from_marker,identified_write_to_marker

public serializable_deserialize_from_marker
public ilog2,generate_unit,integer_with_leading_zeros
```

# 13.6 Implementierung der Prozeduren

### 13.6.1 Methoden für serializable class

```
serializable verify type \( \)
  elemental logical function serializable_verify_type(type) result(match)
    character(*),intent(in)::type
    match=type=="serializable_class"
  end function serializable_verify_type
serializable read target from marker \( \)
  subroutine serializable_read_target_from_marker(this,marker,status)
    ! This is a dummy procedure. Usually, you dont't need to deserialize targets,
    ! so by implementing this dummy we don"t force all descendants to override this
    ! procedure. Then again this is the only way to read targets from markers.
    class(serializable_class), target, intent(out) :: this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    print *,"serializable_read_target_from_marker:"
    print *, "This is a dummy procedure. Usually, this message indicates a missing overridden &
         &read_target_from_marker TPB for "
    call this%write_type(output_unit)
    print *,""
    call this%read_from_marker(marker,status)
  end subroutine serializable_read_target_from_marker
serializable write type \( \)
  subroutine serializable_write_type(this,unit)
    class(serializable_class),intent(in)::this
    integer, intent(in)::unit
    character(:),allocatable::this_type
    call this%get_type(this_type)
    write(unit,fmt='(a)',advance="no")this_type
  end subroutine serializable_write_type
serializable print \( \)
```

```
recursive subroutine serializable_print(this,parents,components,peers,unit)
    class(serializable_class),intent(in)::this
    integer(kind=dik),intent(in)::parents,components,peers
    integer, optional::unit
    if(present(unit))then
       write(unit,'("")')
       write(unit, '("Instance of type: ")',advance="no")
       call this%write_type(unit)
       write(unit,fmt='("")')
       call this%print_to_unit(unit, parents, components, peers)
    else
       write(output_unit,'("")')
       write(output_unit,'("Instance of type: ")',advance="no")
       call this%write_type(output_unit)
       write(output_unit,fmt='("")')
       call this%print_to_unit(output_unit, parents, components, peers)
    end if
  end subroutine serializable_print
serializable print all \( \ \)
  recursive subroutine serializable_print_all(this,unit)
    class(serializable_class),intent(in)::this
    integer, optional::unit
    if(present(unit))then
       write(unit,'("")')
       write(unit,'("Instance of type: ")',advance="no")
       call this%write_type(unit)
       write(unit,fmt='("")')
       call this%print_to_unit(unit,huge(one),huge(one),huge(one))
    else
       write(output_unit,'("")')
       write(output_unit,'("Instance of type: ")',advance="no")
       call this%write_type(output_unit)
       write(output_unit,fmt='("")')
       call this%print_to_unit(output_unit,huge(one),huge(one))
    end if
  end subroutine serializable_print_all
serializable print little \( \ \)
  recursive subroutine serializable_print_little(this,unit)
    class(serializable_class),intent(in)::this
    integer, optional::unit
    if(present(unit))then
       write(unit,'("")')
       write(unit, '("Instance of type: ")',advance="no")
       call this%write_type(unit)
       write(unit,fmt='("")')
       call this%print_to_unit(unit,zero,zero,zero)
    else
       write(output_unit,'("")')
```

```
write(output_unit,'("Instance of type: ")',advance="no")
       call this%write_type(output_unit)
       write(output_unit,fmt='("")')
       call this%print_to_unit(output_unit,zero,zero,zero)
    end if
  end subroutine serializable_print_little
serializable print parents \( \)
  recursive subroutine serializable_print_parents(this)
    class(serializable_class),intent(in)::this
    write(output_unit,'("")')
    write(output_unit,'("Instance of type: ")',advance="no")
       call this%write_type(output_unit)
       write(output_unit,fmt='("")')
    call this%print_to_unit(output_unit, huge(one), zero, zero)
  end subroutine serializable_print_parents
serializable print components \( \ \)
  recursive subroutine serializable_print_components(this)
    class(serializable_class),intent(in)::this
    write(output_unit,'("")')
    write(output_unit, '("Instance of type: ")', advance="no")
       call this%write_type(output_unit)
       write(output_unit,fmt='("")')
    call this%print_to_unit(output_unit,zero,huge(one),zero)
  end subroutine serializable_print_components
serializable print peers \( \)
  recursive subroutine serializable_print_peers(this)
    class(serializable_class),intent(in)::this
    write(output_unit,'("")')
    write(output_unit, '("Instance of type: ")', advance="no")
       call this%write_type(output_unit)
       write(output_unit,fmt='("")')
    call this%print_to_unit(output_unit,zero,zero,huge(one))
  end subroutine serializable_print_peers
serializable print error \( \)
  recursive subroutine serializable_print_error(this)
    class(serializable_class),intent(in)::this
    call this%print_to_unit(error_unit,zero,zero,zero)
  end subroutine serializable_print_error
serializable serialize to unit \
  subroutine serializable_serialize_to_unit(this, unit, name)
    class(serializable_class),intent(in)::this
    integer, intent(in) :: unit
    character (len=*), intent(in) :: name
```

```
logical::opened
    character(32)::file
         gfortran bug
         character::stream
    character::write
    type(marker_type)::marker
         inquire(unit=unit,opened=opened,stream=stream,write=write)
    inquire(unit=unit,opened=opened,write=write)
    if(opened)then
        if(stream=="Y")then
!
          if(write=="Y")then
             print *,"dummy: serializable_serialize_to_unit"
             stop
          else
             print *, "serializable_serialize_to_unit: cannot write to read-only unit."
Ţ
        else
!
           print *,"serializable_serialize_to_unit: access kind of unit is not 'stream'."
    else
       print *,"serializable_serialize_to_unit: file is not opened."
  end subroutine serializable_serialize_to_unit
serializable serialize to file \( \)
  subroutine serializable_serialize_to_file(this,name,file)
    class(serializable_class),intent(in)::this
    character (len=*), intent(in) :: file,name
    type(marker_type)::marker
    call marker%open_for_write_access(file)
    print *, "serializable_serialize_to_file: writing xml preamble to ",file
    call marker%activate_next_page()
    call marker%push('<?xml version="1.0"?>')
    call marker%mark_begin(tag="file",name=file)
    flush(marker%unit)
    call this%serialize_to_marker(marker,name)
    call marker%mark_end("file")
    call marker%close()
    call marker%finalize()
  end subroutine serializable_serialize_to_file
serializable serialize to marker \( \)
  recursive subroutine serializable_serialize_to_marker(this,marker,name)
    class(serializable_class),intent(in)::this
    class(marker_type),intent(inout)::marker
    character (len=*), intent(in) :: name
    if (marker%action==1) then
       call marker%mark_instance(this,name)
    else
       print *, "serializable_serialize_to_marker: Marker is not ready for write access. STOP
```

```
stop
    end if
  end subroutine serializable_serialize_to_marker
serializable deserialize from unit \uparrow
 subroutine serializable_deserialize_from_unit(this,unit,name)
    class(serializable_class),intent(inout)::this
    integer, intent(in) :: unit
    character (len=*), intent(in) :: name
    logical::opened
         gfortran bug
         character::stream
    character::read
    type(marker_type)::marker
         inquire(unit=unit,opened=opened,stream=stream,read=read)
    inquire(unit=unit,opened=opened,read=read)
    if (opened) then
        if(stream=="Y")then
1
          if(read=="Y")then
             print *,"dummy: serializable_serialize_from_unit"
             stop
             print *,"serializable_serialize_from_unit: cannot write from read-only unit."
          end if
        else
           print *, "serializable_serialize_from_unit: access kind of unit is not 'stream'."
        end if
    else
       print *,"serializable_serialize_from_unit: file is not opened."
  end subroutine serializable_deserialize_from_unit
serializable deserialize from marker \( \)
  subroutine serializable_deserialize_from_marker(this,name,marker)
    class(serializable_class),intent(out)::this
    character(*),intent(in)::name
    class(marker_type),intent(inout)::marker
    integer(kind=dik)::status
    if(marker%action==2)then
       call marker%pick_instance(name,this,status)
       print *, "serializable_deserialize_from_ring: Ring is not ready for read access. STOP."
       stop
    end if
  end subroutine serializable_deserialize_from_marker
serializable deserialize from file \( \)
  subroutine serializable_deserialize_from_file(this,name,file)
    class(serializable_class),intent(out)::this
```

```
character(*),intent(in)::name,file
    type(marker_type)::marker
    integer(kind=dik),dimension(2)::p1,p2
    call marker%open_for_read_access(file,"</file>")
    marker%eof_int=huge(one)
    marker%eof_pos=page_ring_position(marker%eof_int)
    call marker%read_page()
    call marker%find('<?', skip=2, proceed=.true., pos=p1)</pre>
    call marker%find('?>',skip=3,proceed=.false.,pos=p2)
    if((p1(2) \le 0).or.(p2(2) \le 0))then
       print *,"no version substring found."
    end if
    call marker%set_position(p2)
    call marker%find('<file ',skip=4,proceed=.true.,pos=p1)</pre>
    call marker%find('>',skip=1,proceed=.false.,pos=p2)
    if((p1(2)>0).and.(p2(2)>0))then
       call marker%push_position(p2)
       call marker%find('name="',skip=4,proceed=.true.,pos=p1)
       call marker%find('"',skip=1,proceed=.false.,pos=p2)
       call marker%pop_position()
       print *,"no file header found. STOP."
       STOP
    end if
    call this%deserialize_from_marker(name, marker)
    call marker%close()
    call marker%finalize()
  end subroutine serializable_deserialize_from_file
13.6.2 Methoden für identified type
```

Überschriebene serializable class Methoden

```
identified write to marker \( \)
  subroutine identified_write_to_marker(this,marker,status)
    class(identified_type),intent(in)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%mark_begin("identified_type")
    call marker%mark("name",this%get_name())
    call marker%mark("id",this%get_id())
    call marker%mark_end("identified_type")
  end subroutine identified_write_to_marker
identified read from marker \( \)
  subroutine identified_read_from_marker(this,marker,status)
    class(identified_type),intent(out)::this
    class(marker_type),intent(inout)::marker
```

```
integer(kind=dik),intent(out)::status
    character(:),allocatable::name
    call marker%pick_begin("identified_type",status=status)
    call marker%pick("name", name, status)
    call marker%pick("id",this%id,status)
    call marker%pick_end("identified_type",status=status)
    this%name=name
  end subroutine identified_read_from_marker
identified print to unit \( \ \)
  subroutine identified_print_to_unit(this,unit,parents,components,peers)
    class(identified_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    write(unit,'("Components of identified_type:")')
                                     ",a)')this%get_name()
    write(unit,'("Name:
    write(unit,'("ID:
                                     ",I10)')this%get_id()
  end subroutine identified_print_to_unit
identified get type \( \)
  pure subroutine identified_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="identified_type")
  end subroutine identified_get_type
identified verify type \( \)
  elemental logical function identified_verify_type(string)
    character(len=*),intent(in)::string
    identified_verify_type=(string=="identified_type")
  end function identified_verify_type
Originäre identified type Methoden
identified initialize \uparrow
  subroutine identified_initialize(this,id,name)
    class(identified_type),intent(out)::this
    integer(kind=dik),intent(in)::id
    character(len=*),intent(in)::name
    this%name=name
    this%id=id
  end subroutine identified_initialize
identified get id \( \ \)
  elemental function identified_get_id(this) result(id)
    class(identified_type),intent(in)::this
    integer(kind=dik)::id
    id=this%id
  end function identified_get_id
```

```
identified get name \( \)
  pure function identified_get_name(this)
    class(identified_type),intent(in)::this
    character(len(this%name))::identified_get_name
    identified_get_name=char(this%name)
  end function identified_get_name
13.6.3 Methoden für unique type
Überschriebene serializable class Methoden
unique print to unit \
  subroutine unique_print_to_unit(this,unit,parents,components,peers)
    class(unique_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    if(parents>0)call identified_print_to_unit(this,unit,parents-1,components&
         &, peers)
    write(unit,'("Unique ID:
                                   ",I10)')this%get_unique_id()
  end subroutine unique_print_to_unit
unique get type
  pure subroutine unique_get_type(type)
    character(:),allocatable,intent(out)::type
    allocate(type,source="unique_type")
  end subroutine unique_get_type
unique verify type
  elemental logical function unique_verify_type(string)
    character(len=*),intent(in)::string
    unique_verify_type=(string=="unique_type")
  end function unique_verify_type
unique write to marker \( \)
  subroutine unique_write_to_marker(this,marker,status)
```

```
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```

class(unique\_type),intent(in)::this
class(marker\_type),intent(inout)::marker
integer(kind=dik),intent(out)::status
call marker%mark\_begin("unique\_type")

call marker%mark\_end("unique\_type")
end subroutine unique\_write\_to\_marker

unique read from marker \( \)

call identified\_write\_to\_marker(this,marker,status)
call marker%mark("unique\_id",this%get\_unique\_id())

```
subroutine unique_read_from_marker(this,marker,status)
    class(unique_type),intent(out)::this
    class(marker_type),intent(inout)::marker
    integer(kind=dik),intent(out)::status
    call marker%pick_begin("unique_type",status=status)
    call identified_read_from_marker(this,marker,status)
    call marker%pick("unique_id",this%unique_id,status)
    call marker%pick_end("unique_type",status)
  end subroutine unique_read_from_marker
Originäre unique type Methoden
unique initialize \
 subroutine unique_initialize(this,id,name)
    class(unique_type),intent(out)::this
    integer(kind=dik),intent(in)::id
    character(len=*),intent(in)::name
    call identified_initialize(this,id,name)
    last_id=last_id+1
    this%unique_id=last_id
  end subroutine unique_initialize
unique get unique id \
  elemental function unique_get_unique_id(this)
    class(unique_type),intent(in)::this
    integer(kind=dik)::unique_get_unique_id
    unique_get_unique_id=this%unique_id
  end function unique_get_unique_id
13.6.4 Methoden für serializable ref type
serializable ref finalize \( \)
  subroutine serializable ref finalize(this)
    class(serializable_ref_type),intent(inout)::this
    class(serializable_ref_type),pointer::next
    do while (associated(this%next))
       next=>this%next
       this%next=>next%next
       nullify(next%ref)
       deallocate(next)
    end do
    if(associated(this%ref))nullify(this%ref)
  end subroutine serializable_ref_finalize
```

## 13.6.5 Methoden für position stack type

```
position stack push head \( \ \)
  subroutine position_stack_push_head(this)
    class(position_stack_type)::this
    class(position_stack_type),pointer::new
    allocate(new)
    new%next=>this%next
    new%position=this%position
    this%next=>new
  end subroutine position_stack_push_head
position stack push given \( \ \)
  subroutine position_stack_push_given(this,position)
    class(position_stack_type)::this
    integer(kind=dik),dimension(2),intent(in)::position
    class(position_stack_type),pointer::new
    allocate(new)
    new%next=>this%next
    new%position=position
    this%next=>new
  end subroutine position_stack_push_given
position stack pop \( \)
  subroutine position_stack_pop(this)
    class(position_stack_type)::this
    class(position_stack_type),pointer::old
    if(associated(this%next))then
       old=>this%next
       this%next=>old%next
       this%position=old%position
       deallocate(old)
    end if
  end subroutine position_stack_pop
position stack drop \( \ \)
  subroutine position_stack_drop(this,position)
    class(position_stack_type)::this
    integer(kind=dik),dimension(2),intent(out)::position
    class(position_stack_type),pointer::old
    if(associated(this%next))then
       old=>this%next
       this%next=>old%next
       position=old%position
       deallocate(old)
    else
       position=[0,0]
    end if
  end subroutine position_stack_drop
```

```
position stack nth position \( \ \)
 function position_stack_nth_position(this,n) result(position)
    class(position_stack_type),intent(in)::this
    integer(kind=dik),intent(in)::n
    integer(kind=dik),dimension(2)::position
    class(position_stack_type),pointer::tmp
    integer(kind=dik)::pos
    tmp=>this%next
    pos=n
    do while(associated(tmp).and.pos>0)
       tmp=>tmp%next
       pos=pos-1
    end do
    if(associated(tmp))then
      position=tmp%position
    else
       position=[0,0]
    end if
  end function position_stack_nth_position
position stack first \
 function position_stack_first(this) result(position)
    class(position_stack_type),intent(in)::this
    integer(kind=dik),dimension(2)::position,tmp_position
    class(position_stack_type),pointer::tmp_stack
    tmp_position=this%position
    tmp_stack=>this%next
    do while(associated(tmp_stack))
       if(page_ring_position_is_before(tmp_stack%position,tmp_position))then
          tmp_position=tmp_stack%position
       end if
       tmp_stack=>tmp_stack%next
  end function position_stack_first
position stack last \
 function position_stack_last(this) result(position)
    class(position_stack_type),intent(in)::this
    integer(kind=dik),dimension(2)::position,tmp_position
    class(position_stack_type),pointer::tmp_stack
    tmp_position=this%position
    tmp_stack=>this%next
    do while(associated(tmp_stack))
       if(page_ring_position_is_before(tmp_position,tmp_stack%position))then
          tmp_position=tmp_stack%position
       end if
       tmp_stack=>tmp_stack%next
    end do
  end function position_stack_last
```

```
position stack range \( \ \)
  pure function position_stack_range(this) result(position)
    class(position_stack_type),intent(in)::this
    integer(kind=dik),dimension(2)::position
    class(position_stack_type),pointer::tmp
  end function position_stack_range
13.6.6 Methoden für page ring type
page ring open for read access \
  subroutine page_ring_open_for_read_access(this,file,eof_string,asynchronous)
    class(page_ring_type),intent(inout)::this
    character(*),intent(in)::file,eof_string
    logical,intent(in),optional::asynchronous
    logical::exist
    this%eof_string=eof_string
    inquire(file=file,exist=exist)
    if(exist)then
       this%action=2
    else
       print *,"page_ring_open: File ",file," is opened for read access but &
       &does not exist. STOP."
       STOP
    end if
    if(present(asynchronous))this%asynchronous=asynchronous
    if(this%unit<0)call generate_unit(this%unit,100,1000)</pre>
    if(this%unit<0)then
       print *,"page_ring_open: No free unit found. STOP."
       STOP
    end if
    this%ring_size=2
    call this%set_position([zero,one])
    this%active_pages=[zero,-one]
    if(allocated(this%ring))deallocate(this%ring)
    allocate(this%ring(zero:this%ring_size-one))
    if (this % asynchronous) then
       open(this%unit,&
            file=file,&
            access="stream",&
            action="read",&
            asynchronous="yes",&
            status="old")
    else
       open(this%unit,&
            file=file,&
            access="stream",&
            action="read",&
```

```
asynchronous="no", &
            status="old")
    end if
    call this%read_page()
  end subroutine page_ring_open_for_read_access
page ring open for write access \
  subroutine page_ring_open_for_write_access(this,file,asynchronous)
    class(page_ring_type),intent(inout)::this
    character(*),intent(in)::file
    logical,intent(in),optional::asynchronous
    this%action=1
    if(present(asynchronous))this%asynchronous=asynchronous
    if(this%unit<0)call generate_unit(this%unit,100,1000)</pre>
    if(this%unit<0)then
       print *,"page_ring_open: No free unit found. STOP."
       STOP
    end if
    this%ring_size=2
    call this%set_position([zero,one])
    this%active_pages=[zero,-one]
    if(allocated(this%ring))deallocate(this%ring)
    allocate(this%ring(zero:this%ring_size-one))
    if(this%asynchronous)then
       open(this%unit,&
            file=file,&
            access="stream",&
            action="write",&
            asynchronous="yes",&
            status="replace")
    else
       open(this%unit,&
            file=file,&
            access="stream",&
            action="write",&
            asynchronous="no", &
            status="replace")
    end if
  end subroutine page_ring_open_for_write_access
page ring close \
 subroutine page_ring_close(this)
    class(page_ring_type),intent(inout)::this
    if(this%action==1)then
       call this%flush()
       !call this%print_position()
       if (this%asynchronous) then
          write(this%unit,asynchronous="yes")&
```

```
&this%ring(this%actual_index())(:this%actual_offset()-1)
       else
          write(this%unit,asynchronous="no")&
               &this%ring(this%actual_index())(:this%actual_offset()-1)
       end if
    end if
    close(this%unit)
  end subroutine page_ring_close
page ring read page \( \)
  subroutine page_ring_read_page(this)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik)::iostat
    character(8)::iomsg
    if(.not.this%eof_reached)then
       call page_ring_activate_next_page(this)
       read(this%unit,iostat=iostat)this%ring(this%last_index())
       if(iostat==iostat_end)then
          this%eof_reached=.true.
          this%eof_pos(1)=this%last_page()
          this%eof_pos(2)=index(this%ring(this%last_index()),char(this%eof_string))
          this%eof_pos(2)=this%eof_pos(2)+len(this%eof_string)-1
          this%eof_int=page_ring_ordinal(this%eof_pos)
       end if
    end if
  end subroutine page_ring_read_page
page ring enlarge \( \ \)
  subroutine page_ring_enlarge(this)
    class(page_ring_type),intent(inout)::this
    character(serialize_page_size),dimension(:),allocatable::tmp_ring
    integer(kind=dik)::n
    call move_alloc(this%ring,tmp_ring)
    allocate(this%ring(0:this%ring_size*2-1))
    do n=this%active_pages(1),this%active_pages(2)
       this%ring(mod(n,this%ring_size*2))=tmp_ring(mod(n,this%ring_size))
    end do
    this%ring_size=this%ring_size*2
  end subroutine page_ring_enlarge
page ring print to unit \( \ \)
  subroutine page_ring_print_to_unit(this,unit,parents,components,peers)
    class(page_ring_type),intent(in)::this
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    write(unit,'("Components of page_ring_type:")')
    print *,"asynchronous: ",this%asynchronous
    print *,"eof reached: ",this%eof_reached
    print *,"ring_size:
                          ",this%ring_size
```

```
print *,"unit:
                           ",this%unit
                           ",this%action
    print *,"action:
    print *,"position:
                           ",this%position_stack%position
    print *,"active_pages: ",this%active_pages
    print *,"file size:
                           ",this%eof_int
    print *,"eof position: ",this%eof_pos
                           ",char(this%eof_string)
    print *,"eof string:
    if(allocated(this%ring))then
       print *,"Ring is allocated."
       if(components>0)call this%print_ring(unit)
    else
       print *,"Ring is not allocated."
    end if
  end subroutine page_ring_print_to_unit
page ring print ring \( \)
  subroutine page_ring_print_ring(this,unit)
    class(page_ring_type),intent(in)::this
    integer,intent(in)::unit
    integer(kind=dik)::n
    write(unit,fmt=*)"Begin of page ring"
    do n=this%active_pages(1),this%active_pages(2)
       write(unit=unit,fmt="('(',I0,')',a)")n,this%ring(mod(n,this%ring_size))
    end do
    write(unit,fmt=*)"End of page ring"
  end subroutine page_ring_print_ring
page ring push string \( \ \)
  recursive subroutine page_ring_push_string(this,string)
    class(page_ring_type),intent(inout)::this
    character(*),intent(in)::string
    integer(kind=dik)::cut,1
    l=len(string)
    if(l<=serialize_page_size-this%actual_offset()+1)then</pre>
       this%ring(this%actual_index())(this%actual_offset():this%actual_offset()+1-1)=string
       if(l==serialize_page_size-this%actual_offset()+1)then
          call this%break()
          call this%flush()
          call this%proceed(1)
       end if
       cut=serialize_page_size-this%actual_offset()+1
       call this%push_string(string(:cut))
       call this%push_string(string(cut+1:))
    end if
  end subroutine page_ring_push_string
page ring push integer dik \
```

```
recursive subroutine page_ring_push_integer_dik(this,int)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),intent(in)::int
    integer(kind=dik)::int1
    if(int<0)then
       call this%push("-")
       call page_ring_push_integer_dik(this,-int)
    else
       if(int>9)call this%push(int/10)
       int1=mod(int,10*one)
       select case (int1)
       case (0)
          call this%push("0")
       case (1)
          call this%push("1")
       case (2)
          call this%push("2")
       case (3)
          call this%push("3")
       case (4)
          call this%push("4")
       case (5)
          call this%push("5")
       case (6)
          call this%push("6")
       case (7)
          call this%push("7")
       case (8)
          call this%push("8")
       case (9)
          call this%push("9")
       end select
  end subroutine page_ring_push_integer_dik
page ring push integer \( \ \)
  subroutine page_ring_push_integer(this,in)
    class(page_ring_type),intent(inout)::this
    integer,intent(in)::in
    call page_ring_push_integer_dik(this,int(in,kind=dik))
  end subroutine page_ring_push_integer
page ring pop integer \( \)
  subroutine page_ring_pop_integer(this,in)
    class(page_ring_type),intent(inout)::this
    integer,intent(out)::in
    integer(kind=dik)::in_dik
    call page_ring_pop_integer_dik(this,in_dik)
    in=int(in_dik)
  end subroutine page_ring_pop_integer
```

```
page ring pop integer dik †
 subroutine page_ring_pop_integer_dik(this,int)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),intent(out)::int
    integer(kind=dik)::int1
    integer(kind=dik)::sign
    character::c
    int=0
    sign=1
    c=" "
    do while(scan(c,serialize_integer_characters)==0)
       call this%pop_character(c)
    end do
    if(c=="-")then
       sign=-1
       call this%pop_character(c)
    end if
    do while(scan(c,serialize_integer_characters)>0)
       int=int*10
       select case (c)
       case ("1")
          int=int+1
       case ("2")
          int=int+2
       case ("3")
          int=int+3
       case ("4")
          int=int+4
       case ("5")
          int=int+5
       case ("6")
          int=int+6
       case ("7")
          int=int+7
       case ("8")
          int=int+8
       case ("9")
          int=int+9
       end select
       call this%pop_character(c)
    end do
    int=int*sign
    if(c=="<")call this%proceed(-one)</pre>
  end subroutine page_ring_pop_integer_dik
page\_ring\_pop \ logical \uparrow
 subroutine page_ring_pop_logical(this,1)
    class(page_ring_type),intent(inout)::this
    logical,intent(out)::1
```

```
character(1)::lc
    call this%pop(lc)
    do while(scan(lc,"tTfF")==0)
       call this%pop(lc)
    end do
    read(lc,fmt="(11)")1
  end subroutine page_ring_pop_logical
page ring push integer array dik \
  subroutine page_ring_push_integer_array_dik(this,int)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),dimension(:),intent(in)::int
    integer(kind=dik)::n
    do n=1,size(int)
       call this%push(int(n))
       call this%push(" ")
  end subroutine page_ring_push_integer_array_dik
page ring push integer array \( \)
  subroutine page_ring_push_integer_array(this,int)
    class(page_ring_type),intent(inout)::this
    integer,dimension(:),intent(in)::int
    integer::n
    do n=1,size(int)
       call this%push(int(n))
       call this%push(" ")
    end do
  end subroutine page_ring_push_integer_array
page ring pop integer array \( \)
  subroutine page_ring_pop_integer_array(this,int)
    class(page_ring_type),intent(inout)::this
    integer,dimension(:),intent(out)::int
    integer::n
    do n=1,size(int)
       call this%pop(int(n))
    end do
  end subroutine page_ring_pop_integer_array
page\_ring\_pop\_integer \ array \ dik \uparrow
   subroutine page_ring_pop_integer_array_dik(this,int)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),dimension(:),intent(out)::int
    integer(kind=dik)::n
    do n=1,size(int)
       call this%pop(int(n))
    end do
  end subroutine page_ring_pop_integer_array_dik
```

```
page ring push double \( \ \)
  subroutine page_ring_push_double(this,dou)
    class(page_ring_type),intent(inout)::this
    real(kind=drk),intent(in)::dou
    integer(kind=dik)::f
     print *,"page_ring_push_double: ",dou
    if(dou==0D0)then
       call this%push("0")
    else
       f=int(scale(fraction(dou),digits(dou)),kind=dik)
       call this%push(digits(dou))
       call this%push(":")
       call this%push(f)
       call this%push(":")
       call this%push(exponent(dou))
    end if
    call this%push(" ")
  end subroutine page_ring_push_double
page ring push double array \( \)
  subroutine page_ring_push_double_array(this,dou)
    class(page_ring_type),intent(inout)::this
    real(kind=drk), dimension(:), intent(in)::dou
    integer(kind=dik)::n
    do n=1,size(dou)
       call this%push(dou(n))
    end do
  end subroutine page_ring_push_double_array
page ring pop double \( \ \)
  subroutine page_ring_pop_double(this,dou,skip)
    class(page_ring_type),intent(inout)::this
    real(kind=drk),intent(out)::dou
    logical, optional, intent(in)::skip
    integer(kind=dik)::d,f,e
    call this%pop(d)
    if(d==zero)then
       dou=0D0
    else
       call this%pop(f)
       call this%pop(e)
       dou=set_exponent(scale(real(f,kind=double),-d),e)
    end if
    if(present(skip))then
       if(.not.skip)call this%proceed(-one)
    end if
  end subroutine page_ring_pop_double
page_ring_pop double array \( \)
```

```
subroutine page_ring_pop_double_array(this,dou,skip)
    class(page_ring_type),intent(inout)::this
    real(kind=drk),dimension(:),intent(out)::dou
    logical,optional,intent(in)::skip
    integer(kind=dik)::n
    call this%pop_double(dou(1))
    do n=2, size(dou)
       call this%pop_double(dou(n))
    end do
    if(present(skip))then
       if(.not.skip)call this%proceed(-one)
    end if
  end subroutine page_ring_pop_double_array
page ring pop character \( \ \)
  subroutine page_ring_pop_character(this,c)
    class(page_ring_type),intent(inout)::this
    character,intent(out)::c
    c=this%ring(this%actual_index())(this%actual_offset():this%actual_offset())
    if(this%actual_offset()==serialize_page_size)call this%read_page
    call this%proceed(one)
  end subroutine page_ring_pop_character
page ring pop string \( \ \)
  recursive subroutine page_ring_pop_string(this,res)
    class(page_ring_type),intent(inout)::this
    character(len=*),intent(out)::res
    integer(kind=dik)::n,cut
    n=len(res)
    cut=serialize_page_size-this%actual_offset()+1
    if(n<=cut)then
       res=this%ring(this%actual_index())(this%actual_offset():this%actual_offset()+n)
       if(n==cut)then
          call this%read_page
       end if
       call this%proceed(n)
    else
       call page_ring_pop_string(this,res(:cut))
       call page_ring_pop_string(this,res(cut+1:))
    end if
  end subroutine page_ring_pop_string
page ring substring2 \(\gamma\)
  pure function page_ring_substring2(this,i1,i2) result(res)
    class(page_ring_type),intent(in)::this
    integer(kind=dik),dimension(2),intent(in)::i1,i2
    character(ring_position_metric2(i1,i2))::res
    integer(kind=dik)::page,pos
    if(i1(1)==i2(1))then
```

```
res=this%ring(mod(i1(1),this%ring_size))(i1(2):i2(2))
    else
       pos=serialize_page_size-i1(2)
       res(1:pos+1)=this%ring(mod(i1(1),this%ring_size))(i1(2):)
       do page=i1(1)+1,i2(1)-1
          res(pos+2:pos+2+serialize_page_size)=this%ring(mod(page,this%ring_size))
          pos=pos+serialize_page_size
       res(pos+2:pos+1+i2(2))=this%ring(mod(page,this%ring_size))(1:i2(2))
  end function page_ring_substring2
page ring substring1 \(\frac{1}{2}\)
  pure function page_ring_substring1(this,i) result(res)
    class(page_ring_type),intent(in)::this
    integer(kind=dik), dimension(2,2), intent(in)::i
    character(ring_position_metric1(i))::res
    integer(kind=dik)::page,pos
    if(i(1,1)==i(1,2))then
       res=this%ring(mod(i(1,1),this%ring_size))(i(2,1):i(2,2))
    else
       pos=serialize_page_size-i(2,1)
       res(1:pos+1)=this\%ring(mod(i(1,1),this\%ring_size))(i(2,1):)
       do page=i(1,1)+1,i(1,1)-1
          res(pos+2:pos+2+serialize_page_size)=this%ring(mod(page,this%ring_size))
          pos=pos+serialize_page_size
       res(pos+2:pos+1+i(2,2))=this\%ring(mod(page,this\%ring_size))(1:i(2,2))
  end function page_ring_substring1
page ring allocate substring \( \)
  subroutine page_ring_allocate_substring(this,p1,p2,string)
    class(page_ring_type),intent(in)::this
    integer(kind=dik), dimension(2), intent(in)::p1,p2
    character(:),allocatable,intent(out)::string
    string=page_ring_substring2(this,p1,p2)
  end subroutine page_ring_allocate_substring
page ring find default \( \ \)
  subroutine page_ring_find_default(this,exp,skip,proceed,pos)
    class(page_ring_type),intent(inout)::this
    character(*),optional,intent(in)::exp
    integer,intent(in)::skip
    logical, intent(in)::proceed
    integer(kind=dik),dimension(2),intent(out)::pos
    call page_ring_find(this,exp,this%position_stack%position,this%eof_pos,skip,proceed,pos)
  end subroutine page_ring_find_default
page ring find \
```

```
recursive subroutine page_ring_find(this,exp,start,limit,skip,proceed,pos)
  class(page_ring_type),intent(inout)::this
  integer(kind=dik),dimension(2),intent(in)::start
  integer(kind=dik), dimension(2), intent(in)::limit
  character(*),intent(in)::exp
  integer,intent(in)::skip
  logical,intent(in)::proceed
  integer(kind=dik),dimension(2),intent(out)::pos
  integer(kind=dik)::page,page2,ind
  page=this%ring_index(start(1))
  if(limit(1)==start(1))then
     ind=index(this%ring(page)(start(2):limit(2)),exp)
     if(ind>0)then
        select case (skip)
        case(1)
           pos=[start(1),start(2)+ind-2]
           if(pos(2)==0)then
              pos(1) = pos(1) - 1
              pos(2)=serialize_page_size
           end if
        case(2)
           pos=[start(1),start(2)+ind-1]
        case(3)
           pos=[start(1),start(2)+ind+len(exp)-2]
        case(4)
           pos=[start(1),start(2)+ind+len(exp)-1]
           if(pos(1)==this%last_page())call this%read_page()
           if(pos(2)>serialize_page_size)then
              pos(1) = pos(1) + 1
              pos(2)=pos(2)-serialize_page_size
           end if
        end select
        if(proceed)call this%set_position(pos)
        print *,"page_ring_find: limit reached."
        pos=[-1,-1]
     end if
  else
     ind=index(this%ring(page)(start(2):),exp)
     if(ind>0)then
        select case (skip)
        case(1)
           pos=[start(1),start(2)+ind-2]
           if(pos(2)==0)then
              pos(1) = pos(1) - 1
              pos(2)=serialize_page_size
           end if
        case(2)
           pos=[start(1),start(2)+ind-1]
        case(3)
           pos=[start(1),start(2)+ind+len(exp)-2]
```

```
pos=[start(1),start(2)+ind+len(exp)-1]
             if(pos(1)==this%last_page())call this%read_page()
             if(pos(2)>serialize_page_size)then
                pos(1)=pos(1)+1
                pos(2) = one
             end if
          end select
          if(proceed)call this%set_position(pos)
       else
          if(start(1)+1>this%active_pages(2))then
             call this%read_page()
             page=this%ring_index(start(1))
          end if
          page2=this%ring_index(start(1)+1)
          ind=index(this%ring(page)(serialize_page_size-len(exp)+1:)&
                    //this%ring(page2)(:len(exp)),exp)
          if(ind>0)then
             select case (skip)
             case(1)
                pos=[start(1), serialize_page_size-len(exp)+ind-1]
                pos=[start(1), serialize_page_size-len(exp)+ind]
             case(3)
                pos=[start(1)+1,ind-1]
             case(4)
                pos=[start(1)+1,ind]
             end select
             if(pos(2)>serialize_page_size)then
                pos(1)=pos(1)+1
                pos(2)=pos(2)-serialize_page_size
             else
                if(pos(2)<0)then
                   pos(1) = pos(1) - 1
                   pos(2)=pos(2)+serialize_page_size
                end if
             end if
             if(proceed)call this%set_position(pos)
             if(proceed)this%active_pages(1)=this%active_pages(2)
             call page_ring_find(this,exp,[start(1)+one,one],limit,skip,proceed,pos)
          end if
       end if
  end subroutine page_ring_find
page ring str equal \( \ \)
 pure logical function page_ring_str_equal(this,string,pos)
    class(page_ring_type),intent(in)::this
    character(*),intent(in)::string
```

case(4)

```
integer(kind=dik),dimension(2,2),intent(in)::pos
    page_ring_str_equal=string==this%substring(pos)
  end function page_ring_str_equal
page ring find pure \( \ \)
  pure recursive function page_ring_find_pure(this,exp,start,limit,skip) result(pos)
    class(page_ring_type),intent(in)::this
    integer(kind=dik),dimension(2),intent(in)::start
    integer(kind=dik), dimension(2), intent(in)::limit
    character(*),intent(in)::exp
    integer,optional,intent(in)::skip
    integer(kind=dik),dimension(2)::pos
    integer(kind=dik)::page,page2,ind,actual_skip
    ! Is the starting point before limit?
    if(start(1)<=limit(1))then
       ! Default skip is what you expect from the build-in index function
       if(present(skip))then
          actual_skip=skip
       else
          actual_skip=2
       end if
       page=mod(start(1),this%ring_size)
       ! Does the scanning region end on the page?
       if(start(1)==limit(1))then
          ind=index(this%ring(page)(start(2):limit(2)),exp)
          ind=index(this%ring(page)(start(2):),exp)
       end if
       if(ind>0)then
          ! substring found on first page
          select case (actual_skip)
          case(1)
             pos=[start(1),start(2)+ind-2]
             if(pos(2)==0)then
                pos(1) = pos(1) - 1
                pos(2)=serialize_page_size
             end if
          case(2)
             pos=[start(1),start(2)+ind-1]
          case(3)
             pos=[start(1),start(2)+ind+len(exp)-2]
          case(4)
             pos=[start(1),start(2)+ind+len(exp)-1]
             if(pos(2)>serialize_page_size)then
                pos(1) = pos(1) + 1
                pos(2)=pos(2)-serialize_page_size
             end if
          end select
       else
          ! Substring not found on first page. Is the next page already read?
```

```
if((start(1)>=limit(1)).or.(start(1)+1>this%active_pages(2)))then
             ! Either the limit is reached or the next page is not ready.
             pos=[0,0]
          else
             ! The next page is available.
             page2=mod(start(1)+1,this%ring_size)
             ! We concatenate the edges. When I is the length of exp, then we want to concat
             ! the 1-1 last characters of page one and the first 1 characters of page two.
             ind=index(this%ring(page)(serialize_page_size-len(exp)+2:)&
                       //this%ring(page2)(:len(exp)),exp)
             if(ind>0)then
                select case (actual_skip)
                case(1)
                   pos=[start(1),serialize_page_size-len(exp)+ind]
                case(2)
                   pos=[start(1),serialize_page_size-len(exp)+ind+1]
                   pos=[start(1)+1,ind]
                case(4)
                   pos=[start(1)+1,ind+1]
                end select
             else
                ! EXP is not found in the overlap region. We recursively search the next pages.
                pos=page_ring_find_pure(this,exp,[start(one)+one,one],limit,skip)
             end if
          end if
       end if
    else
       ! limit is before start
       pos=[0,0]
    end if
  end function page_ring_find_pure
page ring positions by keys \( \)
 pure recursive subroutine page_ring_positions_by_keys&
    (this, exp1, exp2, start, limit, inclusive, length, pos)
    class(page_ring_type),intent(in)::this
    character(*),intent(in)::exp1,exp2
    integer(kind=dik),dimension(2),intent(in)::start,limit
    logical,optional,intent(in)::inclusive
    integer(kind=dik),intent(out),optional::length
    integer(kind=dik),dimension(2,2),intent(out)::pos
    if (inclusive) then
       pos(1:2,1)=this%find_pure(exp1,start,limit,2)
       pos(1:2,1)=this%find_pure(exp1,start,limit,4)
    end if
    !print *,pos1
    if(present(length))then
       length=0
```

```
end if
    if(pos(2,1)>0)then
       if (inclusive) then
          pos(1:2,2)=this\%find\_pure(exp2,pos(1:2,1),limit,3)
       else
          pos(1:2,2)=this%find_pure(exp2,pos(1:2,1),limit,1)
       end if
       !print *,pos2
       if(pos(2,2)>0)then
          if(present(length))then
             length=ring_position_metric1(pos)
          end if
       end if
    end if
  end subroutine page_ring_positions_by_keys
page ring character by keys \( \)
  pure recursive subroutine page_ring_character_by_keys&
    (this, exp1, exp2, start, limit, inclusive, length, string)
    class(page_ring_type),intent(in)::this
    character(*),intent(in)::exp1,exp2
    integer(kind=dik),dimension(2),intent(in)::start,limit
    logical, optional, intent(in)::inclusive
    integer(kind=dik),intent(out),optional::length
    character(:),allocatable,intent(out)::string
    integer(kind=dik), dimension(2,2)::pos
    call this%substring_by_keys(exp1,exp2,start,limit,inclusive,length,pos)
    string=this%substring(pos(:,1),pos(:,2))
  end subroutine page_ring_character_by_keys
page ring pop by keys \( \ \)
  subroutine page_ring_pop_by_keys(this,start,stop,inclusive,res)
    class(page_ring_type),intent(inout)::this
    character(*),intent(in),optional::start
    character(*),intent(in)::stop
    logical,optional,intent(in)::inclusive
    character(len=*),intent(out)::res
    integer(kind=dik),dimension(2)::i1,i2
    if (inclusive) then
       call this%find(start,2,.true.,i1)
       call this%find(stop,3,.false.,i2)
    else
       call this%find(start,4,.true.,i1)
       call this %find(stop, 1, .false., i2)
    end if
    res=this%substring(i1,i2)
    call this%set_position(i2)
  end subroutine page_ring_pop_by_keys
page ring get character \( \)
```

```
elemental function page_ring_get_character(this)
    class(page_ring_type),intent(in)::this
    character::page_ring_get_character
    page_ring_get_character=&
     this%ring(this%actual_index())(this%actual_offset():this%actual_offset())
  end function page_ring_get_character
page ring break \
  subroutine page_ring_break(this)
    class(page_ring_type),intent(inout)::this
    if(this%actual_page()>=this%active_pages(2))call this%activate_next_page()
    call this%turn_page()
  end subroutine page_ring_break
page_ring_turn_page ↑
  subroutine page_ring_turn_page(this)
    class(page_ring_type),intent(inout)::this
    this%position_stack%position(1)=this%position_stack%position(1)+1
    this%position_stack%position(2)=1
  end subroutine page_ring_turn_page
page ring flush \
  subroutine page_ring_flush(this)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik)::page
    do while(this%active_pages(1)<this%actual_page())</pre>
       if (this%asynchronous) then
          write(this%unit,asynchronous="yes")this%ring(mod(this%active_pages(1),this%ring_size))
       else
          write(this%unit,asynchronous="no")this%ring(mod(this%active_pages(1),this%ring_size))
       this%active_pages(1)=this%active_pages(1)+1
    end do
  end subroutine page_ring_flush
page ring activate next page \( \)
  subroutine page_ring_activate_next_page(this)
    class(page_ring_type),intent(inout)::this
    if(this%active_pages(2)-this%active_pages(1)+1>=this%ring_size)call this%enlarge
    this%active_pages(2)=this%active_pages(2)+1
  end subroutine page_ring_activate_next_page
page ring set position \( \ \)
  subroutine page_ring_set_position(this,pos)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),dimension(2),intent(in)::pos
    this%position_stack%position=pos
  end subroutine page_ring_set_position
```

```
page ring put \( \ \)
  subroutine page_ring_put(this)
    class(page_ring_type),intent(inout)::this
  end subroutine page_ring_put
page ring proceed \( \)
  subroutine page_ring_proceed(this,n,deactivate)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),intent(in)::n
    logical,intent(in),optional::deactivate
    integer(kind=dik)::offset
    offset=this%position_stack%position(2)+n
    do while (offset>serialize_page_size)
       if(this%position_stack%position(1)&
          >=this%active_pages(2))call this%activate_next_page()
       this%position_stack%position(1)=this%position_stack%position(1)+1
       offset=offset-serialize_page_size
    this%position_stack%position(2)=offset
    if(present(deactivate))then
       if(deactivate)this%active_pages(1)=this%actual_page()
  end subroutine page_ring_proceed
page ring print position \( \ \)
  subroutine page_ring_print_position(this)
    class(page_ring_type),intent(inout)::this
    print *,&
         this%actual_position(),&
         this%ring(this%actual_index())(:this%actual_offset()-1),&
         this%ring(this%actual_index())(this%actual_offset():)
  end subroutine page_ring_print_position
page ring ring index \( \ \)
  elemental integer(kind=dik) function page_ring_ring_index(this,n)
    class(page_ring_type),intent(in)::this
    integer(kind=dik),intent(in)::n
    page_ring_ring_index=mod(n,this%ring_size)
  end function page_ring_ring_index
page ring ring push given position \( \ \)
  subroutine page_ring_ring_push_given_position(this,pos)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),dimension(2),intent(in)::pos
    call this % position_stack % push (pos)
  end subroutine page_ring_ring_push_given_position
page ring ring pop actual position \( \)
```

```
subroutine page_ring_ring_pop_actual_position(this)
    class(page_ring_type),intent(inout)::this
    call this%position_stack%pop()
  end subroutine page_ring_ring_pop_actual_position
page ring ring push actual position \( \ \)
  subroutine page_ring_ring_push_actual_position(this)
    class(page_ring_type),intent(inout)::this
    call this%position_stack%push()
  end subroutine page_ring_ring_push_actual_position
page ring ring pop given position \( \ \)
  subroutine page_ring_ring_pop_given_position(this,pos)
    class(page_ring_type),intent(inout)::this
    integer(kind=dik),dimension(2),intent(out)::pos
    call this%position_stack%pop(pos)
  end subroutine page_ring_ring_pop_given_position
page ring get position1 \( \ \)
  pure subroutine page_ring_get_position1(this,pos)
    class(page_ring_type),intent(in)::this
    integer(kind=dik),intent(out)::pos
    pos=page_ring_ordinal(this%position_stack%position)
  end subroutine page_ring_get_position1
page ring get position2 \(\frac{1}{2}\)
  pure subroutine page_ring_get_position2(this,pos)
    class(page_ring_type),intent(in)::this
    integer(kind=dik),dimension(2),intent(out)::pos
    pos=this%position_stack%position
  end subroutine page_ring_get_position2
page ring actual index \( \)
  elemental integer(kind=dik) function page_ring_actual_index(this)
    class(page_ring_type),intent(in)::this
    page_ring_actual_index=mod(this%position_stack%position(1),this%ring_size)
  end function page_ring_actual_index
page ring actual page ↑
  elemental integer(kind=dik) function page_ring_actual_page(this)
    class(page_ring_type),intent(in)::this
    page_ring_actual_page=this%position_stack%position(1)
  end function page_ring_actual_page
page ring actual offset \
```

```
elemental integer(kind=dik) function page_ring_actual_offset(this)
    class(page_ring_type),intent(in)::this
    page_ring_actual_offset=this%position_stack%position(2)
  end function page_ring_actual_offset
page ring actual position \( \ \)
  pure function page_ring_actual_position(this)
    class(page_ring_type),intent(in)::this
    integer(kind=dik),dimension(2)::page_ring_actual_position
    page_ring_actual_position=this%position_stack%position
  end function page_ring_actual_position
page ring first index \( \)
  elemental integer(kind=dik) function page_ring_first_index(this)
    class(page_ring_type),intent(in)::this
    page_ring_first_index=mod(this%active_pages(1),this%ring_size)
  end function page_ring_first_index
page ring first page \( \)
  elemental integer(kind=dik) function page_ring_first_page(this)
    class(page_ring_type),intent(in)::this
    page_ring_first_page=this%active_pages(1)
  end function page_ring_first_page
page ring last index \( \ \)
  elemental integer(kind=dik) function page_ring_last_index(this)
    class(page_ring_type),intent(in)::this
    page_ring_last_index=mod(this%active_pages(2),this%ring_size)
  end function page_ring_last_index
page ring last page \( \)
  elemental integer(kind=dik) function page_ring_last_page(this)
    class(page_ring_type),intent(in)::this
    page_ring_last_page=this%active_pages(2)
  end function page_ring_last_page
13.6.7 Methoden für marker type
marker mark begin \
  subroutine marker_mark_begin(this,tag,type,name,target,pointer,shape)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::tag
    character(*),intent(in),optional::type,name
    integer(kind=dik),intent(in),optional::target,pointer
    integer,intent(in),dimension(:),optional::shape
    call this%indent()
    call this%push("<")</pre>
```

```
call this%push(tag)
    if(present(type))call this%push(' type="',//type//'"')
    if(present(name))call this%push(' name="',//name//'"')
    if(present(target))then
       call this%push(' target="')
       call this%push(target)
       call this%push('"')
    end if
    if(present(pointer))then
       call this%push(' pointer="')
       call this%push(pointer)
       call this%push('"')
    end if
    if(present(shape))then
       call this%push(' shape="')
       call this%push(shape)
       call this%push('"')
    end if
    call this%push(">")
    this%indentation=this%indentation+1
  end subroutine marker_mark_begin
marker mark instance begin \
  subroutine marker_mark_instance_begin(this,ser,name,target,pointer,shape)
    class(marker_type),intent(inout)::this
    class(serializable_class),intent(in)::ser
    character(*),intent(in)::name
    integer(kind=dik),intent(in),optional::target,pointer
    integer,intent(in),dimension(:),optional::shape
    character(:),allocatable::this_type
    call ser%get_type(this_type)
    call this%mark_begin("ser",this_type,name,target,pointer,shape)
  end subroutine marker_mark_instance_begin
marker mark end \( \ \)
  subroutine marker_mark_end(this,tag)
    class(marker_type),intent(inout)::this
    character(*),intent(in),optional::tag
    this%indentation=this%indentation-1
    call this%indent()
    if(present(tag))then
       call this%push("</"//tag//">")
    else
       call this%push("</ser>")
    end if
  end subroutine marker_mark_end
marker mark instance end \( \ \)
```

```
subroutine marker_mark_instance_end(this)
    class(marker_type),intent(inout)::this
    call this%mark_end("ser")
  end subroutine marker_mark_instance_end
marker mark logical ↑
  subroutine marker_mark_logical(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    logical,intent(in)::content
    call this%indent()
    call this%push("<"//name//">")
    if(content)then
       call this%push("T")
    else
       call this%push("F")
    call this%push("</"//name//">")
  end subroutine marker_mark_logical
marker mark integer \( \)
  subroutine marker_mark_integer(this, name, content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer,intent(in)::content
    call this%indent()
    call this%push("<"//name//">")
    call this%push(content)
    call this%push("</"//name//">")
  end subroutine marker_mark_integer
marker mark integer array \( \)
  subroutine marker_mark_integer_array(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer,dimension(:),intent(in)::content
    call this%indent()
    call this%push("<"//name//">")
    call this%push(content)
    call this%push("</"//name//">")
  end subroutine marker_mark_integer_array
marker mark integer matrix †
  subroutine marker_mark_integer_matrix(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer,dimension(:,:),intent(in)::content
    integer::n
    integer,dimension(2)::s
```

```
s=shape(content)
    call this%indent()
    call this%push("<"//name//">")
    do n=1,s(2)
       call this%push(content(:,n))
       call this%push(" ")
    end do
    call this%push("</"//name//">")
  end subroutine marker_mark_integer_matrix
marker mark integer dik †
  subroutine marker_mark_integer_dik(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik),intent(in)::content
    call this%indent()
    call this%push("<"//name//">")
    call this%push(content)
    call this%push("</"//name//">")
  end subroutine marker_mark_integer_dik
marker mark integer array dik †
  subroutine marker_mark_integer_array_dik(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik),dimension(:),intent(in)::content
    call this%indent()
    call this%push("<"//name//">")
    call this%push(content)
    call this%push("</"//name//">")
  end subroutine marker_mark_integer_array_dik
marker mark integer matrix dik †
  subroutine marker_mark_integer_matrix_dik(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik),dimension(:,:),intent(in)::content
    integer::n
    integer,dimension(2)::s
    call this%indent()
    call this%push("<"//name//">")
    do n=1,s(2)
       call this%push(content(:,n))
       call this%push(" ")
    end do
    call this%push("</"//name//">")
  end subroutine marker_mark_integer_matrix_dik
marker mark double \( \)
```

```
subroutine marker_mark_double(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    real(kind=drk),intent(in)::content
    call this%indent()
    call this%push("<"//name//">")
    call this%push(content)
    call this%push("</"//name//">")
  end subroutine marker_mark_double
marker mark double array \( \)
  subroutine marker_mark_double_array(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    real(kind=drk), dimension(:), intent(in)::content
    call this%indent()
    call this%push("<"//name//">")
    call this%push(content)
    call this%push("</"//name//">")
  end subroutine marker_mark_double_array
marker mark double matrix \( \ \)
  subroutine marker_mark_double_matrix(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    real(kind=drk), dimension(:,:), intent(in)::content
    integer::n
    integer, dimension(2)::s
    s=shape(content)
    call this%indent()
    call this%push("<"//name//">")
    do n=1,s(2)
       call this%push(content(:,n))
       call this%push(" ")
    end do
    call this%push("</"//name//">")
  end subroutine marker_mark_double_matrix
marker mark string \( \ \)
  subroutine marker_mark_string(this,name,content)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name,content
    call this%indent()
    call this%push("<"//name//">")
    call this%push(content)
    call this%push("</"//name//">")
  end subroutine marker_mark_string
marker mark instance \( \)
```

```
recursive subroutine marker_mark_instance(this,ser,name,target,pointer)
    class(marker_type),intent(inout)::this
    class(serializable_class),intent(in)::ser
    character (len=*), intent(in)::name
    integer(kind=dik),intent(in),optional::target,pointer
    integer(kind=dik)::status
    call this%mark_instance_begin(ser,name,target,pointer)
    call ser%write_to_marker(this,status)
    call this%mark_end("ser")
  end subroutine marker_mark_instance
marker mark target \( \ \)
  recursive subroutine marker_mark_target(this,name,ser)
    class(marker_type),intent(inout)::this
    class(serializable_class),target,intent(in)::ser
    character (len=*), intent(in)::name
    this%n_instances=this%n_instances+1
    call this%push_heap(ser,this%n_instances)
    call this%mark_instance(ser,name,target=this%n_instances)
  end subroutine marker_mark_target
marker mark allocatable \( \)
  subroutine marker_mark_allocatable(this,name,ser)
    class(marker_type),intent(inout)::this
    class(serializable_class),allocatable,intent(in)::ser
    character (len=*), intent(in)::name
    if(allocated(ser))then
       call this%mark_instance(ser,name)
    else
       call this%mark_null(name)
    end if
  end subroutine marker_mark_allocatable
marker mark pointer \( \ \)
  recursive subroutine marker_mark_pointer(this,name,ser)
    class(marker_type),intent(inout)::this
    class(serializable_class), pointer, intent(in)::ser
    character(len=*),intent(in)::name
    character(:),allocatable::type
    integer(kind=dik)::p
    if(associated(ser))then
       call this%search_heap(ser,p)
       if(p>0)then
          call ser%get_type(type)
          call this%push('<ser type="')</pre>
          call this%push(type)
          call this%push('" name="')
          call this%push(name)
          call this%push('" pointer="')
```

```
call this%push(p)
          call this%push('"/>')
          call this % mark_target(name, ser)
       end if
    else
       call this%mark_null(name)
    end if
  end subroutine marker_mark_pointer
marker mark null \( \)
  subroutine marker_mark_null(this,name)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    call this%indent()
    call this%push('<ser type="null" name="')</pre>
    call this%push(name)
    call this%push('"/>')
  end subroutine marker_mark_null
marker mark nothing \( \)
  subroutine marker_mark_nothing(this,name)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    call this%indent()
    call this%push('<')</pre>
    call this%push(name)
    call this%push('/>')
  end subroutine marker_mark_nothing
marker mark empty \( \)
  subroutine marker_mark_empty(this,tag,type,name,target,pointer,shape)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::tag
    character(*),intent(in),optional::type,name
    integer(kind=dik),intent(in),optional::target,pointer
    integer,intent(in),dimension(:),optional::shape
    call this%push("<")</pre>
    call this%push(tag)
    if(present(type))call this%push(' type="',/type//'"')
    if(present(name))call this%push(' name="',/name//'"')
    if(present(target))then
       call this%push(' target="')
       call this%push(target)
       call this%push('"')
    end if
    if(present(pointer))then
       call this%push(' pointer="')
       call this%push(pointer)
```

```
call this%push('"')
    end if
    if(present(shape))then
       call this%push(' shape="')
       call this%push(shape)
       call this%push('"')
    end if
    call this%push("/>")
  end subroutine marker_mark_empty
marker pick begin †
 subroutine marker_pick_begin(this,tag,type,name,target,pointer,shape,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::tag
    integer(kind=dik),dimension(2,2),intent(out),optional::type,name
    integer(kind=dik),intent(out),optional::target,pointer
    integer,dimension(:),allocatable,optional,intent(out)::shape
    integer(kind=dik),intent(out)::status
    integer(kind=dik),dimension(2)::p1,p2,p3
    integer(kind=dik)::1
    call this%find("<",skip=4,proceed=.true.,pos=p1)</pre>
    call this%find(">",skip=1,proceed=.false.,pos=p2)
    p3=this%find_pure(" ",p1,p2,skip=1)
    if(p3(2)>0)then
       if(this%substring(p1,p3)==tag)then
          status=serialize_ok
          if(present(type))then
             call this%substring_by_keys('type="','"',p3,p2,.false.,l,type)
             if(1 \le 0) then
                print *,"marker_pick_begin: No type found"
                status=serialize_wrong_type
             end if
          end if
          if(present(name))then
             call this%substring_by_keys('name="','"',p3,p2,.false.,l,name)
             if(1 \le 0)then
                print *,"marker_pick_begin: No name found"
                status=serialize_wrong_name
                call this%print_position()
                stop
             end if
          end if
          if(present(target))then
             p1=this%find_pure('target="',p3,p2,4)
             if(p1(2)>0)then
                call this%set_position(p1)
                call this%pop(target)
             else
                target=-1
                status=serialize_ok
```

```
end if
          end if
          if(present(pointer))then
             p1=this%find_pure('pointer="',p3,p2,4)
             if(p1(2)>0)then
                call this%set_position(p1)
                call this%pop(pointer)
             else
                pointer=-1
                status=serialize_ok
             end if
          end if
          if(present(shape))then
             p1=this%find_pure('shape="',p3,p2,4)
             if(p1(2)>0)then
                call this%set_position(p1)
                call this%pop(shape)
             else
                status=serialize_ok
             end if
          end if
       else
          print *, "marker_pick_begin: Wrong tag. Expected: "&
          ,tag," Found: ",this%substring(p1,p3)
          status=serialize_wrong_tag
          call this%print_position()
       end if
    else
       if (this%substring(p1,p2)==tag)then
          status=serialize_ok
       else
          print *,"marker_pick_begin: Wrong tag. Expected: "&
          ,tag," Found: ",this%substring(p1,p2)
          status=serialize_wrong_tag
       end if
    end if
    call this%set_position(p2)
    call this%proceed(one*2,.true.)
  end subroutine marker_pick_begin
marker query instance begin \
  subroutine marker_query_instance_begin(this,type,name,target,pointer,shape,status)
    class(marker_type),intent(inout)::this
    integer(kind=dik),dimension(2,2),intent(out),optional::type,name
    integer(kind=dik),intent(out),optional::target,pointer
    integer, dimension(:), allocatable, optional, intent(out)::shape
    integer(kind=dik),intent(out)::status
    call this%pick_begin("ser",type,name,target,pointer,shape,status)
  end subroutine marker_query_instance_begin
marker pick instance begin \( \ \)
```

```
subroutine marker_pick_instance_begin(this,name,type,target,pointer,shape,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik),dimension(2,2),intent(out),optional::type
    integer(kind=dik),intent(out),optional::target,pointer
    integer,dimension(:),allocatable,optional,intent(out)::shape
    integer(kind=dik),intent(out)::status
    integer(kind=dik),dimension(2,2)::read_name
    call this%query_instance_begin(type,read_name,target,pointer,shape,status)
    if(status==serialize ok)then
       if(.not.this%str_equal(name,read_name))status=serialize_wrong_name
    end if
  end subroutine marker_pick_instance_begin
marker pick end \( \)
  subroutine marker_pick_end(this,tag,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::tag
    integer(kind=dik),intent(out)::status
    integer(kind=dik),dimension(2)::p1,p2
    call this%find("</",skip=4,proceed=.true.,pos=p1)</pre>
    call this%find(">",skip=1,proceed=.false.,pos=p2)
    if(tag==this%substring(p1,p2))then
       status=serialize ok
    else
       print *,"marker_pick_end: Wrong tag. Expected: ",tag," Found: ",this%substring(p1,p2)
       print *,"p1=",p1,"p2=",p2
       call this%print_position()
    end if
    call this%set_position(p2)
    call this%proceed(one*2,.true.)
  end subroutine marker_pick_end
marker pick instance end \( \ \)
  subroutine marker_pick_instance_end(this,status)
    class(marker_type),intent(inout)::this
    integer(kind=dik),intent(out)::status
    call this%pick_end("ser",status)
  end subroutine marker_pick_instance_end
marker pick instance \( \ \)
  subroutine marker_pick_instance(this,name,ser,status)
    class(marker_type),intent(inout)::this
    class(serializable_class),intent(out)::ser
    character(*),intent(in)::name
    integer(kind=dik),intent(out)::status
    integer(kind=dik),dimension(2,2)::type,r_name
    call this%pick_begin("ser",type,r_name,status=status)
    if(status==serialize_ok)then
```

```
if(ser%verify_type(this%substring(type)))then
          if(this%str_equal(name,r_name))then
             call ser%read_from_marker(this, status)
             call this%pick_end("ser",status)
          else
             print *, "marker_pick_instance: Name mismatch: Expected: "&
             ,name, "Found: ",r_name
             status=serialize_wrong_name
             call this%print_position
          end if
       else
          print *,"marker_pick_instance: Type mismatch: ",type
          call ser%write_type(output_unit)
          print *,""
          status=serialize_wrong_type
          call this%print_position
       end if
    end if
  end subroutine marker_pick_instance
marker pick target \( \ \)
  subroutine marker_pick_target(this,name,ser,status)
    class(marker_type),intent(inout)::this
    class(serializable_class), target, intent(out)::ser
    character(*),intent(in)::name
    integer(kind=dik),intent(out)::status
    integer(kind=dik), dimension(2,2)::type,r_name
    integer(kind=dik)::target
    call this%pick_begin("ser",type,r_name,target,status=status)
    if(status==serialize_ok)then
       if(ser%verify_type(this%substring(type)))then
          if(this%str_equal(name,r_name))then
             call ser%read_target_from_marker(this,status)
             if(target>0)call this%push_heap(ser,target)
          else
             print *,"marker_pick_instance: Name mismatch: Expected: "&
             ,name, "Found: ",r_name
             status=serialize_wrong_name
          end if
       else
          print *,"marker_pick_instance: Type mismatch: ",type
          status=serialize_wrong_type
       end if
    end if
    call this%pick_end("ser",status)
  end subroutine marker_pick_target
marker pick allocatable \uparrow
  subroutine marker_pick_allocatable(this,name,ser)
    class(marker_type),intent(inout)::this
```

```
character(*),intent(in)::name
    class(serializable_class),allocatable,intent(out)::ser
    class(serializable_class),pointer::ref
    integer(kind=dik), dimension(2,2)::type,r_name
    integer(kind=dik)::status
    call this%pick_begin("ser",type,r_name,status=status)
    if(status==serialize_ok)then
       if(ser%verify_type(this%substring(type)))then
          if(this%str_equal(name,r_name))then
             call this%search_reference(type,ref)
             if(associated(ref))then
                allocate(ser, source=ref)
                call ser%read_from_marker(this,status)
             else
                print *,"marker_pick_allocatable:&
                     & Type ",type," not found on reference stack."
             end if
          else
             print *,"marker_pick_instance: Name mismatch: Expected: ",&
             name," Found: ",r_name
             status=serialize_wrong_name
          end if
       else
          print *,"marker_pick_instance: Type mismatch: ",type
          status=serialize_wrong_type
       end if
    end if
    call this%pick_end("ser", status)
  end subroutine marker_pick_allocatable
marker pick pointer \( \ \)
 recursive subroutine marker_pick_pointer(this, name, ser)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    class(serializable_class),pointer,intent(out)::ser
    class(serializable_class),pointer::ref
    integer(kind=dik),dimension(2,2)::type,r_name
    integer(kind=dik)::status,t,p
    nullify(ser)
    call this%pick_begin("ser",type,r_name,target=t,pointer=p,status=status)
    if(status==serialize_ok)then
       if(.not.this%str_equal("null",type))then
          if(p>0)then
             call this%search_heap(p,ser)
             call this%search_reference(type,ref)
             if(associated(ref))then
                allocate(ser, source=ref)
                call ser%read_target_from_marker(this,status)
                call this%pick_end("ser",status)
```

```
if(t>0)call this%push_heap(ser,t)
             else
                print *,"marker_pick_pointer:&
                     & Type ",type," not found on reference stack."
             end if
          end if
       end if
    end if
  end subroutine marker_pick_pointer
marker pick logical \( \ \)
  subroutine marker_pick_logical(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    logical,intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this%pick_end(name, status)
  end subroutine marker_pick_logical
marker pick integer \( \)
  subroutine marker_pick_integer(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer,intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name,status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this%pick_end(name, status)
    end if
  end subroutine marker_pick_integer
marker pick integer array \( \)
  subroutine marker_pick_integer_array(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer,dimension(:),intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this%pick_end(name, status)
    end if
  end subroutine marker_pick_integer_array
marker pick integer matrix \( \ \)
```

```
subroutine marker_pick_integer_matrix(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer, dimension(:,:), intent(out)::content
    integer(kind=dik),intent(out)::status
    integer::n
    integer, dimension(2)::s
    s=shape(content)
    call this%pick_begin(name,status=status)
    if(status==serialize ok)then
       do n=1,s(2)
          call this%pop(content(:,n))
       end do
       call this%pick_end(name, status)
    end if
  end subroutine marker_pick_integer_matrix
marker pick integer dik ↑
 subroutine marker_pick_integer_dik(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik),intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this%pick_end(name, status)
  end subroutine marker_pick_integer_dik
marker pick integer array dik \
  subroutine marker_pick_integer_array_dik(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik), dimension(:), intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this%pick_end(name,status)
  end subroutine marker_pick_integer_array_dik
marker pick integer matrix dik †
 subroutine marker_pick_integer_matrix_dik(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik),dimension(:,:),intent(out)::content
    integer(kind=dik),intent(out)::status
```

```
integer::n
    integer, dimension(2)::s
    s=shape(content)
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       do n=1,s(2)
          call this%pop(content(:,n))
       end do
       call this%pick_end(name, status)
  end subroutine marker_pick_integer_matrix_dik
marker pick double \( \ \)
  subroutine marker_pick_double(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    real(kind=drk),intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this%pick_end(name, status)
    end if
  end subroutine marker_pick_double
marker pick double array \( \)
  subroutine marker_pick_double_array(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    real(kind=drk), dimension(:), intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this%pick_end(name, status)
  end subroutine marker_pick_double_array
marker pick double matrix \( \ \)
  subroutine marker_pick_double_matrix(this, name, content, status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    real(kind=drk),dimension(:,:),intent(out)::content
    integer(kind=dik),intent(out)::status
    integer::n
    integer, dimension(2)::s
    s=shape(content)
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
```

```
do n=1,s(2)
          call this%pop(content(:,n))
       call this % pick_end(name, status)
    end if
  end subroutine marker_pick_double_matrix
marker pick string \( \)
  subroutine marker_pick_string(this,name,content,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    character(:),allocatable,intent(out)::content
    integer(kind=dik),intent(out)::status
    call this%pick_begin(name, status=status)
    if(status==serialize_ok)then
       call this%pop(content)
       call this % pick_end(name, status)
    end if
  end subroutine marker_pick_string
marker\ verify\_nothing \uparrow
  subroutine marker_verify_nothing(this,name,status)
    class(marker_type),intent(inout)::this
    character(*),intent(in)::name
    integer(kind=dik),intent(out)::status
    integer(kind=dik),dimension(2)::p1,p2
    call this%find("<",skip=4,proceed=.false.,pos=p1)</pre>
    call this%find(">",1,.false.,p2)
    if(name//"/"==this%substring(p1,p2))then
       status=serialize_nothing
       call this%set_position(p2)
       call this%proceed(one*3,.true.)
       if (name==this%substring(p1,p2))then
          status=serialize ok
       else
          status=serialize_wrong_tag
       end if
    end if
  end subroutine marker_verify_nothing
marker indent †
  subroutine marker_indent(this,step)
    class(marker_type),intent(inout)::this
    integer(kind=dik),optional::step
    if(this%do_break)call this%push(new_line(" "))
    if(this%do_indent)then
       if(present(step))this%indentation=this%indentation+step
       call this%push(repeat(" ",this%indentation))
```

```
end if
    this%active_pages(1)=this%actual_page()
  end subroutine marker_indent
marker push heap \( \)
  subroutine marker_push_heap(this,ser,id)
    class(marker_type),intent(inout)::this
    class(serializable_class), target, intent(in)::ser
    integer(kind=dik),intent(in)::id
    class(serializable_ref_type), pointer::new_ref
    allocate(new ref)
    new_ref%next=>this%heap
    new_ref%ref=>ser
    new_ref%id=id
    this%heap=>new_ref
  end subroutine marker_push_heap
marker pop heap ↑
  subroutine marker_pop_heap(this,ser)
    class(marker_type),intent(inout)::this
    class(serializable_class),pointer,intent(out)::ser
    class(serializable_ref_type),pointer::old_ref
    if(associated(this%heap))then
       old_ref=>this%heap
       ser=>old_ref%ref
       this%heap=>this%heap%next
       deallocate(old_ref)
       print('("marker_pop_heap: heap_stack is not associated.")')
    end if
  end subroutine marker_pop_heap
marker search heap by id \
  subroutine marker_search_heap_by_id(this,id,ser)
    class(marker_type),intent(in)::this
    integer(kind=dik),intent(in)::id
    class(serializable_class),pointer,intent(out)::ser
    class(serializable_ref_type),pointer::ref
    ref=>this%heap
    do while(associated(ref))
       if(id==ref%id)then
          ser=>ref%ref
          exit
       end if
       ref=>ref%next
    end do
  end subroutine marker_search_heap_by_id
marker search heap by ref \( \ext{\gamma} \)
```

```
subroutine marker_search_heap_by_ref(this,ref,id)
    class(marker_type),intent(in)::this
    class(serializable_class), pointer, intent(in)::ref
    integer(kind=dik),intent(out)::id
    class(serializable_ref_type),pointer::ref_p
    ref_p=>this%heap
    id=0
    do while(associated(ref_p))
       if(associated(ref,ref_p%ref))then
          id=ref_p%id
          exit
       end if
       ref_p=>ref_p%next
    end do
  end subroutine marker_search_heap_by_ref
marker push reference \( \)
 subroutine marker_push_reference(this,ser,id)
    class(marker_type),intent(inout)::this
    class(serializable_class),target,intent(in)::ser
    integer(kind=dik),intent(in),optional::id
    class(serializable_ref_type), pointer::new_ref
    allocate(new_ref)
    new_ref%next=>this%references
    new_ref%ref=>ser
    if(present(id))then
       new_ref%id=id
    else
      new_ref%id=-1
    end if
    this%references=>new_ref
  end subroutine marker_push_reference
marker pop reference \( \)
 subroutine marker_pop_reference(this,ser)
    class(marker_type),intent(inout)::this
    class(serializable_class),pointer,intent(out)::ser
    class(serializable_ref_type),pointer::old_ref
    if(associated(this%references))then
       old_ref=>this%references
       ser=>old_ref%ref
       this%references=>this%references%next
       deallocate(old_ref)
       print('("marker_pop_reference: reference_stack is not associated.")')
    end if
  end subroutine marker_pop_reference
marker search reference \( \)
```

```
subroutine marker_search_reference(this,type,ser)
    class(marker_type),intent(in)::this
    integer(kind=dik),dimension(2,2),intent(in)::type
    class(serializable_class),pointer,intent(out)::ser
    class(serializable_class), pointer::tmp_ser!nag bug workaround
    class(serializable_ref_type),pointer::ref
    ref=>this%references
    nullify(ser)
    do while(associated(ref))
       tmp ser=>ref%ref
       if(tmp_ser%verify_type(this%substring(type)))then
          ser=>tmp_ser
          exit
       end if
       ref=>ref%next
  end subroutine marker_search_reference
marker reset heap \( \)
  subroutine marker_reset_heap(this)
    class(marker_type),intent(inout)::this
    if(associated(this%heap))then
       call this%heap%finalize()
       deallocate(this%heap)
    end if
  end subroutine marker_reset_heap
marker reset references ↑
  subroutine marker_reset_references(this)
    class(marker_type),intent(inout)::this
    if(associated(this%references))then
       call this%references%finalize()
       deallocate(this%references)
    end if
  end subroutine marker_reset_references
marker finalize \( \)
  subroutine marker_finalize(this)
    class(marker_type),intent(inout)::this
    call this%reset_heap()
    call this%reset_references()
  end subroutine marker_finalize
```

## 13.6.8 Sonstige Prozeduren

```
{\tt serialize\_print\_comp\_pointer}
```

```
recursive subroutine serialize_print_comp_pointer(ser,unit,parents,components,peers,name)
    class(serializable_class), pointer, intent(in)::ser
    integer, intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    character(len=*),intent(in)::name
    if(associated(ser))then
       write(unit,fmt=*)name," is associated."
       if(components>0)then
          write(unit,fmt=*)"Printing components of ",name
          call ser%print_to_unit(unit, parents, components-one, peers)
       else
          write(unit,fmt=*)"Skipping components of ",name
       end if
    else
       write(unit,fmt=*)name," is not associated."
  end subroutine serialize_print_comp_pointer
serialize print peer pointer
  recursive subroutine serialize_print_peer_pointer(ser,unit,parents,components,peers,name)
    class(serializable_class), pointer, intent(in)::ser
    integer,intent(in)::unit
    integer(kind=dik)::parents,components,peers
    character(len=*),intent(in)::name
    if(associated(ser))then
       write(unit,fmt=*)name," is associated."
       if(peers>0)then
          write(unit,fmt=*)"Printing components of ",name
          call ser%print_to_unit(unit, parents, components, peers-one)
       else
          write(unit,fmt=*)"Skipping components of ",name
       end if
    else
       write(unit,fmt=*)name," is not associated."
  end subroutine serialize_print_peer_pointer
serialize print allocatable
  subroutine serialize_print_allocatable(ser,unit,parents,components,peers,name)
    class(serializable_class),allocatable,intent(in)::ser
    integer,intent(in)::unit
    integer(kind=dik),intent(in)::parents,components,peers
    character(len=*),intent(in)::name
    if(allocated(ser))then
       write(unit,fmt=*)name," is allocated."
       if(components>0)then
          write(unit,fmt=*)"Printing components of ",name
          call ser%print_to_unit(unit,parents,components-1,peers)
       else
          write(unit,fmt=*)"Skipping components of ",name
```

```
end if
    else
       write(unit,fmt=*)name," is not allocated."
  end subroutine serialize_print_allocatable
measurable less measurable
  elemental function measurable_less_measurable(mea1,mea2)
    class(measurable_class),intent(in)::mea1,mea2
    logical::measurable_less_measurable
    measurable_less_measurable=mea1%measure()<mea2%measure()</pre>
  end function measurable_less_measurable
measurable less double
  elemental function measurable_less_double(mea1,dou)
    class(measurable_class),intent(in)::mea1
    real(kind=drk),intent(in)::dou
    logical::measurable_less_double
    measurable_less_double=mea1%measure()<dou</pre>
  end function measurable_less_double
measurable less or equal measurable
  elemental function measurable_less_or_equal_measurable(mea1,mea2)
    class(measurable_class),intent(in)::mea1,mea2
    logical::measurable_less_or_equal_measurable
    measurable_less_or_equal_measurable=mea1%measure()<=mea2%measure()</pre>
  end function measurable_less_or_equal_measurable
measurable less or equal double
   elemental function measurable_less_or_equal_double(mea1,dou)
    class(measurable_class),intent(in)::mea1
    real(kind=drk),intent(in)::dou
    logical::measurable_less_or_equal_double
    measurable_less_or_equal_double=mea1%measure()<=dou
  end function measurable_less_or_equal_double
measurable equal measurable
 elemental function measurable_equal_measurable(mea1,mea2)
    class(measurable_class),intent(in)::mea1,mea2
    logical::measurable_equal_measurable
    measurable_equal_measurable=mea1%measure() == mea2%measure()
  end function measurable_equal_measurable
measurable equal double
  elemental function measurable_equal_double(mea1,dou)
    class(measurable_class),intent(in)::mea1
    real(kind=drk),intent(in)::dou
    logical::measurable_equal_double
```

```
measurable_equal_double=mea1%measure()==dou
  end function measurable_equal_double
measurable equal or greater measurable
  elemental function measurable_equal_or_greater_measurable(mea1,mea2)
    class(measurable_class),intent(in)::mea1,mea2
    logical::measurable_equal_or_greater_measurable
    measurable_equal_or_greater_measurable=mea1%measure()>=mea2%measure()
  end function measurable_equal_or_greater_measurable
measurable equal or greater double
  elemental function measurable_equal_or_greater_double(mea1,dou)
    class(measurable_class),intent(in)::mea1
    real(kind=drk),intent(in)::dou
    logical::measurable_equal_or_greater_double
    measurable_equal_or_greater_double=mea1%measure()>=dou
  end function measurable_equal_or_greater_double
measurable greater measurable
  elemental function measurable_greater_measurable(mea1,mea2)
    class(measurable_class),intent(in)::mea1,mea2
    logical::measurable_greater_measurable
    measurable_greater_measurable=mea1%measure()>mea2%measure()
  end function measurable_greater_measurable
measurable greater double
  elemental function measurable_greater_double(mea1,dou)
    class(measurable_class),intent(in)::mea1
    real(kind=drk),intent(in)::dou
    logical::measurable_greater_double
    measurable_greater_double=mea1%measure()>dou
  end function measurable_greater_double
page ring position
  pure function page_ring_position(n)
    integer(kind=dik),intent(in)::n
    integer(kind=dik),dimension(2)::page_ring_position
    page_ring_position(2)=mod(n,serialize_page_size)
    page_ring_position(1)=(n-page_ring_position(2))/serialize_page_size
  end function page_ring_position
page ring ordinal
  pure integer(kind=dik) function page_ring_ordinal(pos)
    integer(kind=dik), dimension(2), intent(in)::pos
    page_ring_ordinal=pos(1)*serialize_page_size+pos(2)
  end function page_ring_ordinal
page ring position is before int pos
```

```
pure logical function page_ring_position_is_before_int_pos(m,n)
    integer(kind=dik),intent(in)::m
    integer(kind=dik),dimension(2),intent(in)::n
    if (m<page_ring_ordinal(n))then
       page_ring_position_is_before_int_pos=.true.
    else
       page_ring_position_is_before_int_pos=.false.
    end if
  end function page_ring_position_is_before_int_pos
page ring position is before pos int
  pure logical function page_ring_position_is_before_pos_int(m,n)
    integer(kind=dik),dimension(2),intent(in)::m
    integer(kind=dik),intent(in)::n
    if(page_ring_ordinal(m)<n)then</pre>
       page_ring_position_is_before_pos_int=.true.
    else
       page_ring_position_is_before_pos_int=.false.
    end if
  end function page_ring_position_is_before_pos_int
page ring position is before pos pos
  pure logical function page_ring_position_is_before_pos_pos(m,n)
    integer(kind=dik), dimension(2), intent(in)::m,n
    if(m(1) < n(1))then
       page_ring_position_is_before_pos_pos=.true.
    else
       if(m(1)>n(1))then
          page_ring_position_is_before_pos_pos=.false.
          if(m(2) < n(2))then
             page_ring_position_is_before_pos_pos=.true.
             page_ring_position_is_before_pos_pos=.false.
          end if
       end if
    end if
  end function page_ring_position_is_before_pos_pos
ring position increase
  subroutine ring_position_increase(pos,n)
    integer(kind=dik),dimension(2),intent(inout)::pos
    integer(kind=dik),intent(in)::n
    pos=page_ring_position(page_ring_ordinal(pos)+n)
  end subroutine ring_position_increase
ring position metric2
```

```
pure integer(kind=dik) function ring_position_metric2(p1,p2)
    integer(kind=dik),dimension(2),intent(in)::p1,p2
    ring_position_metric2=(p2(1)-p1(1))*serialize_page_size+p2(2)-p1(2)+1
  end function ring_position_metric2
ring position metric1
  pure integer(kind=dik) function ring_position_metric1(p)
    integer(kind=dik),dimension(2,2),intent(in)::p
    ring_position_metric1=(p(1,2)-p(1,1))*serialize_page_size+p(2,2)-p(2,1)+1
  end function ring_position_metric1
generate unit
  subroutine generate_unit(unit,min,max)
    integer,intent(out) :: unit
    integer,intent(in),optional :: min,max
    integer :: min_u,max_u
    logical :: is_open
    !print *, "generate_unit"
    unit = -1
    if(present(min))then
       min_u=min
    else
       min_u=10
    end if
    if(present(max))then
       max_u=max
    else
       max_u=huge(max_u)
    end if
    do unit=min_u, max_u
       !print *,"testing ",unit
       inquire(unit,opened=is_open)
       if (.not. is_open) then
          exit
       end if
    end do
  end subroutine generate_unit
ilog2
  subroutine ilog2(int,exp,rem)
    integer,intent(in) :: int
    integer,intent(out) :: exp,rem
    integer :: count
    count = 2
    exp = 1
    do while (count<int)</pre>
       exp=exp+1
       count = ishft(count,1)
    end do
```

```
if (count>int) then
       rem=(int-ishft(count,-1))
    else
       rem=0
    end if
  end subroutine ilog2
character is in
  pure logical function character_is_in(c,array)
    character,intent(in)::c
    character,dimension(:),intent(in)::array
    integer(kind=dik)::n
    character_is_in=.false.
    do n=1,size(array)
       if(c==array(n))then
          character_is_in=.true.
       end if
    end do
  end function character_is_in
integer with leading zeros
  subroutine integer_with_leading_zeros(number,length,string)
    integer,intent(in) :: number,length
    character(len=*),intent(out) :: string
    integer :: zeros
    character::sign
    if(number==0)then
       string = repeat("0",length)
    else
       if(number>0)then
          zeros=length-floor(log10(real(number)))-1
          if(zeros<0)then
             string=repeat("*",length)
          else
             write(string,fmt='(a,I0)') repeat("0",zeros),number
          end if
       else
          zeros=length-floor(log10(real(-number)))-2
          if(zeros<0)then
             string=repeat("*",length)
             write(string,fmt='(a,a,I0)') "-",repeat("0",zeros),abs(number)
          end if
       end if
    end if
  end subroutine integer_with_leading_zeros
```