VanillaICE: Hidden Markov Models for the Assessment of Chromosomal Alterations using High-throughput SNP Arrays

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1 Introduction

Chromosomal DNA is characterized by variation between individuals at the level of entire chromosomes (e.g. aneuploidy in which the chromosome copy number is altered), segmental changes (including insertions, deletions, inversions, and translocations), and changes to small genomic regions (including single nucleotide polymorphisms). A variety of alterations that occur in chromosomal DNA, many of which can be detected using high density single nucleotide polymorphism (SNP) microarrays, are linked to normal variation as well as disease and therefore of particular interest. These include changes in copy number (deletions and duplications) and genotype (e.g. the occurrence of regions of homozygosity). Hidden Markov models (HMM) are particularly useful for detecting such abnormalities, modeling the spatial dependence between neighboring SNPs. Here, we extend previous approaches that utilize HMM frameworks for inference in high throughput SNP arrays by integrating copy number, genotype calls, and the corresponding measures of uncertainty when available. Using simulated and real data, we demonstrate how confidence scores control smoothing in a probabilistic framework. The goal of this vignette is to provide a simple interface for fitting HMMs and plotting functions to help visualize the predicted states alongside the experimental data.

2 Simple Usage

2.1 Vanilla HMM

> library(VanillaICE)

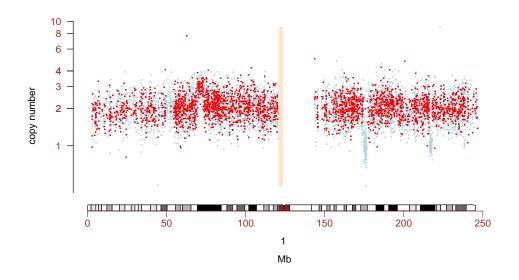
Before fitting the HMM, the data must be organized into one of the following classes for high-throughput SNP data:

- SnpCallSet (genotype calls)
- SnpCopyNumberSet (copy number estimates)
- oligoSnpSet (genotype and copy number estimates)

When pre-processing Affymetrix SNP chips with the R package oligo, an object of one of the above classes is created and can be used directly with the HMMs described in this vignette. These classes can also be created from Illumina data as described in the IlluminaHowTo vignette. The simulated data provided with this package is an instance of class oligoSnpSet

- > data(chromosome1)
- > annotation(chromosome1)

```
[1] "pd.mapping50k.hind240,pd.mapping50k.xba240"
> chromosome1
oligoSnpSet (storageMode: lockedEnvironment)
assayData: 9165 features, 1 samples
  element names: calls, callsConfidence, cnConfidence, copyNumber
experimentData: use 'experimentData(object)'
Annotation: pd.mapping50k.hind240,pd.mapping50k.xba240
phenoData
An object of class "AnnotatedDataFrame"
  sampleNames: NA06993
  varLabels and varMetadata description:
    family: trio variable
    upd: uniparental isodisomy indicator
featureData
An object of class "AnnotatedDataFrame"
  rowNames: SNP_A-1677174, SNP_A-1718890, ..., SNP_A-1677548 (9165 total)
  varLabels and varMetadata description:
    dbsnp_rs_id: dbsnp_rs_id
    chromosome: chrom
    ...: ...
    enzyme: enzyme
    (8 total)
Annotation [1] "pd.mapping50k.hind240,pd.mapping50k.xba240"
   Before deciding whether to fit a HMM, plot the data:
> gp <- new("ParSnpSet")</pre>
> gp <- getPar(gp, chromosome1)</pre>
> plotSnp(object = gp, snpset = chromosome1)
NULL
```



The HMM assumes that the copy number estimates, conditional on the hidden state, are approximately Gaussian. A log transformation will be performed automatically provided that the copy number estimates are all positive. See the documentation pages in the R package VanillaICE for more information about the chromosome1 example dataset. Parameters for fitting the HMM are obtained by generating an instance of the class HmmParameter. By default, the HMM assumes the hidden states are deletion (D), normal (N), LOH (L), and amplification (A). See the HmmParameterClass vignette for more information. An instance of the class is created by the method new:

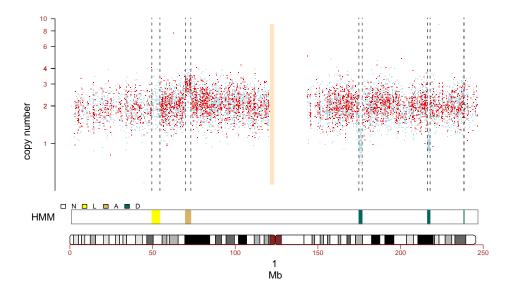
```
> params <- new("HmmParameter", chromosome1, states = c("D",
      "N", "L", "A"), cn.location = c(1, 2, 2, 3)
[1] "Transforming copy number to log2 scale."
[1] "Calculating emission probabilities for genotype calls.... "
[1] "Calculating emission probabilities for copy number estimates..."
> class(params)
[1] "HmmParameter"
attr(,"package")
[1] "VanillaICE"
   We may then fit the HMM by
> fit <- hmm(params, chromosome1)</pre>
[1] "Transforming copy number to log2 scale."
> fit
HmmPredict (storageMode: lockedEnvironment)
assayData: 9165 features, 1 samples
  element names: predictions
phenoData
  sampleNames: NAO6993
  varLabels and varMetadata description:
    family: trio variable
    upd: uniparental isodisomy indicator
featureData
  featureNames: SNP_A-1677174, SNP_A-1718890, ..., SNP_A-1677548 (9165 total)
  fvarLabels and fvarMetadata description:
    chromosome: chromosome
    arm: chromosomal arm
    position: physical position
experimentData: use 'experimentData(object)'
Annotation: pd.mapping50k.hind240,pd.mapping50k.xba240
 SnpClass: oligoSnpSet
hidden states: D N L A
breakpoints:
'data.frame':
                    11 obs. of 9 variables:
 $ id : chr "NA06993" "NA06993" "NA06993" "NA06993" ...
 $ chr : chr "1" "1" "1" "1" ...
 $ state: chr "N" "L" "N" "A" ...
```

```
$ size : num
                48.71
                        4.81 15.34
                                      3.30 101.64 ...
 $ N
                997 102 902 202 3797 ...
        : num
 $ start: num
                0.837 49.598 54.499 69.854 73.174 ...
 $ last : num
                49.5 54.4 69.8 73.2 174.8 ...
 $ prev : num
                NA 49.5 54.4 69.8 73.2 ...
 $ next : num
                49.6 54.4 69.9 73.2 174.8 ...
> tmp <- calculateBreakpoints(fit)
> breakpoints(fit)
          id chr state
                                                       last
                             size
                                            start
1.1 NA06993
                        48.708312
                                         0.836727
                                                   49.54504
                                   997
               1
                     N
1.2 NA06993
                         4.811945
                                   102
                                        49.597810
                                                   54.40975
               1
                     L
1.3 NA06993
                       15.339118
               1
                     N
                                   902
                                        54.498950
                                                   69.83807
1.4 NA06993 1
                     Α
                         3.299434
                                   202
                                        69.854466 73.15390
1.5 NA06993
                     N 101.640222 3797
                                        73.174070 174.81429
               1
1.6 NA06993
                                   100 174.815096 176.80078
              1
                     D
                         1.985684
1.7 NA06993
                        39.439073 1900 176.800844 216.23992
             1
                     N
1.8 NA06993
                     D
                         1.586808
                                    99 216.286002 217.87281
              1
1.9 NA06993
               1
                     N
                        20.410491
                                   901 217.892177 238.30267
1.10 NA06993
               1
                     D
                         0.097921
                                     5 238.319943 238.41786
1.11 NA06993
                     N
                         8.431130 160 238.429864 246.86099
                    next
          prev
1.1
            NA 49.59781
1.2
      49.54504
               54.40975
1.3
     54.40975
                69.85447
1.4
      69.83807 73.17407
1.5
     73.15390 174.81429
1.6 174.81429 176.80084
1.7 176.80078 216.28600
1.8 216.23992 217.89218
1.9 217.87281 238.31994
1.10 238.30267 238.41786
1.11 238.41786 246.86099
   FIXME: prev and next are NA in the breakpoints matrix.
   Summary statistics for the breakpoints (more useful when multiple chromosomes and samples are
in the fit object)
> summary(fit)
$L
  Freq med(length) avg(length) sd(length) med(n.snp) avg(n.snp)
          4811.945
                      4811.945
                                       NA
    1
  sd(n.snp)
         NA
$A
  Freq med(length) avg(length) sd(length) med(n.snp) avg(n.snp)
     1
          3299.434
                      3299.434
                                       NA
                                                 202
                                                             202
  sd(n.snp)
         NA
1
```

See [2] for a more complete description of the simulated dataset and the features detected by this HMM. We may plot the data along with the predictions as follows:

```
> fn <- featureNames(params)
> idx <- match(fn, featureNames(chromosome1))
> chromosome1 <- chromosome1[idx, ]
> gp <- new("ParHmmSnpSet")
> gp <- getPar(gp, snpset = chromosome1)
> plotSnp(object = gp, snpset = chromosome1, hmmPredict = fit)
```

NULL



2.2 Integrating Confidence Estimates (ICE)

In this section, we illustrate how one may fit an HMM that incorporates confidence esimates of the SNP-level summaries for genotype calls and copy number. Confidence scores (inverse of standard errors) are available for this object (see Section 2.3 for how confidence scores were derived). This information is incorporated into the HMM emission probabilities in the following way:

```
> params.ice <- new("HmmParameter", chromosome1, states = c("D",
+ "N", "L", "A"), cn.ICE = TRUE)

[1] "Transforming copy number to log2 scale."
[1] "Calculating emission probabilities for genotype calls...."
[1] "Calculating emission probabilities for copy number estimates..."</pre>
```

We may also incorporate the confidence scores for the genotype calls:

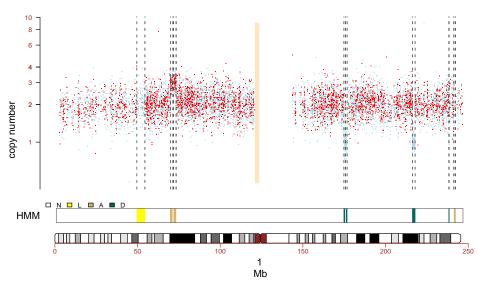
```
> params.ice <- new("HmmParameter", chromosome1, states = c("D",
+ "N", "L", "A"), cn.ICE = TRUE, gt.ICE = TRUE)
We fit the HMM in the usual way</pre>
```

> fit.ice <- hmm(params.ice, chromosome1)</pre>

[1] "Transforming copy number to log2 scale."

and plot the results using the same graphical parameters as above:

> plotSnp(object = gp, snpset = chromosome1, hmmPredict = fit.ice)
NULL



Note that the ICE HMM correctly identifies the simulated normal segments in features B and C (the normal segments were simulated to have high confidence scores). Additionally, the ICE HMM detects the micro-amplification in region E (also simulated to have high confidence scores).

2.3 Confidence scores

Confidence scores for genotype calls We suggest using the CRLMM algorithm [1] for genotype calls. CRLMM (in the R package oligo) provides confidence scores ($S_{\widehat{GT}}$) of the genotype estimates (\widehat{GT}). From 269 HapMap samples assayed on the Affymetrix 50k Xba and Hind chips, we have a gold standard of the true genotype defined by the consensus of the HapMap centers. We use kernal based density estimates to obtain

$$f\left\{\right. \left.S_{\widehat{HOM}} \mid \widehat{HOM}, HOM \right. \left. \right\}, \ f\left\{\right. \left.S_{\widehat{HOM}} \mid \widehat{HOM}, HET \right. \left. \right\}, \ f\left\{\right. \left.S_{\widehat{HET}} \mid \widehat{HET}, HOM \right. \right\}, \quad \text{and} \ f\left\{\right. \left.S_{\widehat{HET}} \mid \widehat{HET}, HET \right. \right\}$$

separately for the Xba and Hind 50k chips. The first term in (1), for example, denotes the density of the scores when the genotype is correctly called homozygous (HOM) and the true genotype is homozygous (HOM). See [2] for a more complete description of the methods. The data needed to estimate these densities is stored in the experiment data package callsConfidence. callsConfidence is available from the author's website.

Confidence scores for copy number estimates To illustrate how standard errors of the copy number estimate could be integrated in the HMM, the R object chromosome1 contains standard errors simulated from a shifted Gamma: Gamma(1,2) + 0.3, where 1 is the shape parameter and 2 is the rate parameter. To ascertain the effect of qualitatively high confidence scores on the ICE HMM, we scaled a robust estimate of the copy number standard deviation by $\frac{1}{2}$. Similarly, to simulate less precise $\widehat{\text{CN}}$ we scaled ϵ by 2. For more detailed information about how the data in the chromosome1 was generated, see the documentation for this object in the R package VanillaICE.

3 The HmmParameter class

The minimal information required to create an instance of class HmmParameter is

- 1. an object inheriting from the class SnpLevelSet. For instance, an oligoSnpSet.
- 2. a vector of names for the hidden states. Only the name for the normal state, "N", requires a controlled vocubulary.
- 3. optionally, one may define any of the following arguments when creating an instance of the class:
 - SCALE
 - tau.scale
 - tau
 - pi
 - beta
 - cn.location
 - cn.scale
 - cn.ICE
 - gt.ICE
 - gt.gte
 - gt.state
 - gt.confidence
 - gt.confidence.states
 - notes
 - annotation

An instance of the class is created by the method new:

```
> params <- new("HmmParameter", chromosome1, states = c("D", "N", "L", "A"), cn.location = log2(c(1, 2, 2, 3)))
```

The object params contains all of the parameters needed for fitting the HMM, including the transition probabilities (tau), emission probabilities (beta), and initial state probabilities (pi). A summary of the parameters contained in the object params is obtained by

> params

```
Formal class 'HmmParameter' [package "VanillaICE"] with 7 slots
  ..@ hmmOptions :Formal class 'HmmOptions' [package "VanillaICE"] with 11 slots
                              : atomic [1:1] oligoSnpSet
  .. .. .. @ SnpClass
  ..... attr(*, "package")= chr "oligoClasses"
                             : chr [1:4] "D" "N" "L" "A"
  .. .. ..@ states
                              : num [1:4] 1 2 2 3
  .. .. ..@ cn.location
                              : Named num 0.31
  .. .. ..@ cn.robustSE
  ..... attr(*, "names")= chr "NA06993"
  .. .. ..@ cn.ICE
                              : logi FALSE
  .. .. ..@ gt.ICE
                              : logi FALSE
                            : chr "not used if gt.ICE=FALSE"
  .. .. ..@ gt.gte
                         : Named num [1:4] 0.999 0.75 0.999 0.75
  .. .. ..@ gte.state
  .. .. .. - attr(*, "names")= chr [1:4] "D" "N" "L" "A"
  .. .. .. @ gt.confidence.states: chr(0)
  .. .. ..@ annotation
                             : chr "pd.mapping50k.hind240,pd.mapping50k.xba240"
  .. .. ..@ notes
                              : chr ", gt.state is P(gte = HOM | state)"
  ..@ tau : num [1:9164] 0.973 0.986 1.000 1.000 1.000 ...
  ..@ tau.scale : num [1:4, 1:4] 1 1 0.75 0.75 1.5 1 1.5 1.5 0.75 1 ...
  ... - attr(*, "dimnames")=List of 2
  .. .. ..$ : chr [1:4] "D" "N" "L" "A"
  .. .. ..$ : chr [1:4] "D" "N" "L" "A"
           : Named num [1:4] -8.006 -0.001 -8.006 -8.006
  ....- attr(*, "names")= chr [1:4] "D" "N" "L" "A"
  ..@ beta : num [1:9165, 1:4, 1] -4.9494 -2.8644 -7.0156 0.0893 -1.0799 ...
  ..@ featureData:Formal class 'AnnotatedDataFrame' [package "Biobase"] with 4 slots
  .. .. ..@ varMetadata
                           :'data.frame': 3 obs. of 1 variable:
  ......$ labelDescription: chr [1:3] "chromosome" "chromosomal arm" "physical position"
                                               9165 obs. of 3 variables:
  .. .. ..@ data
                          :'data.frame':
  ......$ chromosome: chr [1:9165] "1" "1" "1" "1" ...
  .....$ arm : chr [1:9165] "p" "p" "p" "p" ...
  ..... $position : int [1:9165] 836727 2224111 2915399 2926730 2941104 2941694 2963436 3084986
  .....@ dimLabels : chr [1:2] "rowNames" "columnNames"
  .. .. .. @ .__classVersion__:Formal class 'Versions' [package "Biobase"] with 1 slots
  .. .. .. ..@ .Data:List of 1
  .. .. .. .. .. ..$ : int [1:3] 1 1 0
  ..@ notes
                : chr(0)
```

Emission probabilities. The emission probabilities are stored as an array in the params object. The emission probability array has dimension $R \times S \times C$, where S is the number of hidden states, R is the number of rows (SNPs), and C is the number of samples. To obtain the emission probabilities for the ith SNP, one may use [to subset. For instance, the emission probabilities for the 5th SNP are:

Transition probabilities. The probability of remaining in the same state, $P(S_t = S_{t+1})$ (the diagonal of the transition probability matrix) is a function of the distance (d) between SNPs: $e^{-2d(100*1e6)}$.

This value is stored in the slot tau of the params object. The probability of leaving a state is ϵ , where $\epsilon = 1 - P(S_t = S_{t+1})$. The ϵ is split among S-1 states. By default, the probability of transitioning from an altered state back to the normal state is twice as likely as the probability of transitioning between two altered states. The weights for ϵ are provided in the tau.scale matrix in the R object params

> params@tau.scale

```
D N L A
D 1.00 1.5 0.75 0.75
N 1.00 1.0 1.00 1.00
L 0.75 1.5 1.00 0.75
A 0.75 1.5 0.75 1.00
```

and can be adjusted by the SCALE argument when creating an instance of the class. For illustration, one could make the probability of transitioning from an altered state to a normal state 10 times as likely as the probability of transitioning between two altered states by the following commmand:

```
> params <- new("HmmParameter", chromosome1, states = c("D",
+ "N", "L", "A"), cn.location = c(1, 2, 2, 3), SCALE = 10)

[1] "Transforming copy number to log2 scale."
[1] "Calculating emission probabilities for genotype calls.... "

[1] "Calculating emission probabilities for copy number estimates... "

To retrieve the copy number and genotype for the 5th SNP, one should use match:
> i <- match(names(tmp), featureNames(chromosome1))
> c(copyNumber(chromosome1[i, ]), calls(chromosome1[i, + ]))

numeric(0)
```

4 The HmmPredict Class

The output from the HMM is an instance of the HmmPredict class and contains the predicted states as well as the breakpoints for the different states.

> fit

```
HmmPredict (storageMode: lockedEnvironment)
assayData: 9165 features, 1 samples
element names: predictions
phenoData
sampleNames: NAO6993
varLabels and varMetadata description:
family: trio variable
upd: uniparental isodisomy indicator
featureData
featureNames: SNP_A-1677174, SNP_A-1718890, ..., SNP_A-1677548 (9165 total)
fvarLabels and fvarMetadata description:
chromosome: chromosome
arm: chromosomal arm
position: physical position
```

```
experimentData: use 'experimentData(object)'
Annotation: pd.mapping50k.hind240,pd.mapping50k.xba240
SnpClass: oligoSnpSet
hidden states: D N L A
breakpoints:
'data.frame':
                    11 obs. of 9 variables:
               "NA06993" "NA06993" "NA06993" ...
$ id
        : chr
               "1" "1" "1" "1" ...
$ chr : chr
               "N" "L" "N" "A" ...
 $ state: chr
 $ size : num
                48.71
                                       3.30 101.64 ...
                        4.81 15.34
                          902 202 3797 ...
        : num
                997 102
$ start: num
                0.837 49.598 54.499 69.854 73.174 ...
                49.5 54.4 69.8 73.2 174.8 ...
$ last : num
                 NA 49.5 54.4 69.8 73.2 ...
$ prev : num
                49.6 54.4 69.9 73.2 174.8 ...
$ next : num
  The breakpoints are provided as a data.frame:
> breaks <- breakpoints(fit)
> breaks <- breaks[breaks[, "state"] != "N", ]</pre>
  One may order the altered states from biggest to smallest for each chromosome as follows:
> breaks[order(breaks[, "chr"], breaks[, "size"], decreasing = TRUE),
      ]
          id chr state
                           size
                                         start
                                                    last
                                                              prev
                                     49.59781
                                               54.40975
1.2 NA06993
                     L 4.811945 102
                                                          49.54504
1.4 NA06993
                                     69.85447
                     A 3.299434 202
                                                73.15390
1.6 NA06993
                     D 1.985684 100 174.81510 176.80078 174.81429
               1
1.8 NA06993
                     D 1.586808 99 216.28600 217.87281 216.23992
1.10 NA06993
                     D 0.097921
                                  5 238.31994 238.41786 238.30267
               1
          next
1.2
      54.40975
1.4
     73.17407
1.6 176.80084
1.8
    217.89218
1.10 238.41786
```

The summary method returns a list where each element in the list provides statistics for an altered states. For each chromosome, the mean, median, and standard deviation of the size of the features and number of SNPs involved are reported. For instance, in this HMM the altered states were loss of heterozygosity (L), amplification of copy number (A), and deletion of copy number (D). Because we only have one sample and one chromosome in the fit example, the summary method is not that useful:

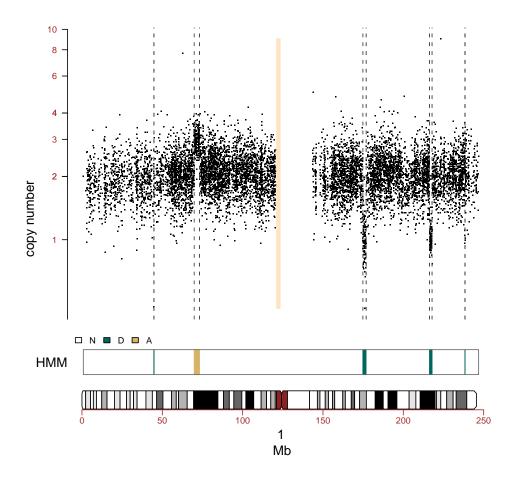
5 HMMs for different classes of data

5.1 Copy number

The method hmm has a different set of underlying hidden states depending on whether copy number estimates, genotype calls, or both are available. When only copy number estimates are available, the hidden states (for autosomes) are hemizygous or homozygous deletion (one or fewer copies), normal (two copies), and amplification (three or more copies). The corresponding data class is SnpCopyNumberSet. To illustrate, we convert the chromosome1 example to an object of this class and fit the HMM.

```
> chr1.cn <- as(chromosome1, "SnpCopyNumberSet")</pre>
> params.cn <- new("HmmParameter", snpset = chr1.cn, cn.location = 1:3,
      states = c("D", "N", "A"))
[1] "Transforming copy number to log2 scale."
[1] "Calculating emission probabilities for copy number estimates..."
> fit.cn <- hmm(params.cn, chr1.cn)</pre>
[1] "Transforming copy number to log2 scale."
> breakpoints(fit.cn)
          id chr state
                             size
                                             start
1.1 NA06993
                        43.865725
                                   877
                                         0.836727
                                                    44.70245
               1
                     N
    NA06993
                     D
                         0.040126
                                     2
                                         44.722116
1.2
               1
                                                    44.76224
1.3 NA06993
               1
                        25.058717 1122
                                         44.779351
                                                    69.83807
1.4 NA06993
                         3.299434
                                  202
                                         69.854466 73.15390
1.5 NA06993
             1
                     N 101.640222 3797
                                         73.174070 174.81429
1.6 NA06993
              1
                     D
                         1.985748 101 174.815096 176.80084
1.7 NA06993
                        39.313361 1899 176.926556 216.23992
                     N
1.8 NA06993
                         1.586808
                                    99 216.286002 217.87281
              1
                     D
                                   901 217.892177 238.30267
1.9 NA06993
                     N
                        20.410491
1.10 NA06993
                     D
                         0.097921
                                     5 238.319943 238.41786
               1
1.11 NA06993
                     N
                         8.431130 160 238.429864 246.86099
          prev
                    next
1.1
            NA
               44.70245
      44.70245
                44.76224
1.2
1.3
      44.76224
                69.85447
```

```
1.4
      69.83807 73.17407
1.5
      73.15390 174.81429
     174.81429 176.80084
1.6
     176.80084 216.28600
1.8
     216.23992 217.89218
     217.87281 238.31994
1.10 238.30267 238.41786
1.11 238.41786 246.86099
> graph.par <- new("ParHmmSnpCopyNumberSet")</pre>
> graph.par <- getPar(graph.par, chr1.cn)</pre>
> plotSnp(graph.par, chr1.cn, fit.cn)
NULL
```

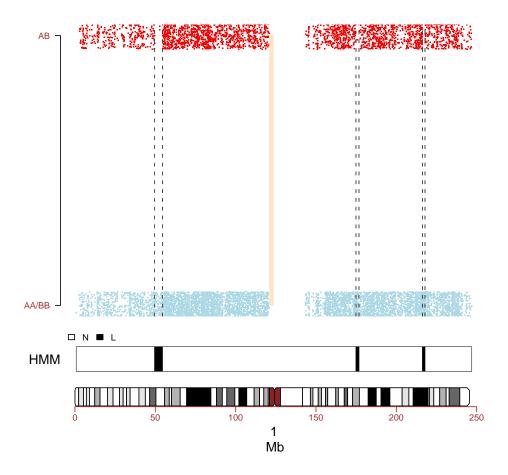


5.2 Genotype calls

When only genotype calls are available, the hidden states are loss and retention (ret) of heterozygosity. We define *loss* to be a sequence of homozygous SNPs longer than what we would expect to observe by chance. Note that many long stretches of homozygosity may occur as a result of a population sharing

a common underlying haplotype structure; loss predictions from an HMM fit to an indvidual do not necessarily reflect the 'loss' of an allele in that individual. For illustration, we convert the chromosome1 example to an object of class HmmSnpCallSet and refit the HMM.

```
> chr1.calls <- as(chromosome1, "SnpCallSet")</pre>
> params.calls <- new("HmmParameter", snpset = chr1.calls,
      states = c("L", "N"))
[1] "Calculating emission probabilities for genotype calls.... "
> fit.calls <- hmm(params.calls, chr1.calls)</pre>
> breakpoints(fit.calls)
         id chr state
                             size
                                      N
                                             start
                                                         last
                                                                   prev
1.1 NA06993
              1
                     N
                        48.708312
                                   997
                                          0.836727
                                                    49.54504
                                                                      NA
1.2 NA06993
              1
                     L
                         4.811945 102
                                         49.597810 54.40975
                                                               49.54504
1.3 NA06993
              1
                     N 120.350649 4907
                                         54.498950 174.84960
1.4 NA06993
                    L
                       1.788366
                                     92 174.915701 176.70407 174.84960
              1
1.5 NA06993
                     N 39.439518 1902 176.800399 216.23992 176.70407
              1
1.6 NA06993
              1
                    L
                        1.485826
                                     97 216.286002 217.77183 216.23992
                     {\tt N} \quad 28.988981 \ 1068 \ 217.872013 \ 246.86099 \ 217.77183
1.7 NA06993
         next
1.1 49.59781
1.2 54.40975
1.3 174.91570
1.4 176.80040
1.5 216.28600
1.6 217.87201
1.7 246.86099
> gp <- new("ParHmmSnpCallSet")</pre>
> graph.par <- getPar(gp, chr1.calls)</pre>
> plotSnp(graph.par, chr1.calls, fit.calls)
NULL
```



5.3 Genotype calls and copy number

Section 2 illustrates how one may fit the HMM to objects of class oligoSnpSet.

More documentation about the classes can be found in the documentation for the R package $\mathit{Vanil-laICE}$.

6 Session Information

The version number of R and packages loaded for generating the vignette were:

- R version 2.7.0 Under development (unstable) (2008-01-28 r44219), powerpc-apple-darwin8.11.0
- Locale: C
- Base packages: base, datasets, grDevices, graphics, methods, stats, tools, utils
- Other packages: Biobase 1.99.0, RColorBrewer 1.0-1, SNPchip 1.3.17, VanillaICE 1.1.14, oligo-Classes 1.1.15

References

- [1] Benilton Carvalho, Henrik Bengtsson, Terence P Speed, and Rafael A Irizarry. Exploration, normalization, and genotype calls of high-density oligonucleotide SNP array data. *Biostatistics*, 8(2):485–499, Apr 2007.
- [2] Robert B Scharpf, Giovanni Parmigiani, Jonathan Pevsner, and Ingo Ruczinski. A hidden Markov model for joint estimation of genotype and copy number in high-throughput SNP chips. Technical Report Working Paper 136, Johns Hopkins University, February 2007.