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Advanced registration of big image data

Outline

Image Registration

- ▶ Transformations
- ▶ Image Geometry
- ▶ Practical algorithmic details
 - ▶ choosing parameters
 - ▶ common pitfalls
 - ▶ big data strategies

Image registration

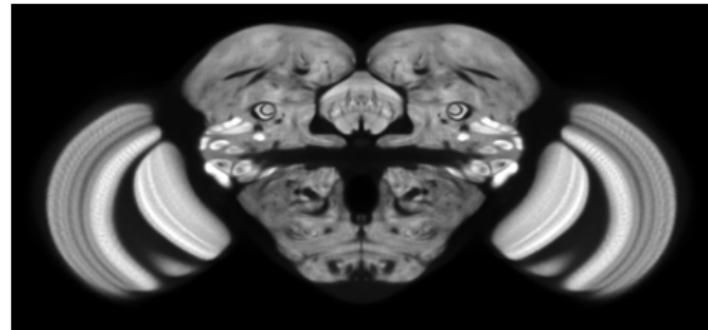
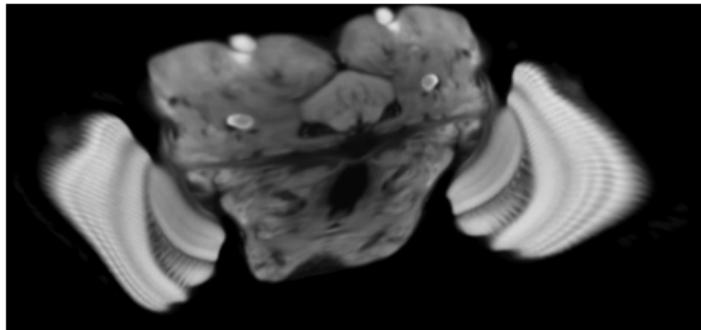


Image registration

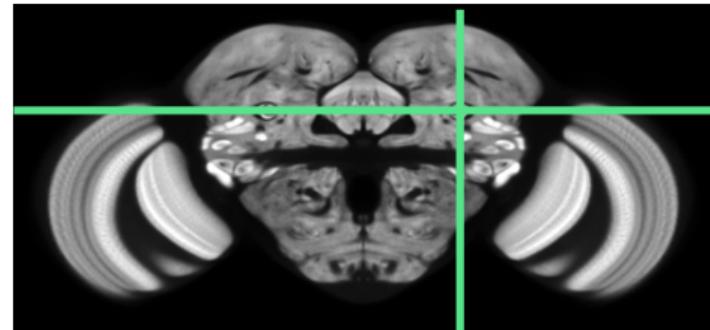
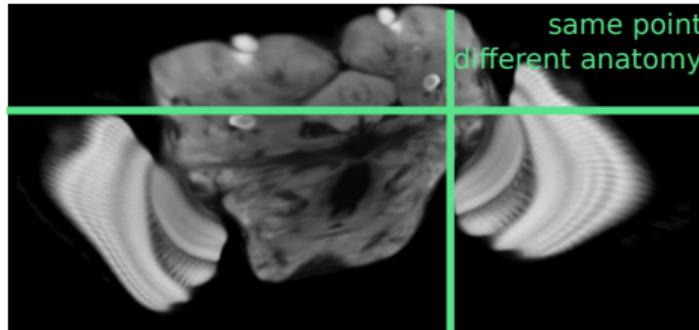


Image registration

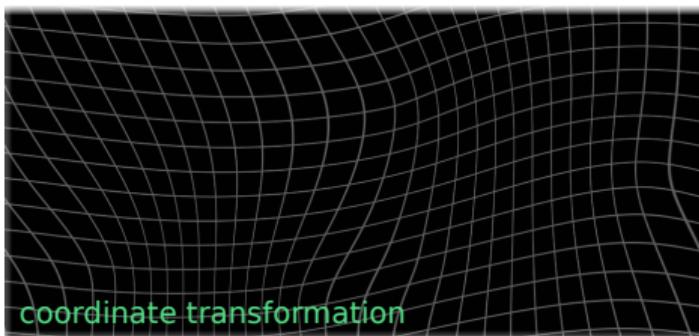
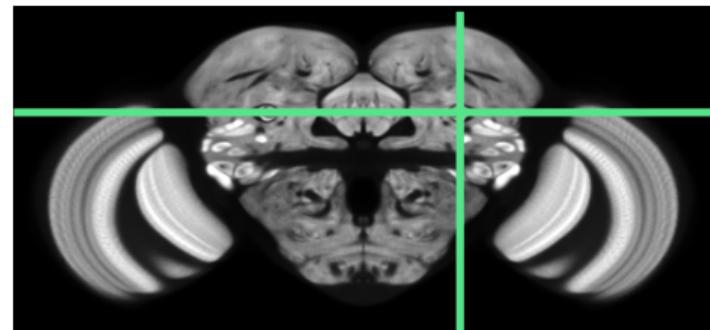
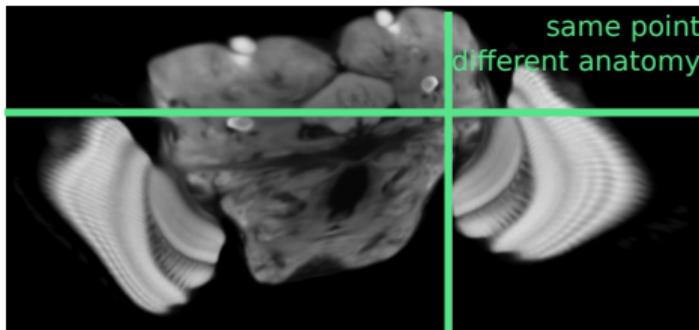
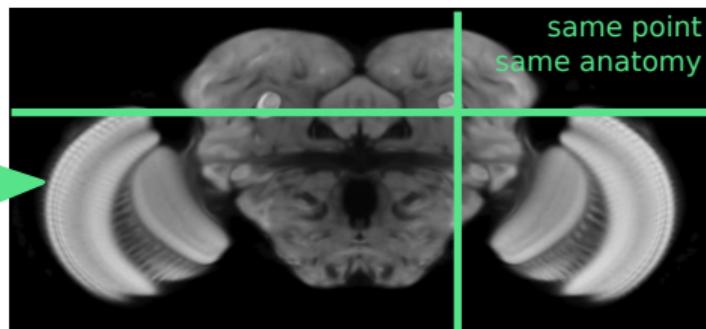
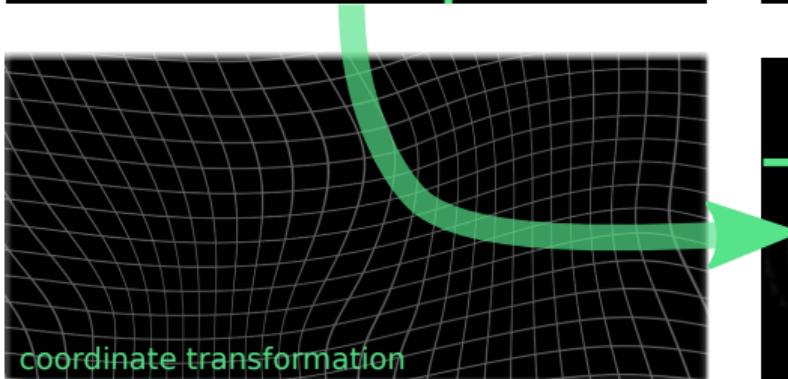
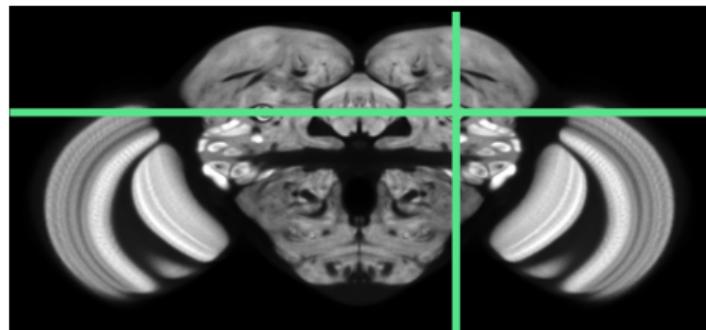
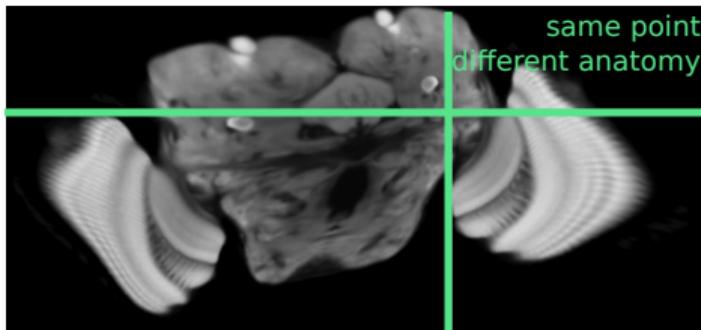


Image registration

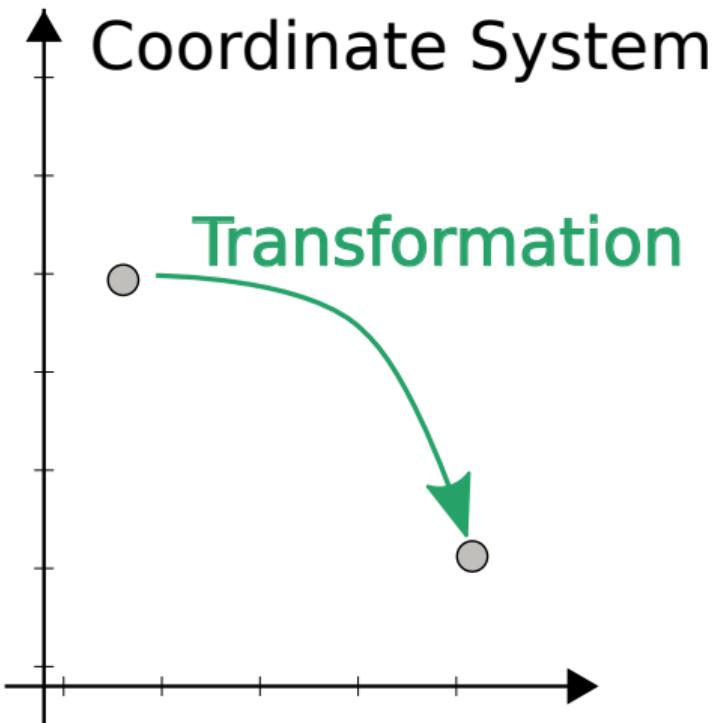


Key idea

The primary output of an image registration algorithm is the *transformation*.

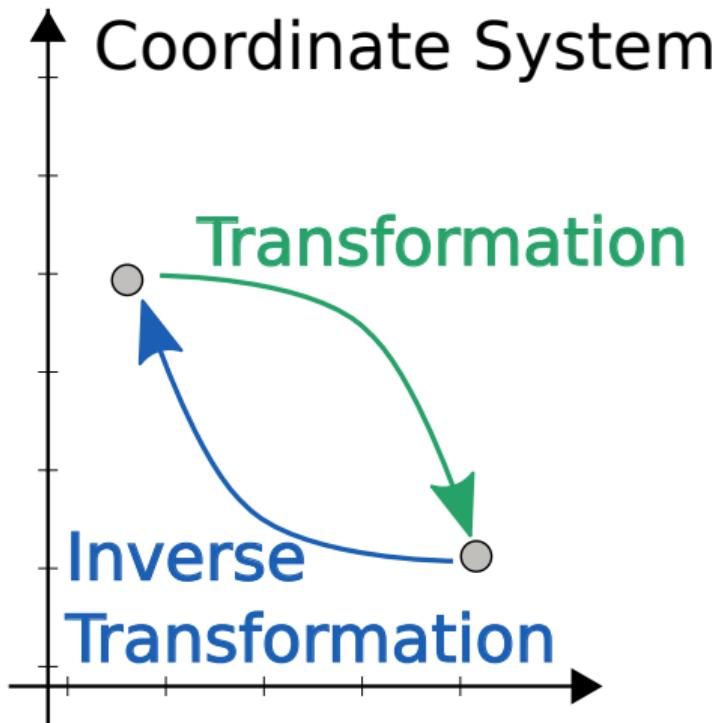
A secondary output of an image registration algorithm is the *transformed moving image*.

What is a transformation



Transformations are functions that:
take points (coordinates) as inputs
produce points (coordinates) as outputs.

What is a transformation



Transformations are functions that:
take points (coordinates) as inputs
produce points (coordinates) as outputs.

The inverse is a transformation that:
given the output of a transformation,
produces the original input point
(un-does the original transformation).

Quiz

If we have the transformation:

$$T(x, y) = (x + 5, y - 12)$$

what is the inverse transformation?

Quiz

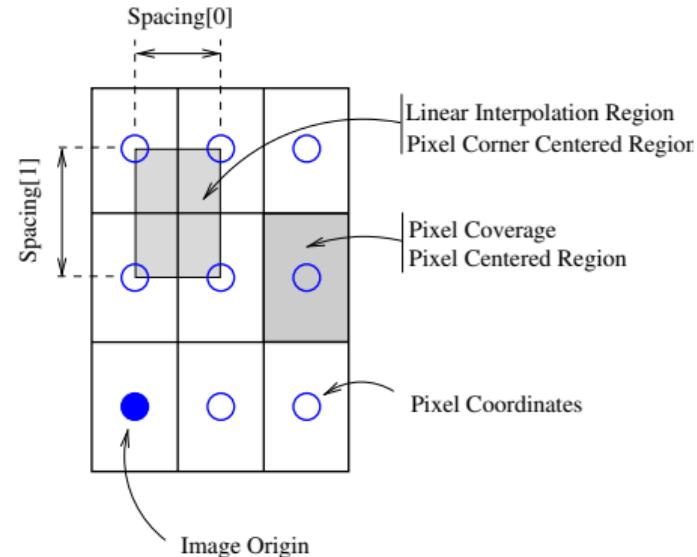
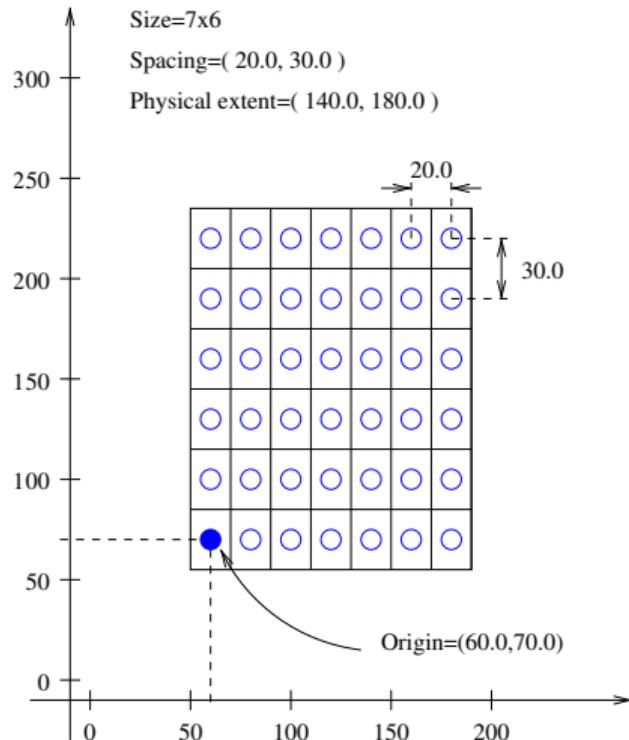
If we have the transformation:

$$T(x, y) = (x + 5, y - 12)$$

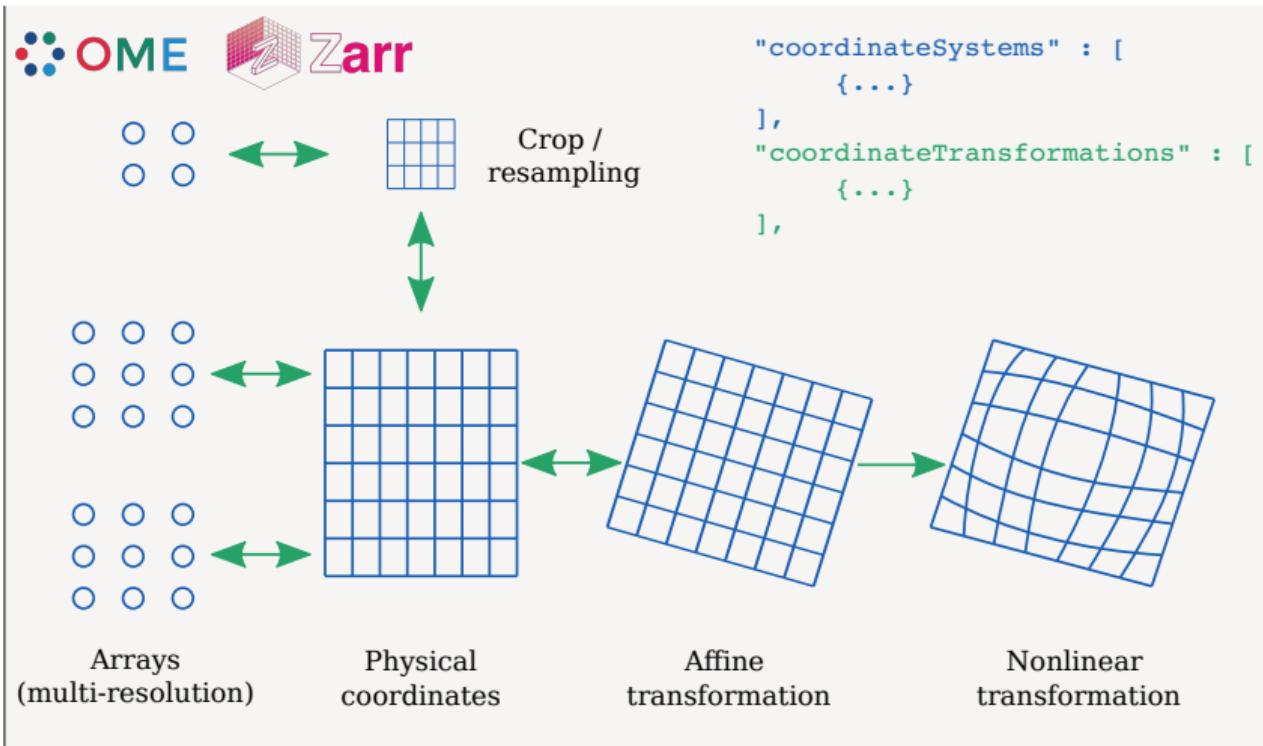
what is the inverse transformation?

$$T^{-1}(x, y) = (x - 5, y + 12)$$

Image geometry



Many relationships are transformations



Join the conversation at github.com/ome/ngff

Key ideas

Pixels (entries in the image array) are *point samples*.

Pixels are located in *physical coordinates*

Reinforce these ideas in `ResampleImages.ipynb`

point and image transformations

Define:

- ▶ The *forward* transformation maps *points* from moving to target space.
- ▶ The *inverse* transformation maps *points* from target to moving space.

point and image transformations

Define:

- ▶ The *forward* transformation maps *points* from moving to target space.
- ▶ The *inverse* transformation maps *points* from target to moving space.

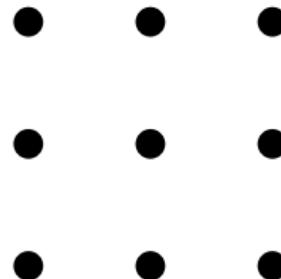
Then:

- ▶ We need the *inverse* transformation to map *images* from moving to target space
- ▶ We need the *forward* transformation to map *images* from target to moving space

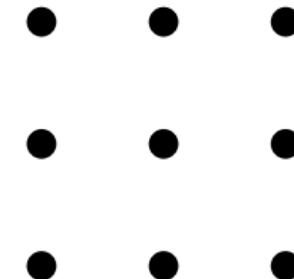
The following will explain why this is the case.

Transforms on a grid

Moving image grid

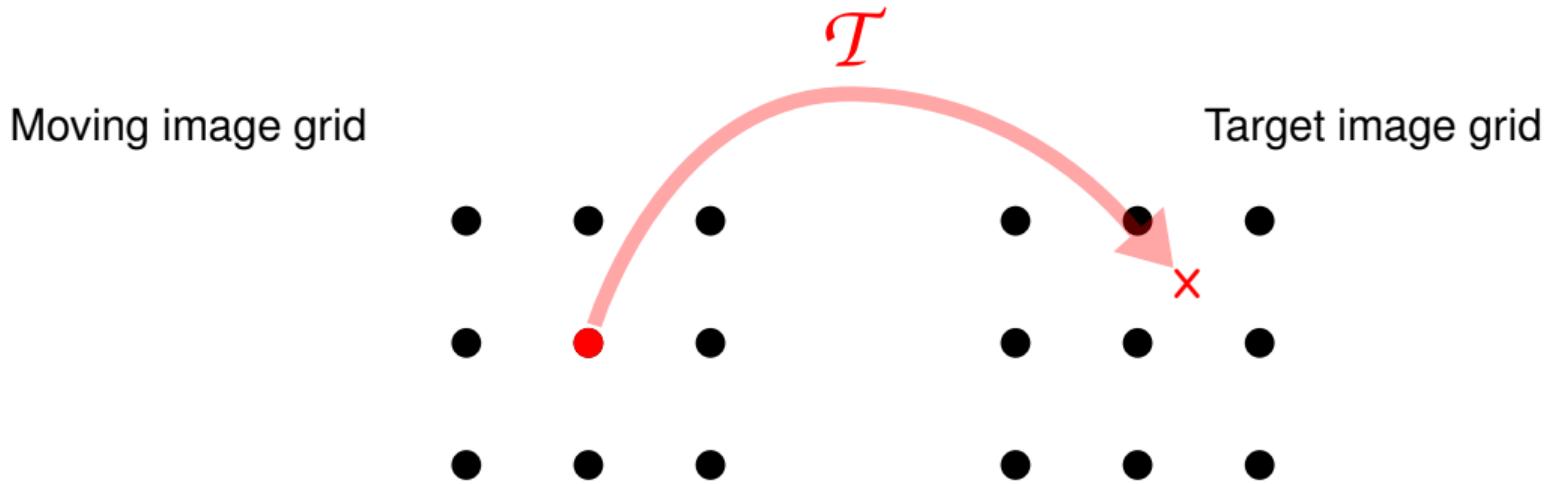


Target image grid



We have a moving image that we want to transform, and render on a new, target image grid.

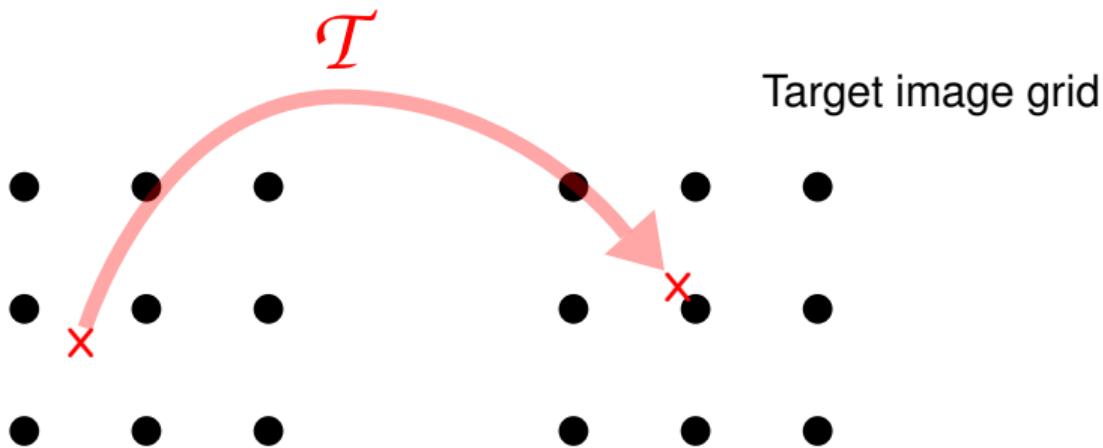
Transforms on a grid



A transformation maps points from the moving space to the target space. But moving grid points may not land on the target grid.

Transforms on a grid

Moving image grid

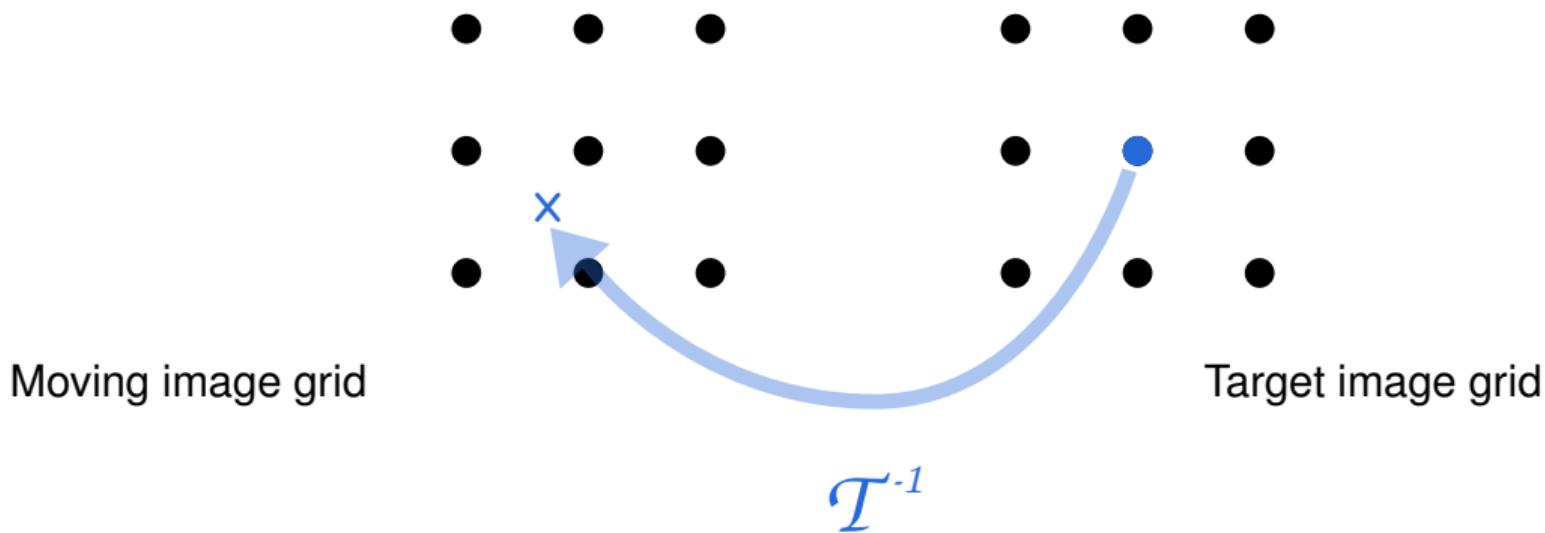


Target image grid

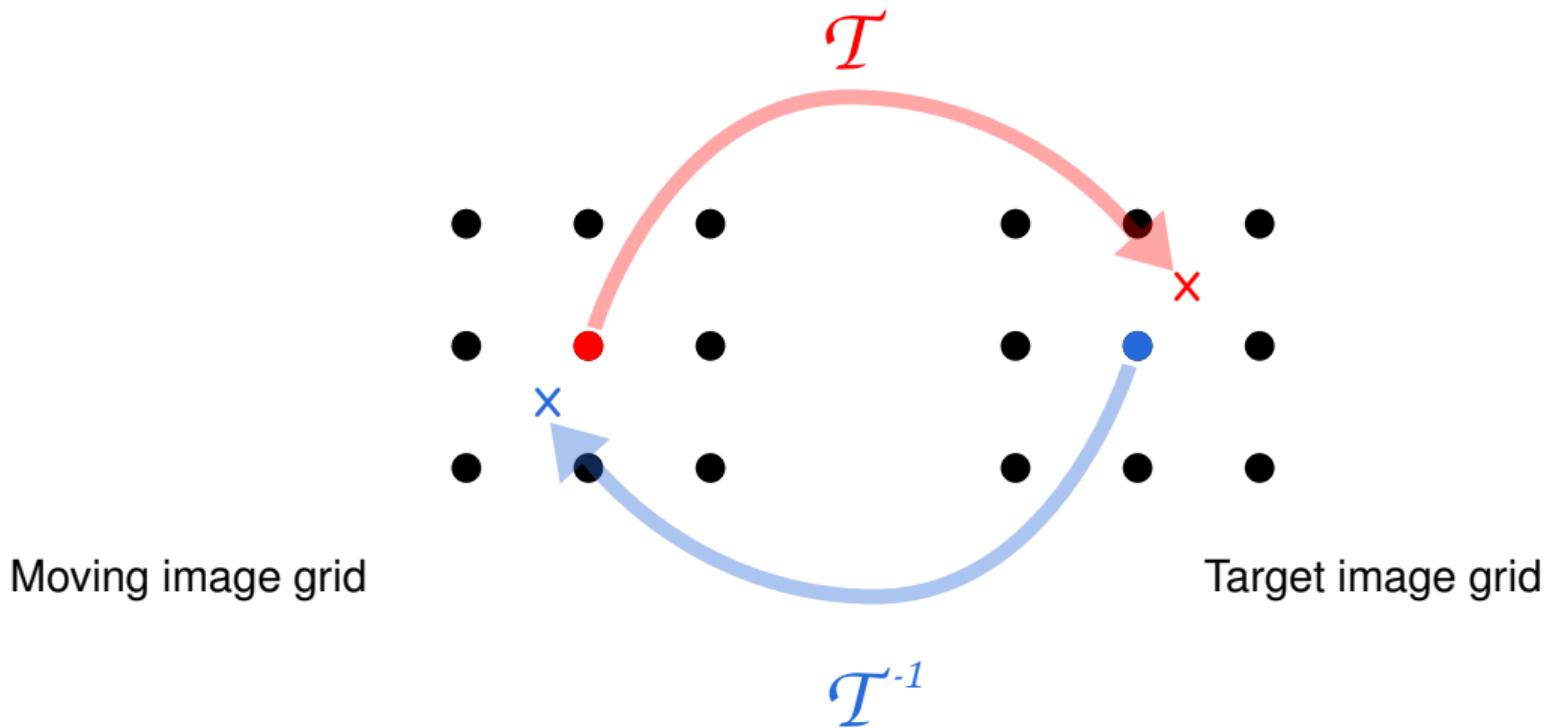
How do we find a point in moving space (possibly between grid points) that maps to a grid point?

Transforms on a grid

Applying the inverse of the transformation to grid points in target space tells us where to sample from in moving space.



Transforms on a grid



point and image transformations

Define:

- ▶ The *forward* transformation maps *points* from moving to target space.
- ▶ The *inverse* transformation maps *points* from target to moving space.

Then:

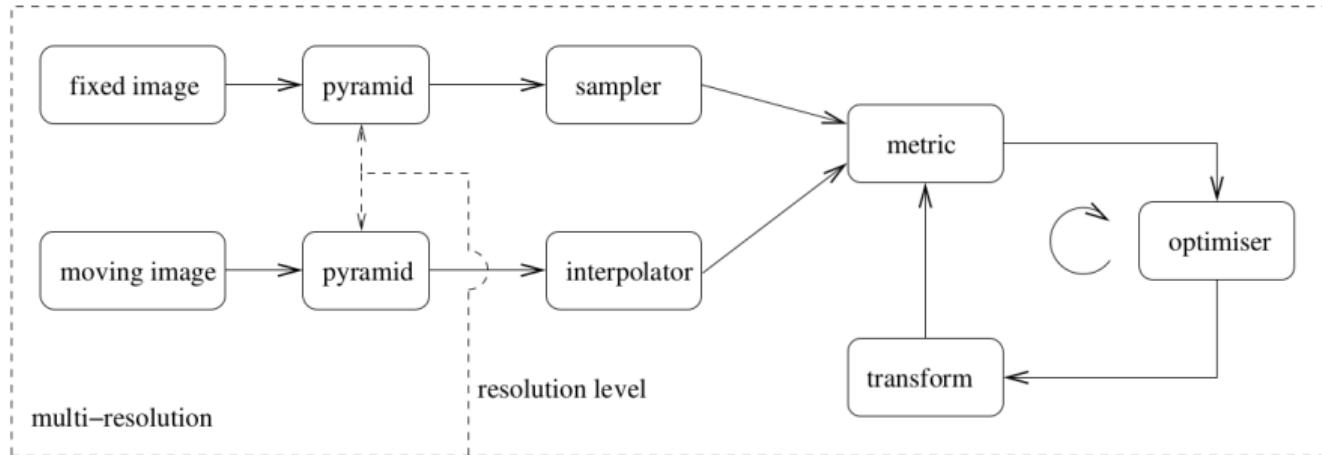
- ▶ We need the *inverse* transformation to map *images* from moving to target space
- ▶ We need the *forward* transformation to map *images* from target to moving space

Remember this when working through `RecoverOffset.ipynb`

“Pixel-based” Image Registration Algorithms

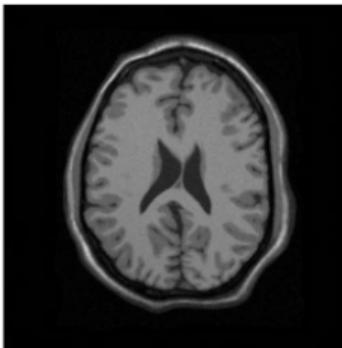
“Feature-based” registration methods will not be covered in this course.

Image registration pipeline

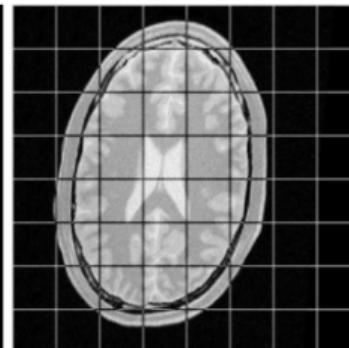


basic registration components

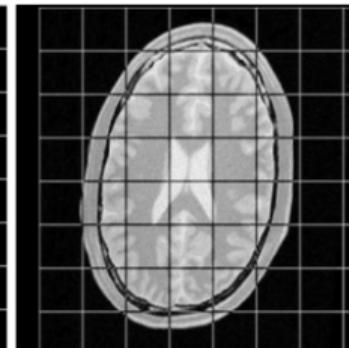
Transformation types



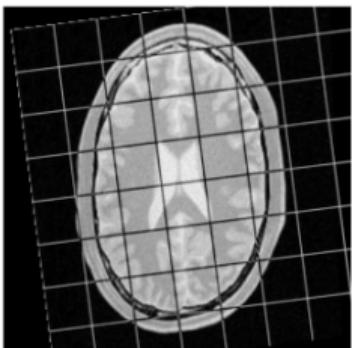
(a) fixed



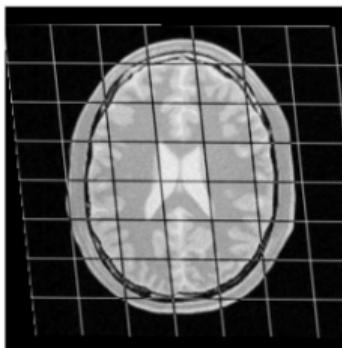
(b) moving



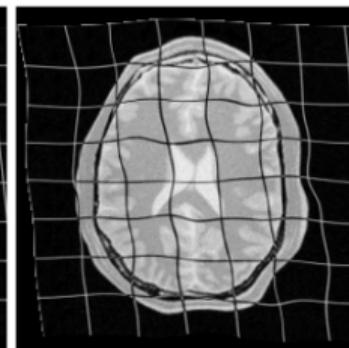
(c) translation



(d) rigid



(e) affine

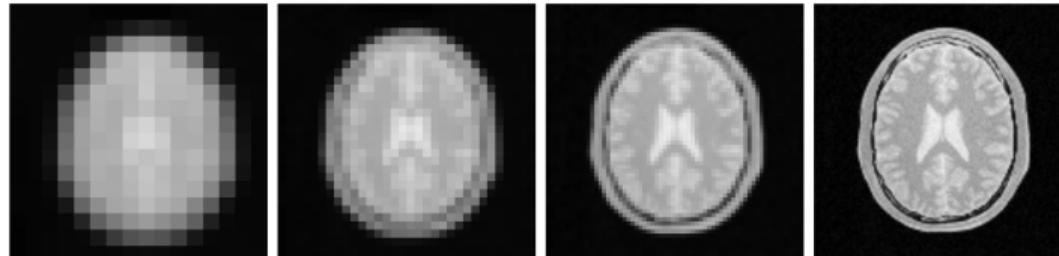


(f) B-spline

image from elastix manual

Multi-resolution registration

Smooth and
downsample



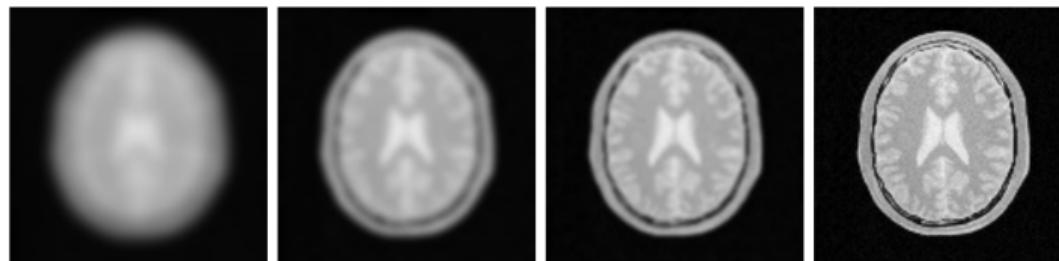
(a) resolution 0

(b) resolution 1

(c) resolution 2

(d) original

Smooth only



(e) resolution 0

(f) resolution 1

(g) resolution 2

(h) original

Optimization

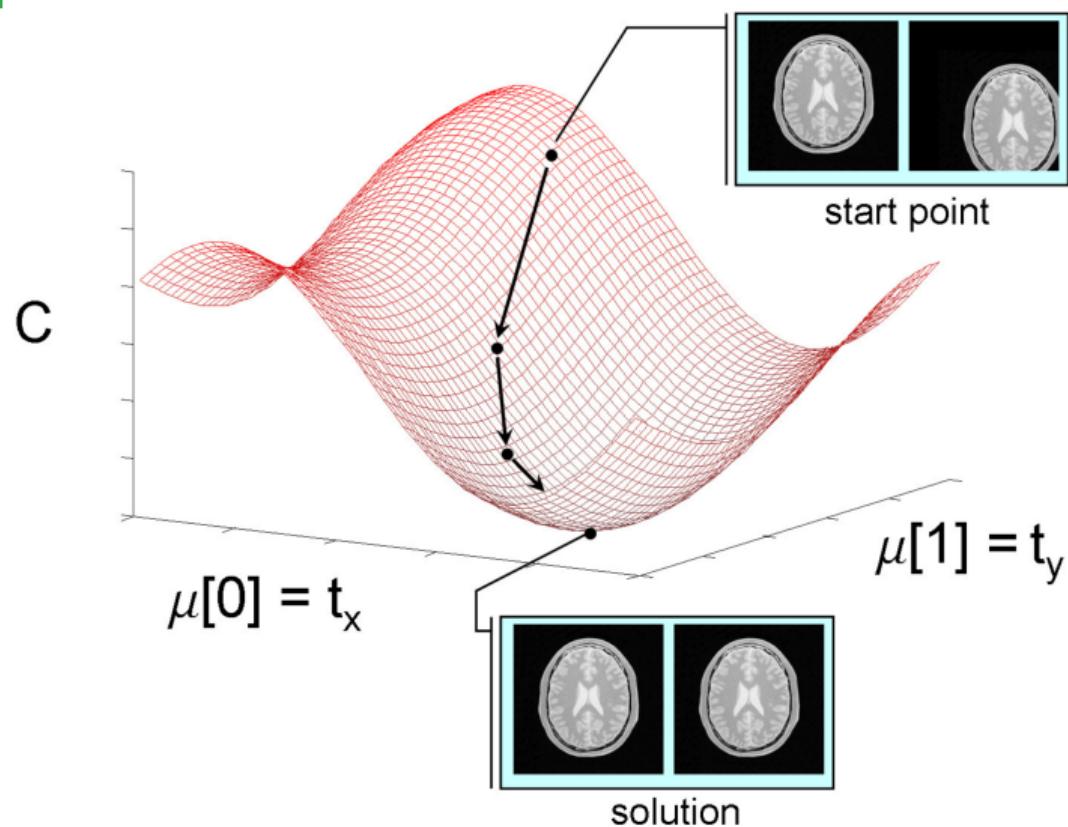


image from elastix manual

Elastix parameters

```
// ***** Image properties *****
(FixedInternalImagePixelType "float")
(MovingInternalImagePixelType "float")
(FixedImageDimension 3)
(MovingImageDimension 3)

// ***** Multiresolution *****
(Registration "MultiResolutionRegistration")
(NumberOfResolutions 4)
(FixedImagePyramid "FixedRecursiveImagePyramid")
(MovingImagePyramid "MovingRecursiveImagePyramid")

// The downsampling/blurring factors for the image pyramids. // There are defaults, but can be provided manually
// (ImagePyramidSchedule 8 8 8 4 4 4 2 2 2 1 1 1 )

// ***** Interpolation and Resampling *****
(Interpolator "BSplineInterpolator")
(ResampleInterpolator "FinalBSplineInterpolator")
(Resampler "DefaultResampler")

(BSplineInterpolationOrder 1)
(FinalBSplineInterpolationOrder 3)
(DefaultPixelValue 0)

// ***** Transformation *****
(Transform "AffineTransform")

// ***** Similarity metric *****
(Metric "AdvancedMattesMutualInformation")

// Some metrics have additional options
(NumberOfHistogramBins 32)
(NumberOfSpatialSamples 2048)
(NewSamplesEveryIteration "true")
(ImageSampler "Random")

// ***** Optimization *****
(Optimizer "AdaptiveStochasticGradientDescent")
(MaximumStepLength 0.5)

(MaximumNumberOfIterations 1000)

// or can have number of iterations per resolution
// (MaximumNumberOfIterations 500 250 100 50 )

// ***** Output options *****
(WriteResultImage "false")
(ResultImagePixelFormat "float")
(ResultImageFormat "nrrd")
```

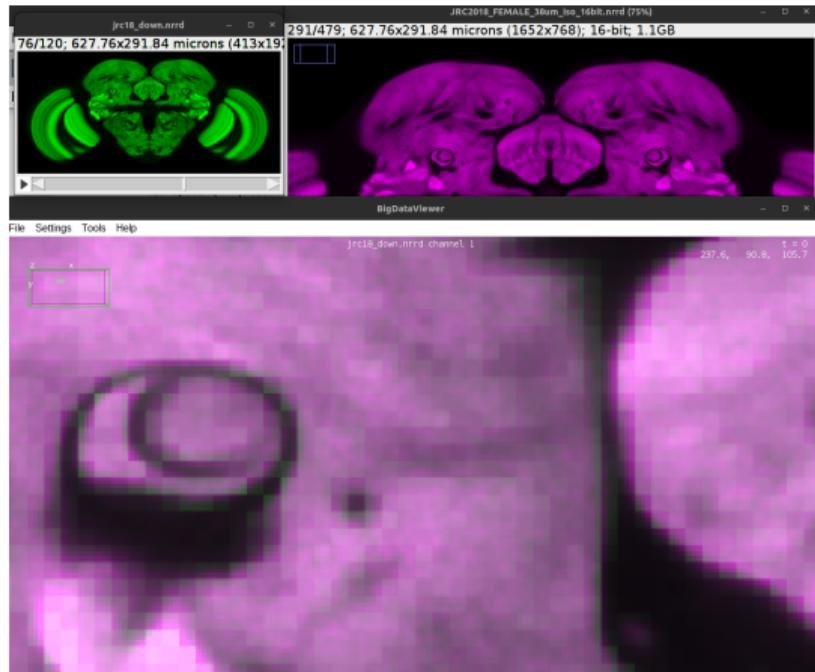
We will learn



- ▶ Reinforce fundamental concepts
- ▶ How to choose an appropriate metric
- ▶ Some properties registration algorithms
 - ▶ the importance of initialization
 - ▶ non-linear registration
- ▶ Strategies for big data
 - ▶ run registration at low resolution
 - ▶ apply transformation at full resolution

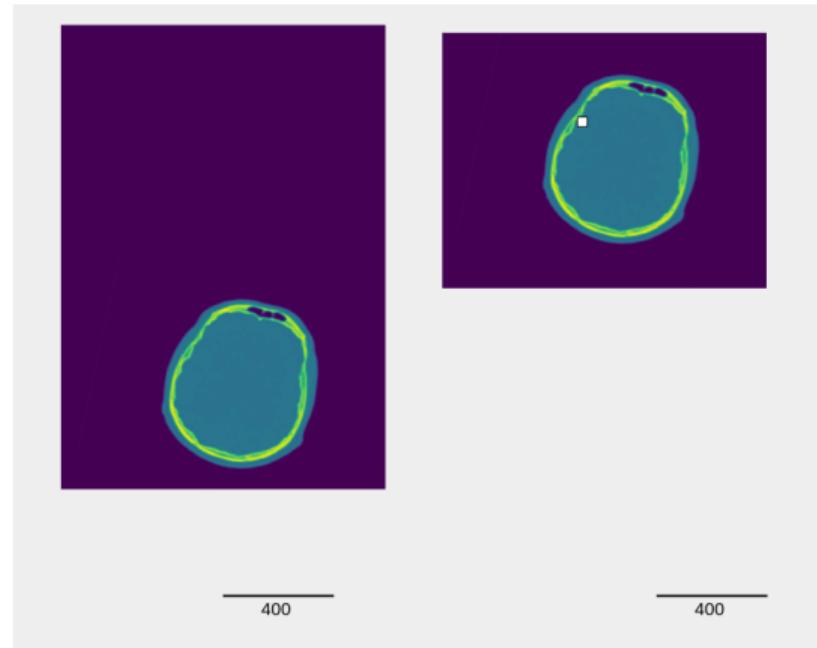
Practical outline

- ▶ resample_images.ipynb
 - ▶ Images have a physical coordinate system
 - ▶ Downsampling strategies might affect physical coordinates
- ▶ translation_INITIALIZATION.ipynb
- ▶ similarity_metrics.ipynb
- ▶ multi_resolution.ipynb
- ▶ nonlinear.ipynb



Practical outline

- ▶ resample_images.ipynb
- ▶ translation_INITIALIZATION.ipynb
 - ▶ Simple image registration (translation)
 - ▶ Initialization can be important
- ▶ similarity_metrics.ipynb
- ▶ multi_resolution.ipynb
- ▶ nonlinear.ipynb



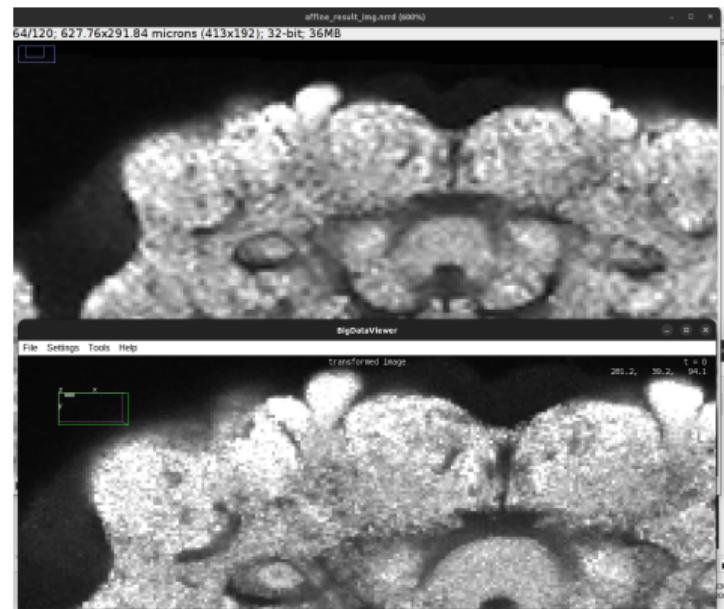
Practical outline

- ▶ resample_images.ipynb
- ▶ translation_INITIALIZATION.ipynb
- ▶ similarity_metrics.ipynb
 - ▶ Choosing an image similarity metric
- ▶ multi_resolution.ipynb
- ▶ nonlinear.ipynb

```
In [9]: compare_overlay(transformedMovingImage, fixedImage)
100
200
300
400
500
600
700
800
In [18]: paramsMI = sitk.ReadParameterFile('../elastixParameters/AffineMI_2d.txt')
sitk.PrintParameterMap( paramsMI )
...
In [19]: elastixImageFilterMI = sitk.ElastixImageFilter()
elastixImageFilterMI.SetParameterMap(paramsMI)
elastixImageFilterMI.SetFixedImage(fixedImage)
elastixImageFilterMI.SetMovingImage(movingImage)
elastixImageFilterMI.Execute()
transformedMovingImageMI = elastixImageFilterMI.GetResultImage()
...
In [20]: compare_overlay(transformedMovingImageMI, fixedImage)
0
100
200
300
400
500
600
700
800
0 200 400 600 800 1000
```

Practical outline

- ▶ resample_images.ipynb
- ▶ translation_INITIALIZATION.ipynb
- ▶ similarity_metrics.ipynb
- ▶ multi_resolution.ipynb
 - ▶ Big data strategies
- ▶ nonlinear.ipynb



Practical outline

- ▶ resample_images.ipynb
- ▶ translation_INITIALIZATION.ipynb
- ▶ similarity_metrics.ipynb
- ▶ multi_resolution.ipynb
- ▶ nonlinear.ipynb
 - ▶ Advanced, non-linear image registration
 - ▶ Measuring smoothness

