ArtiCheck: well-typed generic fuzzing for module interfaces

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Abstract

In spite of recent advances in full program certification, testing remains a widely-used component of the software development cycle. Various flavors of testing exist: popular ones include *unit testing*, which consists in manually crafting test cases for specific parts of the code base, as well as *quickcheck-style* testing, where instances of a type are automatically generated to serve as test inputs.

These classical methods of testing can be thought of as *internal* testing: the test routines access the internal representation of whatever data structure should be checked. We propose a new method of *external* testing where the library only deals with a *module interface*. The data structures are exported as *abstract types*; the testing framework behaves just like regular client code and combines functions exported by the module to build new elements of the various types. Counter-examples, if any, are then presented to the user.

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1. Introduction

Software development is hard. Industry practices still rely, for the better part, on tests to ensure the functional correctness of programs. Even in more sophisticated circles, such as the programming language research community, not everyone has switched to writing all their programs in Coq. Testing is thus a cornerstone of the development cycle. Moreover, even if the end goal is to fully certify a program using a proof assistant, it is still worthwhile to eliminate bugs early by running a cheap, efficient test framework.

Testing boils down to two different processes: generating test cases for test suites; and then verifying that user-written assertions and specifications of program parts are not falsified by the test suites:

QuickCheck is a popular, efficient tool for that purpose. First, it provides a combinator library based on type-classes to build test case generators. Second, it provides a principled way for the users to specify properties over functions. For instance, users may write predicates such as "reverse is an involution". Then, the QuickCheck framework is able to create *instances* of the type being tested, e.g.,

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lists of integers. The predicate is tested against these test cases, and any counter-example is reported to the user.

Our novel approach is motivated by some limitations of the QuickCheck framework. When users create trees, for instance, not only do they have to specify that leaves should be generated more often than nodes (for otherwise the tree generation would not terminate), but they also have to rely on a global size measure to stop generating new nodes after a while. It is thus up to the user of the library to implement their own logic for generating the right instances, within a reasonable size limit, combining the various base cases

We argue that these low-level manipulations should be taken care of by the library. When generating binary search tree instances, one ends up re-implementing a series of random additions and deletions, which are precisely the function that the code to be tested for exports. What if the testing framework could, by itself, combine functions exported by the module we wish to test, in order to build instances of the desired type? As long as the the module exports its correctness properties, all the testing library needs is functions that *return t*'s.

In the present document, we describe a library that does precisely that, dubbed ArtiCheck. The library is written in OCaml. While QuickCheck uses type-classes as a host language feature to conduct value generation, we show how to implement the proof search in library code – while remaining both type-safe and generic over the tested interfaces, thanks to GADTs.

2. The essence of external testing

In the present section, we illustrate the essential idea of external testing through a simple example, which is that of a module SIList whose type t represents sorted integer lists. The invariant is maintained by making t abstract and requiring the user to go through the exported functions empty and add.

This section, unfolding from the initial example, introduces the key ideas of external testing: a GADT type that describes well-typed applications in the simply-typed lambda calculus; a description of module signatures that we wish to test; type descriptors that record all the instances of a type that we managed to construct.

The point of view adopted in this section is intentedly simplistic. The design, as presented here, contains several obvious short-comings. It allows, nonetheless, for a high-level overview of our principles, and paves the way for a more thorough discussion of our design which appears in §3.

Here is the signature for our module of sorted integer lists.

```
module type SIList = sig
  type t

val empty: t
 val add: t -> int -> t
 val check: t -> bool
end
```

The check function represents the *invariant* that the module pretends it preserves. The module admits a straightforward implementation, as follows.

```
module SIList = struct
  type t = int list

let empty = []

let rec add x = function
  | [] -> [x]
  | t::q -> if t<x then t::add x q else x::t::q

let rec check = function
  | [] | [_] -> true
  | t1::(t2::_ as q) -> t1 <= t2 && check q
end</pre>
```

Roughly speaking, our goal is to generate, as if we were *client code* of the module, instances of type t using only the functions exported by the module. Therefore, one of our first requirements is a data structure for keeping track of the t's created so far. We also need to keep track of the integers we have generated so far, since they are necessary to call the add function: ArtiCheck will thus manipulate several ty's for all the types it handles.

```
type 'a ty = {
    (* Other implementation details omitted *)
    mutable enum: 'a list;
    fresh: ('a list -> 'a) option;
}
```

A type descriptor 'a ty keeps track of all the *instances* of 'a we have created so far in its enum field. Built-in types such as int do not belong to the set of types whose invariants we wish to check. For such types, we provide a fresh function that generates an instance different from all that we have generated so far.

From the point of view of the client code, all we can do is combine add and empty to generate new instances. ArtiCheck, as a fake client, should thus behave similarly and automatically perform repeated applications of add so as to generate new instances. We thus need a description of what combinations of functions are legal for ArtiCheck to perform.

In essence, we want to represent well-typed applications in the simply-typed lambda-calculus. This can be embedded in OCaml using generalized algebraic data types (GADTs). We define the GADT ('f, 'r) fn, which describes ways to generate instances of type 'r using a function of type 'f. We call it a function descriptor.

```
type (_,_) fn =
| Ret: 'a ty -> ('a, 'a) fn
| Fun: 'a ty * ('b, 'c) fn -> ('a -> 'b, 'c) fn

(* Helpers for creating [fn]'s. *)
let (@->) ty fd = Fun (ty,fd)
let returning ty = Ret ty
```

The Ret case describes a constant value, which has type 'a and produce one instance of type 'a. For reasons that will soon become apparent, we also record the descriptor of type 'a. Fun describes the case of a function from 'a to 'b: using the descriptor of type 'a, we can apply the function to obtain instances of type 'b; combining that with the other ('b, 'c) fn gives us a way to produce elements of type 'c, hence the ('a -> 'b, 'c) fn conclusion.

```
let (>>=) li f = List.flatten (List.map f li)
```

The eval function is central: taking a function descriptor fd, it recurses over it, thus refining the type of its argument f. The use of GADTs allows us to statically prove that the eval function only ever produces instances of type b. The codom function allows one to find the type descriptor associated to the return value (the codomain) of an fn.

Using the two functions above, it then becomes trivial to generate new instances of 'b.

```
let use (fd: ('a, 'b) fn) (f: 'a) =
  let prod = eval fd f in
  let ty = codom fd in
  List.iter (fun x ->
    if mem x ty then () else ty.enum <- x::ty.enum
) prod</pre>
```

The function takes a function descriptor along with a matching function. The prod variable contains all the instances of 'b we just managed to create; ty is the descriptor of 'b. We store the new instances of 'b in the corresponding type descriptor.

In order to wrap this up nicely, one can define *signature descriptors*. An entry in a signature descriptor is merely a function of a certain type 'a along with its corresponding function descriptor. Once this is done, the user can finally call our library and test the functions found in the signature description.

```
type sig_elem = Elem : ('a,'b) fn * 'a -> elem
type sig_descr = (string * sig_elem) list
let si_t =
    (* create a descriptor for [SIList.t]... *)
let int_t =
    (* ...and one for [int], with a [fresh] function *)

let sig_of_silist = [
    ("empty", (returning si_t, SIList.empty));
    ("add", (int_t @-> si_t @-> returning si_t, SIList.add));
]

let _ =
    Arti.check sig_of_silist SIList.check
```

The Arti.check function repeatedly calls use on the items found in the signature, until the desired number of instances have been created. The library calls use for each function in the signature several times: failing that, the only applications we could ever build would be of the form add empty n. The library then fetches the descriptor for SIList.t and check that each instance satisfies the SIList.check predicate.

3. Implementing ArtiCheck

The simplistic design we introduced in §2 conveys the main ideas behind ArtiCheck, yet fails to address a wide variety of problems. The present section reviews the issues with the current design and incrementally addresses them.

3.1 A better algebra of types

The simply-typed lambda calculus that we introduced only contains constants and functions. While one can theoretically encode sums and products using functions, it seems reasonable to have a built-in notion of sums and products in our language.

One of the authors naïvely suggested that the data type be extended with cases for products and sums, such as:

```
| Prod: ('a,'c) fn * ('b,'c) fn -> ('a * 'b,'c) fn
```

It turns out that the branch above does not describe products. If 'a is int -> int and 'b is int -> float, not only do the 'c parameters fail to match, but the 'a * 'b parameter in the conclusion represents a pair of functions, rather than a function that returns a pair! Another snag is that the type of eval makes no sense in the case of a product. If the first parameter of type ('a, 'b) fn represents a way to obtain a 'b from the product type 'a, then what use is the second parameter of eval?

In light of these limitations, we take inspiration from the literature on focusing and break the fn type into two distinct GADTs.

- The GADT ('a, 'b) negative (neg for short) represents a computation of type 'a that produces a result of type 'b.
- The GADT 'a positive (pos for short) represents a value, that is, the result of a computation.

```
type (_, _) neg =
| Fun : 'a pos * ('b, 'c) neg -> ('a -> 'b, 'c) neg
| Ret : 'a pos -> ('a, 'a) neg

and _ pos =
| Ty : 'a ty -> 'a pos
| Sum : 'a pos * 'b pos -> ('a, 'b) sum pos
| Prod : 'a pos * 'b pos -> ('a * 'b) pos
| Bij : 'a pos * ('a, 'b) bijection -> 'b pos

and ('a, 'b) sum = L of 'a | R of 'b
```

The pos type represents first-order data types: products, sums and atomic types, that is, whatever is on the rightmost side of an arrow. We provide an injection from positive to negative types via the Ret constructor: a value of type 'a is also a constant computation.

We do *not* provide an injection from negative types to positive types: this would allow nested arrows, that is, higher-order types. One can take the example of the map function, which has type ('a -> 'b) -> 'a list -> 'b list: we explicitly disallow representing the 'a -> 'b part as a Fun constructor, as it would require us to synthesize instances of a function type. Rather, we ask the user to represent 'a -> 'b as a Ty constructor; in other words, we ask the user to supply their own test functions as if they were a built-in type.

Our GADT does not accurately model tagged, n-ary sums of OCaml, nor records with named fields. We thus add a last Bij case; it allows the user to provide a two-way mapping between a builtin type (say, 'a option) and its ArtiCheck representation (() + 'a). That way, ArtiCheck can work with regular OCaml data types by converting them back-and-forth.

This change of representation incurs some changes on our evaluation functions as well. The eval function is split into several parts, which we detail right below.

```
let rec apply: type a b. (a, b) neg -> a -> b list =
  fun ty v -> match ty with
  | Fun (p, n) ->
     produce p |> concat_map (fun a -> apply n (v a))
     ...
and produce: type a. a pos -> a list =
```

Let us first turn to the case of *values*. In order to understand what ArtiCheck ought to do, one may ask themselves what the user can do with values. The user may destruct them: given a pair of type 'a * 'b, the user may keep just the first element, thus obtaining a new 'a. The same goes for sums. We thus provide a destruct function, which breaks down positives types by pattern-matching, populating the descriptions of the various types it encounters as it goes. (The remember function records all instances we haven't encountered yet in the type descriptor ty.)

Keeping this in mind, we must realize that if a function takes an 'a, the user may use any 'a it can produce to call the function. For instance, in the case that 'a is a product type 'a1 * 'a2, then any pair of 'a1 and 'a2 may work. We introduce a function called produce, which reflects the fact the user may choose any possible pair: the function exhibits the entire set of instances we can build for a given type.

Finally, the apply function, just like before, takes a *computation* along with a matching description, and generates a set of b. However, it now relies on product to exhaustively exhibit all possible arguments one can pass to the function.

We are now able to accurately model a calculus rich enough to test realistic signatures involving records, option types, and various ways to create functions.

3.2 Efficient representation of a set of instances

The (assuredly naïve) scenario above reveals several pain points with the current design.

- We represent our sets using lists. We could use a more efficient data structure.
- If some function takes, say, a tuple, the code as it stands will
 construct the set of all possible tuples, map the function over
 the set, then finally call destruct on each resulting element
 to collect instances. Naturally, memory explosion ensues. We
 propose a symbolic algebra for sets of instances that mirrors
 the structure of positive types and avoids the need for holding
 all possible combinations in memory at the same time.
- A seemingly trivial optimization sends us off the rails by generating an insane number of instances. We explain how to optimize further the code while still retaining a well-behaved generation.
- Fairness issues arise. Take the example of logical formulas. One
 may try to be smart: starting with constants, one may apply
 mk_and, then pass the freshly generated instances to mk_xor.

A consequence is that all the formulas with two combinators start with xor. If we just keep an iterative process and do not chain the instance generation process, formulas containing three combinators are only reached after we've exhausted all possible instances with two or less combinators. This breadth-first search of the instance space is sub-optimal. Can we do better?

Sets of instances The first, natural optimization that comes to mind consists in dropping lists in favor of a more sophisticated data type. We replace lists with a module PSet of polymorphic, persistent sets implemented as red-black trees.

Not holding sets in memory A big source of inefficiency is the call to the cartesian_product function above (§3.1). We hold in memory at the same time all possible products, then pipe them into the function calls so as to generate an even bigger set of elements. Only when the set of all elements has been constructed do we actually run destruct, only to extract the instances that we have created in the process.

Holding in memory the set of all possible products is too expensive. We adopt instead a *symbolic representation of sets*, where unions and products are explicitly represented using constructors. This mirrors our algebra of positive types.

```
type _ set =
   | Set : 'a PSet.t -> 'a set
   | Bij : 'a set * ('a, 'b) bijection -> 'b set
   | Union : 'a set * 'b set -> ('a, 'b) sum set
   | Product : 'a set * 'b set -> ('a * 'b) set
```

This does not suppress the combinatorial explosion. The instance space is still exponentially large; what we gained by changing our representation is that we no longer hold all the "intermediary" instances in memory *simultaneously*. This allows us to write an iter function that constructs the various instances on-the-fly.

Piping and non-termination In order to push the optimization above further, one can choose to perform the call to remember directly inside the Ret case of apply. That way, apply could just fill in the type descriptors using the global, mutable state and return unit, thus avoiding the need for intermediary lists of instances. Also, calling remember directly eliminates the need to store duplicate items, as the function automatically takes care of dropping an instance if we are already aware of it.

This seemingly innocuous optimization raised combinatorial explosion issues. We explain why, in the hope that it serves as an example for future generations ("kids, don't do mutable state").

Consider the case of a function that has type t -> t -> t and a corresponding type descriptor for t named ty. The outer call to apply binds the list of instances of t via let 1 = ty.enum. For each element of 1, a recursive call to apply takes place (for the inner t -> t function), which looks up the current value of ty.enum. Since each inner call populates ty.enum itself, for each new recursive call of apply, the value of ty.enum grows bigger and bigger. The programs terminates by exhausting its memory space without even returning from the outer call to apply.

We solved this by taking a snapshot of our negative types before calling apply. No copy is involved: function arguments (positive types) are represented in memory as persistent, pure symbolic sets. That way, we keep a copy of the arguments that are to be applied in each Fun case.

Fairness of our search space Snapshotting enforces a breadth-first search of the instance space. The initial set of instances is fed through the available functions, and we iterate the process, until we've obtained a satisfactory number of instances for each one of the types we wish to test.

The distribution of instances is skewed: there are more instances obtained after n calls than there are after n+1 calls. It may thus be the case that by the time we reach three of four consecutive function calls, we've hit the maximum limit of instances allowed for the type, since it often is the case that the number of instances grow exponentially.

We plan to implement a random search of the instance space and tweak our exploration procedures so that "interesting" instances pop up early.

3.3 Instance generation as a fixed point computation

The apply/destruct combination only demonstrates how to generate new instances from one specific element of the signature. We need to iterate this recipe on the whole signature, by feeding the new instances that we obtain to other functions that can in turn consume them.

This part of the problem naturally presents itself as a fixpoint computation, defined by a system of equations. Equations between variables (type descriptors) describe ways of obtaining new instances (by applying functions to other type descriptors). Of course, to ensure termination, we need to put a bound on the number of generated instances. When presenting an algorithm as a fixpoint problem, it is indeed a fairly standard technique to make the lattice space artificially finite in order to obtain the termination property.

Implementing an efficient fixpoint computation is a *surprisingly interesting* activity, and we are happy to use an off-the-shelf fixpoint library, François Pottier's Fix, to perform the work for us. Fix can be summarized by the signature below, obtained from user-defined instantiations of the types variable and property.

```
module Fix = sig
  type valuation = variable -> property
  type rhs = valuation -> property
  type equations = variable -> rhs

val lfp: equations -> valuation
end
```

A system of equations maps a variable to a right-hand side. Each right-hand side can be evaluated by providing a valuation so as to obtain a property. Valuations map variables to properties. Solving a system of equations amounts to calling the lfp function which, given a set of equations, returns the corresponding valuation.

A perhaps tempting way to fit in this setting would be to define variables to be our 'a ty (type descriptor) and properties to be 'a lists (the instances we have built so far); the equations derived from any signature would then describe ways of obtaining new instances by applying any function of the signature. This doesn't work as is: since there will be multiple values of 'a (we generate instances of different types simultaneously), type mismatches are to be expected. One could, after all, use yet another GADT and hide the 'a type parameter behind an existential variable.

```
type variable = Atom: 'a ty -> variable
type property = Props: 'a set -> property
```

The problem is that there is no way to statically prove that having an 'a var named x, calling valuation x yields an 'a property with a matching type parameter. This is precisely where the mutable state in the 'a ty type comes handy: even though it is only used as the *input* parameter for the system of equations, we "cheat" and use its mutable enum field to store the output. That way, the property type needs not mention the type variable 'a anymore, thus removing any typing difficulty – or the need to change the interface of Fix.

We still, however, need the property type to be a rich enough lattice to let Fix decide when to stop iterating: it should come with equality- and maximality-checking functions, used by Fix to detect that the fixpoint is reached. The solution is to define property as the number of instances generated so far along with the bound we have chosen in advance:

```
type variable = Atom : 'a ty -> variable
type property = { required : int; produced : int }
let equal p1 p2 = p1.produced = p2.produced
let is_maximal p = p.produced >= p.required
```

Expressing correctness properties

We mentioned in the SIList example the check function; among other things, what it does is call counter_example:

The function takes a description of some (positive) datatype 'a, iterates on the generated instances of this type and checks that a predicate 'a -> bool holds for all instances, or returns a counterexample otherwise. At a more abstract level, this means that we are checking a property of the form

$$\forall (x \in t), T(x)$$

where T(x) is simply a boolean expression. Multiple quantifiers can be simulated through the use of product types, such as in the typical formula of association maps:

```
\forall (m \in \text{map}(K, V)) \ \forall (k \in K) \ \forall (v \in V),
      lookup(k, insert(k, v, m)) = v
```

which can be expressed as follows (where *@ is the operator for creating product type descriptors):

```
let lookup_insert_prop (k, v, m) =
 lookup k (insert k v m) = v
let () = assert (None =
 let kvm_t = k_t *@ v_t *@ map_t in
 counter_example kvm_t lookup_insert_prop)
```

One then naturally wonders what a good language would be for describing the correctness properties we wish to check. In the example above, we naturally veered towards first-order logic, so as to express formulas with only prenex, universal quantification. The universal quantifiers are to be understood with a "test semantics", that is, they mean to quantify over all the random instances we generated. Can we do better? In particular, can we capture the full language of first-order logic, as a reasonable test description language for a practical framework?

It feels natural to use first-order logic as a specification language in the context of structured verification, such as with SMT solvers or a finite model [?]. However, supporting full first-order logic as a specification language for randomly-generated tests is hard for various reasons.

For instance, giving "test semantics" to an existentially-quantified formula such as $\exists (x \in t).T(x)$ is awkward. Intuitively, there is not much meaning to the formula. The number of generated instances is finite; that none satisfies T may not indicate a bug, but rather that

the wrong elements have been tested for the property. Conversely, finding a counter-example to a universally-quantified formula always means that a bug has been found. Trying to distinguish absolute (positive or negative) results from probabilistic results opens a world of complexity that we chose not to explore.

Surprisingly enough, there does not seem to be a consensus in the literature about random testing for an expressive, well-defined subset of first-order logic. The simplest subset one directly thinks of is formulas of the form:

$$\forall x_1 \dots x_n, P(x_1, \dots, x_n) \Rightarrow T(x_1, \dots, x_n)$$

where $P(x_1, \ldots, x_n)$ (the *precondition*) and $T(x_1, \ldots, x_n)$ (the test) are both quantifier-free formulas.

The reason this implication is given a specific status is to make it possible to distinguish tests that succeeded because the test was effectively successful from tests that succeeded because the precondition was not met. The latter are "aborted" tests that bring no significant value, and should thus be disregarded. In ArtiCheck, we chose to restrict ourselves to this last form of formulas.

5. Examples

5.1 Red-black trees

The (abridged) interface exported by red-black trees is as follows. The module provides iteration facilities over the tree structure val counter_example: 'a pos -> ('a -> bool) -> 'a optionthrough the use of zippers. Our data structures are persistent.

```
module type RBT = sig
  type 'a t
  val empty : 'a t
  val insert : 'a -> 'a t -> 'a t
  type direction = Left | Right
  (* type 'a zipper *)
  type 'a ptr (* = 'a t * 'a zipper *)
  val zip_open : 'a t -> 'a ptr
  val zip_close : 'a ptr -> 'a t
  val move_up : 'a ptr -> 'a ptr option
  val move : direction -> 'a ptr -> 'a ptr option
end
```

This examples highlights several strengths of ArtiCheck.

First, two different types are involved: the type of trees and the type of zippers. While an aficionado of internal testing may use the empty and insert functions repeatedly to create new instances of 'a t, it becomes harder to type-check calls to either insert or zip_open. Our framework, thanks to GADTs, generates instances of both types painlessly and automatically.

Second, we argue that a potential mistake is detected trivially by ArtiCheck, while it may turn out to be harder to detect using internal testing. If one removes the comments, the signature reveals that pointers into a tree are made up of a zipper along with a tree itself. It seems fairly natural that the developer would want to reveal the zipper type; it is, after all, a fundamental feature of the module. An undercaffeinated developer, when writing internal test functions, would probably perform sequences of calls to the various functions. What they would fail to do, however, is destructing pairs so as to produce a zipper associated with the wrong tree. This particularly wicked usage would probably be overlooked. ArtiCheck successfully destructs the pair and performs recombinations, to finally output:

```
TODO: fix the code so that it terminates
  ... and put the error message here
```

5.2 Binary Decision Diagrams

Binary Decision Diagrams (BDDs) represent trees for deciding logical formulas. The defining characteristic of BDDs is that they enforce *maximal sharing*: wherever two structurally equal subformulas appear, they are guaranteed to refer to the same object in memory. A consequence is that performing large numbers of function calls does not necessarily means using substantially more memory: it may very well be the case that significant sharing occurs.

We mentioned earlier that our strategy for external testing amounted, in essence, to representing series of well-typed function calls in the simply typed lambda calculus using in GADT. If we only did that and skipped section §3, externally-testing BDDs would be infeasible, as we would end up representing a huge number of function calls in memory.

Conversely, with the design we exposed earlier, we merely record new instances as they appear without holding the entire set of potential function calls in memory. This allows for an efficient, non-redundant generation of test cases (instances).

5.3 AVL trees

AVL trees are a classic of programming interviews; many a graduate student has been scared by the mere mention of them. It turns out that tenured professors *should* be scared too: the OCaml implementation of maps, written using AVL trees by a respectable researcher, contained a bug that went unnoticed for more than ten years. The bug was discovered when another enthusiastic researcher set out to formalize the said library in Coq. The bug was fixed, and all was well. Out of curiosity, we decided to run ArtiCheck on the faulty version of the library. After registering only four functions with ArtiCheck, the bug was correctly identified by our library, with arguably less pain than the full Coq formalization required.

6. Related and Future Work

Genericity of value generation The idea of generating random sequences of operations instead of random internal values is not novel; for example, QuickCheck was used as is to test imperative programs [?], by generating random values of an AST of operations, paired to a monadic interpreter of those syntactic descriptions. However, those examples in the literature only involve operations for a single return type, corresponding to the return type of the AST evaluation function. To integrate operations of distinct return types in the same interface description, one needs GADTs or some other form of type-level reasoning.

When multiple value types are involved, we found it helpful to think of well-typed value generation as term/proof search. Our well-typed rule to generate random values at type τ from a function at type $\sigma \to \tau$ and random values at type σ could be expressed, in term of QuickCheck Arbitrary instances, as a deduction rule of the form instance Arbitrary b, Arbitrary (a -> b) => Arbitrary b where ...; but Haskell's type-class mechanism would not allow this instance deduction rule, which does not respect its restrictions for principled, coherent instance elaboration. Type classes are a helpful and convenient host-language mechanism, but they are designed for code inference rather than arbitrary proof search. Our library-level implementation of well-typed proof search using GADTs gives us more freedom, and is the central idea of ArtiCheck.

It is of course possible to see chaining of function/method calls as a metaprogramming problem, and generate a reified description of those calls, to interpret through an external script or reflection/JIT capability, as done in the testing tool Randoop [?]. Doing the generation as a richly-typed host language library gives

us stronger type safety guarantees: even if our value generator is buggy, it will never compose operations in a type-incorrect way.

Testing of higher-order or polymorphic interfaces The type description language we use captures a first-order subset of the simply-typed lambda-calculus. A natural question is whether it would be possible to support random function generation – embed negative types into positives. Generating a function of type $\sigma \to \tau$ would entail adding its argument to the base of known value at type σ , and generating random values at type τ using the operations of the signature. This may result in genuinely new values if the argument passed is not reachable otherwise; consider a signature with two abstract types t, u and a single operation of type $(t \to t) \to u$: the only way to produce a u is to generate the identity function. QuickCheck function generation support use the function argument as additional entropy, but does not use the argument otherwise, and could not synthesize the identity function here.

It would also be interesting to support representation of polymorphic operations; we currently only describe monomorphic instantiations. Bernardy, Jansson and Claessen [?] have proposed a parametricity-based technique to derive specific monomorphic instances for type arguments, that also reduces the search space of values to be tested. Supporting this technique would be a great asset of a testing library, but it is not at all obvious how their pen-and-paper derivation could be automatized – and even less so whether this can be done internally, in the host language of the implementations being tested.

Bottom-up or top-down generation We have presented the ArtiCheck implementation as a bottom-up process: from a set of already-discovered values at the types of interest, we use the constructors of the interface to produce new values. In contrast, most random checking tools present generation in a top-down fashion: pick the head constructor of the data value, then we'll generate its sub-components recursively. One notable exception is SmallCheck [?], which performs exhaustive testing for values of bounded depth.

The distinction is however blurred by several factors. Our demand-driven computation of fixpoints, implemented by the Fix library, will result in more elements generated for the types most useful to the properties we wish to check, giving bottom-up search a top-down flavor. Relatedly, SmallCheck has a Lazy SmallCheck variant that uses laziness (demand-driven computation) to avoid fleshing out value parts that are not inspected by the property being tested.

Furthermore, the genericity of our high-level interface makes Articheck amenable to change in the generation technique; we could implement direct top-down search without changing the signature description language, or most parts of the library interface.

Richer property languages We discussed in Section 4 the difficulty of isolating an expressive fragment of first-order logic as a property language that could be given a realizable testing semantics. As it does exhaustive search (up to a bound), SmallCheck is able to give a non-surprising semantics to existential quantification. As we let user control for each interface datatype whether an exhaustive collection or random reservoir sampling should be used, we could support existential on exhaustively collected types only.

Otherwise, the work that stands out by supporting full-fledged first-order logic for random checking is Blanchette and Nipkow implementation of QuickCheck for Isabelle [?]. In the Isabelle proof assistant, it is common to define computations as inductive relations/predicates that can be given a (potentially non-deterministic) functional mode; instead of directly turning correctness formulas into testing programs, they translate formulas into inductive datatypes, which are then given a computational interpretation.

This is remarkable as it not only allows them to support a rich specification language, but also gives a principled explanation for the ad-hoc semantics of preconditions in testing frameworks (a failing precondition does not count as a passed test); instead of seeing a precondition P[x] as returning a boolean from a randomlygenerated x, they choose a mode assignment that inverts it into a logic program generating the xs accepted by the precondition. This gives a logic-based justification to various heuristics used in other works to generate random values more likely to pass the precondition, either domain-specific [?] or SAT-based [?].

Conclusion

We have presented the design of ArtiCheck, a novel library that allows one to check the invariants of a module signature by simulating user interaction with the module. ArtiCheck behaves like a fake client: it calls functions, constructs and destructs products or sums, and for each element check that the invariants are verified. The key to performing this in a generic, abstract manner relies on GADTs, which abstract the different types that may be manipulated into a common representation.

We identified various performance problems that arise. The library handles them via a symbolic representation of types in combination with a little bit of mutable state to avoid handling large, intermediary results in memory.

The result is a self-contained library that wraps the core concepts of *external testing* and offers clients a cheap and efficient way to test their programs. The library, for instance, successfully detects infamous issues such as the AVL re-balancing issue in the standard library of OCaml, with a much lower cost than a complete machine-assisted verification of the module.

While the library exposes the essence of *external testing* and has already proven worthwhile, we believe there is potential for improvement and expansion into a fully-fledged testing library.

References