Using asremlPlus, in conjunction with asreml, to do the analysis of a wheat experiment that includes choosing a local spatial variation model using AICs

Chris Brien

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This vignette shows how to use asremlPlus (Brien, 2023), in conjunction with asreml (Butler et al., 2023), to select the terms to be included in a mixed model for an experiment that involves spatial variation by comparing of information criteria. It also illustrates diagnostic checking and prediction production and presentation for this experiment. Here, asremlPlus and asreml are packages for the R Statistical Computing environment (R Core Team, 2023).

It is divided into the following main sections:

- 1. Set up the initial model for this experiment
- 2. Compare a series of information criteria to select a linear mixed model for the data
- 3. Diagnostic checking using residual plots and variofaces
- 4. Prediction production and presentation

## 1. Set up the initial model for this experiment

```
library(asreml, quietly=TRUE)

## Offline License checked out Sun Oct 29 16:34:07 2023

## Loading ASReml-R version 4.2

library(asremlPlus)
library(parallel)
library(doParallel)

## Loading required package: foreach

## Loading required package: iterators

library(foreach)
suppressMessages(library(qqplotr, quietly=TRUE))
options(width = 100)
```

#### Get data available in asremlPlus

The data are from a 1976 spring wheat experiment and are taken from Gilmour et al. (1995). An analysis is presented in the asreml manual by Butler et al. (2023, Section 7.6), although they suggest that it is a barley experiment.

```
data(Wheat.dat)
```

#### Add row and column covariates for the spatial modelling

#### Fit an initial model - Row and column random

In the following, an initial model is fitted that has the terms that would be included for a balanced lattice. In addition, a term WithinColPairs has been included to allow for extraneous variation arising between pairs of adjacent lanes.

#### Intialize a model sequence by loading the current fit into an asrtests object

In creating the asrtests object, IClikelihood is set to full so that the full Restricted Maximum Likelihood (full REML) of Verbyla, 2019 is incorporated into the tests.summary of the asrtests object.

## Check for and remove any boundary terms and print a summary of the fit in the asrtests object

```
current.asrt <- rmboundary(current.asrt)</pre>
print(current.asrt)
##
## #### Summary of the fitted variance parameters
##
##
                component std.error z.ratio bound %ch
## Row
                 5943.898 3815.514 1.557824
                                                  P 0.0
## Column
                12380.527 6323.542 1.957847
                                                  P 0.3
## Row:Column!R 20477.280 2896.642 7.069316
                                                  P 0.0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
```

```
##
                  Df denDF
                             F.inc
## (Intercept)
                      14.9 1390.00 0.0000
                      25.3
                              6.04 0.0008
## WithinColPairs 1 10.4
                              0.49 0.4998
## Variety
                  24 104.8
                              4.71 0.0000
##
## #### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
             terms DF denDF p
                                    AIC
                                             BIC
                                                          action
                          3 NA 1720.891 1823.253 Starting model
## 1 Initial model 31
```

The test.summary output shows that no changes have been made to the model loaded using as.asrtests. The pseudo-anova table shows that Varieties are highly significant (p < 0.001)

# 2. Compare a series of information criteria to select a linear mixed model for the data

In this section, models are compared using Akaike Information Criterion (AICs) based on the full REML.

#### Check the need for the term for within Column pairs (a post hoc factor)

```
current.asrt <- changeModelOnIC(current.asrt, dropFixed = "WithinColPairs",</pre>
                                 label = "Try dropping withinColPairs", IClikelihood = "full")
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
print(current.asrt)
##
##
## #### Summary of the fitted variance parameters
##
##
                component std.error z.ratio bound %ch
## Row
                 5941.153
                           3813.586 1.557891
## Column
                11165.335
                           5583.267 1.999785
                                                  Ρ
                                                      0
## Row:Column!R 20472.402 2895.582 7.070219
                                                      0
##
##
  #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
               Df denDF
                          F.inc
               1 15.3 1466.00 0e+00
## (Intercept)
## Rep
                5
                   26.7
                           6.11 7e-04
               24 105.3
## Variety
                           4.73 0e+00
##
```

##

```
## #### Sequence of model investigations
##
  (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##
##
                           terms DF denDF
                                           р
                                                      AIC
                                                                  BTC
                                                                              action
## 1
                                         3 NA 1720.891308 1823.25291 Starting model
                   Initial model 31
## 2 Try dropping withinColPairs -1
                                         O NA
                                                -2.281894
                                                            -5.29253
                                                                             Swapped
```

It is clear in the call to changeModelOnIC that the model is being changed by dropping the withinColPairs term, which could also be achieved using update.asreml. However, an asremlPlus model-changing function operates on an asrtests object, that includes an asreml object, and, except for changeTerms.asrtests, results in an asrtests object that may contain the changed model or the supplied model depending on the results of hypothesis tests or comparisons of information criteria. In addition, the result of the test or comparison will be added to a test.summary data.frame stored in the new asrtests object and, if the model was changed, the wald.tab in the new asrtests object will have been updated for the new model.

In this case, as can be seen from the summary of current.asrt after the call, the model without withinColPairs had a smaller AIC and so now the model stored in current.asrt does not include withinColPAirs. The wald.tab has been updated for the new model.

#### Choose a model for local spatial variation from several potential models

This example has been analyzed using a model for the local spatial variation based on a separable a separable autocorrelation process of order one (Butler et al., 2023). The need for this model can be assessed using the function addSpatialModelOnIC from asremlPlus that uses a forward selection strategy for fitting a correlation model (see output below). For this function, the spatial model to be fitted, the centred covariates for the two dimensions of the grid, and the factors corresponding to the covariates must be specified. Also, checkboundaryonly is set to TRUE so that no terms are removed until the final model has been fitted and IClikelihood is set to full so that the likelihood will be based on the full REML. Because the model that incorporates the spatial model has a smaller AIC, it is the model returned in spatial.ar1.asrt.

The print of spatial.ar1.asrt shows that an ar1 model for Row was tried first and was found to reduce the AIC by 11.898 and so became the current model. Next a model that incorporates an ar1 function for Column was similarly tried and became the current model. Then an appraisal of the need for a nugget term was made by comparing the fits with the residual variance unfixed and fixed at one. The model with the unfixed residual variance was chosen and is the model to be returned. The nugget term represents non-spatial variance, such as measurement error.

## Warning in infoCriteria.asreml(new.asrtests.obj\$asreml.obj, IClikelihood = ic.lik, : The following b

Column

```
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in infoCriteria.asreml(asrtests.obj$asreml.obj, IClikelihood = ic.lik, : The following bound
## Column
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.lik, bound.exclusions = bound.exclusion
## Column, Row:Column!R
## Warning in rmboundary.asrtests(as.asrtests(asreml.obj, wald.tab, test.summary, : In analysing yield,
                 but not removed because checkboundaryonly = TRUE:
##
## Column
## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, IClikelihood = ic.lik, : The following b
## Column, Row:Column!R
spatial.ar1.asrt <- rmboundary(spatial.ar1.asrt)</pre>
infoCriteria(list(nonspatial = current.asrt$asreml.obj,
                  ar1 = spatial.ar1.asrt$asreml.obj))
##
              fixedDF varDF NBound
                                        AIC
                                                         loglik
## nonspatial
                    0
                          3
                                 0 1409.023 1417.386 -701.5117
## ar1
                          5
                                 0 1353.762 1367.700 -671.8811
print(spatial.ar1.asrt)
##
##
## #### Summary of the fitted variance parameters
##
##
                            component
                                         std.error
                                                     z.ratio bound %ch
                                                                 P 0.1
                         2.198328e+03 8.220282e+03 0.2674273
## Row
## Row:Column
                         5.182588e+04 3.379434e+04 1.5335669
                                                                  P 0.0
## Row:Column!Row!cor
                         7.121382e-01 9.571017e-02 7.4405696
                                                                  U 0.0
## Row:Column!Column!cor 8.599817e-01 1.104239e-01 7.7880028
                                                                  U 0.0
## Row:Column!R
                         4.821208e+03 1.717263e+03 2.8074958
                                                                  P 0.0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##
               Df denDF
                          F.inc
## (Intercept) 1
                    1.8 194.600 0.0076
               5 21.8
                          0.559 0.7303
## Rep
## Variety
               24 74.3 10.560 0.0000
##
##
## #### Sequence of model investigations
##
```

```
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
                            terms DF denDF p
##
                                                       AIC
                                                                    BIC
                                                                                action
                                         3 NA 1720.891308 1823.252908 Starting model
## 1
                   Initial model 31
## 2 Try dropping withinColPairs -1
                                         O NA
                                                 -2.281894
                                                             -5.292530
                                                                               Swapped
                    Try ar1(Row)
                                   0
                                         2 NA
                                                -11.897710
                                                             -5.876439
                                                                               Swapped
## 3
## 4
                 Try ar1(Column)
                                                            -55.401009
                                                                               Swapped
                                         O NA
                                                -55.401009
                                                             -1.201255
## 5 Try fixed residual variance
                                                                             Unswapped
                                   0
                                        -1 NA
                                                  1.809381
## 6
                           Column
                                        NA NA
                                                                              Boundary
```

However, the spatial models that are available in asremlPlus also include those based on two-dimensional tensor-product natural cubic smoothing splines (TPNCSS), as described by Verbyla et al. (2018), and on two-dimensional tensor-product P-splines (TPPS), as described by Rodriguez-Alvarez et al. (2018) and Piepho, Boer and Williams (2022). The P-splines have been implemented using functions from the R package TPSbits authored by Sue Welham (2022)

The asremlPlus function chooseSpatialModelOnIC allows one to select the best model from amongst these spatial correlation models using the AIC. The four models from which it selects are (i) a separable autocorrelation model on both row and column dimensions (corr), (ii) a two-dimensional tensor-product natural cubic smoothing spline (TPNCSS), (ii) a two-dimensional tensor-product cubic P-spline with second-difference penalties (TPPCS), and (iii) a tensor-product two-dimensional linear P-spline with first-difference penalties (TPP1LS). By default all four are fitted and compared, but the trySpatial argument can be used to specify a subset of them.

The call to chooseSpatialModelOnIC, in addition to the arguments specifying covariates and factors, has further arguments: (i) dropRowTerm and dropColTerm that are needed in fitting P-splines, if overall Row and Column terms have been fitted in the supplied model, because the code also automatically includes these terms, (ii) rotateX and ngridangles so that a grid of angles of every five degrees between 0 and 90 in both directions is explored for rotating the eigenvectors of the penalty matrix for the linear component of the P-splines (requiring  $(30+1)^2=961$  re-analyses), (iii) nrotacores for setting the number course to use in analyzing, for each column angle, the set of row angles being investigates, (iv) an asreml.option argument to specify that the grp method be used in fitting the P-spline terms, this being required for nrotacores greater than one, and (v) return.asrts to specify which asrtests objects are to be returned. Here we specify all so that asrtests objects for the fits for all four spatial models will be returned. In this case, neither the checkboundaryonly nor the IClikelihood arguments were set because their defaults for chooseSpatialModelOnIC are appropriate.

Note that this function can take a substantial amount of time to execute (more than 45 minutes), principally because of the re-analyses required to search the grid of  $31 \times 31$  angles.

```
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
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## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
## sc: 0 thetas: 0, 90 elapsed time: 75.33 seconds
## sc: 1 thetas: 3, 90 elapsed time: 135 seconds
## sc: 2 thetas: 6, 90 elapsed time: 210.69 seconds
## sc: 3 thetas: 9, 90 elapsed time: 279.66 seconds
## sc: 4 thetas: 12, 90 elapsed time: 352.97 seconds
## sc: 5 thetas: 15, 90 elapsed time: 417.22 seconds
## sc: 6 thetas: 18, 90 elapsed time: 482.02 seconds
## sc: 7 thetas: 21, 90 elapsed time: 548.86 seconds
## sc: 8 thetas: 24, 90 elapsed time: 618.96 seconds
## sc: 9 thetas: 27, 90 elapsed time: 682.35 seconds
## sc: 10 thetas: 30, 90 elapsed time: 762.69 seconds
## sc: 11 thetas: 33, 90 elapsed time: 835.1 seconds
## sc: 12 thetas: 36, 90 elapsed time: 903.14 seconds
## sc: 13 thetas: 39, 90 elapsed time: 970.44 seconds
## sc: 14 thetas: 42, 90 elapsed time: 1035.64 seconds
## sc: 15 thetas: 45, 90 elapsed time: 1099.77 seconds
## sc: 16 thetas: 48, 90 elapsed time: 1163.74 seconds
## sc: 17 thetas: 51, 90 elapsed time: 1231.02 seconds
## sc: 18 thetas: 54, 90 elapsed time: 1300.35 seconds
## sc: 19 thetas: 57, 90 elapsed time: 1366.5 seconds
## sc: 20 thetas: 60, 90 elapsed time: 1440.04 seconds
## sc: 21 thetas: 63, 90 elapsed time: 1507.02 seconds
## sc: 22 thetas: 66, 90 elapsed time: 1571.83 seconds
## sc: 23 thetas: 69, 90 elapsed time: 1639.72 seconds
## sc: 24 thetas: 72, 90 elapsed time: 1704.08 seconds
## sc: 25 thetas: 75, 90 elapsed time: 1752.63 seconds
## sc: 26 thetas: 78, 90 elapsed time: 1804.91 seconds
## sc: 27 thetas: 81, 90 elapsed time: 1858.8 seconds
## sc: 28 thetas: 84, 90 elapsed time: 1921.66 seconds
## sc: 29 thetas: 87, 90 elapsed time: 1980.97 seconds
## sc: 30 thetas: 90, 90 elapsed time: 2037.02 seconds
## #### Optimal thetas: 21,66
## Notice : Spline design points closer than .000900 have been merged
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## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
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## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
```

```
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
```

#### Output the results

```
print(spatial.asrts$spatial.IC)
              {\tt fixedDF} \ {\tt varDF}
                                           BIC
                                 AIC
                                                  loglik
## nonspatial
                   30
                          3 1718.609 1817.960 -826.3047
                   30
                          5 1651.317 1756.689 -790.6583
## corr
## TPNCSS
                   33
                          6 1639.489 1756.904 -780.7445
## TPPCS
                   33
                          7 1642.838 1763.263 -781.4190
## TPP1LS
                   30
                          3 1708.443 1807.794 -821.2214
print(spatial.asrts$best.spatial.mod)
## [1] "TPNCSS"
print(spatial.asrts$asrts$TPNCSS)
##
## #### Summary of the fitted variance parameters
##
##
                           component std.error z.ratio bound %ch
## spl(cRow):cColumn
                            523.2004 372.8016 1.403429
                                                                 0
## dev(cRow)
                           7664.0211 4442.0646 1.725329
                          13338.7348 9236.0511 1.444203
## spl(cColumn)
                                                                 0
                                                                 0
## spl(cColumn):cRow
                            366.7707 322.7484 1.136399
                                                             Ρ
## spl(cRow):spl(cColumn) 3630.2187 2186.1497 1.660554
                                                             Ρ
                                                                 0
## Row:Column!R
                           7658.0113 1312.2026 5.835998
                                                                 0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##
                Df denDF
                           F.inc
                                     Pr
## (Intercept)
                 1
                     6.8 2645.00 0.0000
## Rep
                 5
                   41.3
                           20.45 0.0000
                24 86.5
## Variety
                           10.15 0.0000
                 1
                     7.0
                            0.07 0.7954
## cRow
                 1 30.1
                           20.30 0.0001
## cColumn
                           22.00 0.0000
## cRow:cColumn 1 64.3
##
##
## #### Sequence of model investigations
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##
                           terms DF denDF p
                                                      AIC
                                                                 BIC
                                                                              action
```

```
## 1
                   Initial model 31
                                        3 NA 1720.891308 1823.25291 Starting model
## 2 Try dropping withinColPairs -1
                                        O NA
                                               -2.281894
                                                           -5.29253
                                                                           Swapped
         Try tensor NCS splines 3
                                        3 NA -79.120426 -61.05661
                                                                           Swapped
## 4
                    dev(cColumn) 1
                                       NA NA 1639.488959 1756.90374
                                                                          Boundary
## 5
                       spl(cRow) 1
                                       NA NA 1639.489011 1756.90379
                                                                          Boundary
printFormulae(spatial.asrts$asrts$TPNCSS$asreml.obj)
##
##
## #### Formulae from asreml object
##
## fixed: yield ~ Rep + Variety + cRow + cColumn + cRow:cColumn
## random: ~ spl(cColumn) + dev(cRow) + spl(cRow):cColumn + spl(cColumn):cRow + spl(cRow):spl(cColumn)
## residual: ~ Row:Column
```

The output shows that the TPNCSS model has the lowest AIC and so is selected as the best model. The model fitted for the TPNCSS model has been printed using printFormulae.asreml. The fitted model includes the term dev(cRow) that is equivalent to a random Row term and measures the deviations of the Row trend from a linear trend, the spl(cRow) term having been dropped because it was estimated to be zero. The Wald F-statistic for Variety is now 10.15 with 86.5 denominator degrees of freedom, as compared to 10.56 and 74.3 for the correlation model and 4.71 and 105.3 for the initial nonspatial model.

#### 3. Diagnosting checking using residual plots and variofaces

Get current fitted asreml object and update to include standardized residuals

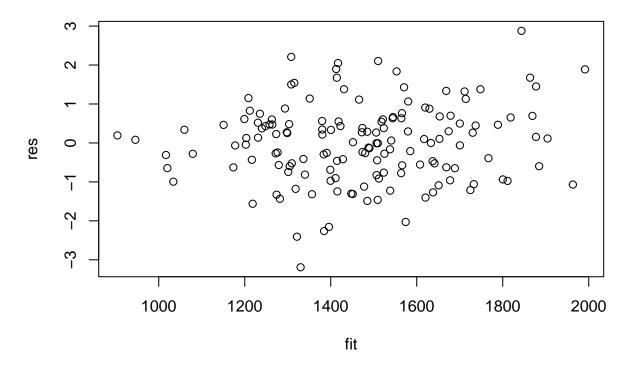
```
current.asr <- spatial.asrts$asrts$TPNCSS$asreml.obj
current.asr <- update(current.asr, aom=TRUE)

## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
Wheat.dat$res <- residuals(current.asr, type = "stdCond")
Wheat.dat$fit <- fitted(current.asr)</pre>
```

#### Do diagnostic checking

Do residuals-versus-fitted values plot

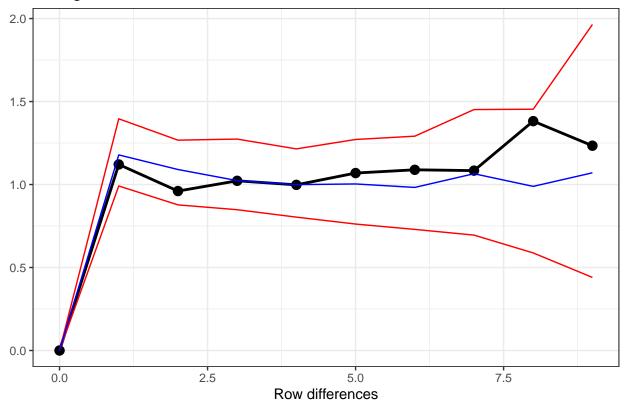
```
with(Wheat.dat, plot(fit, res))
```



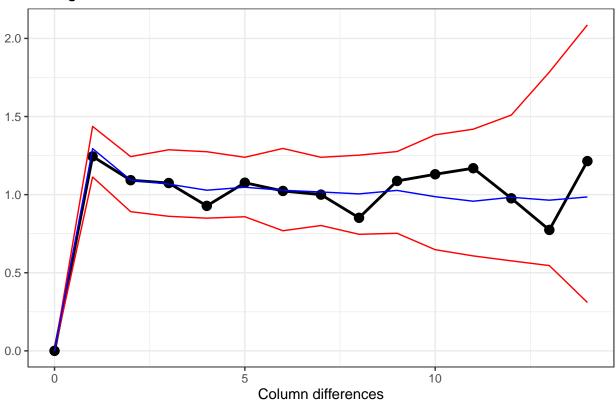
#### Plot variofaces

## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged

## Variogram face of Standardized conditional residuals for Row



## Variogram face of Standardized conditional residuals for Column

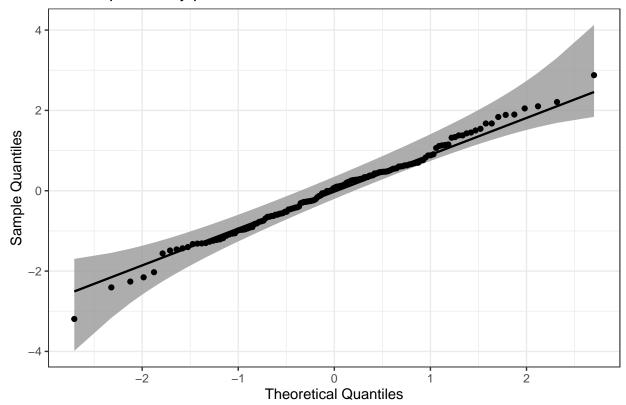


The variofaces are the lag 1 plots of the sample semivariogram with simulated confidence envelopes (Stefanova et al., 2009).

#### Plot normal quantile plot

The plot is obtained using the ggplot function with extensions available from the qqplotr package (Almeida et al., 2023).

#### Normal probability plot



### 4. Prediction production and presentation

Get Variety predictions and all pairwise prediction differences and p-values

```
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
```

```
##
##
##
  #### Predictions for yield from Variety
##
## Notes:
## - The predictions are obtained by averaging across the hypertable
     calculated from model terms constructed solely from factors in
     the averaging and classify sets.
## - Use 'average' to move ignored factors into the averaging set.
## - spl(cRow) evaluated at average value of 0.00000
## - spl(cColumn) evaluated at average value of 0.00000
## - The simple averaging set: Rep
##
##
      Variety predicted.value standard.error upper.halfLeastSignificant.limit
## 1
           10
                      1196.214
                                      64.11316
                                                                        1255.028
## 2
            9
                      1266.442
                                      69.62176
                                                                        1325.255
## 3
           16
                      1268.206
                                     74.01873
                                                                        1327.020
## 4
            1
                      1273.794
                                      69.30592
                                                                        1332.608
## 5
           14
                      1310.806
                                      70.75661
                                                                        1369.620
## 6
           23
                      1329.114
                                     73.70238
                                                                        1387.928
## 7
           11
                      1340.668
                                     75.07426
                                                                        1399.481
## 8
            4
                      1406.408
                                                                        1465.222
                                     76.83336
## 9
            3
                      1408.543
                                     71.85868
                                                                        1467.356
## 10
            7
                      1414.471
                                     72.23082
                                                                        1473.284
## 11
           12
                      1423.303
                                     71.18629
                                                                        1482.117
## 12
            8
                      1445.533
                                     75.37805
                                                                        1504.347
## 13
            5
                      1480.687
                                      70.31499
                                                                        1539.500
## 14
           15
                      1485.249
                                     74.28025
                                                                        1544.063
## 15
           17
                      1495.212
                                     71.09930
                                                                        1554.026
## 16
           21
                      1512.767
                                     72.53109
                                                                        1571.580
## 17
            6
                      1520.841
                                     72.50721
                                                                        1579.654
## 18
           24
                      1563.649
                                      65.33308
                                                                        1622.463
## 19
           18
                                                                        1627.700
                      1568.887
                                      71.06200
## 20
           25
                      1579.929
                                      70.52509
                                                                        1638.743
## 21
            2
                                     74.96623
                                                                        1644.211
                      1585.398
## 22
           22
                      1633.080
                                     71.38265
                                                                        1691.894
## 23
           13
                      1637.119
                                      66.24775
                                                                        1695.932
## 24
           19
                      1651.533
                                     74.93686
                                                                        1710.347
                      1657.612
## 25
           20
                                                                        1716.426
                                      68.65452
      lower.halfLeastSignificant.limit est.status
## 1
                               1137.400 Estimable
## 2
                               1207.628
                                          Estimable
## 3
                               1209.393
                                         Estimable
## 4
                                          Estimable
                               1214.980
## 5
                               1251.993
                                          Estimable
## 6
                               1270.300
                                          Estimable
## 7
                               1281.854 Estimable
## 8
                               1347.594 Estimable
## 9
                               1349.729
                                          Estimable
## 10
                                          Estimable
                               1355.657
## 11
                               1364.490 Estimable
## 12
                               1386.720 Estimable
## 13
                               1421.873 Estimable
```

```
## 14
                               1426.435 Estimable
## 15
                               1436.399
                                        Estimable
## 16
                               1453.953
                                        Estimable
## 17
                               1462.027
                                         Estimable
## 18
                               1504.836
                                         Estimable
                                        Estimable
## 19
                               1510.073
## 20
                                         Estimable
                               1521.115
## 21
                               1526.584
                                         Estimable
## 22
                               1574.266
                                         Estimable
## 23
                               1578.305
                                         Estimable
## 24
                               1592.719
                                         Estimable
  25
                               1598.798 Estimable
##
##
##
## LSD values
##
## minimum LSD = 109.6008
##
## mean LSD = 117.6273
##
## maximum LSD = 126.3422
##
## (sed range / mean sed = 0.142)
```

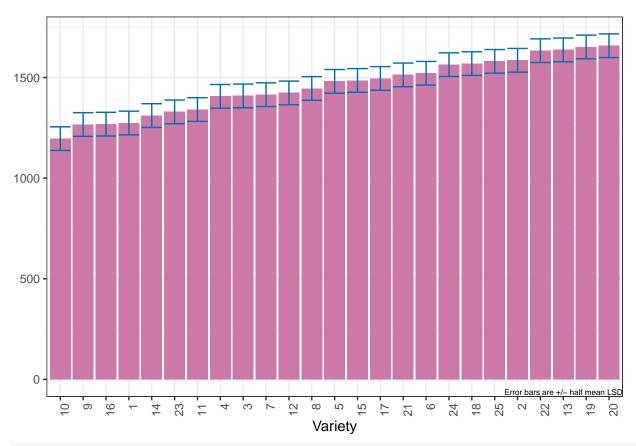
We have set error.intervals to halfLeast so that the limits for each prediction  $\pm$  (0.5 LSD) are calculated. When these are plotted overlapping error bars indicate predictions that are not significant, while those that do not overlap are significantly different (Snee, 1981).

Also set was sortFactor, so that the results would be ordered for the values of the predictions for Variety.

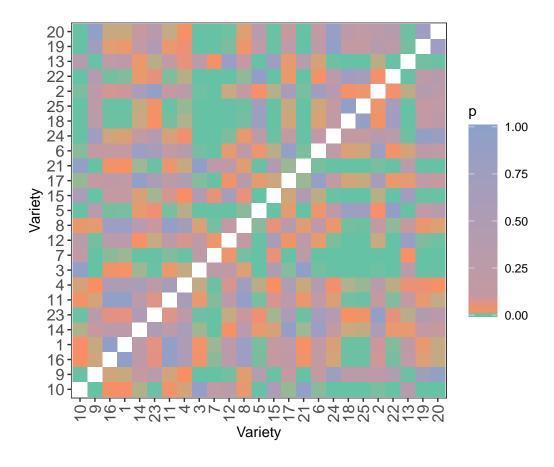
The function predictPlus returns an alldiffs object, a list consisting of the following components:

- predictions: the predictions, their standard errors and error intervals;
- vcov: the variance matrix of the predictions;
- differences: all pairwise differences between the predictions,
- p.differences: p-values for all pairwise differences between the predictions;
- sed: the standard errors of all pairwise differences between the predictions;
- LSD: the mean, minimum and maximum of the LSDs.

#### Plot the Variety predictions, with halfLSD intervals, and the p-values



plotPvalues(Var.diffs)



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