# Using asreml and asremlPlus for the Ladybird example from Welham et al. (2014)

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## Introduction

This vignette shows how to use asremlPlus (Brien, 2025a), and dae (Brien, 2024b), for exploring and presenting predictions (estimated marginal means: EMMs) from a linear mixed model analysis, the predictions having been produced using asreml (Butler et al., 2023). Here, asremlPlus, dae and asreml are packages for the R Statistical Computing environment (R Core Team, 2025).

The context is a three-factor factorial experiment on ladybirds (Welham et al., 2014, Example 8.2) that aims to answer the question "Will ladybirds transfer fungus to aphids on plants?" The experiment consists of 2 runs of 36 containers, each with a plant and aphids. There are three factors that results in 12 treatments: Host plant (beans, trefoil), infected Cadavers (5, 10, 20), Ladybird (-, +). These are randomized to the containers within a run so that each is replicated 3 times within a run. The response to be analysed is the logit of the proportion of live aphids that were infected.

## Initialize

```
library(knitr)
opts_chunk$set("tidy" = FALSE, comment = NA)
suppressMessages(library(asreml))

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packageVersion("asreml")

## [1] '4.2.0.370'
suppressMessages(library(asremlPlus))
packageVersion("asremlPlus")

## [1] '4.4.50'
suppressMessages(library("dae"))
packageVersion("dae")

## [1] '3.2.30'
```

```
options(width = 95, show.signif.stars = FALSE)
```

## Get data available in asremlPlus

```
data("Ladybird.dat")
```

## Do an ANOVA of logits

```
Error: Run
            Sum Sq Mean Sq F value Pr(>F)
        1 0.06766 0.06766
Residuals
Error: Run:Plant
                     Df Sum Sq Mean Sq F value
                                               Pr(>F)
Host
                      1 13.599 13.599 59.172 1.82e-10
                               8.514 37.044 3.78e-11
Cadavers
                      2 17.027
Ladybird
                      1 11.091 11.091 48.257 3.33e-09
                      2 0.308 0.154 0.670 0.5158
Host:Cadavers
                      1 0.228 0.228
                                       0.992
                                               0.3234
Host:Ladybird
Cadavers:Ladybird
                      2 1.735
                                0.867
                                        3.774
                                               0.0287
Host:Cadavers:Ladybird 2 0.200
                              0.100
                                       0.435
                                               0.6493
Residuals
                     59 13.560
                                0.230
```

The anova table gives the F-tests for the three-factor effects and interactions. Note the Residuals Mean Sq value for Run:Plant of 0.230. Also, it is clear that the Run component is negative, given that the Residuals Mean Sq value for Run is less than that for Run:Plant; it is (0.06766-0.230)/36). From the table it is seen that the only significant interaction is Cadavers:Ladybird and that the Host main effect is significant.

## Use asreml to analyse the logits

## Mixed model analysis of logits

```
ASReml Version 4.2 17/07/2025 23:38:34

LogLik Sigma2 DF wall
1 3.071301 0.2262391 60 23:38:34 ( 1 restrained)
```

```
2
       3.642605
                     0.2269125
                                   60
                                        23:38:34
                                                   ( 1 restrained)
3
                     0.2271056
                                        23:38:34
                                                   (
                                                      1 restrained)
       3.712498
                                   60
                                                      1 restrained)
4
       3.717213
                     0.2271206
                                   60
                                        23:38:34
5
                                                      1 restrained)
       3.717512
                     0.2271216
                                   60
                                        23:38:34
```

#### summary(m)\$varcomp

```
component std.error z.ratio bound %ch Run 2.298309e-08 NA NA B NA Run:Plant!R 2.271216e-01 0.04156985 5.463612 P 0
```

As expected the Run component is bound (B) at approximately zero. This results in a change in the estimate of the residual variance to 0.227. To allow for a negative estimate we will unconstrain the Run component. As Littell et al. (2006, p.150) say

if you do not set the negative variance component estimate to zero, but allow it to remain negative, you get better control over Type I error and, for cases of negative wholeplot error variance estimates, greater power. Therefore, this is the recommended procedure.

#### Unconstrain Reps to make the analysis equivalent to ANOVA

```
m <- setvarianceterms(m$call, terms = "Run", bounds = "U")
ASReml Version 4.2 17/07/2025 23:38:34</pre>
```

```
LogLik
                                   DF
                        Sigma2
                                           wall
1
       3.071301
                     0.2262391
                                   60
                                         23:38:34
                                                   ( 1 restrained)
2
       3.642605
                     0.2269125
                                   60
                                         23:38:34
                                                   (
                                                      1 restrained)
3
       3.802834
                     0.2274541
                                   60
                                        23:38:34
                                                   ( 1 restrained)
4
       3.839487
                     0.2334176
                                   60
                                        23:38:34
5
       3.955683
                     0.2309710
                                   60
                                        23:38:34
6
       3.973334
                     0.2300353
                                   60
                                         23:38:34
7
       3.974051
                     0.2298346
                                   60
                                        23:38:34
```

```
summary(m)$varcomp
```

```
        component
        std.error
        z.ratio
        bound
        %ch

        Run
        -0.004504789
        0.002896281
        -1.555370
        U 0.1

        Run:Plant!R
        0.229834648
        0.042316936
        5.431269
        P 0.0
```

Now the Run component is negative and the Run:Plant variance estimate is now equal to that for the Residuals Mean Sq for Run:Plant from the anova table.

## Set up an asrtests object

```
current.asrt <- as.asrtests(m)
print(current.asrt, which = "pseudoanova")</pre>
```

#### #### Pseudo-anova table for fixed terms

Wald tests for fixed effects.

Response: logitP

	Df	${\tt denDF}$	F.inc	Pr
(Intercept)	1	1	1550.00	0.0162
Host	1	59	59.17	0.0000
Cadavers	2	59	37.04	0.0000
Ladybird	1	59	48.26	0.0000
Host:Cadavers	2	59	0.67	0.5158
Host:Ladybird	1	59	0.99	0.3234
Cadavers:Ladybird	2	59	3.77	0.0287
Host:Cadavers:Ladybird	2	59	0.44	0.6493

The asrtests object contains a wald.tab component which can be printed by specifying that the pseudoanova is printed. The F-values for the fixed terms in this table are the same as those in the anova table.

## Obtain the marginality matrix for the fixed terms

The pstructure function from the dae package (Brien, 2024b) produce the marginality matrix for a formula as a side effect and we take advantage of that to obtain the matrix required here.

	Host	Cadavers	Host:Cadavers	Ladybird	Host:Ladybird	Cadavers:Ladybird
Host	1	0	1	0	1	0
Cadavers	0	1	1	0	0	1
Host:Cadavers	0	0	1	0	0	0
Ladybird	0	0	0	1	1	1
Host:Ladybird	0	0	0	0	1	0
Cadavers:Ladybird	0	0	0	0	0	1
Host:Cadavers:Ladybird	. 0	0	0	0	0	0

	Host:Cadavers:Ladybird
Host	1
Cadavers	1
Host:Cadavers	1
Ladybird	1
Host:Ladybird	1
Cadavers:Ladybird	1
Host:Cadavers:Ladybird	1

This marginality matrix is interpreted by taking a row term and noting that it is marginal to any column term with a one in this row.

#### Choose marginality-compliant model

```
chosen <- chooseModel(current.asrt, terms.marginality = HCL.marg)
current.asrt <- chosen$asrtests.obj
print(current.asrt, which = "test", omit.columns = c("AIC", "BIC"))</pre>
```

#### Sequence of model investigations for logitP

```
terms DF denDF
                                                 action
1 Host:Cadavers:Ladybird 2
                               59 0.6493 Nonsignificant
2
       Cadavers:Ladybird 2
                               59 0.0287
                                            Significant
3
          Host:Ladybird 1
                               59 0.3234 Nonsignificant
          Host:Cadavers 2
4
                               59 0.5158 Nonsignificant
5
                               59 0.0000
                                            Significant
                    Host 1
```

```
(chosen$sig.terms)
```

```
[[1]]
[1] "Cadavers:Ladybird"

[[2]]
[1] "Host"
```

The chooseModel function produces a list with components sig.terms, a list with the terms in the marginality-compliant model, and asrtests.obj, the asrtests object resulting from the model selection. In particular, the asrtests object contains a test.summary that details the tests performed in choosing the model; the AIC and BIC columns are omitted from test.summary because their inclusion has not been requested. Note that chooseModel does not test the main effects for Cadavers or Ladybird, because these are marginal to the significant two-factor interaction Cadavers:Ladybird.

#### Form formula for selected model

```
chosen.mod <- paste(unlist(chosen$sig.terms), collapse = " + ")
(chosen.mod <- as.formula(paste("~", chosen.mod)))</pre>
```

~Cadavers:Ladybird + Host

## Obtain predictions under the chosen model and form an alldiffs object

```
Joining with 'by = join_by(fac.comb)'
Joining with 'by = join_by(Host)'
```

#### Predictions for logitP transform(s) from Host:Ladybird:Cadavers

#### Notes:

The original predictions, obtained as described below, have been linearly transformed to form estimated marginal means.

- The predictions are obtained by averaging across the hypertable calculated from model terms constructed solely from factors in the averaging and classify sets.
- Use 'average' to move ignored factors into the averaging set.
- The ignored set: Run

	Host	Ladybird	${\tt Cadavers}$	<pre>predicted.value</pre>	${\tt standard.error}$	<pre>upper.halfLeastSignificant.limit</pre>		
1	bean	_	5	-1.6038338	0.1417454	-1.4080222		
2	bean	-	10	-1.1454308	0.1417454	-0.9496192		
3	bean	-	20	-0.7448097	0.1417454	-0.5489981		
4	bean	+	5	-1.0195475	0.1417454	-0.8237359		
5	bean	+	10	-0.5983440	0.1417454	-0.4025323		
6	bean	+	20	0.4786704	0.1417454	0.6744820		
7	trefoil	-	5	-2.4730339	0.1417454	-2.2772223		
8	trefoil	_	10	-2.0146309	0.1417454	-1.8188193		
9	trefoil	-	20	-1.6140098	0.1417454	-1.4181982		
10	trefoil	+	5	-1.8887476	0.1417454	-1.6929360		
11	trefoil	+	10	-1.4675441	0.1417454	-1.2717325		
12	trefoil	+	20	-0.3905297	0.1417454	-0.1947181		
	lower halfleagtSignificant limit est status							

lower.halfLeastSignificant.limit est.status

1	-1.7996454	Estimable
2	-1.3412425	Estimable
3	-0.9406214	Estimable
4	-1.2153592	Estimable
5	-0.7941556	Estimable
6	0.2828588	Estimable
7	-2.6688455	Estimable
8	-2.2104426	Estimable
9	-1.8098215	Estimable
10	-2.0845593	Estimable
11	-1.6633557	Estimable
12	-0.5863414	Estimable

## LSD values

```
minimum LSD = 0.3916233 \ 0.3916233
mean LSD = 0.3916233 \ 0.3916233
```

maximum LSD = 0.3916233 0.3916233

(sed range / mean sed = 1.28e-15 1.13e-15 )

Setting the terms argument to Host:Ladybird:Cadavers requests predictions for all combinations of the three factors and the linear.transformation argument is used to obtain estimated marginal means (EMMs) that conform to the chosen model. The wald.tab is supplied so that it can be used to get the degrees of freedom for the t-value to be used in calculating the LSD; the degrees of freedom to the source for the terms argument will be used. The error.intervals argument has been set to "halfLeast", the LSDtype argument to "factor.combination" and the LSDby argument to "Host" so that the average LSD will be calculated for each Host. This necessary because, under the chosen model, the LSDs differ between Hosts. It results in lower.halfLeastSignificant.limit and upper.halfLeastSignificant.limit being added to the predictions component of the alldiffs object.

Or, caclulate predictions to check first and then transform to conform to chosen model

```
Joining with 'by = join_by(fac.comb)'
Joining with 'by = join_by(Host)'
```

#### Predictions for logitP transform(s) from Host:Ladybird:Cadavers

#### Notes:

The original predictions, obtained as described below, have been linearly transformed to form estimated marginal means.

- The predictions are obtained by averaging across the hypertable calculated from model terms constructed solely from factors in the averaging and classify sets.
- Use 'average' to move ignored factors into the averaging set.
- The ignored set: Run

	Host	Ladybird	Cadavers	predicted.value	standard.error	upper.halfLeastSignificant.limit
1	bean	_	5	-1.6038338	0.1417454	-1.4080222
2	bean	-	10	-1.1454308	0.1417454	-0.9496192
3	bean	-	20	-0.7448097	0.1417454	-0.5489981
4	bean	+	5	-1.0195475	0.1417454	-0.8237359
5	bean	+	10	-0.5983440	0.1417454	-0.4025323
6	bean	+	20	0.4786704	0.1417454	0.6744820
7	trefoil	_	5	-2.4730339	0.1417454	-2.2772223
8	trefoil	-	10	-2.0146309	0.1417454	-1.8188193
9	trefoil	-	20	-1.6140098	0.1417454	-1.4181982
10	trefoil	+	5	-1.8887476	0.1417454	-1.6929360
11	trefoil	+	10	-1.4675441	0.1417454	-1.2717325

```
12 trefoil
                          20
                                  -0.3905297
                                                  0.1417454
                                                                                   -0.1947181
   lower.halfLeastSignificant.limit est.status
                         -1.7996454 Estimable
1
2
                         -1.3412425
                                    Estimable
3
                         -0.9406214
                                     Estimable
4
                         -1.2153592 Estimable
5
                         -0.7941556 Estimable
                          0.2828588 Estimable
6
7
                         -2.6688455 Estimable
8
                         -2.2104426 Estimable
9
                         -1.8098215 Estimable
10
                         -2.0845593 Estimable
                         -1.6633557 Estimable
11
12
                         -0.5863414 Estimable
LSD values
minimum LSD = 0.3916233 0.3916233
mean LSD = 0.3916233 0.3916233
maximum LSD = 0.3916233 0.3916233
(sed range / mean sed = 1.28e-15 1.13e-15)
```

The above LSD values can only be used to compare pairs of EMMs for the same Host.

#### Explore the LSDs

To investigate the errors that would result from using the overall LSDs as opposed to the LSDs computed for each Host, the exploreLSDs, pickLSDstatistics and plotLSDerrors functions are used, firstly with the default value of "overall" for LSDtype and finally with the LSDtype set to "factor.combination" and LSDby to "Host".

The exploreLSDs function produces tables of statistics for the LSDs computed for the settings of the LSDtype and LSDby; the settings of these arguments does not have to match those used in producing the alldiffs object. For LSDtype set to "overall', a single LSD statistic is computed that is the based on the standard errors of all pairwise differences. To ascertain the errors that arise from using this LSD value for determining, for all pairwise comparisons, whether a comparison is significant, exploreLSDs compares the results using the LSD value with the p-values in the p.differences component of the alldiffs object. For LSDtype set to "factor.combination" and LSDby to "Host", the LSD statistics are calculated from standard errors of the pairwise differences for each Host. Examination of the sed component of diffs reveals that there are only three different values for the standard errors of pairwise differences and, hence, only three unique values for the LSD. Of the statistics shown, there is no single value that will not result in errors.

Here are the tables of the numbers of false positive and negative error in using the values of the various LSD statistics for determining the significance of the 66 pairwise comparisons of the 12 predictions.

```
exploreLSDs(diffs, LSDtype = "overall")
```

#### Statistics calculated from LSD values

```
c min quant10 quant25 mean median quant75 quant90 max 1 66 0.2261038 0.3916233 0.3916233 0.4090372 0.3916233 0.4522076 0.4522076 0.4522076
```

#### False positives resulting from the use of various LSD statistics

```
c min quant10 quant25 mean median quant75 quant90 max false.pos 66 7 2 2 2 2 0 0 0 0 ^{\circ}
```

#### False negatives resulting from the use of various LSD statistics

```
c min quant10 quant25 mean median quant75 quant90 max false.neg 66 0 0 0 2 0 4 4 4
```

The function findLSDminerrors can be used to find a value of the LSD that minimizes the number of false positive (negative) errors i.e. declaring a pairwise difference to be significant (not significant) when it is not significant (significant). The function has an argument false.pos.wt that specifies how many false negatives are equivalent to one false positive; the default for false.pos.wt is 10, which is a conservative approach because it greatly favours false negatives over false positives.

#### (findLSDminerrors(diffs))

#### \$overall

#### \$overall\$lsd

- [1] 0.3916233 0.3916230 0.3916230 0.3916230 0.3916230 0.3916230 0.3916230 0.3916230 0.3916230 0.3916230 0.3916200 0.3916200 0.3916200 0.3916200 0.3916200 0.391600 0.3916000 0.3916000 0.3916000 0.3916000 0.3
- [10] 0.3916233 0.3916233 0.3916233 0.3916233 0.3916233 0.3916233 0.2261038 0.4522076 0.4522076 [19] 0.4522076 0.4522076 0.4522076 0.4522076 0.4522076 0.4522076 0.4522076 0.4522076
- [28] 0.3916233 0.4522076 0.4522076 0.2261038 0.4522076 0.4522076 0.3916233 0.3916233
- [37] 0.4522076 0.4522076 0.4522076 0.2261038 0.4522076 0.4522076 0.3916233 0.3916233
- $[46] \quad 0.4522076 \quad 0.4522076 \quad 0.4522076 \quad 0.4522076 \quad 0.2261038 \quad 0.4522076 \quad 0.3916233 \quad 0.3916233 \quad 0.3916233$
- $[55] \ \ 0.3916233 \ \ 0.4522076 \ \ 0.4522076 \ \ 0.4522076 \ \ 0.4522076 \ \ 0.2261038 \ \ 0.3916233 \ \ 0.3916233$
- [64] 0.3916233 0.3916233 0.3916233

#### \$overall\$dif

- [1] -0.45840297 -0.85902408 -0.40062111 -0.58428627 -0.12588330 0.27473781 -1.00548982
- [8] -0.54708685 -0.14646574 -0.42120355 -2.08250420 -1.62410123 -1.22348012 -1.49821793
- $\begin{bmatrix} 22 \end{bmatrix} \quad 0.41079715 \quad 0.86920012 \quad 1.26982123 \quad 0.99508342 \quad 1.41628697 \quad 2.49330135 \quad -0.45840297 \quad 1.41628697 \quad 1.$
- $[29] \quad 0.01017604 \quad 0.46857901 \quad 0.86920012 \quad 0.59446231 \quad 1.01566586 \quad 2.09268024 \quad -0.85902408$
- [43] -0.58428627 -0.12588330 0.27473781 -0.13628970 0.32211327 0.72273438 0.44799657
- [50] 0.86920012 1.94621450 -1.00548982 -0.54708685 -0.14646574 -0.42120355 -1.21330408
- [64] -1.22348012 -1.49821793 -1.07701438

## \$overall\$sig.actual

[46] FALSE FALSE

- [1] TRUE TRUE TRUE TRUE FALSE FALSE TRUE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE
- [16] TRUE TRUE TRUE TRUE TRUE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE TRUE FALSE TRUE
- [31] TRUE TRUE TRUE TRUE TRUE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE TRUE FALSE FALSE

TRUE TRUE FALSE TRUE TRUE TRUE FALSE TRUE FALSE

[61] TRUE TRUE TRUE TRUE TRUE TRUE

TRUE FALSE

TRUE

TRUE

```
LSD false.pos false.neg false.criterion
overall 0.4489466
                                                       0
                                                                             4
                                                                                                               4
(minLSDpos <- findLSDminerrors(diffs, false.pos.wt = 1))</pre>
$overall
$overall$1sd
  [1] 0.3916233 0.3916233 0.3916233 0.3916233 0.3916233 0.3916233 0.3916233 0.3916233 0.3916233
 \begin{smallmatrix} [10] & 0.3916233 & 0.3916233 & 0.3916233 & 0.3916233 & 0.3916233 & 0.3916233 & 0.2261038 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4522076 & 0.4520
[19] 0.4522076 0.4522076 0.4522076 0.4522076 0.2261038 0.4522076 0.4522076 0.4522076 0.4522076
[28] 0.3916233 0.4522076 0.4522076 0.2261038 0.4522076 0.4522076 0.4522076 0.3916233 0.3916233
[37] 0.4522076 0.4522076 0.4522076 0.2261038 0.4522076 0.4522076 0.3916233 0.3916233 0.3916233
[46] 0.4522076 0.4522076 0.4522076 0.4522076 0.2261038 0.4522076 0.3916233 0.3916233 0.3916233
[55] 0.3916233 0.4522076 0.4522076 0.4522076 0.4522076 0.4522076 0.2261038 0.3916233 0.3916233
[64] 0.3916233 0.3916233 0.3916233
$overall$dif
   \begin{bmatrix} 1 \end{bmatrix} -0.45840297 -0.85902408 -0.40062111 -0.58428627 -0.12588330 \quad 0.27473781 -1.00548982 
  [8] -0.54708685 -0.14646574 -0.42120355 -2.08250420 -1.62410123 -1.22348012 -1.49821793
[15] -1.07701438
                                      0.86920012
                                                               1.32760308
                                                                                         1.72822420
                                                                                                                   1.45348638
                                                                                                                                            1.87468994
                                                                                                                                                                      2.95170432
[22]
            0.41079715
                                      0.86920012
                                                                1.26982123
                                                                                         0.99508342
                                                                                                                   1.41628697
                                                                                                                                            2.49330135 -0.45840297
[29]
            0.01017604
                                      0.46857901
                                                                0.86920012
                                                                                         0.59446231
                                                                                                                                            2.09268024 -0.85902408
                                                                                                                   1.01566586
[36] -0.40062111
                                      0.28491385
                                                                0.74331682
                                                                                         1.14393793
                                                                                                                   0.86920012
                                                                                                                                             1.29040367
                                                                                                                                                                      2.36741805
[43] -0.58428627 -0.12588330
                                                               0.27473781 -0.13628970
                                                                                                                   0.32211327
                                                                                                                                             0.72273438
                                                                                                                                                                    0.44799657
[50]
           0.86920012 1.94621450 -1.00548982 -0.54708685 -0.14646574 -0.42120355 -1.21330408
[57] -0.75490112 -0.35428000 -0.62901781 -0.20781426
                                                                                                                   0.86920012 -2.08250420 -1.62410123
[64] -1.22348012 -1.49821793 -1.07701438
$overall$sig.actual
            TRUE
                                                                                                                                             TRUE
  [1]
                         TRUE
                                      TRUE
                                                   TRUE FALSE FALSE
                                                                                         TRUE
                                                                                                      TRUE FALSE
                                                                                                                                TRUE
                                                                                                                                                          TRUE
                                                                                                                                                                       TRUE
                                                                                                                                                                                   TRUE
[16]
            TRUE
                         TRUE
                                      TRUE
                                                   TRUE
                                                                TRUE
                                                                            TRUE FALSE
                                                                                                      TRUE
                                                                                                                   TRUE
                                                                                                                                TRUE
                                                                                                                                             TRUE
                                                                                                                                                          TRUE
                                                                                                                                                                       TRUE FALSE
```

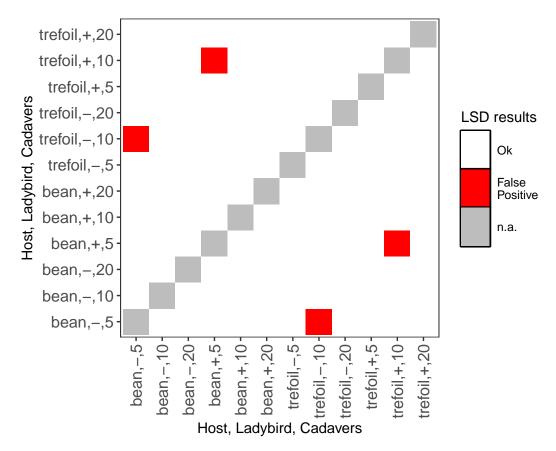
TRUE TRUE [31] TRUE TRUE TRUE TRUE TRUE FALSE TRUE TRUE TRUE TRUE TRUE TRUE FALSE FALSE TRUE TRUE FALSE TRUE TRUE [46] FALSE FALSE TRUE FALSE TRUE TRUE TRUE TRUE FALSE TRUE TRUE [61] TRUE TRUE TRUE TRUE

```
LSD false.pos false.neg false.criterion overall 0.354983 2 0 2
```

The smallest value of the LSD that results in the minimum weighted sum of the false positives and negatives is 0.4489466 when the weight is 10 and is 0.354983 when the weight is one. These values result in 4 false negatives and 2 false positives respectively.

To see which of the two pairwise comparisons will be falsely identified as being significant when the LSD value is set to minimum LSD, the LSDs stored in the alldiffs object need to be recalculated to be based on this LSD value. Then plot the errors or save the return values obtained using the function plotLSDerrors. The plot below shows that the two pairs whose differences are incorrectly identified as significant have the same level of the Ladybird factor, but differ in both of the levels for the Host and Cadaver factors.

```
diffs.overall <- recalcLSD(diffs, LSDtype = "supplied", LSDsupplied = minLSDpos["LSD"])
plotLSDerrors(diffs.overall)</pre>
```



This raises the question of whether the minimum LSD should be used. There are at least four alternatives: (i) use it without restriction, on the basis that it can be concluded that using it is unlikely to result in seriously flawed conclusions; (ii) use it with the restriction that it only be applied to assess pairwise comparisons that have the same Host or the same Cadaver treatment; (i11) investigate the use of the minimum LSD with only false negative errors; and (iv) rather than use an overall LSD value, use LSD values computed from the LSDs within each Host level.

Because LSDtype was set to "factor.combination" and LSDby to "Host" in forming the object diffs, the LSDs for alternative (iv) are stored in the LSD component of the object diffs. Printing out the LSD component will summarize how those LSD values perform. Otherwise, the following call to exploreLSDs will display the properties of the LSDs for various LSD statistics:

```
exploreLSDs(diffs, LSDtype = "factor.combination", LSDby = "Host")
```

The following shows the contents of the LSD component of diffs:

trefoil 15 0.3916233 0.3916233 0.3916233

```
(diffs$LSD)

c minLSD meanLSD maxLSD assignedLSD accuracyLSD falsePos falseNeg
bean 15 0.3916233 0.3916233 0.3916233 0.3916233 8.504778e-16 0 0
```

0.3916233 7.087315e-16

0

0

Because the minimum and maximum LSD values are equal, it follows that there is only one value of the LSD for all pairwise comparisons within each Host level and it happens that the values for the two Hosts are also equal. The table shows that zero false positive and negative errors will result from the use of the value of 0.39 for the 30 within-Host comparisons. Thus, using findLSDminerrors(diffs, LSDtype = "factor.combinations", LSDby = "Host") to select the minimum LSDs would only confirm what is already obvious.

#### Plot the predictions

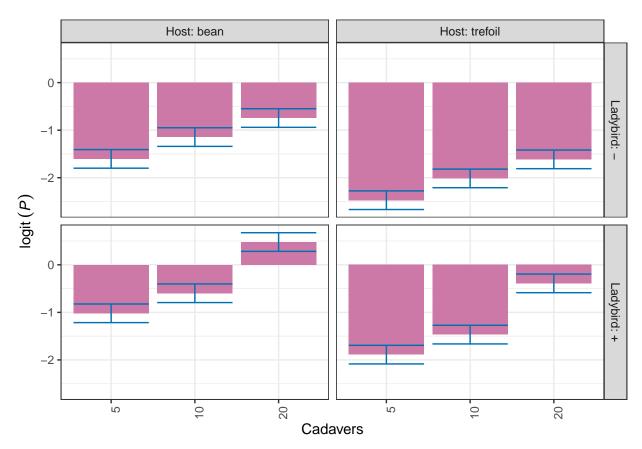


Figure 1. Estimated marginal means (EMMs) for logit(P), where P is the proportion of live aphids that were infected, for two Hosts, two Ladybird levels and three Cadaver levels. Error bars are an EMM  $\pm$  half-LSD (5%). The two EMMs for the same Host are significantly different ( $p \le 0.05$ ) if their error bars do not overlap.

The function plotPredictions uses ggplot to produce the plot and the ggplotFuncs argument allows the addition of ggplot functions to modify the plot. In this case, the facet.grid function is respecified to include prepender functions that modify the labels of the facets to include the factor names. Note the statement in the legend of Figure 1 that restricts the use of the error bars to determining the significance of differences for the pairwise comparisons of EMMs for the same Host.

#### Get and plot the predictions with a single function call

The predictPresent function combines the functionality of predictPlus and plotPredictions, as demonstrated now. Also, the use of plotPvalues to plot the pairwise p-values is displayed. The predictPresent function has the capability of producing alldiffs objects for multiple terms and these are stored in a list each of which is named for the term whose alldiffs object it stores. Thus, the term has to be specified in referencing components of diffs.

```
Joining with 'by = join_by(fac.comb)'
Joining with 'by = join_by(Host)'
```

```
plotPvalues(diffs$Host.Ladybird.Cadavers, factors.per.grid = 1, show.sig = TRUE)
```

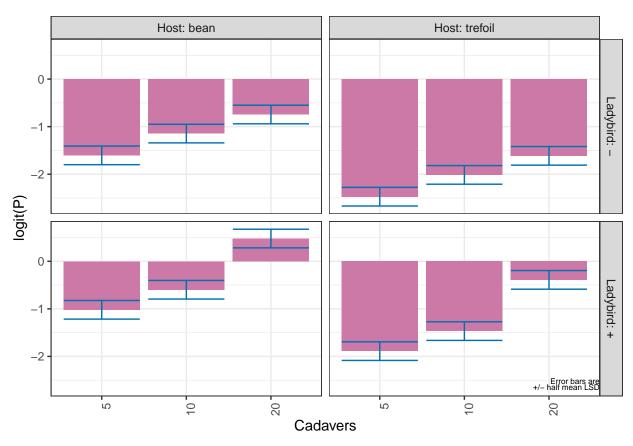


Figure 2. Estimated marginal means (EMMs) for logit(P), where P is the proportion of live aphids that were infected, for two Hosts, two Ladybird levels and three Cadaver levels. Error bars are an EMM  $\pm$  half-LSD (5%). The two EMMs for the same Host are significantly different ( $p \le 0.05$ ) if their error bars do not overlap.

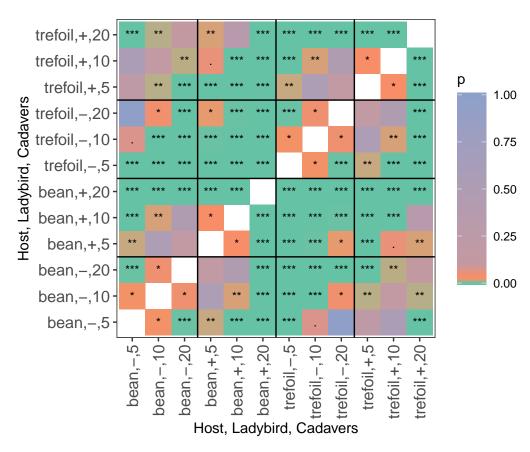


Figure 3. The p-values for each of the pairwise comparisons of the estimated marginal means for logit(P), where P is the proportion of live aphids that were infected, for two Hosts, two Ladybird levels and three Cadaver levels

#### options(width = 90)

diffs\$Host.Ladybird.Cadavers\$differences

```
bean, -, 5 bean, -, 10 bean, -, 20
                                                 bean,+,5 bean,+,10 bean,+,20
bean, -, 5
              0.00000000 - 0.4584030 - 0.8590241 - 0.5842863 - 1.0054898 - 2.0825042
              0.45840297 0.0000000 -0.4006211 -0.1258833 -0.5470869 -1.6241012
bean, -, 10
                         0.4006211 0.0000000 0.2747378 -0.1464657 -1.2234801
bean,-,20
              0.85902408
bean,+,5
              0.58428627 0.1258833 -0.2747378 0.0000000 -0.4212036 -1.4982179
bean,+,10
              1.00548982 0.5470869 0.1464657 0.4212036 0.0000000 -1.0770144
bean,+,20
              2.08250420 1.6241012 1.2234801 1.4982179 1.0770144 0.0000000
trefoil,-,5 -0.86920012 -1.3276031 -1.7282242 -1.4534864 -1.8746899 -2.9517043
trefoil,-,10 -0.41079715 -0.8692001 -1.2698212 -0.9950834 -1.4162870 -2.4933014
trefoil,-,20 -0.01017604 -0.4685790 -0.8692001 -0.5944623 -1.0156659 -2.0926802
trefoil,+,5 -0.28491385 -0.7433168 -1.1439379 -0.8692001 -1.2904037 -2.3674180
trefoil,+,10 0.13628970 -0.3221133 -0.7227344 -0.4479966 -0.8692001 -1.9462145
trefoil,+,20 1.21330408 0.7549011 0.3542800 0.6290178 0.2078143 -0.8692001
             trefoil,-,5 trefoil,-,10 trefoil,-,20 trefoil,+,5 trefoil,+,10 trefoil,+,20
bean, -,5
               0.8692001
                            0.4107972
                                        0.01017604
                                                     0.2849139
                                                                 -0.1362897
                                                                              -1.2133041
bean,-,10
               1.3276031
                            0.8692001
                                        0.46857901
                                                     0.7433168
                                                                  0.3221133
                                                                              -0.7549011
bean,-,20
               1.7282242
                            1.2698212
                                        0.86920012
                                                     1.1439379
                                                                  0.7227344
                                                                              -0.3542800
                            0.9950834
                                        0.59446231
                                                                  0.4479966
                                                                              -0.6290178
bean,+,5
               1.4534864
                                                     0.8692001
               1.8746899
                                        1.01566586
                                                     1.2904037
                                                                  0.8692001
                                                                              -0.2078143
bean,+,10
                            1.4162870
bean,+,20
               2.9517043
                            2.4933014
                                        2.09268024
                                                     2.3674180
                                                                  1.9462145
                                                                               0.8692001
trefoil,-,5
               0.0000000
                           -0.4584030
                                       -0.85902408
                                                    -0.5842863
                                                                 -1.0054898
                                                                              -2.0825042
trefoil,-,10
               0.4584030
                            0.0000000
                                       -0.40062111
                                                    -0.1258833
                                                                 -0.5470869
                                                                              -1.6241012
                                                                              -1.2234801
trefoil,-,20
               0.8590241
                            0.4006211
                                        0.00000000
                                                     0.2747378
                                                                 -0.1464657
trefoil,+,5
              0.5842863
                            0.1258833
                                       -0.27473781
                                                     0.0000000
                                                                 -0.4212036
                                                                              -1.4982179
trefoil,+,10
               1.0054898
                            0.5470869
                                        0.14646574
                                                     0.4212036
                                                                  0.0000000
                                                                              -1.0770144
trefoil,+,20
               2.0825042
                            1.6241012
                                        1.22348012
                                                     1.4982179
                                                                  1.0770144
                                                                               0.0000000
```

```
bean,-,5 bean,-,10 bean,-,20 bean,+,5 bean,+,10 bean,+,20 trefoil,-,5
bean, -, 5
                    NA 0.1957142 0.1957142 0.1957142 0.1957142 0.1957142
                                                                           0.1129957
                              NA 0.1957142 0.1957142 0.1957142 0.1957142
             0.1957142
                                                                           0.2259913
bean, -, 10
             0.1957142 0.1957142
                                        NA 0.1957142 0.1957142 0.1957142
                                                                           0.2259913
bean,-,20
bean,+,5
             0.1957142 0.1957142 0.1957142
                                                  NA 0.1957142 0.1957142
                                                                           0.2259913
             0.1957142 0.1957142 0.1957142 0.1957142
bean,+,10
                                                            NA 0.1957142
                                                                           0.2259913
             0.1957142 0.1957142 0.1957142 0.1957142 0.1957142
                                                                           0.2259913
bean,+,20
                                                                      NA
trefoil,-,5 0.1129957 0.2259913 0.2259913 0.2259913 0.2259913 0.2259913
                                                                                  NA
trefoil,-,10 0.2259913 0.1129957 0.2259913 0.2259913 0.2259913 0.2259913
                                                                           0.1957142
trefoil,-,20 0.2259913 0.2259913 0.1129957 0.2259913 0.2259913 0.2259913
                                                                           0.1957142
trefoil,+,5 0.2259913 0.2259913 0.2259913 0.1129957 0.2259913 0.2259913
                                                                           0.1957142
trefoil,+,10 0.2259913 0.2259913 0.2259913 0.2259913 0.1129957 0.2259913
                                                                           0.1957142
trefoil,+,20 0.2259913 0.2259913 0.2259913 0.2259913 0.2259913 0.1129957
                                                                           0.1957142
             trefoil,-,10 trefoil,-,20 trefoil,+,5 trefoil,+,10 trefoil,+,20
bean, -,5
                0.2259913
                             0.2259913
                                         0.2259913
                                                      0.2259913
                                                                   0.2259913
bean,-,10
                0.1129957
                             0.2259913
                                         0.2259913
                                                      0.2259913
                                                                   0.2259913
bean,-,20
                0.2259913
                             0.1129957
                                         0.2259913
                                                      0.2259913
                                                                   0.2259913
                                                                   0.2259913
                             0.2259913
                                                      0.2259913
bean,+,5
                0.2259913
                                         0.1129957
bean,+,10
                0.2259913
                             0.2259913
                                         0.2259913
                                                      0.1129957
                                                                   0.2259913
bean,+,20
                0.2259913
                             0.2259913
                                         0.2259913
                                                      0.2259913
                                                                   0.1129957
trefoil,-,5
                0.1957142
                             0.1957142
                                         0.1957142
                                                      0.1957142
                                                                   0.1957142
trefoil,-,10
                             0.1957142
                                         0.1957142
                                                      0.1957142
                                                                   0.1957142
                       NA
trefoil,-,20
                                         0.1957142
                                                      0.1957142
                0.1957142
                                    NA
                                                                   0.1957142
                0.1957142
                                                      0.1957142
                                                                   0.1957142
trefoil,+,5
                             0.1957142
                                                NA
trefoil,+,10
                0.1957142
                             0.1957142
                                                                   0.1957142
                                         0.1957142
                                                             NA
trefoil,+,20
                0.1957142
                             0.1957142
                                         0.1957142
                                                      0.1957142
                                                                          NA
```

## Perform the analysis with just selected model fitted

The model with nonsignificant fixed terms dropped is obtained in order to compare it with the fit when they are retained and the estimated marginal means for the chosen model are obtained.

```
ns.terms <- current.asrt$test.summary$terms[current.asrt$test.summary$action == "Nonsignificant"]
red.asrt <- changeTerms(current.asrt, dropFixed = paste(ns.terms, collapse = "+"))</pre>
WARN [2025-07-17 23:38:43] Some components changed by more than 1% on the last iteration
Warning in asreml(fixed = logitP ~ Host + Cadavers + Ladybird + Cadavers:Ladybird, : Some
components changed by more than 1% on the last iteration
WARN [2025-07-17 23:38:43] Some components changed by more than 1% on the last iteration
Warning in asreml(fixed = logitP ~ Host + Cadavers + Ladybird + Cadavers:Ladybird, : Some
components changed by more than 1% on the last iteration
summary(red.asrt$asreml.obj)$varcomp
                                     z.ratio bound %ch
              component
                          std.error
Run
           -0.004328175 0.002777746 -1.558161
                                                  U 1.1
Run:Plant!R 0.223456033 0.039510023 5.655680
                                                  P 0.0
print(red.asrt, which = "pseudoanova")
#### Pseudo-anova table for fixed terms
Wald tests for fixed effects.
Response: logitP
                 Df denDF F.inc
(Intercept)
                       1 1551.00 0.0162
                  1
Host
                  1
                       64 60.88 0.0000
Cadavers
                  2 64 38.12 0.0000
Ladybird
                  1 64 49.65 0.0000
Cadavers:Ladybird 2
                       64 3.88 0.0256
diffs.red <- predictPlus(red.asrt$asreml.obj,</pre>
                        classify = "Host:Ladybird:Cadavers",
                        wald.tab = current.asrt$wald.tab,
                        error.intervals = "halfLeast", interval.annotate = FALSE,
                        LSDtype = "factor.combination", LSDby = "Host",
                        tables = "predictions")
Joining with 'by = join_by(fac.comb)'
Joining with 'by = join by(Host)'
```

#### Predictions for logitP from Host:Ladybird:Cadavers

#### Notes:

- The predictions are obtained by averaging across the hypertable calculated from model terms constructed solely from factors in the averaging and classify sets.
- Use 'average' to move ignored factors into the averaging set.
- The ignored set: Run

```
Host Ladybird Cadavers predicted.value standard.error
                                 -1.6038338
1
     bean
                         5
                                                0.1398332
2
     bean
                         10
                                 -1.1454308
                                                0.1398332
3
     bean
                         20
                                 -0.7448097
                                                0.1398332
4
                        5
     bean
                                 -1.0195475
                                                0.1398332
5
     bean
                        10
                                -0.5983440
                                                0.1398332
6
     bean
                         20
                                 0.4786704
                                                0.1398332
7 trefoil
                        5
                                -2.4730339
                                                0.1398332
8 trefoil
                       10
                                -2.0146309
                                                0.1398332
9 trefoil
                        20
                                -1.6140098
                                                0.1398332
10 trefoil
                                -1.8887476
                 +
                        5
                                                0.1398332
11 trefoil
                         10
                                 -1.4675441
                                                0.1398332
12 trefoil
                 +
                         20
                                 -0.3905297
                                                0.1398332
  upper.halfLeastSignificant.limit lower.halfLeastSignificant.limit est.status
1
                        -1.4107942
                                                        -1.7968734 Estimable
2
                        -0.9523913
                                                        -1.3384704 Estimable
3
                        -0.5517702
                                                        -0.9378493 Estimable
4
                        -0.8265080
                                                        -1.2125871 Estimable
5
                        -0.4053044
                                                        -0.7913835 Estimable
6
                         0.6717100
                                                         0.2856308 Estimable
7
                        -2.2799944
                                                        -2.6660735 Estimable
8
                        -1.8215914
                                                        -2.2076705 Estimable
9
                        -1.4209703
                                                        -1.8070494 Estimable
10
                        -1.6957081
                                                        -2.0817872 Estimable
11
                        -1.2745045
                                                        -1.6605837 Estimable
```

## LSD values

12

```
minimum LSD = 0.3860791 0.3860791

mean LSD = 0.3860791 0.3860791

maximum LSD = 0.3860791 0.3860791

(sed range / mean sed = 1.29e-15 1.29e-15 )
```

-0.1974902

```
options(width = 90)
print(diffs.red$sed)
```

bean,-,5 bean,-,10 bean,-,20 bean,+,5 bean,+,10 bean,+,20 trefoil,-,5

-0.5835693 Estimable

```
bean, -,5
                    NA 0.1929435 0.1929435 0.1929435 0.1929435 0.1929435
                                                                              0.1113960
             0.1929435
bean, -, 10
                               NA 0.1929435 0.1929435 0.1929435 0.1929435
                                                                             0.2227920
                                                                              0.2227920
bean, -, 20
             0.1929435 0.1929435
                                         NA 0.1929435 0.1929435 0.1929435
bean,+,5
             0.1929435 0.1929435 0.1929435
                                                   NA 0.1929435 0.1929435
                                                                             0.2227920
bean, +, 10
             0.1929435 0.1929435 0.1929435 0.1929435
                                                              NA 0.1929435
                                                                              0.2227920
bean, +, 20
             0.1929435 0.1929435 0.1929435 0.1929435 0.1929435
                                                                              0.2227920
                                                                        NA
             0.1113960 0.2227920 0.2227920 0.2227920 0.2227920 0.2227920
trefoil,-,5
                                                                                     NA
trefoil,-,10 0.2227920 0.1113960 0.2227920 0.2227920 0.2227920 0.2227920
                                                                             0.1929435
trefoil,-,20 0.2227920 0.2227920 0.1113960 0.2227920 0.2227920 0.2227920
                                                                              0.1929435
trefoil,+,5 0.2227920 0.2227920 0.1113960 0.2227920 0.2227920
                                                                              0.1929435
trefoil,+,10 0.2227920 0.2227920 0.2227920 0.2227920 0.1113960 0.2227920
                                                                              0.1929435
trefoil,+,20 0.2227920 0.2227920 0.2227920 0.2227920 0.2227920 0.1113960
                                                                              0.1929435
             trefoil,-,10 trefoil,-,20 trefoil,+,5 trefoil,+,10 trefoil,+,20
bean, -, 5
                0.2227920
                              0.2227920
                                          0.2227920
                                                        0.2227920
                                                                     0.2227920
                              0.2227920
                                                        0.2227920
                                                                     0.2227920
bean, -, 10
                0.1113960
                                          0.2227920
bean,-,20
                0.2227920
                              0.1113960
                                          0.2227920
                                                        0.2227920
                                                                     0.2227920
bean,+,5
                0.2227920
                              0.2227920
                                          0.1113960
                                                        0.2227920
                                                                     0.2227920
bean, +, 10
                0.2227920
                              0.2227920
                                          0.2227920
                                                        0.1113960
                                                                     0.2227920
bean,+,20
                                                                     0.1113960
                0.2227920
                              0.2227920
                                          0.2227920
                                                        0.2227920
trefoil,-,5
                0.1929435
                              0.1929435
                                          0.1929435
                                                        0.1929435
                                                                     0.1929435
trefoil,-,10
                        NA
                              0.1929435
                                          0.1929435
                                                        0.1929435
                                                                     0.1929435
trefoil,-,20
                                          0.1929435
                                                        0.1929435
                                                                     0.1929435
                0.1929435
                                     NA
trefoil,+,5
                                                        0.1929435
                0.1929435
                             0.1929435
                                                                     0.1929435
                                                 NA
                              0.1929435
trefoil,+,10
                0.1929435
                                          0.1929435
                                                               NA
                                                                     0.1929435
trefoil,+,20
                0.1929435
                              0.1929435
                                          0.1929435
                                                        0.1929435
                                                                            NA
```

## References

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