

Employing **asremlPlus**, in conjunction with **asreml**, to calculate and use information criteria

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This vignette illustrates the facilities in **asremlPlus** (Brien, 2025), in conjunction with **asreml** (Butler et al., 2023), for calculating and using information. Here, **asremlPlus** and **asreml** are packages for the R Statistical Computing environment (R Core Team, 2025).

It is divided into the following main sections:

1. Set up the maximal model for this experiment
2. Obtaining information criteria for separate models
3. Obtaining information criteria for a prescribed sequence of model changes
4. Using information criteria to decide model changes

1. Set up the maximal model for this experiment

```
library(knitr)
opts_chunk$set("tidy" = FALSE, comment = NA)
suppressMessages(library(asreml, quietly=TRUE))

## Offline License checked out Mon Jan 6 22:33:51 2025

packageVersion("asreml")

## [1] '4.2.0.332'

suppressMessages(library(asremlPlus))
packageVersion("asremlPlus")

## [1] '4.4.44'

options(width = 100)
```

Get data available in **asremlPlus**

The data are from a 1976 spring wheat experiment and are taken from Gilmour et al. (1995). An analysis is presented in the **asreml** manual by Butler et al. (2023, Section 7.6), although they suggest that it is a barley experiment.

```
data(Wheat.dat)
```

Fit the maximal model

In the following a model is fitted that has the terms that would be included for a balanced lattice. In addition, a term WithinColPairs has been included to allow for extraneous variation arising between pairs of adjacent lanes. Also, separable ar1 residual autocorrelation has been included. This model represents the maximal anticipated model,

```
max.asr <- asreml(yield ~ WithinColPairs + Variety,  
                 random = ~ Rep/(Row + Column) + units,  
                 residual = ~ ar1(Row):ar1(Column),  
                 data=Wheat.dat)
```

ASReml Version 4.2 06/01/2025 22:33:51

	LogLik	Sigma2	DF	wall	
1	-724.1213	23034.14	124	22:33:51	
2	-717.4149	9206.931	124	22:33:51	(2 restrained)
3	-694.8752	26492.99	124	22:33:51	(2 restrained)
4	-694.1600	33101.80	124	22:33:51	(1 restrained)
5	-692.0020	36912.26	124	22:33:51	(1 restrained)
6	-691.7892	46701.51	124	22:33:51	(2 restrained)
7	-691.8336	46208.51	124	22:33:51	(1 restrained)
8	-691.7749	47698.26	124	22:33:51	
9	-691.7711	47041.85	124	22:33:51	

Warning in asreml(yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components changed by more than 1% on the last iteration

The warning from asreml is probably due to a bound term.

Initialize a testing sequence by loading the current fit into an asrtests object

```
max.asrt <- as.asrtests(max.asr, NULL, NULL)
```

Check for and remove any boundary terms

```
max.asrt <- rmboundary(max.asrt)  
summary(max.asrt$asreml.obj)$varcomp
```

	component	std.error	z.ratio	bound	%ch
Rep:Row	4.293282e+03	3.199458e+03	1.3418779	P	0.0
Rep:Column	1.575689e+02	1.480357e+03	0.1064398	P	0.7
units	5.742689e+03	1.652457e+03	3.4752438	P	0.0
Row:Column!R	4.706787e+04	2.515832e+04	1.8708669	P	0.0
Row:Column!Row!cor	7.920301e-01	1.014691e-01	7.8056280	U	0.0
Row:Column!Column!cor	8.799559e-01	7.370402e-02	11.9390486	U	0.0

```
print(max.asrt, which = "testsummary")
```

```
#### Sequence of model investigations for yield
```

(If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)

```
terms DF denDF p AIC BIC action
1 Rep 1 NA NA NA NA Boundary
```

Rep has been removed because it has been constrained to zero. Following the recommendation of Littell et al. (2006, p. 150), the bound on all variance components is set to unconstrained (U) using `setvariances.asreml` so as to avoid bias in the estimate of the residual variance. Alternatively, one could move Rep to the fixed model.

Unbind Rep, Row and Column components and reload into an asrtests object

```
max.asr <- setvarianceterms(max.asr$call,
                           terms = c("Rep", "Rep:Row", "Rep:Column"),
                           bounds = "U")
```

```
ASReml Version 4.2 06/01/2025 22:33:53
```

	LogLik	Sigma2	DF	wall
1	-724.1213	23034.14	124	22:33:53
2	-717.4149	9206.931	124	22:33:53 (2 restrained)
3	-694.8752	26492.99	124	22:33:53 (2 restrained)
4	-693.9744	33129.65	124	22:33:53 (1 restrained)
5	-692.8856	39662.12	124	22:33:53
6	-691.4276	53103.83	124	22:33:53
7	-691.2387	48092.17	124	22:33:53
8	-691.1808	47278.94	124	22:33:53
9	-691.1710	46850.98	124	22:33:53
10	-691.1700	46690.46	124	22:33:53

Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:53] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:53] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components changed by more than 1% on the last iteration

```
max.asrt <- as.asrtests(max.asr, NULL, NULL)
max.asrt <- rmboundary(max.asrt)
summary(max.asrt$asreml.obj)$varcomp
```

	component	std.error	z.ratio	bound	%ch
Rep	-2462.3785858	1.191435e+03	-2.066734	U	0.2
Rep:Row	5012.4021415	3.396848e+03	1.475604	U	0.1
Rep:Column	920.5936391	1.704008e+03	0.540252	U	1.1
units	5964.9099377	1.608792e+03	3.707695	P	0.1
Row:Column!R	46690.4620387	2.731906e+04	1.709080	P	0.0
Row:Column!Row!cor	0.8152180	9.988929e-02	8.161216	U	0.1
Row:Column!Column!cor	0.8857252	7.487875e-02	11.828793	U	0.0

```
print(max.asrt, which = "testsummary")
```

Sequence of model investigations for yield

(If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)

```
[1] terms DF denDF p AIC BIC action
<0 rows> (or 0-length row.names)
```

Now the Rep component estimate is negative.

The `test.summary` output shows that no changes have been made to the model loaded using `as.asrtests`. The pseudo-anova table shows that Varieties are highly significant ($p < 0.001$)

2. Obtaining information criteria for separate models

The method `infoCriteria` has two methods for calculating information criteria. One, `infoCriteria.asreml`, is a method for `asreml` objects and the other, `infoCriteria.list`, if for 'listobjects, the components of thelistbeingasreml' objects.

Single models

Firstly, `infoCriteria` is called with the default `IClikelihood`, which is `REML`. Then it is called with `IClikelihood` set to `full` (Verbyla, 2019).

```
infoCriteria(max.asr)
```

	fixedDF	varDF	NBound	AIC	BIC	loglik
1	0	7	0	1396.34	1416.082	-691.17

```
infoCriteria(max.asr, IClikelihood = "full")
```

	LogLik	Sigma2	DF	wall
1	-691.1700	46641.98	124	22:33:54

Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Log-likelihood not converged

	fixedDF	varDF	NBound	AIC	BIC	loglik
1	26	7	0	1647.194	1746.545	-790.5968

A list of models

Now, a second model, from which the `withinColPairs` term has been omitted, is fitted; to be consistent, the variance components are unconstrained using `setvariances.asreml`. Then the `asreml` objects for this model and the maximal model are combined into a `list` and a `data.frame` produced that includes their information criteria.

```
m1.asr <- asreml(yield ~ Variety,
  random = ~ Rep/(Row + Column) + units,
  residual = ~ ar1(Row):ar1(Column),
  data=Wheat.dat)
```

ASReml Version 4.2 06/01/2025 22:33:54

	LogLik	Sigma2	DF	wall
1	-727.7742	22898.99	125	22:33:54
2	-721.0966	9190.303	125	22:33:54 (2 restrained)
3	-698.3135	26671.76	125	22:33:54 (2 restrained)
4	-697.5170	32677.28	125	22:33:54 (1 restrained)
5	-695.4192	36662.27	125	22:33:54 (1 restrained)
6	-695.2077	46263.96	125	22:33:54 (2 restrained)
7	-695.1975	46156.63	125	22:33:54
8	-695.1906	46630.21	125	22:33:54

Warning in asreml(yield ~ Variety, random = ~Rep/(Row + Column) + units, : Some components changed by more than 1% on the last iteration

```
m1.asr <- setvarianceterms(m1.asr$call,
  terms = c("Rep", "Rep:Row", "Rep:Column"),
  bounds = "U")
```

ASReml Version 4.2 06/01/2025 22:33:54

	LogLik	Sigma2	DF	wall
1	-727.7742	22898.99	125	22:33:55
2	-721.0966	9190.303	125	22:33:55 (2 restrained)
3	-698.3135	26671.76	125	22:33:55 (2 restrained)
4	-697.3331	32689.33	125	22:33:55 (1 restrained)
5	-697.0164	39975.97	125	22:33:55
6	-695.0695	54825.30	125	22:33:55
7	-694.7571	47637.20	125	22:33:55
8	-694.6436	46775.41	125	22:33:55
9	-694.6181	46175.06	125	22:33:55
10	-694.6152	45940.69	125	22:33:55

Warning in asreml(fixed = yield ~ Variety, random = ~Rep/(Row + Column) + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:55] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep/(Row + Column) + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:55] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep/(Row + Column) + : Some components changed by more than 1% on the last iteration

```
mods <- list(max = max.asr, m1 = m1.asr)
ic <- infoCriteria(mods, IClikelihood = "full")
print(ic)
```

	fixedDF	varDF	NBound	AIC	BIC	loglik
max	26	7	0	1647.194	1746.545	-790.5968
m1	25	7	0	1645.326	1741.666	-790.6629

3. Obtaining information criteria for a prescribed sequence of model changes

The use of `changeTerms.asrtests` is demonstrated for a sequence of models, starting with the maximal model.

Drop the term for within Column pairs (a post hoc factor)

```
current.asrt <- as.asrtests(max.asrt$asreml.obj, NULL, NULL,
                           label = "Maximal model", IClikelihood = "full")
```

Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Log-likelihood not converged

```
current.asrt <- changeTerms(current.asrt, dropFixed = "WithinColPairs",
                           label = "Drop withinColPairs", IClikelihood = "full")
```

WARN [2025-01-06 22:33:56] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:56] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:57] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:57] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

```
print(current.asrt, which = "testsummary", omit.columns = "p")
```

Sequence of model investigations for yield

(If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)

	terms	DF	denDF	AIC	BIC	action
1	Maximal model	26	7	1647.194	1746.545	Starting model
2	Drop withinColPairs	25	7	1645.326	1741.666	Changed fixed

So the same values of the information criteria have been obtained as when `infoCriteria.list` was used on a list containing the `asreml` objects for the two models. The difference is that here there is ultimately only one fitted model, the model stored in the `asreml` object in the `asrtests` object named `current.asrt`: this is the model with `withinColPairs` omitted.

Note this use of the `omit.columns` argument from `print.test.summary` to omit the irrelevant column `p` from the `test.summary`.

Drop nugget term

```
current.asrt <- changeTerms(current.asrt, dropRandom = "units",  
                             label = "Drop units", ICLikelihood = "full")
```

WARN [2025-01-06 22:33:59] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:59] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:59] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:33:59] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

Check Row autocorrelation

```
current.asrt <- changeTerms(current.asrt, newResidual = "Row:ar1(Column)",  
                             label="Row autocorrelation", ICLikelihood = "full")
```

WARN [2025-01-06 22:34:01] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:01] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:01] Log-likelihood not converged

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Log-likelihood not converged

WARN [2025-01-06 22:34:01] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:01] Log-likelihood not converged

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Log-likelihood not converged

WARN [2025-01-06 22:34:01] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

Warning in newfit.asreml(asreml.obj, fixed. = fix.form, random. = ran.form, :

```
print(current.asrt, which = "testsummary", omit.columns = "p")
```

Sequence of model investigations for yield

(If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)

	terms	DF	denDF	AIC	BIC	action
1	Maximal model	26	7	1647.194	1746.545	Starting model
2	Drop withinColPairs	25	7	1645.326	1741.666	Changed fixed
3	Drop units	25	6	1650.115	1743.445	Changed random
4	Row autocorrelation	25	5	1660.788	1751.107	Changed residual - old uncovered

4. Using information criteria to decide model changes

This sections illustrates the use of `changeModelOnIC.asrtests` to decide between consecutive models in a sequence of models. The default information criterion to use for this is the AIC. However, `which.IC` can be used to specify the use of the BIC or both. Here we use the AIC and the full likelihood.

Check the term for within Column pairs (a post hoc factor)

As before, we start with the maximal model, in which the variance components have been unconstrained and look to decide whether or not to drop the `withinColPairs` term.

```
current.asrt <- as.asrtests(max.asrt$asreml.obj, NULL, NULL,  
                           label = "Maximal model", ICLikelihood = "full")
```

```
Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Log-likelihood  
not converged
```

```
current.asrt <- iterate(current.asrt)
```

```
WARN [2025-01-06 22:34:03] Some components changed by more than 1% on the last iteration
```

```
Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components  
changed by more than 1% on the last iteration
```

```
WARN [2025-01-06 22:34:03] Some components changed by more than 1% on the last iteration
```

```
Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components  
changed by more than 1% on the last iteration
```

```
current.asrt <- changeModelOnIC(current.asrt, dropFixed = "WithinColPairs",  
                                label = "withinColPairs",  
                                ICLikelihood = "full", which.IC = "AIC",  
                                allow.unconverged = FALSE)
```

```
WARN [2025-01-06 22:34:04] Some components changed by more than 1% on the last iteration
```

```
Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components  
changed by more than 1% on the last iteration
```

```
WARN [2025-01-06 22:34:05] Some components changed by more than 1% on the last iteration
```

```
Warning in asreml(fixed = yield ~ WithinColPairs + Variety, random = ~Rep/(Row + : Some components  
changed by more than 1% on the last iteration
```

```
WARN [2025-01-06 22:34:05] Some components changed by more than 1% on the last iteration
```

```
Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components  
changed by more than 1% on the last iteration
```

WARN [2025-01-06 22:34:05] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

```
print(current.asrt, which = "testsummary", omit.columns = "p")
```

Sequence of model investigations for yield

(If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)

	terms	DF	denDF	AIC	BIC	action
1	Maximal model	26	7	1647.193601	1746.544565	Starting model
2	withinColPairs	-1	0	-1.874126	-4.884762	Swapped

Given the warning about a lack of convergence, we use `iterate.asrtests` to perform additional iterations of the fitting process. It seems that it was successful.

It can be seen from the `test.summary` that the term has been swapped out and this has the effect of reducing the number of fixed parameters by one and makes no change to the variance parameters.

Check the nugget term

```
current.asrt <- changeModelOnIC(current.asrt, dropRandom = "units",  
                                label = "units", IClikelihood = "full",  
                                allow.unconverged = FALSE)
```

WARN [2025-01-06 22:34:07] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:07] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:08] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:08] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + Rep:Row + Rep:Column, : Some components changed by more than 1% on the last iteration

Check Row autocorrelation

```
current.asrt <- changeModelOnIC(current.asrt, newResidual = "Row:ar1(Column)",
                                label="Row autocorrelation", IClikelihood = "full",
                                allow.unconverged = FALSE)
```

WARN [2025-01-06 22:34:10] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:10] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:10] Log-likelihood not converged

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Log-likelihood not converged

WARN [2025-01-06 22:34:10] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

WARN [2025-01-06 22:34:10] Log-likelihood not converged

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Log-likelihood not converged

WARN [2025-01-06 22:34:10] Some components changed by more than 1% on the last iteration

Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components changed by more than 1% on the last iteration

Warning in newfit.asreml(asreml.obj, fixed. = fix.form, random. = ran.form, :

Check Column autocorrelation (depends on whether Row autocorrelation retained)

```
{
  last.action <- current.asrt$test.summary$action[current.asrt$test.summary$terms ==
                                                    "Row autocorrelation"]
  if (grepl("Unswapped", last.action, fixed = TRUE) |
      grepl("Unchanged", last.action, fixed = TRUE))
    current.asrt <- changeModelOnIC(current.asrt, newResidual = "ar1(Row):Column",
                                    label="Col autocorrelation", IClikelihood = "full",
                                    allow.unconverged = FALSE)
  else
    current.asrt <- testresidual(current.asrt, newResidual = "Row:Column",
                                  label="Col autocorrelation", IClikelihood = "full",
                                  allow.unconverged = FALSE)
}
```

```
WARN [2025-01-06 22:34:12] Some components changed by more than 1% on the last iteration
```

```
Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components
changed by more than 1% on the last iteration
```

```
WARN [2025-01-06 22:34:12] Some components changed by more than 1% on the last iteration
```

```
Warning in asreml(fixed = yield ~ Variety, random = ~Rep + units + Rep:Row + : Some components
changed by more than 1% on the last iteration
```

```
Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.lik, bound.exclusions = bound.exclusions):
Row:Column!Row!cor
```

```
Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, IClikelihood = ic.lik, : The following bound
Row:Column!Row!cor
```

Output the results

```
print(current.asrt, which = "test", omit.columns = "p")
```

```
#### Sequence of model investigations for yield
```

(If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)

	terms	DF	denDF	AIC	BIC	action
1	Maximal model	26	7	1647.193601	1746.544565	Starting model
2	withinColPairs	-1	0	-1.874126	-4.884762	Swapped
3	units	0	-1	4.789424	1.778789	Unswapped
4	Row autocorrelation	0	0	0.000000	0.000000	Unchanged - new unconverged
5	Col autocorrelation	0	-2	19.478447	13.457177	Unswapped

```
summary(current.asrt$asreml.obj)$varcomp
```

	component	std.error	z.ratio	bound	%ch
Rep	-2392.1616314	1.199592e+03	-1.9941460	U	0.4
Rep:Row	5033.2850607	3.408523e+03	1.4766764	U	0.2
Rep:Column	760.1498938	1.617038e+03	0.4700879	U	2.5
units	5929.0518909	1.609478e+03	3.6838361	P	0.0
Row:Column!R	45940.6913909	2.634982e+04	1.7434920	P	0.0
Row:Column!Row!cor	0.8101561	9.995026e-02	8.1055925	U	0.1
Row:Column!Column!cor	0.8846454	7.504265e-02	11.7885681	U	0.0

The `test.summary` shows us that the model without the autocorrelation failed to converge and so no change was made to the model. It, and the messages from checking the Column autocorrelation, also show us that the omission of the Column autocorrelation resulted in the Row autocorrelation becoming bound. That is, dropping the Column autocorrelation resulted in the dropping of two variance parameters

The function `printFormulae.asreml` is used to display the fitted model.

```
printFormulae(current.asrt$asreml.obj)
```

```
#### Formulae from asreml object
```

```
fixed: yield ~ Variety  
random: ~ Rep + units + Rep:Row + Rep:Column  
residual: ~ ar1(Row):ar1(Column)
```

References

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