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El teorema de los cuatro colores à

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Resumen

In this paper, we will review the definitions about the hyperbolic functions, trigonometric functions and deduce their inverse functions in terms of logarithms and exponentials introducing complex numbers. Hence, we will show the mathematical interrelation between this types of functions. Having already present the established definitions for the hyperbolic functions will look for an analog representation for the trigonometric functions.

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Palabras clave: four-color theorem, Kempe's chain, planar graphs

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URL: www.blogdeoromion.pe.hu (J. Navío Torres) ¹ Since 1880.

2. El "camino" hacia la demostración

- 3. Aplicaciones
- 4. Conclusiones

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[☆]This paper are available on GitHub.

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^{1.} Introducción

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