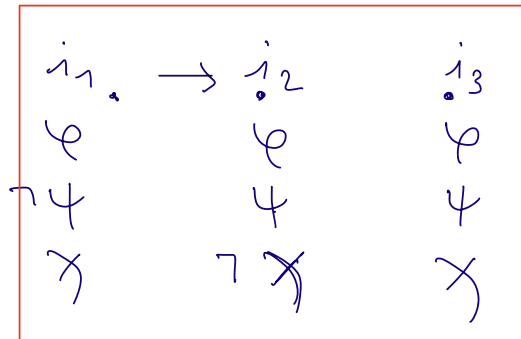


line 564, file ODLcube.thy.

This is the model shown by nitpick. We have  $P(\varphi/\varphi \vee \psi)$ ,  $P(\psi/\psi \vee \chi)$  and  $P(\varphi/\varphi \vee \chi)$

$i_1 \rightarrow i_2$  means  $i_1 \geq i_2$   
( $\cap i_1 i_2$ )  
no arrow means  $\neq$

$\|A\|$  = set of worlds  
where A holds



Verification :

$$\max(\|\varphi \vee \psi\|) = \{i_1, i_3\} \cap \|\varphi\| = \{i_1, i_3\}$$

$\hookrightarrow P(\varphi/\varphi \vee \psi)$  holds

$$\max(\|\psi \vee \chi\|) = \{i_1, i_3\} \cap \|\psi\| = \{i_3\}$$

$\hookrightarrow P(\psi/\psi \vee \chi)$

$$\max(\|\varphi \vee \chi\|) = \{i_1, i_3\} \cap \{\chi\}$$

$\hookrightarrow P(\varphi/\varphi \vee \chi)$

However, the law does not hold in general, if I change the value of  $\varphi$ ,  $\psi$  and  $\chi$ .

$$P(\overbrace{(\varphi \wedge \psi \wedge \neg \chi)}^{\varphi} / \overbrace{(\varphi \wedge \psi \wedge \neg \chi)}^{\varphi} \vee \overbrace{(\varphi \wedge \psi \wedge \chi)}^{\psi} \vee \overbrace{(\varphi \wedge \neg \psi \wedge \chi)}^{\chi}) \text{ is true}$$

$$P(\overbrace{(\varphi \wedge \psi \wedge \chi)}^{\psi} \vee \overbrace{(\varphi \wedge \neg \psi \wedge \chi)}^{\psi} / \overbrace{(\varphi \wedge \psi \wedge \chi)}^{\psi} \vee \overbrace{(\varphi \wedge \neg \psi \wedge \chi)}^{\psi} \vee \overbrace{(\varphi \wedge \neg \psi \wedge \neg \chi)}^{\chi}) \text{ is true}$$

$$P(\overbrace{(\varphi \wedge \psi \wedge \neg \chi)}^{\varphi} / \overbrace{(\varphi \wedge \psi \wedge \neg \chi)}^{\varphi} \vee \overbrace{(\varphi \wedge \neg \psi \wedge \neg \chi)}^{\psi}) \text{ is false}$$

proof :

$$\begin{aligned} \max(i_2, i_3) \cap \{i_2\} &\neq \emptyset \\ \max(i_1, i_2, i_3) \cap \{i_2, i_3\} &\neq \emptyset \\ \max(i_2, i_1) \cap \{i_2\} &= \emptyset \end{aligned}$$