Article Title

LogiKEy Workbench: Deontic Logics, Logic Combinations and Expressive Ethical and Legal Reasoning (Isabelle/HOL Dataset)

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Abstract

The LogiKEy workbench for ethical and legal reasoning is presented. This workbench simultaneously supports development, experimentation, assessment and deployment of formal logics and ethical and legal theories at different conceptual layers. More concretely, it comprises, in form of a data set (Isabelle/HOL theory files), formal encodings of multiple deontic logics, logic combinations, deontic paradoxes and normative theories in the higher-order proof assistent system Isabelle/HOL. The data was acquired through application of the LogiKEy methodology, which supports experimentation with different normative theories, in different application scenarios, and which is not tied to specific logics or specific logic combinations. Our workbench consolidates related research contributions of the authors and it may serve as a starting point for further studies and experiments in flexible and expressive ethical and legal reasoning. It may also support hand-on teaching of non-trivial logic formalisms in lecture courses and tutorials.

Keywords

Thrustworthy and responsible AI; Knowledge representation and reasoning; Automated theorem proving; Model finding; Normative reasoning; Normative systems; Philosophical and ethical issues; Semantical embedding; Higher-order logic

Specifications Table

Subject	Computer Science
Specific subject area	Artificial intelligence; Knowledge representation and reasoning; Normative reasoning
Type of data	formal theories (.thy files) encoded in Isabelle/HOL syntax, readable (.png or .pdf) views of this data
How data were acquired	The data was acquired through manual encoding of various deontic logics, logic combinations, examples of contrary-to-duty paradoxes, excerpts of legal texts and exemplary ethical theories utilizing the LogiKEy methodology [8], which is itself based on shallow semantical embeddings (SSEs) [1] of logics and theories in classical higher-order logic. The concrete encodings were conducted in the higher-order proof assistant system Isabelle/HOL [25]; however, they are conceptually transferable to many other expressive reasoning systems.

Data format	Raw, processed, analyzed and cleaned data. The data is provided in the syntax format of the Isabelle/HOL proof assistant, which has been used to process, analyze and verify it; the data files were also annotated by hand. Isabelle/HOL is freely available: `https://isabelle.in.tum.de`
Parameters for data collection	One objective was to empirically assess the expressivity and proof automation capabilities of Isabelle/HOL and its integrated tools in normative reasoning when utilising the LogiKEy methodology and the SSE approach. Another objective was to provide a reusable foundation for further experiments in expressive ethical and legal reasoning.
Description of data collection	The data was manually constructed and curated. As part of the data collection process it has been demonstrated that non-trivial, normative reasoning is supported in the provided framework. This in particular included studies of paradoxes in normative reasoning [10] and whether and how they can eventually be avoided. An integral aspect of the data collection process also has been to provide evidence for the practical normative reasoning performance of the various reasoning tools integrated with Isabelle/HOL when utilizing the LogiKEy approach. Useful comments were added to the data files. The practical performance of the logic encodings can be independently assessed by users in combination with the Isabelle/HOL system. It has also been demonstrated how deontic logics can be flexible combined with other logic formalisms within the LogiKEy approach.
Data source location	The data is hosted on `github.com`.
Data accessibility	The data is accessible via `logikey.org`, which redirects to the repository `https://github.com/cbenzmueller/LogiKEy` on `github.com`, where the data is hosted and maintained. The two subdirectories `2020-DataInBrief-Article` and `2020-DataInBrief-Data` are associated with this article; the latter contains the data set.
Related research article	C. Benzmüller, X. Parent, and L. van der Torre. Designing normative theories of ethical and legal reasoning: LogiKEy framework, methodology, and tool support. Artificial Intelligence (to appear), 2020. Preprint: `https://arxiv.org/abs/1903.10187`. Further related research articles include: [4, 5, 7, 14, 15, 16]

Value of the Data

- The provided data can be reused, independent of the related research article(s), as a starting point for further studies and experiments in expressive ethical and legal reasoning. Moreover, it can be reused, extended and adapted to support also other various other application directions, including, e.g., the study of deontic modality and quantifiers in linguistics.
- The data collection is beneficial for research and application in a range of areas, including but not limited to: machine ethics (ethico-legal governor systems), explainable and trustworthy AI, regulatory technologies, argumentation, natural language semantics. To that end the data includes reusable SSEs of a portfolio of deontic logics, logic combinations, paradoxes in normative reasoning and ethical theories in classical higher-order logic (HOL), aka Church's type theory [3], interpretable in the Isabelle/HOL proof assistant system [25]. The data set may also be used to support the teaching of expressive, classical and non-classical logic formalisms and their combinations in lecture courses and tutorials.
- To reuse the data interested researchers, students and practitioners only need to download the provided data files, include them in their formalization projects and suitably extend or adapt them. For example, the contributed data includes a sample encoding of selected statements from the GDPR (General Data Protection Regulation) and an encoding of Gewirth's ethical argument and principle, known as the Principle of Generic Consistency (PGC) [17], in a suitable extension of higher-order deontic logic. These are two examples in the area of knowledge representation and reasoning with an emphasis on regulatory and ethical aspects. They can be reused as a starting point for the encoding and automated solution of similar ethico-legal theories.

- Fourty years after Von Wright's invention of deontic logic, the question has always been how deontic logics and normative theories can be used in computer science applications. The LogiKEy workbench and associated methodology addresses this challenge; it has the potential to revolutionize the area of deontic logic itself.
- The data set is useful also for stimulation of cross-fertilization effects between different research communities including the deontic logics and normative reasoning communities, the area of higher-order logics, and the area of interactive and automated theorem proving with its various sub-communities targeting very different logic formalisms.
- The presented encodings put a particular emphasis on the modeling of (regulative) norms. We agree with, e.g., Jones and Sergot [19] that deontic logic is needed when it is necessary to make explicit, and then reason about, the distinction between what ought to be the case and what is the case. Furthermore, the adequate handling of norm violation (also called contrary-to-duty situations) has posed a core challenge for knowledge representation frameworks. This problem motivated the design of deontic logics (and logic combinations) more sophisticated than traditional ones, like modal logic. These frameworks are automatized for the first time.

Data Description

The data is provided in form of Isabelle/HOL source files, which are hosted at `logikey.org`. The individual data files belong to different categories.

Contributed data files in category I are listed in Table 1. They provide encodings of SSEs, and associated tests, of various deontic logics in meta-logic HOL. A category I example file is displayed in Figs. 1–2; this data file contains (an extension of) the SSE of dyadic deontic logic (DDL) by Carmo and Jones [11] in HOL and studies, resp. verifies, its properties.

Contributed data files in category II are listed in Table 2. They study paradoxes and smaller examples of normative reasoning. An example is displayed in Fig. 3, which presents an analysis of Chisholm's paradox [13] in standard deontic logic SDL.

Contributed data files in category III are listed in Table 3. They provide encodings of (excerpts of) legal and ethical theories and arguments formalized using the deontic logics as provided in category I files and further examined in the category II files.

In addition to data listed in Tables 1—3 the data set provided at `logikey.org` also includes the following:

- Subdirectory `2020-DataInBrief-Data/Course-Material-1` contains Isabelle/HOL data files stemming from a lecture course on deontic logic at University of Luxembourg based on [26].
- Subdirectory `2020-DataInBrief-Data/Climate-Engineering` contains Isabelle/HOL data files related to the formalization and assessment [16] of selected arguments in climate engineering.
- Subdirectory `2020-DataInBrief-Data/US-Constitution-Loophole` contains Isabelle/HOL data files related to a formalization and assessment [29] of Kurt Gödel's claim that the US Constitution contains a loophole for establishing a dictatorship.
- Subdirectory `2020-DataInBrief-Data/WiseMenPuzzle` contains Isabelle/HOL data files related to a formalization and study [1] of the well known Wise Men Puzzle; this data set, which has been published before [2], is included here to make it better available for `logikey.org` users.

Further related data sets, including selected formalisations in computational metaphysics (cf. [1, 22] and the references therein), will be added to `logikey.org` as useful and appropriate.

Experimental Design, Materials, and Methods

The data was acquired through manual encodings of logics, theories and arguments in the Isabelle/HOL [25] proof assistant system. The modeling process was following the LogiKEy methodology depicted in Fig. 4. This methodology supports formalization projects in the area of ethical and legal reasoning at different layers of abstraction. This methodology is briefly explained below at hand of selected examples from our contributed data set; we address all three different layers and discuss examples.[1]

Layer L1 example development (files CJ_DDL.thy and CJ_DDL_Tests.thy): File CJ_DDL.thy contains the encoding (of a quantified extension) of the DDL of Carmo and Jones in HOL. This encoding of DDL in HOL is exemplary for *Layer L1* developments in LogiKEy. First, the desired object *logic* was selected (Step 1); Carmo and Jones's DDL in the given case. A *semantics* (Step 2) for this object logic was sought and

[1] For a general description of the LogiKEy framework, methodology and tool support see the related research article [8].

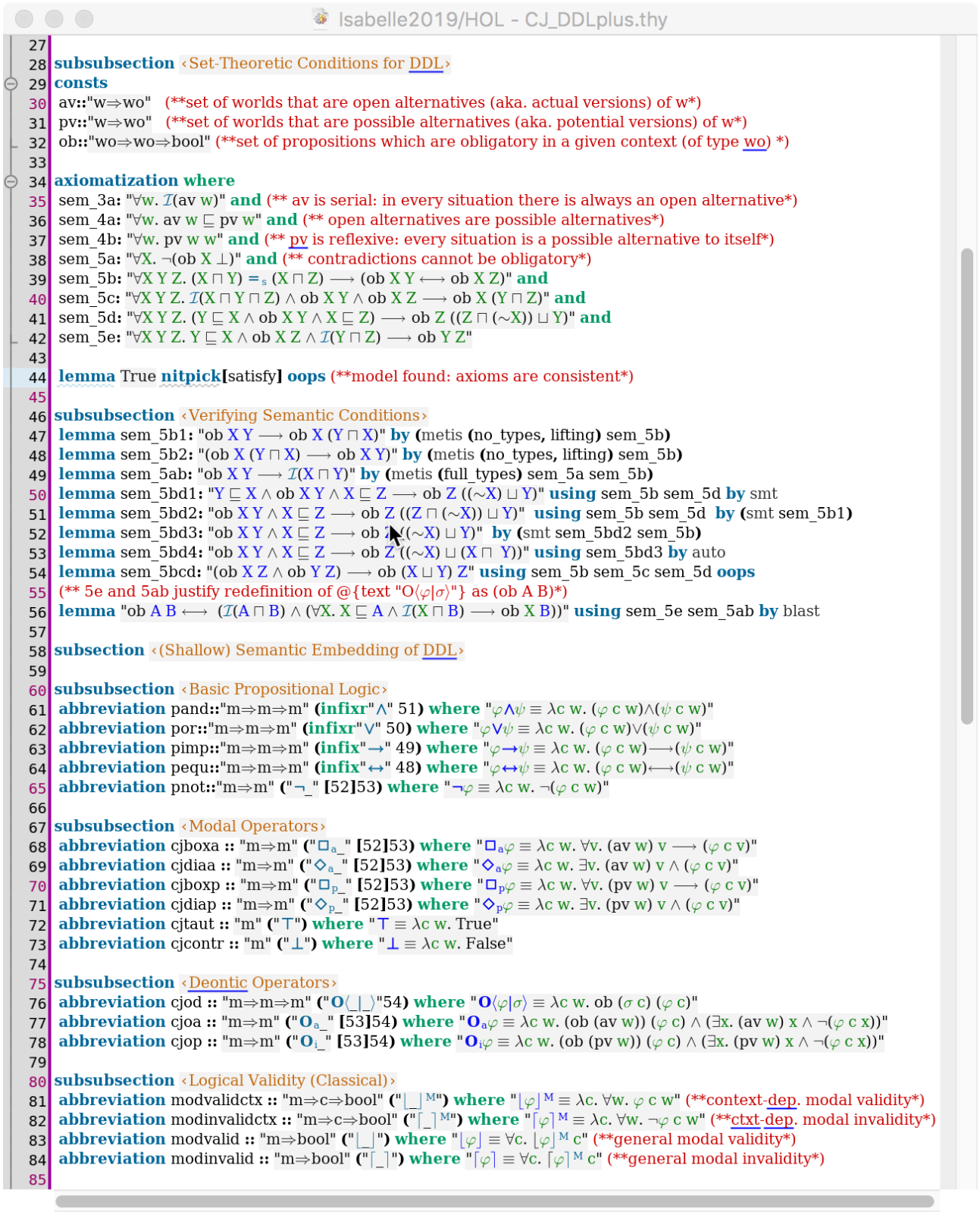

Figure 1: Data file CJ_DDLplus.thy; in lines 29–85 the SSE of the DDL by Carmo and Jones [11] in HOL is presented

found in the original papers by Carmo and Jones [10, 11]; such a mathematical description of a semantics, a neighborhood semantics in the given case, constitutes the ideal starting point for the definition of a SSE of the object logic in HOL, which in turn enables its *automation* (Step 3) with off-the-shelf reasoning tools for HOL. The automation of DDL was subsequently assessed (Step 4) with automated theorem provers and model finders integrated with Isabelle/HOL. Then, by pen and paper means on a theoretical level, the *faithfulness* (Step 4) of the embedding of DDL in HOL was studied and proved; this proof has been published [5, 6]. Furthermore, *implications* of the embedding of DDL in HOL were studied (Step 5); see

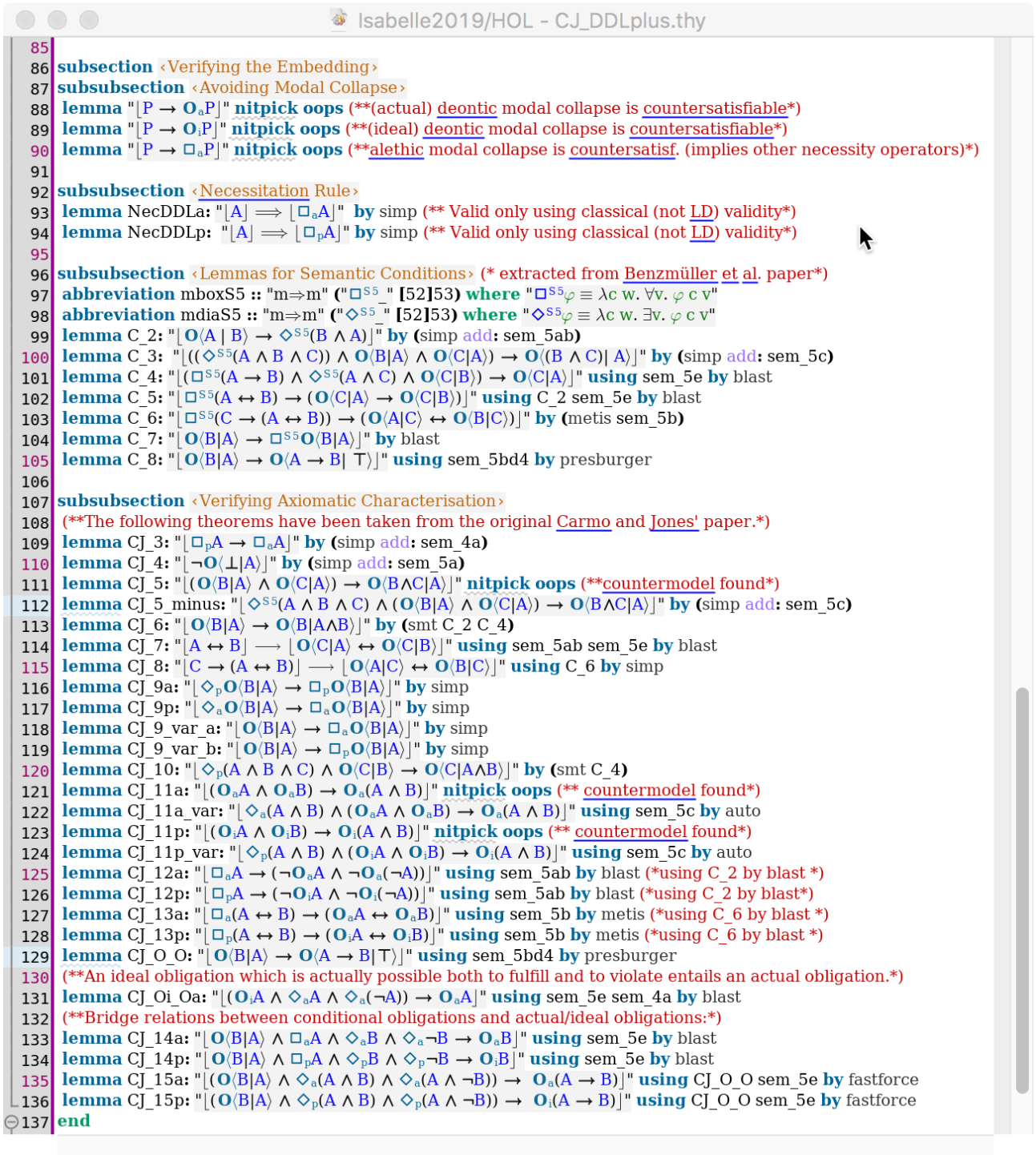

Figure 2: Data file CJ_DDLplus.thy; in lines 87–137 lemmata from Carmo and Jones paper [11] are proved

for example the additional theorems in file CJ_DDL_Tests.thy and the contrary-to-duty studies conducted in files Chisholm_DDL_Monadic.thy and Chisholm_DDL_Dyadic.thy. Since the DDL of Carmo and Jones has not been automated before with other systems or approaches, there are no *benchmarks* (Step 7) available that we could use to properly assess and compare the competitiveness of our solution. The publication of this data set can be seen as first step towards the built-up and *contribution* (Step 8) of such a benchmark suite to the community; future work includes the conversion of our Isabelle/HOL encodings into TPTP THF format [28], so that they can be used as challenge problems in the yearly CASC world-championship competitions [27].

Layer L2 example development (file GDPR_CJ_DDL.thy): In file GDPR_CJ_DDL.thy we *selected* (Step 1) statements from the General Data Protection Regulation (GDPR) for formalisation. The *analysis* (Step 2) of these statements revealed that obligation aspects in the context of data processing needed to be adressed

Table 1: Category I data files — deontic logics, extensions of deontic logics and logic combinations

File	Dependency	Reading	Description
SDL.thy	Main.thy	[9, 12]	Provides a consistent SSE of standard deontic logic (SDL) in HOL. An unary deontic operator is defined. The D axiom is postulated and correspondence to seriality of the accessibility is proved. The added first-order and higher-order quantifiers are constant domain (possibilist notion of quantification). This is verified by proving the Barcan formula and its converse.
CJ_DDL.thy	Main.thy	[5]	Provides a consistent SSE of a dyadic deontic logic (DDL) by Carmo and Jones [11] in HOL. Different modal operators are introduced: dyadic deontic obligation, monadic deontic operator for actual obligation, monadic deontic operator for primary obligation, and further alethic modalities. Moreover, constant domain first-order and higher-order quantifiers are added.
CJ_DDL_Tests.thy	CJ_DDL.thy	[5]	Contains soundness and proof automation tests for the embedding of DDL in HOL given in CJ_DDL.thy. For example, the monadic modal operators $\Box$, $\Box_p$ and $\Box_a$ are identified as S5, KT and KD modalities, respectively. Relevant lemmata from the original work of Carmo and Jones [11] are automated.
E.thy	Main.thy	[7],[8, Fig.6]	Provides a consistent SSE of a quantified extension of Aqvist's System E in HOL. The file also runs a number of reasoning tasks (validity checking, refutation, correspondance theory).
Lewis_DDL.thy	Main.thy	[23]	Provides a consistent SSE of Lewis's DDL. The file also runs a number of reasoning tasks (validity checking, refutation, correspondance theory). The relationship with Åqvist's dyadic deontic operator is also studied.
IO_out2_STIT.thy	Main.thy	[4]	Provides a consistent SSE of a quantified extension of IO logic (out2) [24, 26] and elements of STIT logics [18] in HOL. The file also contains proof automation tests and soundness checks.
CJ_DDLplus.thy	Main.thy	[14, 15]	A modification of the SSE developed in file CJ_DDL.thy is presented; see Figs. 1 and 2. This theory provides the starting point for an extension of a higher-order variant of DDL into a two-dimensional semantics as originally presented by Kaplan for his logic of demonstratives [20, 21]. The logic extension is completed in file Extended_CJ_DDL.thy. The displayed lines in Fig. 2 show automations of various lemmata from the original paper of Carmo and Jones [11], where they were proved manually with pen and paper.
Extended_CJ_DDL.thy	CJ_DDLplus.thy	[14, 15]	Contains a further extension and combination of the higher-order DDL encoded in file CJ_DDLplus.thy with relevant parts (for the work presented in the related research article [8]) of Kaplan's logic of demonstratives (LD) [20, 21].

Table 2: Category II data files: paradoxes and examples of normative reasoning

File	Dependency	Reading	Description
Chisholm_SDL.thy	SDL.thy	–	Contains a detailed analysis of Chisholm's contrary-to-duty paradox [13] in SDL, including an independence analysis for all wide and narrow scoping options that arise in the axiomatization of the paradox; see Fig. 3.
Chisholm_CJ_DDL_Monadic.thy	CJ_DDL.thy	–	Contains a study analogous to Chisholm_SDL.thy for monadic obligation in DDL.
Chisholm_CJ_DDL_Dyadic.thy	CJ_DDL.thy	–	Contains a study analogous to Chisholm_SDL.thy for dyadic obligation in DDL.
Chisholm_E.thy	CJ_DDL.thy	–	Contains a study analogous to Chisholm_SDL.thy for deontic logic E.
IO_Experiments	IO_out2_STIT	–	Contains a study of different paradoxes from the literature in IO logic (out2).

Table 3: Category III data files: (excerpts of) legal and ethical theories and arguments

File	Dependency	Reading	Description
GDPR_SDL.thy	SDL.thy	[8, Fig. 7]	Contains a modeling of selected statements from the GDPR in SDL. It is demonstrated that this modeling leads to contrary-to-duty issues, i.e., inconsistency and explosion.
GDPR_CJ_DDL.thy	CJ_DDL.thy	—	Contains a modeling of selected statements from the GDPR in DDL. It is demonstrated that this modeling is stable against the contrary-to-duty issues identified in GDPR_SDL.thy, i.e., inconsistency and explosion is avoided and inferences are supported as expected.
GDPR_E.thy	E.thy	[8, Fig. 8]	Contains a modeling of selected statements from the GDPR in logic E. It is demonstrated that this modeling is stable against the contrary-to-duty issues identified in GDPR_SDL.thy, i.e., inconsistency and explosion is avoided and inferences are supported as expected.
GewirthArgument.thy	Extended_CJ_DDL.thy.	[15, 14], [8, Fig. 10]	Contains a formalization and partial automation of Gewirth's supporting argument for his *Principle of Generic Consistency*. This principle constitutes, loosely speaking, an emendation of the *Golden Rule*, i.e., the principle of treating others as one's self would wish to be treated. Gewirth's argument and theory is assessed, emended (minor corrections) and verified.

and that natural language phrases in the studied parts of the GDPR indeed contains challenge deontic modalities. This motivated the choice of a suitable deontic *logic* (Step 3), such as DDL, for the formal encoding of these challenges aspects. In the given case it became apparent that a propositional encoding would hardly suffice in practical applications, so the selected deontic logic DDL, needed to be *combined with*, respectively extended by, a notion of quantification, which led to the addition of quantifiers to the file CJ_DDL.thy. Subsequently the two GDPR articles were *formalized* (Step 4) using logical connectives

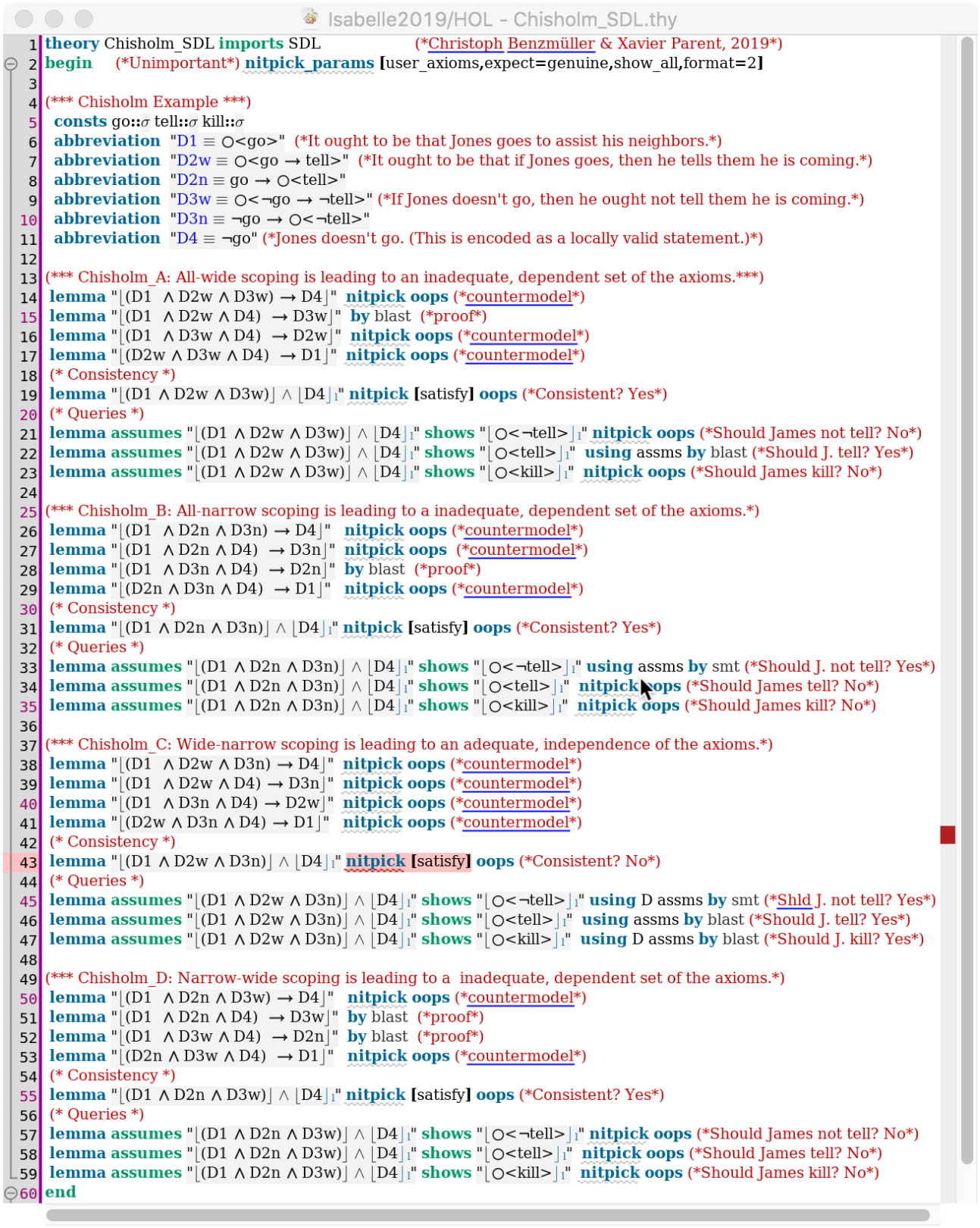

Figure 3: Data file Chisholm_SDL.thy studies Chisholm's paradox in combination with wide-narrow scoping issues

as provided in the imported file CJ_DDL.thy, and then some *exploration* (Step 5) and assessment studies were conducted. This included the contrary-to-duty studies as reported in related research articles [8, 5]. With our data set we *contribute* (Step 6) this work to the wider research community and enable its reuse.

Layer L3 example development: Layer L3 example developments have just started. The idea is to populate regulatory governor architectures [8] with ethical and legal theories from Layer L2, so that reasoning with the theories can be utilized to explain and control the behaviour of (autonomous) AI systems. To realize

such applications it is required to *select* (Step 1) some ethical and/or legal theory from Layer L2, to devise and implement (or reuse) a respective *governor architecture* (Step 2), to *populate* (Step 3) this governor system with the selected ethical and/or legal theory, and to *assess* (Step 4) the well-functioning of this system in empirical studies.

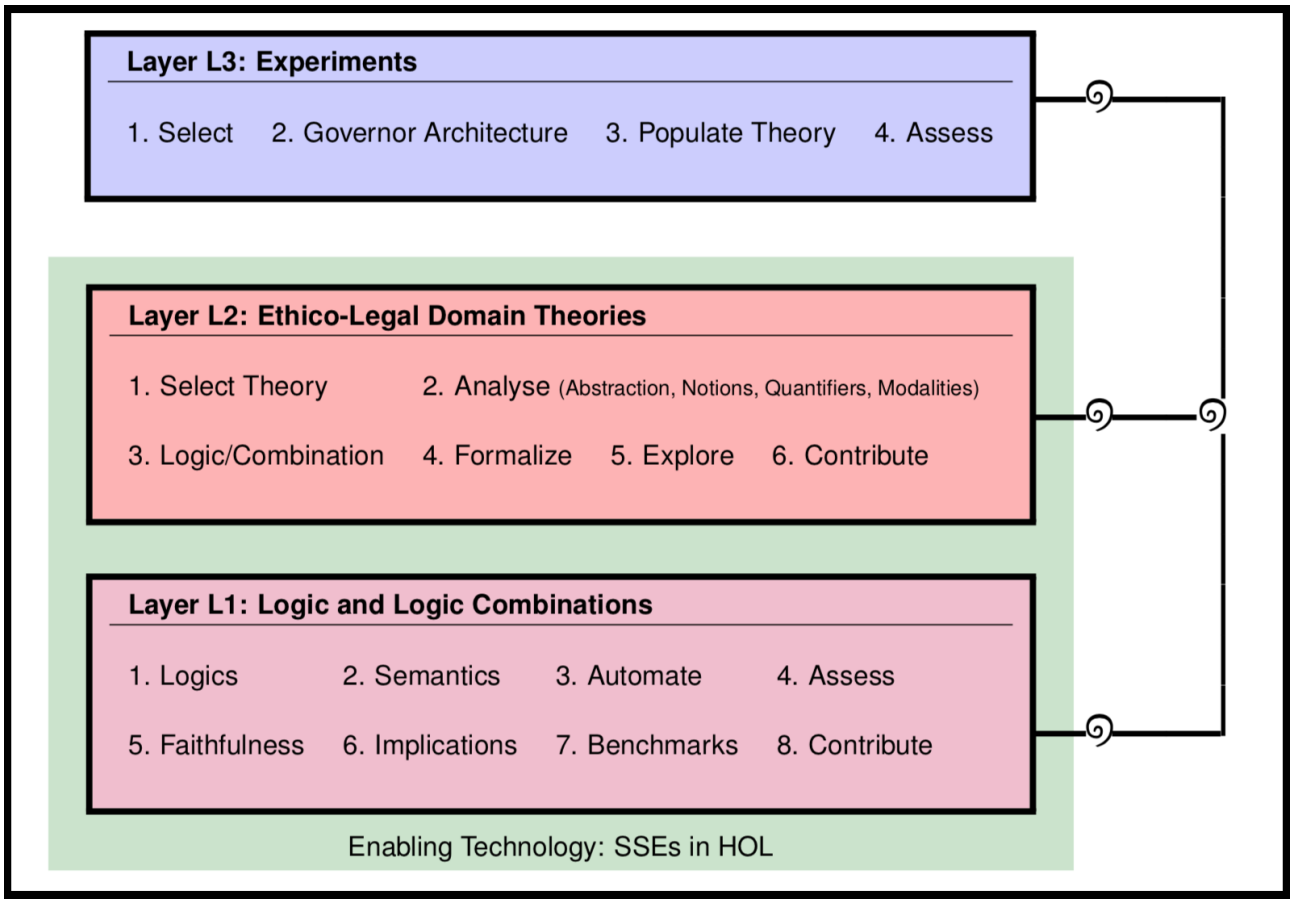

Figure 4: The LogiKEy logic and knowledge development methodology

Acknowledgments

We thank all our collaborators and students from University of Luxembourg and Freie Universität Berlin that have already utilized and tested the LogiKEy methodology in several projects not reported here.

Competing Interests

Benzmüller was funded by the VolkswagenStiftung under grant CRAP (Consistent Rational Argumentation in Politics). Parent and van der Torre were supported by the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement MIREL (MIning and REasoning with Legal texts) No 690974.

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